



PAUL G. ALLEN SCHOOL  
OF COMPUTER SCIENCE & ENGINEERING

# CSE 341

## Section 5

Winter 2018

# Midterm Review!

- Variable Bindings, Shadowing, Let Expressions
- Boolean, Comparison and Arithmetic Operations
  - Equality Types
- Types, Datatypes, Type synonyms
  - Tuples, Records and Lists
- Case statement, Pattern Matching
- Functions, Anonymous Functions, Higher Order Functions
  - Actually Taking in Tuples, Function Closures
  - Tail Recursion
  - Currying
  - Filter, Map, Fold

# Midterm Review!

- Lexical Scope vs Dynamic Scope
- Type Inference, Polymorphic Types and Type Generality
- Modules
- Equivalence

# Variable Bindings

- SML evaluation creates bindings in the environments (static and dynamic) rather than change values store in variables.
- Repeated Variable names?
  - Shadowing
- Let Expression allows us to create bindings in a smaller Scope

# Boolean, Comparison and Arithmetic Operations

- Boolean Operators
  - `andalso`, `orelse` evaluates for booleans only, they are not functions (you cannot do partial evaluation with them)
  - `not` is a function
    - `- op not;`
    - `val it = fn : bool -> bool`
    - `- List.map not [true, true, false];`
    - `val it = [false,false,true] : bool list`

# Boolean, Comparison and Arithmetic Operations

- Comparison and Arithmetic Operators
  - =, <>, equality types
  - >, <, >=, <=, +, -, \*, must take the same type on both sides
  - '*div*' for integers, '/' for reals
  - You cannot divide on integer by a real or vice versa
  - Because these operators are all functions!

# Types, Datatypes, Type synonyms

- Built-in types
  - *String, int, real, bool, records, lists*
  - What about tuples?
    - They are just syntactic sugar for records
- *datatype* keyword
  - Allows you to create types by yourself
  - “one of type” and recursive type
- *type* keyword
  - “each of type”, just renaming the existing types

# Case statement, Pattern Matching

```
case e0 of
  p1 => e1
  | p2 => e2
  ...
  | pn => en
```

- Values and variables form patterns
- SML is essentially creating variable bindings of the variable with the actual value in  $e0$ .
- It is not checking if the value stored in the variable equals to what's in the current environment



# Functions, Anonymous Functions, Higher Order Functions

- Functions actually takes in a ***pattern***, for example,  $(x : int, y : bool)$ .
- By pattern matching, it creates bindings of variables and values. Then the environment is ***bound***
- The *bounded environment* along with *the code* creates ***function closure***.

# Functions, Anonymous Functions, Higher Order Functions

- Anonymous Functions use keyword *fn* rather than *fun*, which cannot be recursive
- Tail Recursion
  - You are not doing any more operation after getting returned value from your recursive call

# Functions, Anonymous Functions, Higher Order Functions

- Currying is taking a function with “several arguments” and make it into nested functions, which takes *one argument at a time*
- Partial evaluation: since curried functions are just nested functions, we can pass in one argument at a time **in order**
- We can take in functions as arguments
  - Higher order functions are just those functions that return or take in functions

# Functions, Anonymous Functions, Higher Order Functions

- Classic higher order functions
  - List.filter
  - List.map
  - List.foldl
  - List.foldr
- What do they do?

# Lexical Scope vs Dynamic Scope

- Lexical scope: use environment where function is defined
- Our Function Closure so far is in lexical scope
- Dynamic scope: use environment where function is called

# Type Inference, Polymorphic Types and Type Generality

- Polymorphic types means it can be any type
- So ``a list * `a list -> `a list` is more general than `int list * int list -> int list`
- But not more general than `int list * string list -> int list`
- Polymorphic type can be any type
- More general means you can substitute one type by another ***consistently***

# Modules

- You can hide a function by using signatures

```
structure MyModule = struct bindings end
```

```
signature SIGNAME =  
sig types-for-bindings end
```

```
structure MyModule :> SIGNAME =  
struct bindings end
```

# Modules

- Remember from lecture you can ensure constraints on values

```
structure Rational3 =  
struct  
  type rational = int * int  
  exception BadFrac  
  
  fun make_frac (x,y) = ...  
  fun Whole i = (i,1) (* needed for RATIONAL_C *)  
  fun add ((a,b) (c,d)) = (a*d+b*c,b*d)  
  fun toString r = ... (* reduce at last minute *)  
end
```



# Equivalence

- Given equivalent arguments, two equivalent pieces of code:
  - Produce equivalent results
  - Have the same (non-)termination behavior
  - Mutate (non-local) memory in the same way
  - Do the same input/output
  - Raise the same exceptions
- Look for function closures, dynamic and static environments and side effects like print

# Good Luck!