

Priority Queues: Binary Min Heaps

CSE 373
Data Structures and Algorithms

10/12/2012

1

Today's Outline

- **Announcements**
 - Assignment #2 due Fri, Oct 12 at the BEGINNING of lecture
 - Midterm #1, Fri, Oct 19.
 - Assignment #3 coming soon, due Thurs, Oct 25.
- **Today's Topics:**
 - **Dictionary**
 - **Balanced Binary Search Trees - (AVL Trees)**
 - **Priority Queues**
 - **Binary Min Heap**

10/12/2012

2

Priority Queue ADT

1. **PQueue data** : collection of data with **priority**
2. **PQueue operations**
 - insert
 - deleteMin

(also: create, destroy, is_empty)
3. **PQueue property**: for two elements in the queue, x and y , if x has a **lower** **priority value** than y , x will be deleted before y

10/12/2012

3

Applications of the Priority Q

- Select print jobs in order of decreasing **length**
- Forward packets on network routers in order of **urgency**
- Select most **frequent** symbols for compression
- Sort numbers, picking **minimum** first
- **Anything greedy**

10/12/2012

4

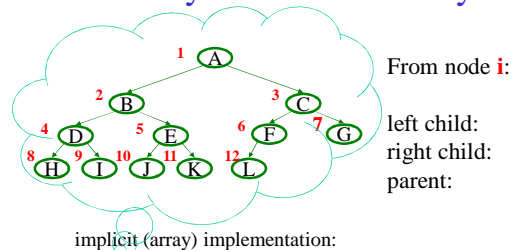
Implementations of Priority Queue ADT

	insert	deleteMin
Unsorted list (Array)		
Unsorted list (Linked-List)		
Sorted list (Array)		
Sorted list (Linked-List)		
Binary Search Tree (BST)		

10/12/2012

5

Representing Complete Binary Trees in an Array



	A	B	C	D	E	F	G	H	I	J	K	L	
0	1	2	3	4	5	6	7	8	9	10	11	12	13

10/12/2012

6

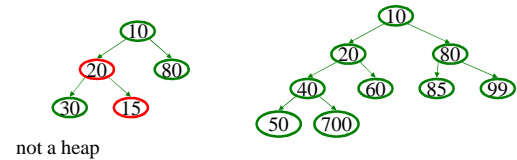
Why better than tree with pointers?

10/12/2012

7

Heap Order Property

Heap order property: For every non-root node X, the value in the parent of X is less than (or equal to) the value in X.

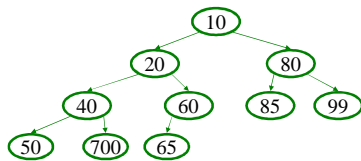


10/12/2012

8

Heap Operations

- findMin:
- insert(val): percolate up.
- deleteMin: percolate down.



10/12/2012

9

Heap – Insert(val)

Basic Idea:

1. Put val at “next” leaf position
2. Repeatedly exchange node with its parent if needed

10/12/2012

10

Insert pseudo Code (optimized)

```
void insert(Object o) {
    assert(!isFull());
    size++;
    newPos =
    percolateUp(size,o);
    Heap[newPos] = o;
}

int percolateUp(int hole,
                Object val) {
    while (hole > 1 &&
           val < Heap[hole/2])
        Heap[hole] = Heap[hole/2];
        hole /= 2;
    return hole;
}
```

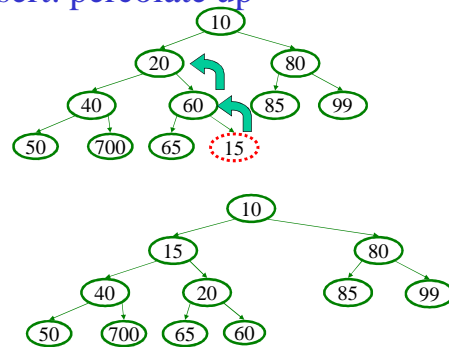
runtime:

(Java code in book)

10/12/2012

11

Insert: percolate up



10/12/2012

12

Heap – Deletemin

Basic Idea:

1. Remove root (that is always the min!)
2. Put “last” leaf node at root
3. Find smallest child of node
4. Swap node with its smallest child if needed.
5. Repeat steps 3 & 4 until no swaps needed.

10/12/2012

13

DeleteMin pseudo Code (Optimized)

```

Object deleteMin() {
    assert(!isEmpty());
    returnVal = Heap[1];
    size--;
    newPos =
        percolateDown(1,
            Heap[size+1]);
    Heap[newPos] =
        Heap[size + 1];
    return returnVal;
}

int percolateDown(int hole,
    Object val) {
    while (2*hole <= size) {
        left = 2*hole;
        right = left + 1;
        if (right <= size &&
            Heap[right] < Heap[left])
            target = right;
        else
            target = left;
        if (Heap[target] < val) {
            Heap[hole] = Heap[target];
            hole = target;
        }
        else
            break;
    }
    return hole;
}
    
```

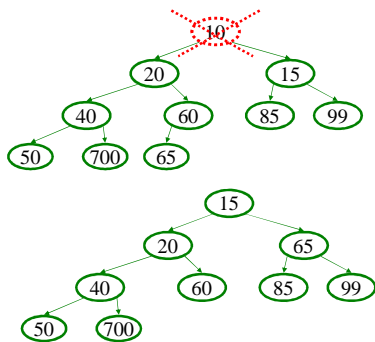
runtime:

(Java code in book)

10/12/2012

14

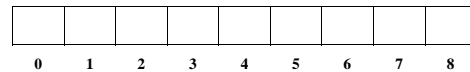
DeleteMin: percolate down



10/12/2012

15

Insert: 16, 32, 4, 69, 105, 43, 2



10/12/2012

16

Other Priority Queue Operations

- **decreaseKey**
 - given a pointer to an object in the queue, reduce its priority value
 - Solution: change priority and _____
- **increaseKey**
 - given a pointer to an object in the queue, increase its priority value
 - Solution: change priority and _____

Why do we need a pointer? Why not simply data value?

10/12/2012

17

Other Heap Operations

- decreaseKey(objPtr, amount):** raise the priority of a object, percolate up
- increaseKey(objPtr, amount):** lower the priority of a object, percolate down
- remove(objPtr):** remove a object, move to top, then delete.
 - 1) decreaseKey(objPtr, ∞)
 - 2) deleteMin()

Worst case Running time for all of these:

FindMax?

ExpandHeap – when heap fills, copy into new space.

10/12/2012

18

