

# Data III & Integers I

CSE 351 Winter 2024

## Instructor:

Justin Hsia

## Teaching Assistants:

Adithi Raghavan

Aman Mohammed

Connie Chen

Eyoel Gebre

Jiawei Huang

Malak Zaki

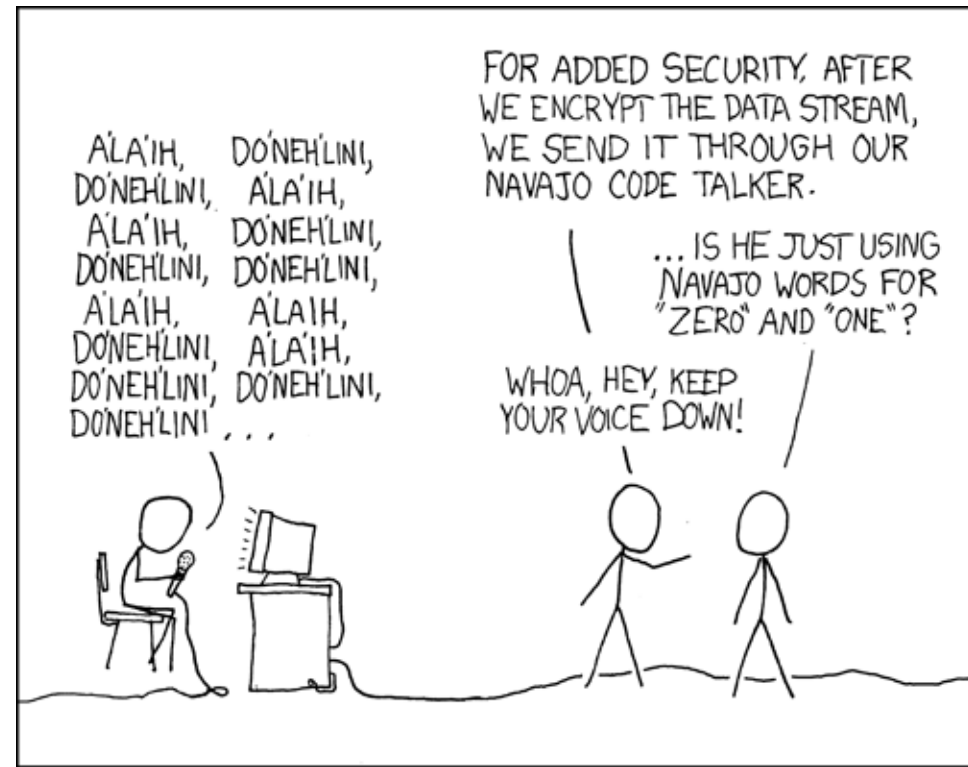
Naama Amiel

Nathan Khuat

Nikolas McNamee

Pedro Amarante

Will Robertson



<http://xkcd.com/257/>

# Relevant Course Information

- ❖ HW2 due tonight, HW3 due Friday, HW4 due next Wednesday
  
- ❖ Lab 1a released
  - Some later functions require *bit shifting*, covered in Lesson 5
  - Workflow:
    - 1) Edit `pointer.c`
    - 2) Run the Makefile (`make clean` followed by `make`) and check for compiler errors & warnings
    - 3) Run ptest (`./ptest`) and check for correct behavior
    - 4) Run rule/syntax checker (`python3 d1c.py`) and check output
  - Due Monday 1/15, will overlap a bit with Lab 1b
    - We grade just your *last* submission
    - Don't wait until the last minute to submit – need to check autograder output

# Lab Synthesis Questions

- ❖ All subsequent labs (after Lab 0) have a “synthesis question” portion
  - Can be found on the lab specs and are intended to be done *after* you finish the lab
  - You will type up your responses in a .txt file for submission on Gradescope
  - These will be graded “by hand” (read by TAs)
- ❖ Intended to check your understand of what you should have learned from the lab
  - Also great practice for short answer questions on the exams

A detailed, colorful image of a microchip die, showing a complex grid of circuitry and various colored regions (purple, blue, yellow, green, red) representing different functional blocks.

# Data III & Integers I

# Lesson Summary (1/2)

## ❖ Bit-level operators allow for fine-grained manipulation

- Bitwise AND (&), OR (|), XOR (^) and NOT (~) operate on the individual bits of the data
- Especially useful with bitmasks, chosen bit vectors used with &, |, or ^
  - $b \& 0 = 0$ ,  $b \& 1 = b$  (set to zero or keep as-is)
  - $b | 0 = b$ ,  $b | 1 = 1$  (keep as-is or set to one)
  - $b \wedge 0 = b$ ,  $b \wedge 1 = \sim b$  (keep as-is or flip the bit)

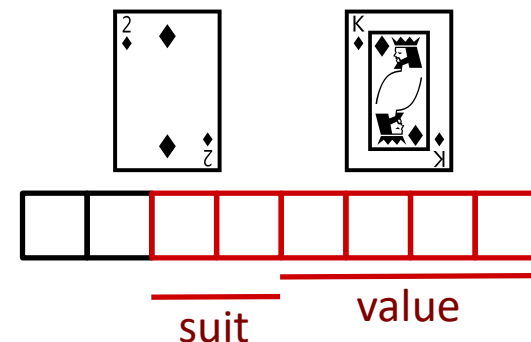
<b>AND</b> Outputs 1 only when both input bits are 1: <table style="margin: auto;"> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">&amp;</td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">1</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">0</td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">0</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">1</td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">1</td></tr> </table>	&	0	1	0	0	0	1	0	1	<b>OR</b> Outputs 1 when either input bit is 1: <table style="margin: auto;"> <tr><td style="border-right: 1px solid black; padding: 2px 5px;"> </td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">1</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">0</td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">1</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">1</td><td style="padding: 2px 5px;">1</td><td style="padding: 2px 5px;">1</td></tr> </table>		0	1	0	0	1	1	1	1
&	0	1																	
0	0	0																	
1	0	1																	
	0	1																	
0	0	1																	
1	1	1																	
<b>XOR</b> Outputs 1 when either input is <i>exclusively</i> 1: <table style="margin: auto;"> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">^</td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">1</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">0</td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">1</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">1</td><td style="padding: 2px 5px;">1</td><td style="padding: 2px 5px;">0</td></tr> </table>	^	0	1	0	0	1	1	1	0	<b>NOT</b> Outputs the opposite of its input: <table style="margin: auto;"> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">~</td><td style="padding: 2px 5px;"></td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">0</td><td style="padding: 2px 5px;">1</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">1</td><td style="padding: 2px 5px;">0</td></tr> </table>	~		0	1	1	0			
^	0	1																	
0	0	1																	
1	1	0																	
~																			
0	1																		
1	0																		

## ❖ Logical operators work on “truthiness” of data

- 0 = False, anything else = True
- Logical AND (&&), OR (||), and NOT (!) → always evaluate to 1 for True

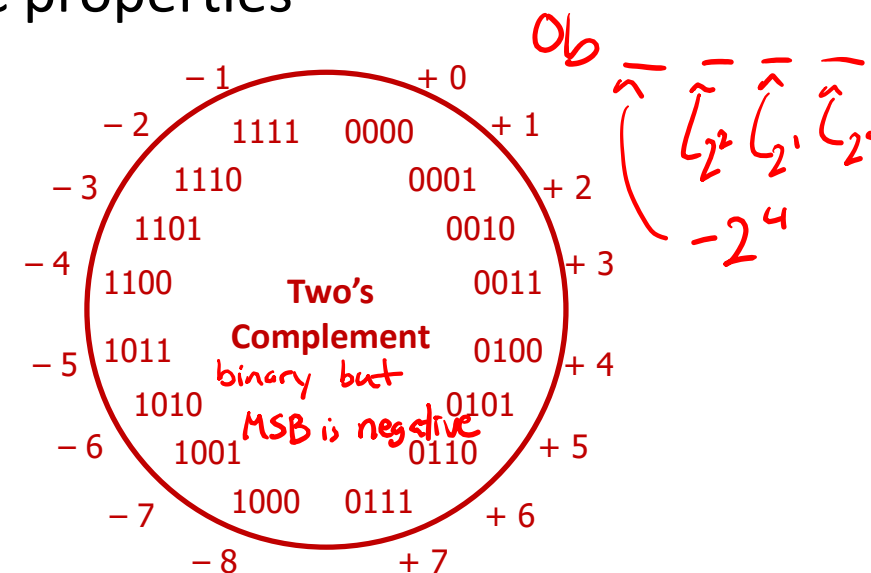
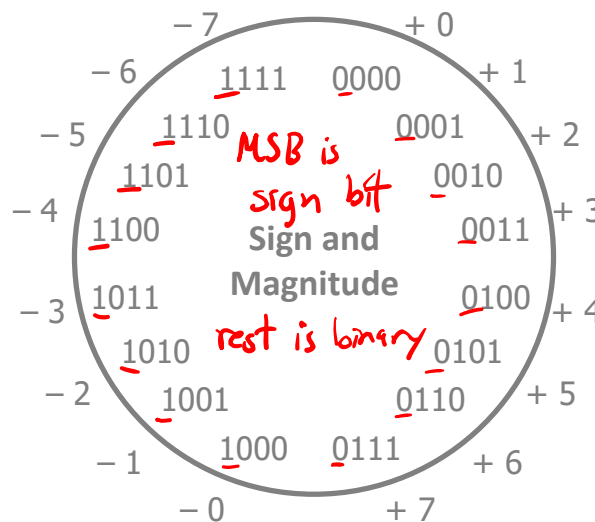
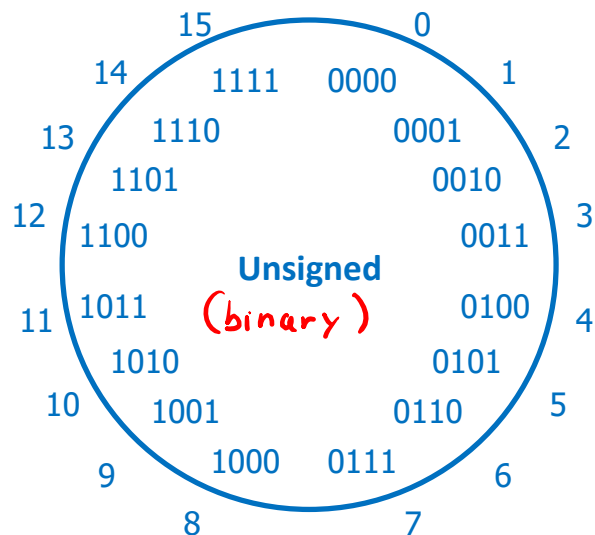
# Lesson Summary (2/2)

- ❖ Choice of *encoding scheme* is important
  - Tradeoffs based on size requirements and desired operations



- ❖ Integers represented using unsigned and two's complement representations (sign and magnitude not used in practice)

- Limited by fixed bit width, satisfy desirable arithmetic properties



# Lesson Q&A

- ❖ Learning Objectives:
  - Compute the effects of bit shifting, bitwise, logical, and arithmetic operations on integers.
  - Analyze the benefits and drawbacks of different integer representations (Unsigned, Sign and Magnitude, Two's Complement) and custom encoding schemes.
- ❖ What lingering questions do you have from the lesson?
  - Chat with your neighbors about the lesson for a few minutes to come up with questions

A detailed, colorful microchip die image serves as the background for the title. The die is densely packed with various colored regions (purple, blue, yellow, green, red) representing different functional blocks and interconnects.

# Data III & Integers I – Practice



# Practice Questions (1/2)

❖ Compute the result of the following expressions for

char c = 0x81; // 0b 1000 0001

■  $c \wedge c = 0x00$

$$\begin{array}{r} 1000\ 0001 \\ 1000\ 0001 \\ \hline 0000\ 0000 \end{array}$$

■  $\sim c \ \& \ 0xA9 = 0x28$

$$\begin{array}{r} 0b0111\ 1110 \\ 0b1010\ 1001 \\ \hline 0010\ 1000 \end{array}$$

■  $c \ || \ 0x80 = 0x01$

"true" "true" "true"

■  $!(!c) = 0x01$

"false" 0x0

❖ Compute the value of signed char sc = 0xF0; (Two's Complement)

$$-sc = \sim sc + 1 = 0b0000\ 1111 + 1 = 0b0001\ 0000 = +16$$

$$= 0b1111\ 0000 = -2^7 + 2^6 + 2^5 + 2^4 = -16$$

**sc = -16**

## Practice Questions (2/2)

- ❖ Take the 4-bit number encoding  $x = 0b1011$ 
  - MSB
- ❖ Which of the following numbers is NOT a valid interpretation of  $x$  using any of the number representation schemes discussed today?
  - Unsigned, Sign and Magnitude, Two's Complement

A. -4

**B. -5**

~~C. 11~~

~~D. -3~~

~~E. We're lost...~~

unsigned:  $8 + 2 + 1 = 11$

sign + mag:  $1011 \rightarrow -(2+1) = -3$

two's:  $-8 + 2 + 1 = -5$

$-x = 0b\ 0100 + 1 = 5 \rightarrow x = -5$

A detailed, colorful micrograph of a microchip die, showing a complex grid of circuitry and various colored regions (purple, blue, yellow, green, red) representing different functional blocks.

# Data III & Integers I – Context

# Integer Hardware

- ❖ In practice, all modern system use **unsigned** and **two's complement** encoding schemes for integers
  - Sign and magnitude for integers is a historical artifact, but useful context for design decision and for floating point (next unit)
  - Much of the same hardware can be used for both encoding schemes (*e.g.*, addition, subtraction)
- ❖ Fun fact: Java was designed to only support signed data types
  - *Assumed easier for beginners to understand* than having unsigned as well (*i.e.*, eliminate potential sources of error)
  - Unsigned operation support provided with Unsigned Integer API (starting with Java SE 8 in 2014)

# Discussion Questions

- ❖ Discuss the following question(s) in groups of 3-4 students
  - I will call on a few groups afterwards so please be prepared to share out
  - Be respectful of others' opinions and experiences
- ❖ Thinking about the (implicit and explicit) design decisions for Two's Complement, what are some of the *advantages* and *disadvantages* of choosing to:
  - Represent consecutive (*i.e.*, no gaps) integers  
*example, if only representing even integers, what should happen when we compute 6/2 ?*
  - Represent the same number of positives and negatives  
*the bias should make sense in the context of our application* *arithmetic might get weird again...*
  - Positive number encodings match unsigned  
*no need to convert anything when changing interpretations*

# Group Work Time

- ❖ During this time, you are encouraged to work on the following:
  - 1) If desired, continue your discussion
  - 2) Work on the homework problems
  - 3) Work on the lab (if applicable)
  
- ❖ Resources:
  - You can revisit the lesson material
  - Work together in groups and help each other out
  - Course staff will circle around to provide support