Asymptotic Analysis

CSE 373 Data Structures & Algorithms **Ruth Anderson** Autumn 2012

Today's Outline

Announcements

- Assignment #1, due Thurs, Oct 4 at 11pm Assignment #2, posted later this week, due Fri Oct 12 at BEGINNING of lecture

2

3

- Algorithm Analysis
 - How to compare two algorithms?
 - Analyzing code
 - Big-Oh

10/01/2012

Comparing Two Algorithms...

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What we want

- Rough Estimate
- Ignores Details

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Big-O Analysis

Ignores "details"

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Gauging performance

- Uh, why not just run the program and time it?
 - Too much variability; not reliable:
 - Hardware: processor(s), memory, etc.
 - OS, version of Java, libraries, drivers
 - Programs running in the background
 - Implementation dependent
 - Choice of input
 - Timing doesn't really evaluate the *algorithm*; it evaluates an *implementation* in one very specific scenario

4

6

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Comparing algorithms

When is one *algorithm* (not *implementation*) better than another?

- Various possible answers (clarity, security, ...)
- But a big one is *performance*: for sufficiently large inputs, runs in less time (our focus) or less space
- We will focus on large inputs (n) because probably any algorithm is "plenty good" for small inputs (if *n* is 10, probably anything is fast enough)

Answer will be *independent* of CPU speed, programming language, coding tricks, etc.

7

Answer is general and rigorous, complementary to "coding it up and timing it on some test cases" — Can do analysis before coding!

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Why Asymptotic Analysis?

- Most algorithms are fast for small n
 Time difference too small to be noticeable
 - External things dominate (OS, disk I/O, ...)
- BUT *n* is often large in practice
 Databases, internet, graphics, ...
- Time difference really shows up as *n* grows!

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Analyzing code ("worst case")

Basic operations take "some amount of" constant time

- Arithmetic (fixed-width)
- Assignment
- Access one Java field or array index
- Etc.
- (This is an approximation.)

Consecutive statements Conditionals Loops Calls Recursion Sum of times Time of test plus slower branch Sum of iterations Time of call's body Solve *recurrence equation*

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E	Example	
	2 3 5 16 37 50 73 75 126	
Fi	nd an integer in a <i>sorted</i> array	
	<pre>// requires array is sorted // returns whether k is in array boolean find(int[]arr, int k){ ??? }</pre>	
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16 37 50 73 75 126

Best case:

Worst case:

11

Linear search

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return false;

}

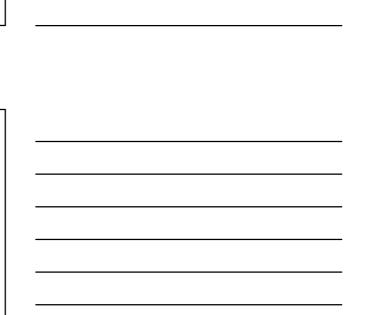
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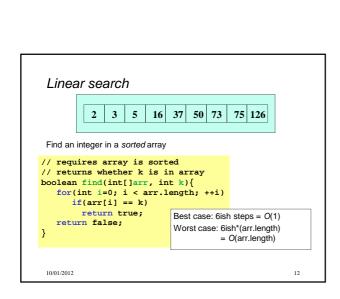
Find an integer in a sorted array

3 5

// requires array is sorted
// returns whether k is in array
boolean find(int[]arr, int k){

for(int i=0; i < arr.length; ++i)
 if(arr[i] == k)
 return true;</pre>







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	2 3	5	16 37	50	73	75	126			
Find an	integer in a	sorted	array							
<pre>// requires array is sorted // returns whether k is in array boolean find(int[]arr, int k){ return help(arr,k,0,arr.length); }</pre>										
<pre>boolean help(int[]arr, int k, int lo, int hi) { int mid = (hi+lo)/2; //i.e., lo+(hi-lo)/2 if(lo=hi) return false; if(arr[mid]==k) return true; if(arr[mid]< k) return help(arr,k,mid+1,hi);</pre>										
el } 10/01/2012	se	:	return l	nelp(arr	,k,10	o,mid);	13	



