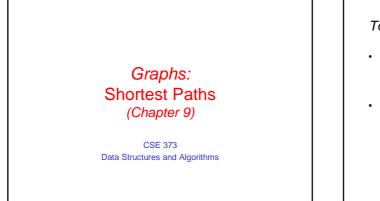
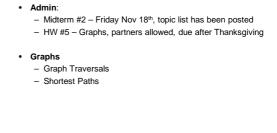
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Today's Outline



Single source shortest paths

- Done: BFS to find the minimum path length from \bm{v} to \bm{u} in O(|E|+(|V|)
- Actually, can find the minimum path length from v to every node

 Still O(|E|+(|V|))
 - No faster way for a "distinguished" destination in the worst-case
- Now: Weighted graphs

Given a weighted graph and node v, find the minimum-cost path from v to every node

• As before, asymptotically no harder than for one destination

Unlike before, BFS will not work

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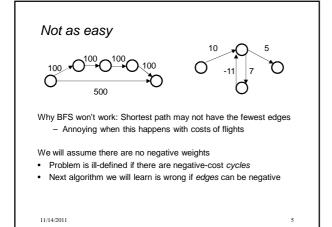
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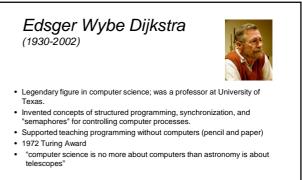
Applications

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- Network routing
- Driving directions
- Cheap flight tickets
- Critical paths in project management (see textbook)

- ...





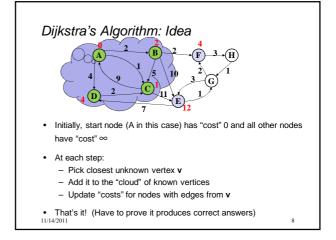
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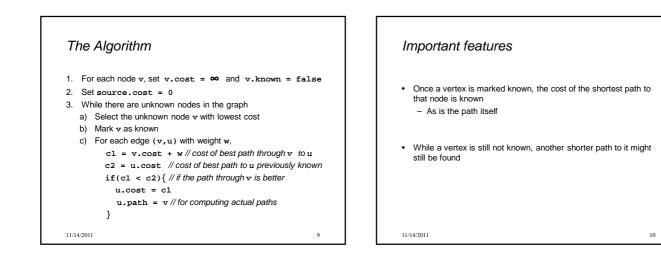
Dijkstra's Algorithm

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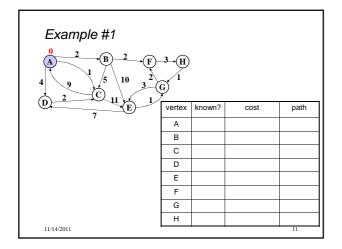
The idea: reminiscent of BFS, but adapted to handle weights

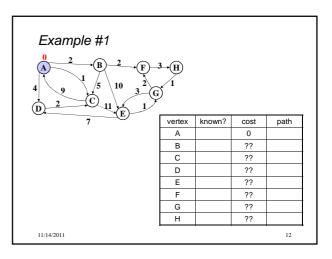
- A priority queue will prove useful for efficiency (later)
- Will grow the set of nodes whose shortest distance has been computed
- Nodes not in the set will have a "best distance so far"

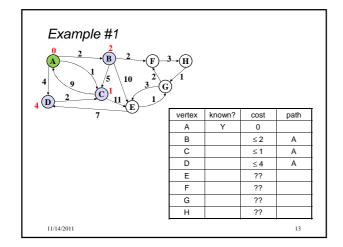


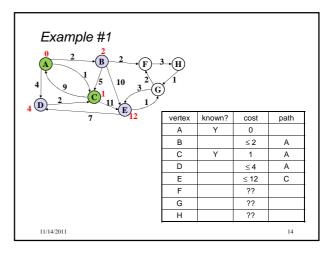


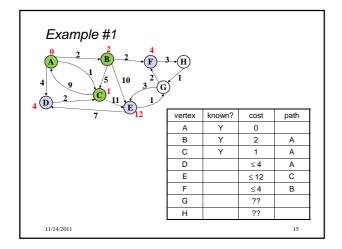
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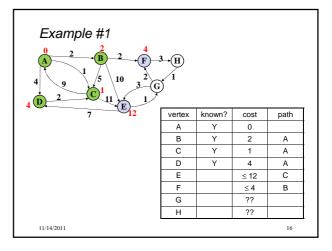


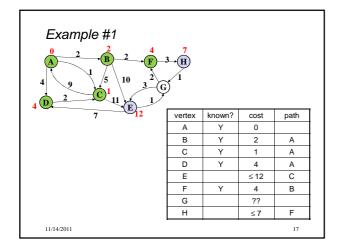


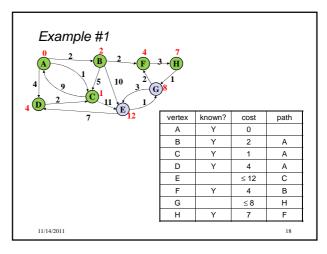


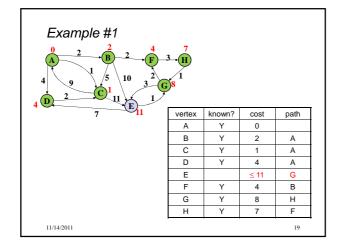


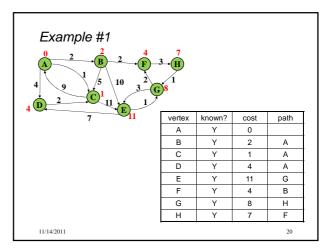


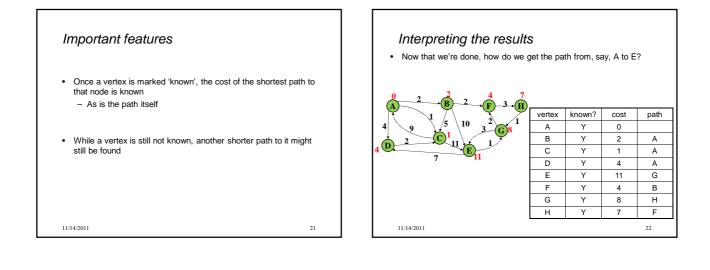


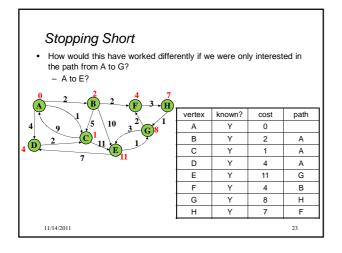


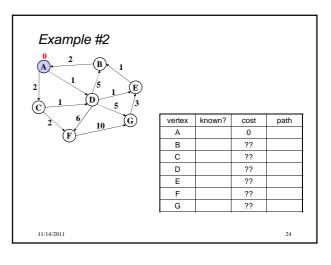


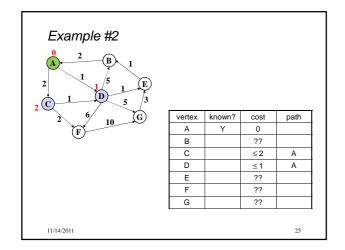


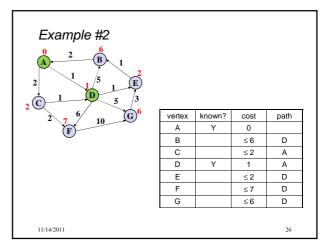


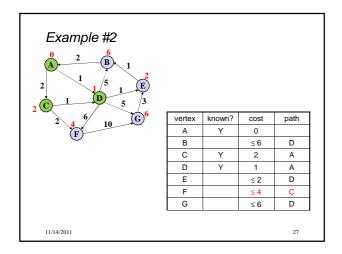


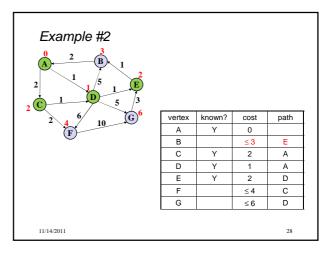


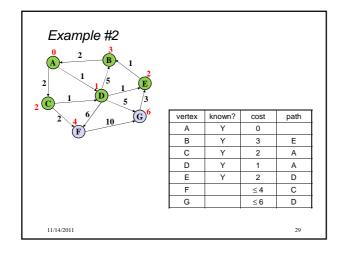


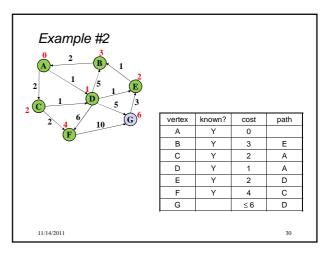


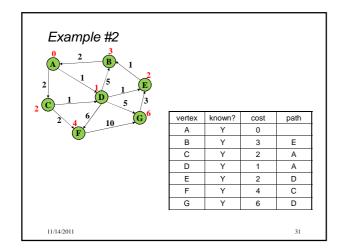


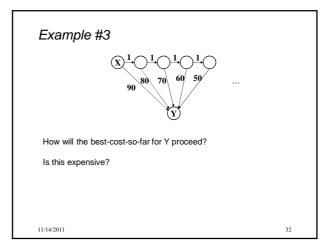


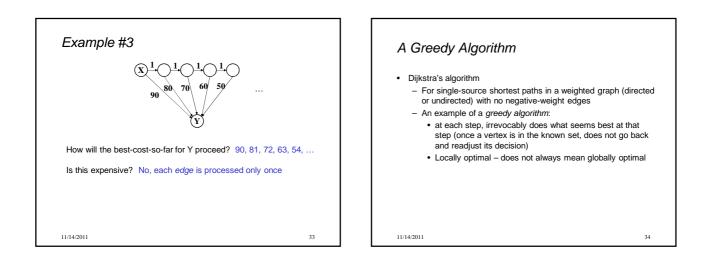


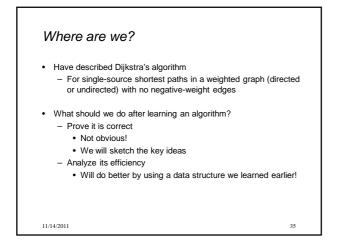


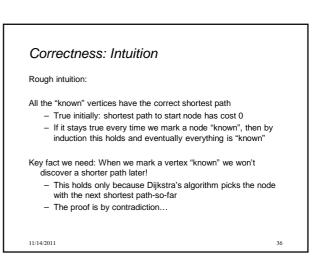


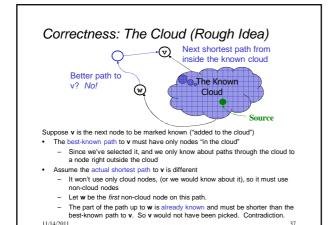


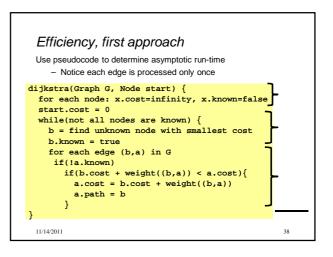


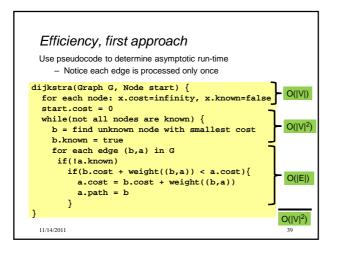


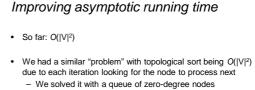












 But here we need the lowest-cost node and costs can change as we process edges

40

- Solution?
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