

Integers II

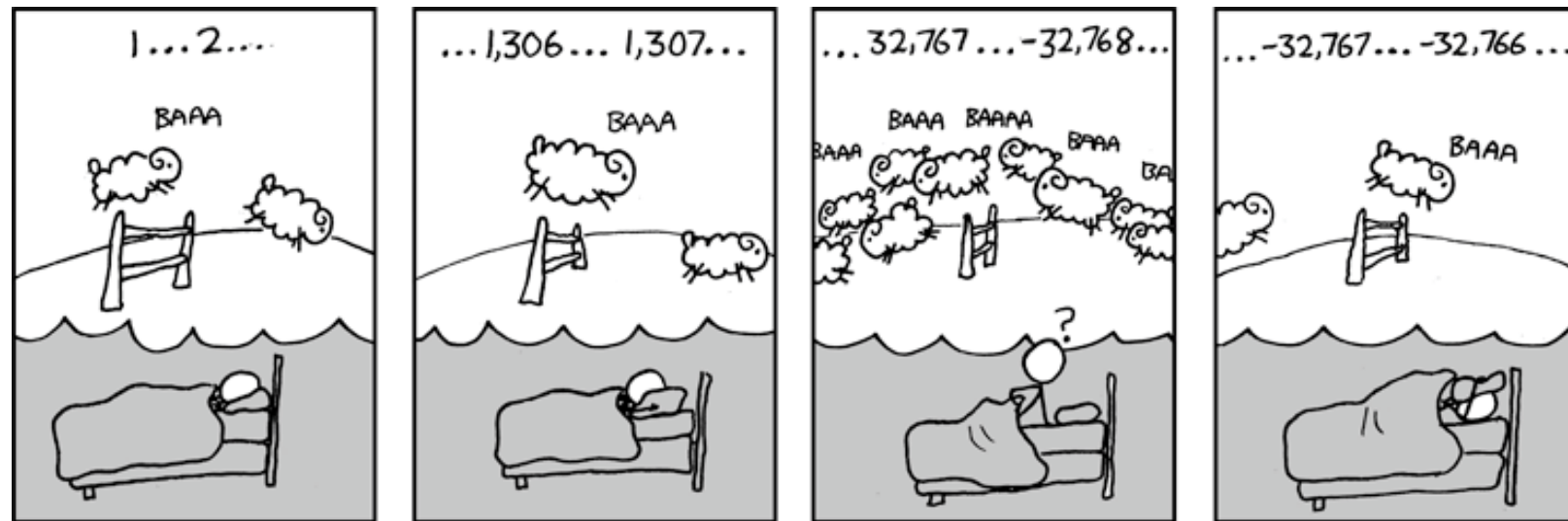
CSE 351 Winter 2024

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<http://xkcd.com/571/>

Relevant Course Information

- ❖ Monday is MLK Jr. Holiday
 - There will still be some virtual support hours
- ❖ HW4 due Wednesday, HW5 due next Friday
- ❖ Lab 1a due Monday (1/15)
 - Use `pctest` and `d1c.py` to check your solution for correctness (on the CSE Linux environment)
 - Submit `pointer.c` and `lab1Asynthesis.txt` to Gradescope
 - Make sure you pass the File and Compilation Check – all the correct files were found and there were no compilation or runtime errors
- ❖ Lab 1b released today, due 1/22
 - Bit manipulation on a custom encoding scheme

Runnable Code Snippets on Ed

- ❖ Ed allows you to embed runnable code snippets (*e.g.*, readings, homework, discussion)
 - These are *editable* and *rerunnable*!
 - Hides compiler warnings, but will show compiler errors and runtime errors
- ❖ Suggested use
 - Good for experimental questions about basic behaviors in C
 - *NOT* entirely consistent with the CSE Linux environment, so should not be used for any lab-related work

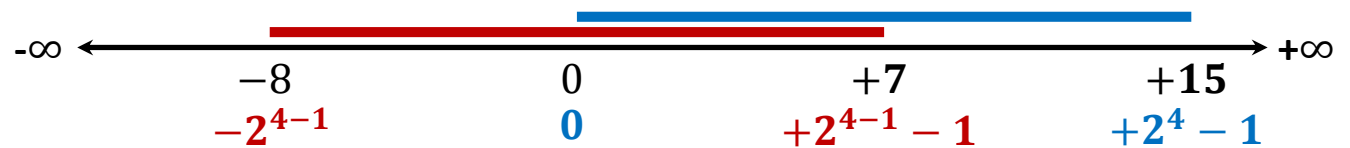
A detailed, colorful micrograph of a microchip die, showing a complex grid of circuitry and various colored regions (purple, blue, yellow, green, red) representing different functional blocks.

Integers II

Lesson Summary (1/3)

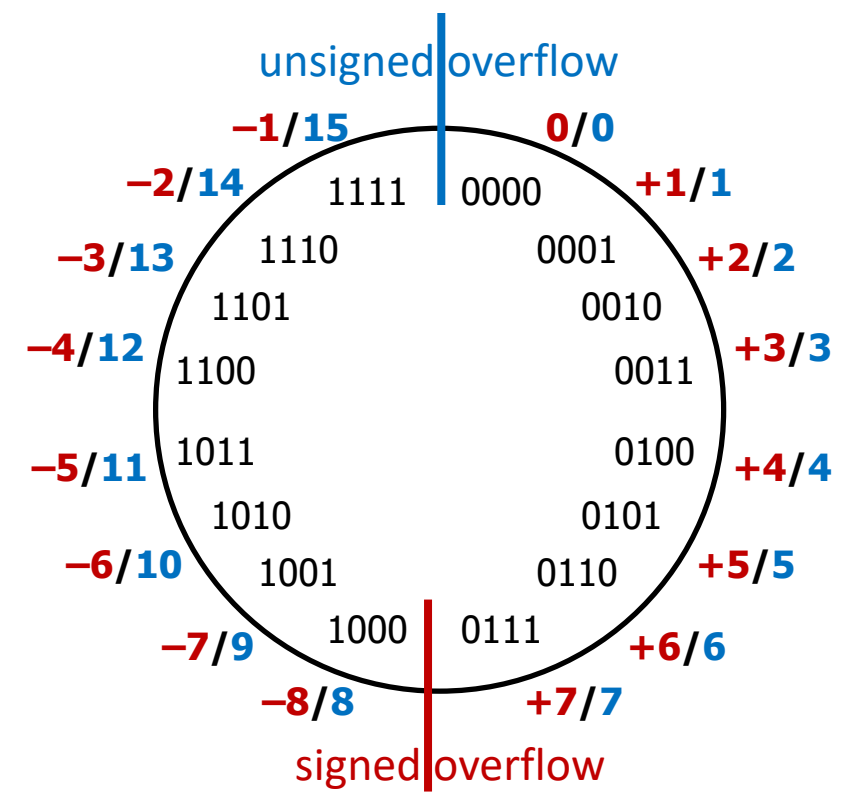
❖ We can only represent a limited range of numbers in w bits (2^w things)

- Unsigned: [UMin, UMax]
- Signed: [TMin, TMax]



❖ Integer arithmetic is the same in hardware regardless of interpretation

- When we exceed the limits, *arithmetic overflow* occurs following the rules of modular arithmetic
 - Signed vs. unsigned overflow depends on interpretation of numbers:



Lesson Summary (2/3)

- ❖ Data types determine size, interpretations, and operator behaviors
- ❖ Casting (implicit or explicit) can convert values between different data types
 - Be careful of the possible consequences of casting (truncation, zero/sign extension, change in interpreted value, change in operator behaviors like comparisons and shifting)

```
int i = -1;
long c = i;           // changed size (sign extension)
unsigned int ui = i; // changed interpretation

// i < 1 (True) is different than ui < 1 (False)
```

Lesson Summary (3/3)

- ❖ Shifting is a useful bitwise operator
 - Throw away (drop) extra bits that “fall off” the end
 - Left shifting always fills with 0’s
 - Right shifting can be **arithmetic** (fill with copies of sign bit) or **logical** (fill with 0’s)
 - Shifts by $n < 0$ or $n \geq w$ (w is bit width) are *undefined*
- ❖ Common use cases: constant multiplication, bit masking
 - `x = x << 3; // equivalent to 8*x`
 - `x = (x >> 8) << 8; // zeros out lowest byte of x`

Lesson Q&A

- ❖ Learning Objectives:
 - Identify when integer limitations are encountered (*e.g.*, overflow).
 - Identify the effect of C casts (both implicit and explicit) on stored values and the behavior of operations.
- ❖ What lingering questions do you have from the lesson?
 - Chat with your neighbors about the lesson for a few minutes to come up with questions

A detailed, colorful micrograph of a microchip die, showing a complex grid of circuitry and various colored regions (purple, blue, yellow, green, red) representing different functional blocks.

Integers II – Practice

Practice Problems (1/2)

❖ What is the value (and encoding) of TMin for a fictional 6-bit wide integer data type?

$$0b \frac{1}{-2^5} \frac{0}{2^4} \frac{0}{2^3} \frac{0}{2^2} \frac{0}{2^1} \frac{0}{2^0}$$

$$-2^{n-1} = -2^5 = \boxed{-32}$$

signed
most negative
represent $2^6 = 64$ numbers

❖ For unsigned char uc = 0xA1;, what are the produced data for the cast (unsigned short)uc?

2 bytes

unsigned → zero extension

$$\boxed{0x00A1}$$

❖ What is the result of the following expressions?

- (signed char)uc >> 2
- (unsigned char)uc >> 3

signed: $0b \underline{1}010 \cancel{0001} \xrightarrow{\text{arithmetic}} 0b \underline{111}01000 = \boxed{0xE8}$

unsigned: $0b 1010 \cancel{0001} \xrightarrow{\text{logical}} 0b \underline{000}10100 = \boxed{0x14}$

Practice Problems (2/2)

❖ Assuming 8-bit integers:

- $0x27 = 39$ (signed) = 39 (unsigned)
- $0xD9 = -39$ (signed) = 217 (unsigned)
- $0x7F = 127$ (signed) = 127 (unsigned)
- $0x81 = -127$ (signed) = 129 (unsigned)

$$[TMin, TMax] = [-128, 127]$$

$$[UMin, UMax] = [0, 255]$$

❖ For the following additions, did signed and/or unsigned overflow occur?

- $0x27 + 0x81$

signed: $39 + (-127) = -88$
no signed overflow

unsigned: $39 + 129 = 168$
no unsigned overflow

- $0x7F + 0xD9$

signed: $127 + (-39) = 88$
no signed overflow

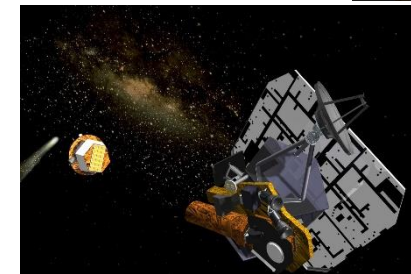
unsigned: $127 + 217 = 344$
unsigned overflow



Integers II – Context

Integer Representation Issues in Real Life

- ❖ **1985:** Therac-25 radiation therapy machine
 - Overdoses of radiation due to arithmetic overflow of incrementing a 1-byte safety flag variable
- ❖ **2000:** Y2K problem
 - Limited representation (two-digit decimal year)
- ❖ **2013:** Deep Impact spacecraft lost
 - Suspected integer overflow from storing time as tenth-seconds in unsigned int: 8/11/2013, 00:38:49.6
- ❖ **2038:** Unix epoch time rollover (seconds since 1/1/1970)
 - Signed 32-bit integer representation rolls over to TMin in 2038



Unix Epoch:
00:00:00
January 1, 1970

Discussion Question

- ❖ Discuss the following question(s) in groups of 3-4 students
 - I will call on a few groups afterwards so please be prepared to share out
 - Be respectful of others' opinions and experiences
- ❖ Given that **arithmetic overflow** is a well-known property of integers in computing, what do you think are some of the *causes* and *pressures* that perpetuate these issues?
 - Think broadly! Ideas could be technical, economic, societal, etc.

Group Work Time

- ❖ During this time, you are encouraged to work on the following:
 - 1) If desired, continue your discussion
 - 2) Work on the homework problems
 - 3) Work on the lab (if applicable)

- ❖ Resources:
 - You can revisit the lesson material
 - Work together in groups and help each other out
 - Course staff will circle around to provide support