

Name: \_\_\_\_\_

# CSE 341 : Programming Languages

## Midterm, Spring 2014

Please do not turn the page until 12:30.

*Rules:*

- Closed-book, closed-note, except for one side of one 8.5x11in piece of paper.
- Please stop promptly at 1:20.
- You can separate pages, but please staple them back together before you leave.
- There are 100 points total, distributed unevenly among 6 questions.
- When writing code, style matters, but don't worry too much about indentation.

*Advice:*

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit.
- The questions are not in order of difficulty. Skip around. Get to all the problems.
- If you have questions, ask.
- Don't worry too much; you're here to learn. You are smart and can totally do this!!!

1. (25 points) In this question we will use `map` and `fold` over lists to implement `tmap` and `tfold` over variable arity trees. Assume these implementations of `map` and `fold` for lists:

```
(* map : ('a -> 'b) -> 'a list -> 'b list *)
fun map f [] = []
  | map f (h::t) = f h :: map f t

(* fold : ('a -> 'b -> 'b) -> 'b -> 'a list -> 'b *)
fun fold f base [] = base
  | fold f base (h::t) = f h (fold f base t)
```

Consider this implementation of variable arity trees:

```
datatype 'a tree = Node of 'a * ('a tree list)
```

How should we fill in the blank to map function `f` over an entire tree?

```
(* tmap : ('a -> 'b) -> 'a tree -> 'b tree *)
fun tmap f (Node (x, ts)) = _____
```

(9 points) Circle the correct way to fill in the blank (only **one** of the options is correct):

- (a) `map f (x :: tmap f ts)`
- (b) `Node (f x, map f (tmap ts))`
- (c) `map f (tmap f (x :: ts))`
- (d) `Node (f x, tmap (map f) ts)`
- (e) `Node (f x, map (tmap f) ts)`
- (f) `map f (x :: (tmap map) f ts)`

How should we fill in the blank to fold function `f` with `base` over an entire tree?

```
(* tfold : ('a -> 'b -> 'b) -> 'b -> 'a tree -> 'b *)
fun tfold f base (Node (x, ts)) = _____
```

**(9 points)** Circle the correct way to fill in the blank (only one of the options is correct):

- (a) `f x (tfold (fold (fn t => fn acc => f t acc) base ts)`
- (b) `f x (fold (fn acc => fn t => tfold f acc t) ts base)`
- (c) `Node (x, tfold f (fold (tfold f) ts))`
- (d) `f x (fold (fn t => fn acc => tfold f acc t) base ts)`
- (e) `f x (tfold (fn t => fn acc => fold f t acc) base ts)`
- (f) `Node (f x, fold (tfold f) base ts)`

**(4 points)** Use `foldt` and the `add` function below to fill in the blank for `sumt`, a function which adds up all the ints in an int tree. Note that `sumt` uses a `val` binding!

```
fun add a b = a + b
```

```
val sumt = _____
```

**(3 points)** Fill in the blank to show the type of `sumt`:

```
sumt : _____
```

2. (15 points) Rewrite this function to be tail recursive (keep the same order!):

```
fun pairUp x [] = []  
  | pairUp x (h::t) = (x, h) :: pairUp x t
```

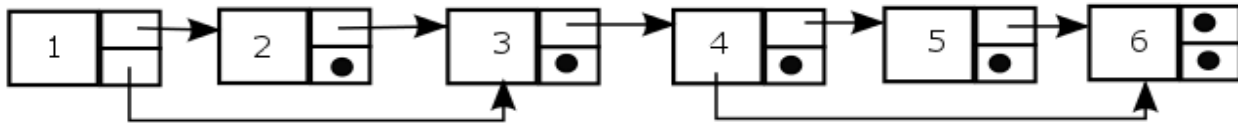
Rewrite this function to be tail recursive (keep the same order!):

```
fun xprod [] ys = []  
  | xprod (x::xs) ys = pairUp x ys @ xprod xs ys
```

3. (15 points) Consider the following datatype:

```
datatype SkipList = Null | Node of int * SkipList * SkipList
```

We can use SkipList to represent lists where we can “skip ahead” to later parts of a list. For example the bindings below represent the following list:



```
val n6 = Node(6, Null, Null)
val n5 = Node(5, n6, Null)
val n4 = Node(4, n5, n6)
val n3 = Node(3, n4, Null)
val n2 = Node(2, n3, Null)
val n1 = Node(1, n2, n3)
```

Consider these two functions which attempt to flatten a SkipList into an ordinary list:

```
fun flatten slist =
  case slist of
    Node (x, s11, s12) => x :: (flatten s12)
  | Node (x, s11, Null) => x :: (flatten s11)
  | Null => []

exception NullListError

fun flatten_again slist =
  case slist of
    Node(x, s11, Node(a, b, c)) => x :: (flatten_again s11)
  | Node(x, s11, Null) => x :: (flatten_again s11)
  | Node(x, Null, Null) => [0]
  | Null => raise NullListError
```

**(6 points)** Assuming the implementation of `fold` and `add` from Problem #1 and the definitions above, what value will `sum1` be bound to below? If `sum1` will fail to evaluate due to an uncaught exception, write the name of the thrown exception in the blank.

```
val sum1 = fold add 0 (flatten n1)
```

`sum1 = _____`

What value will `sum2` be bound to below? If `sum1` will fail to evaluate due to an uncaught exception, write the name of the thrown exception in the blank.

```
val sum2 = fold add 0 (flatten_again n1)
```

`sum2 = _____`

**(5 points)** Provide a `SkipList` built with the `Node` constructor that will cause `flatten_again` to throw an exception, or if that is not possible explain why.

**(4 points)** Using all the same lines in `flatten`, but in a different order, write a function `flatten_yet_again` such that `flatten_yet_again n1` evaluates to `[1, 3, 4, 6]`:

```
fun flatten_yet_again slist =
```

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4. **(15 points)** This question has **three** parts. We treat each part as though it were in its own separate namespace: bindings defined in previous parts are not valid in subsequent parts.

**(5 points)** Assuming the implementation of `map` from Problem #1, what is `ans` bound to after this code executes?

```
val (a, b) = (2, 4)
val add1   = (fn x => x + 1)
val times5 = (fn x => x * 5)
val square = (fn x => x * x)

fun f x y z =
  let
    val g = (fn (a, b') => a b)
  in
    y g x
  end

val foo = [(add1, true), (times5, false), (square, true)]
val ans = f foo map (fn x => [x, x])
```

ans = \_\_\_\_\_

**(5 points)** Consider the following bindings. What will `ans` be bound to after this code executes?

```
val (a, b, c, x, y) = (2, 4, 6, 8, 10)
fun f x y =
  (let
    val x = y
    val b = a
    val b = b
  in
    c * b - b
  end) + x + b
val ans = y + f 3 5 - x
```

ans = \_\_\_\_\_

**(5 points)** Consider the following two bindings:

```
fun h f = fn x => f x * f x
```

```
val v = h (h (h (fn y => y * y)))
```

Is `v` an int or a function? If it is an int, write its value. If it is a function, write its type and describe what the function computes.

**(Optional bonus problem: 3 extra credit points)** The bindings below define an int called `num`, and four functions called `f`, `g`, `h`, and `factorial`, where `factorial` is the familiar factorial function. Using each of `f`, `g`, `h`, `factorial`, and `num` **exactly once**, write an expression in the blank that will make it so that `ans` is bound to the factorial of `num`.

```
val num = 5

fun f a b c d = b a d c
fun g a b c = c a b
fun h a b = b a
fun factorial 0 = 1
  | factorial n = n * factorial (n - 1)
```

`ans = _____`



5. (15 points) Consider this program:

```
val x = ref 0

fun foo y =
  let
    val _ = x := (!x + 1);
    val _ = print (Int.toString (!x) ^ " ")
  in
    !x + y
  end

val _ = print (Int.toString (foo 1) ^ " ")
val _ = print (Int.toString (foo 1) ^ " ")
val _ = x := 5
val _ = print (Int.toString (foo 1) ^ " ")
val x = ref 10
val _ = print (Int.toString (foo 1) ^ " ")
```

(8 points) What will it print? (Only one option is correct.)

- (a) 0 1 1 2 5 6 6 7
- (b) 1 2 1 2 1 2 1 2
- (c) 1 2 2 3 6 7 11 12
- (d) 1 2 1 2 6 7 6 7
- (e) 1 2 2 3 6 7 7 8
- (f) 1 2 2 3 3 4 11 12

Now consider this program:

```
fun bar y =  
  let  
    val z = ref 0  
    val _ = z := !z + 1  
    val _ = print (Int.toString (!z) ^ " ")  
  in  
    !z + y  
  end  
  
val _ = print (Int.toString (bar 1) ^ " ")  
val _ = print (Int.toString (bar 1) ^ " ")  
val z = ref 10  
val _ = print (Int.toString (bar 1) ^ " ")
```

**(7 points)** What will it print? (Only one option is correct.)

- (a) 0 1 1 2 2 3
- (b) 1 2 1 2 1 2
- (c) 1 2 2 3 11 12
- (d) 1 2 1 2 11 12
- (e) 1 2 2 3 3 4

6. (15 points) Implement a module satisfying this signature:

```
signature STACK = sig
  type 'a t
  exception Empty
  val empty : 'a t
  val push  : 'a -> 'a t -> 'a t
  val pop   : 'a t -> 'a * 'a t
end
```

Your implementation should satisfy the following two properties:

- (1) `pop empty` should raise the `Empty` exception
- (2) `pop (push x stack)` should return `(x, stack)`

*(Hint: use lists!)*