## Syntactic Analysis

Syntactic analysis, or parsing, is the second phase of compilation: The token file is converted to an abstract syntax tree.


## Syntactic Analysis / Parsing

- Goal: Convert token stream to abstract syntax tree
- Abstract syntax tree (AST):
- Captures the structural features of the program
- Primary data structure for remainder of analysis
- Three Part Plan
- Study how context-free grammars specify syntax
- Study algorithms for parsing / building ASTs
- Study the miniJava Implementation


## Context-free Grammars

- Compromise between
- REs, which can't nest or specify recursive structure
- General grammars, too powerful, undecidable
- Context-free grammars are a sweet spot
- Powerful enough to describe nesting, recursion
- Easy to parse; but also allow restrictions for speed
- Not perfect
- Cannot capture semantics, as in, "variable must be declared," requiring later semantic pass
- Can be ambiguous
- EBNF, Extended Backus Naur Form, is popular notation


## CFG Terminology

- Terminals -- alphabet of language defined by CFG
- Nonterminals -- symbols defined in terms of terminals and nonterminals
- Productions -- rules for how a nonterminal (lhs) is defined in terms of a (possibly empty) sequence of terminals and nonterminals
- Recursion is allowed!
- Multiple productions allowed for a nonterminal, alternatives
- Start symbol -- root of the defining language

Program : : = Stmt
Stmt : : = if ( Expr ) then Stmt else Stmt
Stmt : : = while ( Expr ) do Stmt

## EBNF Syntax of initial MiniJava

```
Program ::= MainClassDecl { ClassDecl }
MainClassDecl ::= class ID {
            public static void main
            ( String [ ] ID ) { { Stmt } }
ClassDecl ::= class ID [ extends ID ] {
                            { ClassVarDecl } { MethodDecl } }
ClassVarDecl ::= Type ID ;
MethodDecl ::= public Type ID
            ( [ Formal { , Formal } ] )
            { { Stmt } return Expr ; }
Formal ::= Type ID
Type ::= int |boolean | ID
```


## Initial miniJava [continued]

```
Stmt ::= Type ID ;
    | { {Stmt} }
    |f ( Expr ) Stmt else Stmt
    | while ( Expr ) Stmt
    System.out.println (Expr ) ;
    | ID = Expr ;
Expr ::= Expr Op Expr
    | Expr
    | Expr . ID( [ Expr { , Expr } ] )
    | ID | this
    | Integer | true | false
    | ( Expr )
Op ::= + | - * * /
    |< | <= | >= | > | == | != | &&
```

```
    RE Specification of initial MiniJava Lex
Program ::= (Token | Whitespace)*
Token ::= ID | Integer | ReservedWord | Operator |
        Delimiter
ID ::= Letter (Letter | Digit)*
Letter ::= a | ... | z | A | ... | z
Digit ::= 0 | ... | 9
Integer ::= Digit+
ReservedWord::= class | public | static| extends |
void | int | boolean | if | else |
    while|return|true|false| this | new | String
    | main | System.out.println
Operator : := + | - | * | | < | <= | >= | > | == |
    != | && | !
Delimiter : := ; | . | , | = | ( | ) | { | } | [ |
```


## Derivations and Parse Trees

Derivation: a sequence of expansion steps, beginning with a start symbol and leading to a sequence of terminals
Parsing: inverse of derivation

- Given a sequence of terminals (alkla tokens) want to recover the nonterminals representing structure

Can represent derivation as a parse tree, that is, the concrete syntax tree

```
            Example Grammar
E ::= E Op E | - E| ( E ) | id
op ::= + | - | * | /
```


## Ambiguity

- Some grammars are ambiguous
- Multiple distinct parse trees for the same terminal string
- Structure of the parse tree captures much of the meaning of the program
- ambiguity implies multiple possible meanings for the same program

```
    Famous Ambiguity: "Dangling Else"
    Stmt ::= ... |
        if ( Expr ) Stmt |
        if ( Expr ) Stmt else Stmt
```

    if \(\left(e_{1}\right)\) if \(\left(e_{2}\right) s_{1}\) else \(s_{2}\) : if \(\left(e_{1}\right)\) if \(\left(e_{2}\right) s_{1}\) else \(s_{2}\)
    
## Resolving Ambiguity

## - Option 1: add a meta-rule

- For example "else associates with closest previous if"
- works, keeps original grammar intact
- ad hoc and informal


## Resolving Ambiguity [continued]

Option 2: rewrite the grammar to resolve ambiguity explicitly

```
Stmt ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
    if ( Expr ) MatchedStmt else MatchedStmt
UnmatchedStmt ::= if ( Expr ) Stmt |
    if ( Expr ) MatchedStmt else UnmatchedStmt
```

- formal, no additional rules beyond syntax
- sometimes obscures original grammar

```
    Resolving Ambiguity Example
Stmt ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
    if ( Expr ) MatchedStmt else MatchedStmt
UnmatchedStmt ::= if ( Expr ) Stmt |
    if ( Expr ) MatchedStmt else UnmatchedStmt
if (e (e) if (e (e) s
```


## Resolving Ambiguity [continued]

Option 3: redesign the language to remove the ambiguity

```
Stmt : := ... |
    if Expr then Stmt end |
    if Expr then Stmt else Stmt end
- formal, clear, elegant
- allows sequence of Stmts in then and else
    branches, no \{, \} needed
- extra end required for every if
```

$$
\begin{aligned}
& \text { Another Famous Example } \\
& \mathrm{E}::=\mathrm{E} \text { Op } \mathrm{E}|-\mathrm{E}| \text { (E) id } \\
& \text { Op }::=+|-|*| / \\
& \mathrm{a}+\mathrm{b} \text { * } \mathrm{b} \quad: \mathrm{a}+\mathrm{b} \text { * } \mathrm{c}
\end{aligned}
$$

## Resolving Ambiguity (Option 1)

Add some meta-rules, e.g. precedence and associativity rules

| Example:$\begin{aligned} & \text { E: : }=\mathrm{E} \text { Op E \| }-\mathrm{E} \mid \mathrm{E}++ \\ &\|(\mathrm{E})\| \text { id } \end{aligned}$ | Operator | Preced | Assoc |
| :---: | :---: | :---: | :---: |
|  | Postfix ++ | Highest | Left |
|  | Prefix - |  | Right |
| $\mathrm{op}::=\begin{gathered} +\|-\|*\|\| \mid \% \\ \|* *\|==\|<\| \& \& \end{gathered}$ | ** (Exp) |  | Right |
|  | *, /, \% |  | Left |
|  | +, - |  | Left |
|  | ==, < |  | None |
|  | \&\& |  | Left |
|  | II | Lowest | Left |

## Removing Ambiguity (Option 2)

Option2: Modify the grammar to explicitly resolve the ambiguity
Strategy:

- create a nonterminal for each precedence level
- expr is lowest precedence nonterminal, each nonterminal can be rewritten with higher precedence operator, highest precedence operator includes atomic exprs
- at each precedence level, use:
- left recursion for left-associative operators
- right recursion for right-associative operators
- no recursion for non-associative operators


## Redone Example

```
E ::= E0
```

E0 : : = E0 || E1 | E1

E1 : := E1 \&\& E2 E2
E2 : := E3 (== | <) E3 | E3
E3 : : = E3 (+ | -) E4 | E4
E4 : := E4 (* | / \% ) E5 | E5
E5 : : = E6 ** E5 | E6
E6 : : = - E6| E7
E7 : : = E7 ++ E8
E8 : := id ( E )

```
left associative
left associative
non associative
left associative
left associative
right associative
right associative
left associative
```


## Designing A Grammar

## Concerns:

- Accuracy
- Unambiguity
- Formality
- Readability, Clarity
- Ability to be parsed by a particular algorithm:
- Top down parser ==> LL(k) Grammar
- Bottom up Parser ==> LR(k) Grammar
- Ability to be implemented using particular approach
- By hand
- By automatic tools


## Parsing Algorithms

Given a grammar, want to parse the input programs

- Check legality
- Produce AST representing the structure
- Be efficient
- Kinds of parsing algorithms
- Top down
- Bottom up


## Top Down Parsing

Build parse tree from the top (start symbol) down to leaves (terminals)
Basic issue:

- when "expanding" a nonterminal with some r.h.s., how to pick which r.h.s.?
E.g.

Stmts $::=$ Call $\mid$ Assign | If | While
Call $::=\operatorname{Id}($ Expr $\{, E x p r\})$
Assign $::=$ Id $=$ Expr ;
If $::=$ if Test then Stmts end
| if Test then Stmts else Stmts end
While ::= while Test do Stmts end
Solution: look at input tokens to help decide

## Predictive Parser

Predictive parser: top-down parser that can select rhs by looking at most $k$ input tokens (the lookahead)

## Efficient:

- no backtracking needed
- linear time to parse

Implementation of predictive parsers:

- recursive-descent parser
- each nonterminal parsed by a procedure
- call other procedures to parse sub-nonterminals, recursively
- typically written by hand
- table-driven parser
- PDA:like table-driven FSA, plus stack to do recursive FSA calls
- typically generated by a tool from a grammar specification


## LL(k) Grammars

Can construct predictive parser automatically / easily if grammar is $\operatorname{LL}(k)$

- Left-to-right scan of input, Leftmost derivation
- $\mathbf{k}$ tokens of look ahead needed, $\geq 1$

Some restrictions:

- no ambiguity (true for any parsing algorithm)
- no common prefixes of length $\geq \mathrm{k}$ :

If : := if Test then Stmts end |
if Test then Stmts else Stmts end

- no left recursion:

E : : = E Op E | ...

- a few others

Restrictions guarantee that, given k input tokens, can always select correct rhs to expand nonterminal. Easy to do by hand in recursive-descent parser

## Eliminating common prefixes

Can left factor common prefixes to eliminate them

- create new nonterminal for different suffixes
- delay choice till after common prefix
- Before:

```
If ::= if Test then Stmts end |
    if Test then Stmts else Stmts end
```

- After:

If : : if Test then Stmts IfCont
IfCont : := end | else Stmts end

## Eliminating Left Recursion

- Can Rewrite the grammar to eliminate left recursion
- Before

```
E ::= E + T |
T ::= T * F | F
F ::= id | ...
```

- After
$\mathrm{E} \quad::=\mathrm{T}$ ECon
ECon : : = + T ECon $\mid \varepsilon$
T : : = F TCon
TCon : : = * F TCon $\mid \varepsilon$
F : : = id | ...


## Bottom Up Parsing

Construct parse tree for input from leaves up

- reducing a string of tokens to single start symbol (inverse of deriving a string of tokens from start symbol)
"Shift-reduce" strategy:
- read ("shift") tokens until seen r.h.s. of "correct" production xyzabcdef $A::=b c . D$
- reduce handle to l.h.s. nonterminal, then continue
- done when all input read and reduced to start nonterminal


## LR(k)

- LR(k) parsing
- Left-to-right scan of input, Rightmost derivation
- $\boldsymbol{k}$ tokens of look ahead
- Strictly more general than $\operatorname{LL}(k)$
- Gets to look at whole rhs of production before deciding what to do, not just first $k$ tokens of rhs
- can handle left recursion and common prefixes fine
- Still as efficient as any top-down or bottom-up parsing method
- Complex to implement
- need automatic tools to construct parser from grammar


## LR Parsing Tables

Construct parsing tables implementing a FSA with a stack

- rows: states of parser
- columns: token(s) of lookahead
- entries: action of parser
- shift, goto state x
- reduce production "x : := RHS"
- accept
- error

Algorithm to construct FSA similar to algorithm to build DFA from NFA

- each state represents set of possible places in parsing
$L R(k)$ algorithm builds huge tables


## LALR-Look Ahead LR

$\operatorname{LALR}(k)$ algorithm has fewer states ==> smaller tables

- less general than $\mathrm{LR}(k)$, but still good in practice
- size of tables acceptable in practice
- $k==1$ in practice
- most parser generators, including yacc and jflex, are LALR(1)


## Global Plan for LR(0) Parsing

- Goal: Set up the tables for parsing an LR(0) grammar
- Add S' --> S\$ to the grammar, i.e. solve the problem for a new grammar with terminator
- Compute parser states by starting with state 1 containing added production, S' --> .S\$
- Form closures of states and shifting to complete diagram
- Convert diagram to transition table for PDA
- Step through parse using table and stack


## LR(0) Parser Generation

Example grammar:
$S^{\prime}::=$ S $\$ \quad /$ always add this production
S : := beep | \{ L \}
$\mathrm{L}::=\mathrm{S} \mid \mathrm{L}$; S

- Key idea: simulate where input might be in grammar as it reads tokens
- "Where input might be in grammar" captured by set of items, which forms a state in the parser's FSA
- LR(0) item: lhs $::=$ rhs production, with dot in rhs somewhere marking what's been read (shifted) so far
- LR(k) item: also add $k$ tokens of lookahead to each item
- Initial item: $\mathrm{S}^{\prime}$ : := . S \$


## Closure

Initial state is closure of initial item

- closure: if dot before non-terminal, add all productions for that non-terminal with dot at the start
- "epsilon transitions"

Initial state (1):
$S^{\prime}:=$. $S$
S ::= . beep
S : := . \{ L \}

## State Transitions

Given set of items, compute new state(s) for each symbol (terminal and non-terminal) after dot

- state transitions correspond to shift actions

New item derived from old item by shifting dot over symbol

- do closure to compute new state Initial state (1):

S' ::= . S \$ S ::= . beep S ::= .\{ L \}

- State (2) reached on transition that shifts $S$ :

S' : := S . \$

- State (3) reached on transition that shifts beep:

```
S ::= beep .
S : := \{ . L \}
```

- State (4) reached on transition that shifts \{:

L : : = . S
L ::= . L ; S
S ::= . beep
S ::= . \{ L \}

## Accepting Transitions

If state has $s^{\prime}::=\ldots$. $\$$ item, then add transition labeled\$ to the accept action

## Example:

S' : := S . \$
has transition labeled \$ to accept action

## Reducing States

If state has $1 \mathrm{hs}::=$ rhs . item, then it has a reduce lhs : : = rhs action

Example:
S ::= beep .
has reduce $S$ : := beep action

No label; this state always reduces this production

- what if other items in this state shift, or accept?
- what if other items in this state reduce differently?


## Rest of the States, Part 1

State (4): if shift beep, goto State (3)
State (4): if shift $\mathfrak{l}, \quad$ goto State (4)
State (4): if shift S, goto State (5)
State (4): if shift L, goto State (6)
State (5):
L : : = S .
State (6):
S : : = \{ L . \}
L : : = L . ; S
State (6): if shift \},
goto State (7)
State (6): if shift ;
goto State (8)

## Rest of the States (Part 2)

State (7):
$S::=\{\mathrm{L}\}$.
State (8):
L : := L ; . S
S ::= . beep
S : : = . \{ L \}
State (8): if shift beep, goto State (3)
State (8): if shift \{, goto State (4)
State (8): if shift S, goto State (9)
State (9):
L : : = L ; S .
(whew)

## LR(0) State Diagram

$S^{\prime}::=$ S \$
S ::= beep | \{ L \}
$\mathrm{L}::=\mathrm{S} \mid \mathrm{L}$; S


## Building Table of States \& Transitions

Create a row for each state
Create a column for each terminal, non-terminal, and \$
For every "state (i): if shift $X$ goto state ( $j$ )" transition:

- if $X$ is a terminal, put "shift, goto $j$ " action in row $i$, column $X$
- if $X$ is a non-terminal, put "goto $j$ " action in row $i$, column $X$

For every "state ( $i$ ): if \$ accept" transition:

- put "accept" action in row $i$, column \$

For every "state ( $i$ ): Ihs $::=$ rhs." action:

- put "reduce lhs : := rhs" action in all columns of row $i$


## Table of This Grammar

| State | \{ | \} | beep | ; | S | L | \$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | s,g4 |  | s,g3 |  | g2 |  |  |
| 2 |  |  |  |  |  |  | a! |
| 3 | reduce S : := beep |  |  |  |  |  |  |
| 4 | s,g4 |  | s,g3 |  | g5 | g6 |  |
| 5 | reduce L : : = S |  |  |  |  |  |  |
| 6 |  | s,g7 |  | s,g8 |  |  |  |
| 7 | reduce S : := \{ L \} |  |  |  |  |  |  |
| 8 | s,g4 |  | s,g3 |  | g9 |  |  |
| 9 | reduce L : := L ; S |  |  |  |  |  |  |

## Example

```
    S'::= S $
    S ::= beep | { L }
    L ::= S L L ; S
```

1
1 \{ 4
\{ 4 beep 3
1 \{ 4 S 5
1\}4L6

1) 4 L6. 8
1 \{ 4 L 6 ; 8 \{ 4
1 \{ $4 L 6 ; 8$ \{ 4 beep 3
1\}4L6;8\}4S5
144L6:844L6
$1\{4 \mathrm{~L} 6 ; 8\{4 \mathrm{~L} 6\} 7$
1)4L6;8S9
$1\{4 L 6 ; 8$
$1\{4 L 6$
$1\{4 L 6\} 7$
$1\{4 L 6\} 7$
1 S 2
accept

| St | I | \} | beep | ; | S | L | \$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | s,g4 |  | s,g3 |  | g2 |  |  |
| 2 |  |  |  |  |  |  | a! |
| 3 | reduce S : := beep |  |  |  |  |  |  |
| 4 | s,g4 |  | s,g3 |  | g5 | g6 |  |
| 5 | reduce L : : = S |  |  |  |  |  |  |
| 6 |  | s,g7 |  | s,98 |  |  |  |
| 7 | reduce S : := \{ L \} |  |  |  |  |  |  |
| 8 | s,g4 |  | s,g3 |  | g9 |  |  |
| 9 | reduce L : : = L ; S |  |  |  |  |  |  |

[^0]
## Problems In Shift-Reduce Parsing

Can write grammars that cannot be handled with shift-reduce parsing

Shift/reduce conflict:

- state has both shift action(s) and reduce actions

Reduce/reduce conflict:

- state has more than one reduce action


## Shift/Reduce Conflicts

LR(0) example:
$\mathrm{E}::=\mathrm{E}+\mathrm{T} \mid \mathrm{T}$
State: E : : = E . + T
E : : = T.

- Can shift +
- Can reduce E : : = T

LR(k) example:
$S$ : := if $E$ then $S$ |
if E then $S$ else $S$ | ...
State: $S$ : := if $E$ then $S$.
S : : = if E then S . else $S$

- Can shift else
- Can reduce $S$ : := if $E$ then $S$


## Avoiding Shift-Reduce Conflicts

Can rewrite grammar to remove conflict

- E.g. Matched Stmt vs. Unmatched Stmt

Can resolve in favor of shift action

- try to find longest r.h.s. before reducing
works well in practice
yacc, jflex, et al. do this


## Reduce/Reduce Conflicts

## Example:

```
Stmt : : = Type id ; | LHS = Expr ; | ...
```

    LHS : := id | LHS [ Expr ] | ...
    Type :: = id | Type [] | ...
    State: Type ::= id .
LHS ::= id.
Can reduce тype $^{\text {: }:=~ i d ~}$
Can reduce ins ::= id

## Avoid Reduce/Reduce Conflicts

Can rewrite grammar to remove conflict

- can be hard
- e.g. C/C++ declaration vs. expression problem
- e.g. MiniJava array declaration vs. array store problem

Can resolve in favor of one of the reduce actions

- but which?
- yacc, jflex, et al. Pick reduce action for production listed textually first in specification


## Abstract Syntax Trees

The parser's output is an abstract syntax tree (AST) representing the grammatical structure of the parsed input

- ASTs represent only semantically meaningful aspects of input program, unlike concrete syntax trees which record the complete textual form of the input
- There's no need to record keywords or punctuation like (), ; , else
- The rest of compiler only cares about the abstract structure


## AST Node Classes

Each node in an AST is an instance of an AST class

- IfStmt, AssignStmt, AddExpr, VarDecl, etc.

Each AST class declares its own instance variables holding its AST subtrees

- IfStmt has testExpr, thenStmt, and elseStmt
- AssignStmt has lhsVar and rhsExpr
- AddExpr has arg1Expr and arg2Expr
- VarDecl has typeExpr and varName


## AST Class Hierarchy

AST classes are organized into an inheritance hierarchy based on commonalities of meaning and structure

- Each "abstract non-terminal" that has multiple alternative concrete forms will have an abstract class that's the superclass of the various alternative forms
- Stmt is abstract superclass of IfStmt, AssignStmt, etc.
- Expr is abstract superclass of AddExpr, VarExpr, etc.
- Type is abstract superclass of Int Type, ClassType, etc.


## AST Extensions For Project

New variable declarations:

- StaticVarDecl

New types:

- DoubleType
- ArrayType

New/changed statements:

- IfStmt can omit else branch
- ForStmt
- BreakStmt
- ArrayAssignStmt

New expressions:

- DoubleLiteralExpr
- OrExpr
- ArrayLookupExpr
- ArrayLengthExpr
- ArrayNewExpr


## Automatic Parser Generation in MiniJava

We use the CUP tool to automatically create a parser from a specification file, Parser/minijava. cup
The MiniJava Makefile automatically rebuilds the parser whenever its specification file changes

A CUP file has several sections:

- introductory declarations included with the generated parser
- declarations of the terminals and nonterminals with their types
- The AST node or other value returned when finished parsing that nonterminal or terminal
- precedence declarations
- productions + actions


## Terminal and Nonterminal Declarations

## Terminal declarations we saw before:

```
/* reserved words: */
```

terminal CLASS, PUBLIC, STATIC, EXTENDS;
/* tokens with values: */
terminal String IDENTIFIER;
terminal Integer INT_LITERAL;

Nonterminals are similar:
nonterminal Program Program;
nonterminal MainClassDecl MainClassDecl;
nonterminal List/*<...>*/ ClassDecls;
nonterminal RegularClassDecl ClassDecl;
nonterminal List/*<Stmt>*/ Stmts;
nonterminal Stmt Stmt;
nonterminal List/*<Expr>*/ Exprs;
nonterminal List/*<Expr>*/ MoreExprs;
nonterminal Expr Expr;
nonterminal String Identifier;

## Precedence Declarations

Can specify precedence and associativity of operators

- equal precedence in a single declaration
- lowest precedence textually first
- specify left, right, or nonassoc with each declaration


## Examples:

precedence left AND_AND;
precedence nonassoc EQUALS_EQUALS, EXCLAIM_EQUALS;
precedence left LESSTHAN, LESSEQUAL,
GREATEREQUAL, GREATERTHAN;
precedence left PLUS, MINUS;
precedence left STAR, SLASH;
precedence left EXCLAIM;
precedence left PERIOD;

## Productions

All of the form:

```
LHS ::= RHS1 {: Java code 1 :}
    | RHS2 {: Java code 2 :}
    | ...
    RHSn {: Java code n :};
```

Can label symbols in RHS with : var suffix to refer to its result value in Java code

- varleft is set to line in input where var symbol was
E.g.: Expr ::= Expr:arg1 PLUS Expr:arg2
\{: RESULT = new AddExpr( arg1,arg2,arg1left);:\}
| INT_LITERAL:value\{: RESULT = new IntLiteralExpr( value.intValue(), valueleft);:\}
| Expr:rcvr PERIOD Identifier:message OPEN_PAREN Exprs:args CLOSE_PAREN
\{: RESULT = new MethodCallExpr(
rcvr,message, args,rcvrleft);:\}
| ... ;


## Error Handling

How to handle syntax error?
Option 1: quit compilation

+ easy
- inconvenient for programmer

Option 2: error recovery

+ try to catch as many errors as possible on one compile
- difficult to avoid streams of spurious errors

Option 3: error correction

+ fix syntax errors as part of compilation
- hard!!


## Panic Mode Error Recovery

When finding a syntax error, skip tokens until reaching a "landmark"

- landmarks in MiniJava: ;, ), \}
- once a landmark is found, hope to have gotten back on track

In top-down parser, maintain set of landmark tokens as recursive descent proceeds

- landmarks selected from terminals later in production
- as parsing proceeds, set of landmarks will change, depending on the parsing context
In bottom-up parser, can add special error nonterminals, followed by landmarks
- if syntax error, then will skip tokens till seeing landmark, then reduce and continue normally
- E.g. Stmt : : = ... | error ; | \{ error \}

Expr ::=... | ( error )


[^0]:    \{ beep ; \{ beep \} \}

