



We can nest patterns as deep as we want - Just like we can nest expressions as deep as we want - Often avoids hard-to-read, wordy nested case expressions CSE341: Programming Languages So the full meaning of pattern-matching is to compare a pattern Lecture 6 against a value for the "same shape" and bind variables to the "right parts" **Nested Patterns** More precise recursive definition coming after examples **Exceptions Tail Recursion** Dan Grossman Spring 2013 Spring 2013 CSE341: Programming Languages 2 Useful example: zip/unzip 3 lists Style fun zip3 lists = case lists of · Nested patterns can lead to very elegant, concise code ([],[],[]) => [] Avoid nested case expressions if nested patterns are simpler (hd1::tl1,hd2::tl2,hd3::tl3) => and avoid unnecessary branches or let-expressions (hd1,hd2,hd3):::zip3(t11,t12,t13) Example: unzip3 and nondecreasing | _ => raise ListLengthMismatch - A common idiom is matching against a tuple of datatypes to fun unzip3 triples = compare them case triples of • Examples: zip3 and multsign [] => ([],[],[]) | (a,b,c)::tl => · Wildcards are good style: use them instead of variables when let val (11, 12, 13) = unzip3 tl you do not need the data in - Examples: len and multsign (a::11,b::12,c::13) end More examples to come (see code files) Spring 2013 CSE341: Programming Languages 3 Spring 2013 CSE341: Programming Languages 4

Nested patterns

(Most of) the full definition

The semantics for pattern-matching takes a pattern p and a value v and decides (1) does it match and (2) if so, what variable bindings are introduced.

Since patterns can nest, the definition is elegantly recursive, with a separate rule for each kind of pattern. Some of the rules:

- If *p* is a variable *x*, the match succeeds and *x* is bound to *v*
- If *p* is _, the match succeeds and no bindings are introduced
- If *p* is (*p*1,...,*pn*) and *v* is (*v*1,...,*vn*), the match succeeds if and only if *p*1 matches *v*1, ..., *pn* matches *vn*. The bindings are the union of all bindings from the submatches
- If *p* is *C p*1, the match succeeds if *v* is *C v*1 (i.e., the same constructor) and *p*1 matches *v*1. The bindings are the bindings from the submatch.
- ... (there are several other similar forms of patterns)

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Examples

pairs of pairs

- Pattern a::b::c::d matches all lists with >= 3 elements

- Pattern a::b::c::[] matches all lists with 3 elements

- Pattern ((a,b), (c,d)) :: e matches all non-empty lists of

Exceptions

An exception binding introduces a new kind of exception

```
exception MyFirstException
exception MySecondException of int * int
```

The raise primitive raises (a.k.a. throws) an exception

```
raise MyFirstException
raise (MySecondException(7,9))
```

A handle expression can handle (a.k.a. catch) an exception - If doesn't match, exception continues to propagate

```
e1 handle MyFirstException => e2
e1 handle MySecondException(x,y) => e2
```

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Actually ...

Exceptions are a lot like datatype constructors...

- Declaring an exception adds a constructor for type exn •
- Can pass values of exn anywhere (e.g., function arguments) Not too common to do this but can be useful
- handle can have multiple branches with patterns for type exn

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Call-stacks

have started but not yet returned

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While a program runs, there is a *call stack* of function calls that

- When a call to **f** finishes, it is popped from the stack

Due to recursion, multiple stack-frames may be calls to the same

These stack-frames store information like the value of local

variables and "what is left to do" in the function

- Calling a function f pushes an instance of f on the stack

Recursion

Should now be comfortable with recursion:

- No harder than using a loop (whatever that is ③)
- Often much easier than a loop
 - When processing a tree (e.g., evaluate an arithmetic expression)
 - Examples like appending lists
 - Avoids mutation even for local variables
- Now:
 - How to reason about efficiency of recursion
 - The importance of tail recursion
 - Using an accumulator to achieve tail recursion
 - [No new language features here]

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Example

fact0: 1

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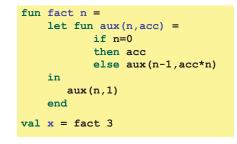
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function

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Example Revised



Still recursive, more complicated, but the result of recursive calls *is* the result for the caller (no remaining multiplication)

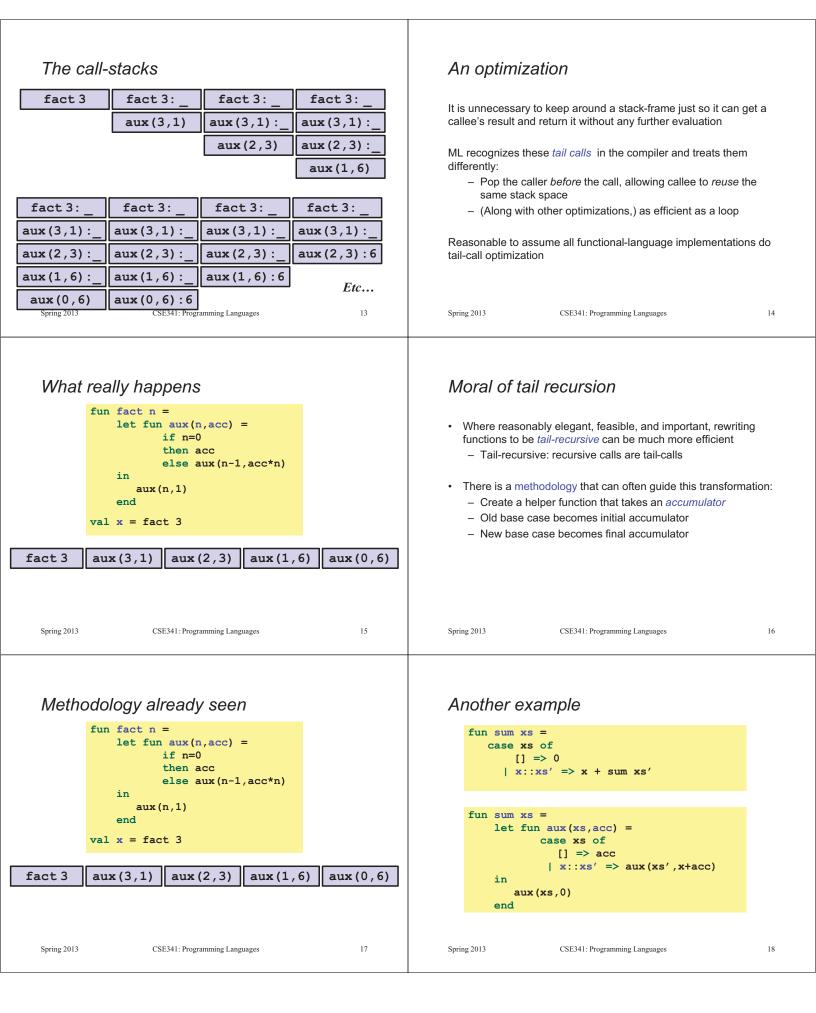
```
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```

fun fact n = if n=0 then 1 else n*fact(n-1)val x = fact 3

fact3	fact 3: 3*_	fact 3: 3*_	fact 3: 3*_
	fact2	fact 2: 2*_	fact 2: 2*_
		fact1	fact 1: 1*_
			fact0
fact 3: 3*_	fact 3: 3*_	fact 3: 3*_	fact 3: 3*2
fact 2: 2*_	fact 2: 2*_	fact 2: 2*1	
fact1:1*_	fact 1: 1*1		

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```
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```



And another			Actually much better					
fun rev xs								
case xs [] =			fur	n rev xs = case xs of				
x::xs' => (rev xs') @ [x]			[] => []					
				x::xs' => (rev xs') @ [x]				
fun rev xs let fun	= aux(xs,acc) =		Eor fact on	d tail requireign is faster but both way	va lingar timo			
<pre>case xs of [] => acc x::xs' => aux(xs',x::acc) in aux(xs,[]) end</pre>			 For fact and sum, tail-recursion is faster but both ways linear time Non-tail recursive rev is quadratic because each recursive call uses append, which must traverse the first list 					
						 And 1+2++(length-1) is almost length*length/2 Moral: beware list-append, especially within outer recursion Cons constant-time (and fast), so accumulator version much better 		
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Always tail-recursive?			What is a tail-call?					
,								
	cases where recursive functions cannot b	е						
evaluated in a constant amount of space			 The "nothing left for caller to do" intuition usually suffices If the result of f x is the "immediate result" for the enclosing function body, then f x is a tail call 					
Most obvious examples are functions that process trees								
			Dutwo con dof					
In these cases, the natural recursive approach is the way to go — You could get one recursive call to be a tail call, but rarely			But we can define "tail position" recursively — Then a "tail call" is a function call in "tail position"					
worth the co		-						
Also beware the wr	rath of premature optimization							
 Favor clear, 								
 But do use le 	ess space if inputs may be large							
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Precise defi	nition							
A tail call is a funct	tion call in tail position							
If an expression	is not in tail position, then no subeypress	ions are						
If an expression is not in tail position, then no subexpressions are								
-	e, the body e is in tail position							
	e2 else e3 is in tail position, then e2 a on (but e1 is not). (Similar for case-expres							
• If let b1 br	n in e end is in tail position, then e is in							
 position (but no binding expressions are) Function-call arguments e1 e2 are not in tail position 								
•								
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