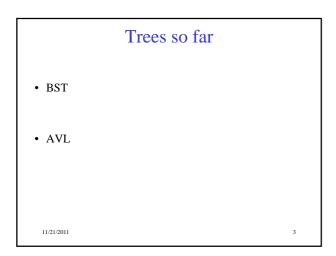
B-Trees (4.7 in Weiss) **CSE 373** Data Structures & Algorithms **Ruth Anderson** 11/21/2011

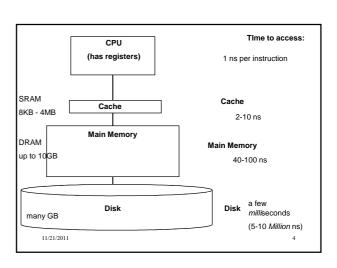
Today's Outline - Midterm #2 - Friday Nov 18th, topic list has been posted - HW #5 - Graphs, partners due Wed 23 at 11pm, due Thurs Dec 1 at 11pm - Minimum Spanning Trees • Dictionaries - B-Trees

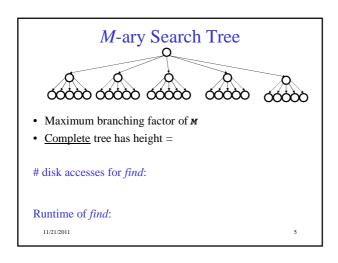
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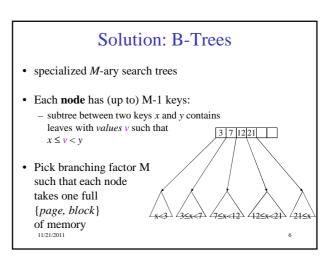
· Graphs

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B-Trees

What makes them disk-friendly?

- 1. Many keys stored in a node
 - All brought to memory/cache in one access!
- 2. Internal nodes contain only keys;

Only leaf nodes contain keys and actual data

- The tree <u>structure</u> can be loaded into memory irrespective of data object size
- · Data actually resides in disk

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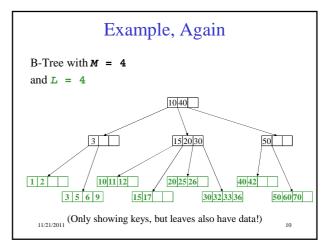
B-Tree: Example B-Tree with M = 4 (# pointers in internal node) and L = 4(# data items in Leaf) 10 40 50 3 15 20 30 20 25 26 10 11 12 1 2 AB xG 3 5 6 9 30 32 33 36 50 60 70 15 17 Data objects, that I'll ignore in slides 11/21/2011 Note: All leaves at the same depth!

B-Tree Properties ‡

- Data is stored at the leaves
- All leaves are at the same depth and contain between $\lceil L/2 \rceil$ and L data items
- Internal nodes store up to *M-1* keys
- Internal nodes have between $\lceil M/2 \rceil$ and M children
- Root (special case) has between 2 and M children (or root could be a leaf)

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‡These are technically B+-Trees



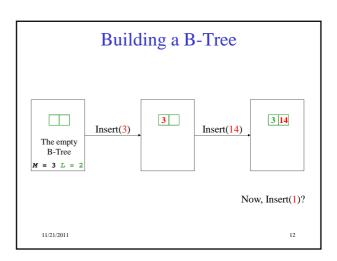
B-trees vs. AVL trees

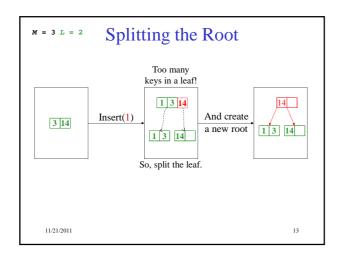
Suppose we have 100 million items (100,000,000):

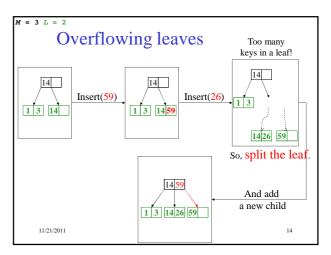
- · Depth of AVL Tree
- Depth of B+ Tree with M = 128, L = 64

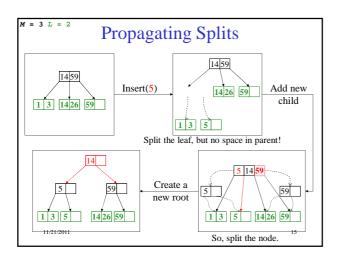
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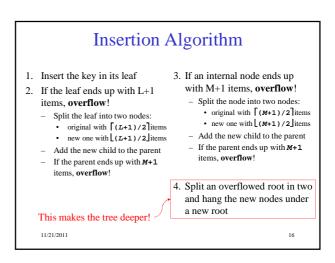
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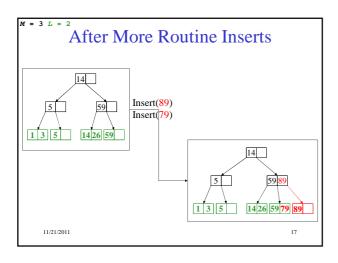


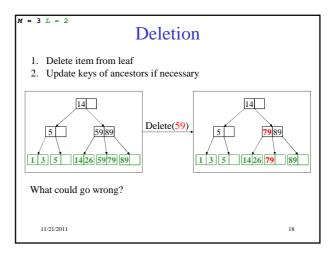


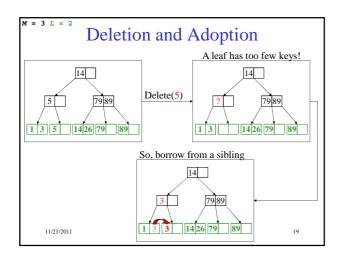


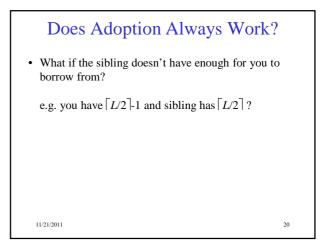


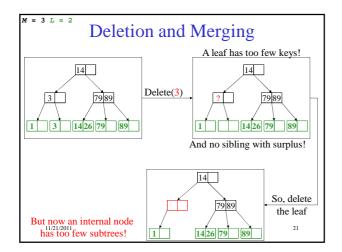


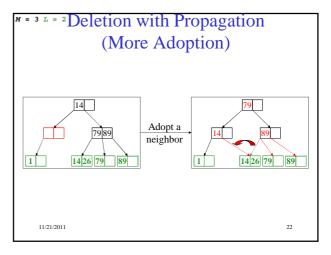


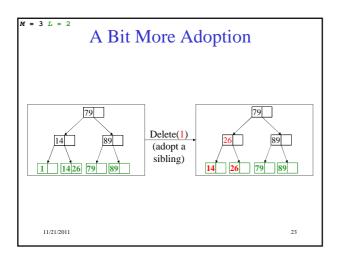


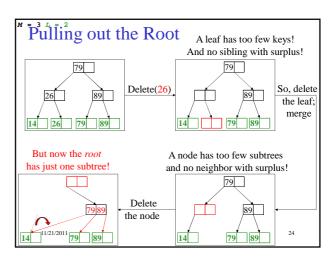


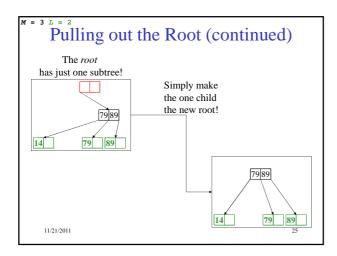


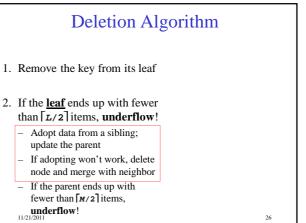












Deletion Slide Two 3. If an internal node ends up with fewer than M/2 items, underflow! - Adopt from a neighbor; update the parent - If adoption won't work, merge with neighbor - If the parent ends up with fewer than [M/2] items, underflow! This reduces the 4. If the root ends up with only one height of the tree! child, make the child the new root of the tree 11/21/2011 27

