# CSE 401 – Compilers

# Parsing & Context-Free Grammars Hal Perkins Winter 2010



#### Agenda for Today

- Parsing overview
- Context free grammars
- Ambiguous grammars
- Reading: Cooper & Torczon 3.1-3.2
  - Dragon book is also particularly strong on grammars and languages



### Syntactic Analysis / Parsing

- Goal: Convert token stream to abstract syntax tree
- Abstract syntax tree (AST):
  - Captures the structural features of the program
  - Primary data structure for remainder of compilation
    - At least remainder of front-end in production compilers
- Three Part Plan
  - Study how context-free grammars specify syntax
  - Study algorithms for parsing / building ASTs
  - Study the miniJava Implementation (in section)



#### **Context-free Grammars**

- The syntax of most programming languages can be specified by a context-free grammar (CGF)
- Compromise between
  - REs, can't nest or specify recursive structure
  - General grammars, too powerful, undecidable
- Context-free grammars are a sweet spot
  - Powerful enough to describe nesting, recursion
  - Easy to parse; but also allow restrictions for speed
- Not perfect
  - Cannot capture semantics, as in, "variable must be declared," requiring later semantic pass
  - Can be ambiguous



#### **Derivations and Parse Trees**

- Derivation: a sequence of expansion steps, beginning with a start symbol and leading to a sequence of terminals
- Parsing: inverse of derivation
  - Given a sequence of terminals (a\k\a tokens) want to recover the nonterminals representing structure
- Can represent derivation as a parse tree, that is, the concrete syntax tree



program ::= statement | program statement
statement ::= assignStmt | ifStmt
assignStmt ::= id = expr;
ifStmt ::= if ( expr ) stmt
expr ::= id | int | expr + expr
Id ::= a | b | c | i | j | k | n | x | y | z
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

program

```
w \rightarrow a = 1; if (a + 1) b = 2;
```

# Parsing

- Parsing: Given a grammar G and a sentence w in L(G), traverse the derivation (parse tree) for w in some standard order and do something useful at each node
  - The tree might not be produced explicitly, but the control flow of the parser corresponds to a traversal



#### "Standard Order"

- For practical reasons we want the parser to be deterministic (no backtracking), and we want to examine the source program from left to right.
  - (i.e., parse the program in linear time in the order it appears in the source file)



#### Common Orderings

- Top-down
  - Start with the root
  - Traverse the parse tree depth-first, left-to-right (leftmost derivation)
  - LL(k), recursive-descent
- Bottom-up
  - Start at leaves and build up to the root
    - Effectively a rightmost derivation in reverse(!)
  - LR(k) and subsets (LALR(k), SLR(k), etc.)



### "Something Useful"

- At each point (node) in the traversal, perform some semantic action
  - Construct nodes of full parse tree (rare)
  - Construct abstract syntax tree (common)
  - Construct linear, lower-level representation (more common in later parts of a modern compiler)
  - Generate target code on the fly (used in 1-pass compiler; not common in production compilers)
    - Can't generate great code in one pass, but useful if you need a quick 'n dirty working compiler



#### **Context-Free Grammars**

- Formally, a grammar G is a tuple  $\langle N, \Sigma, P, S \rangle$  where
  - N a finite set of non-terminal symbols
  - Σ a finite set of terminal symbols
  - P a finite set of productions
    - A subset of  $N \times (N \cup \Sigma)^*$
  - S the start symbol, a distinguished element of N
    - If not specified otherwise, this is usually assumed to be the non-terminal on the left of the first production



#### Standard Notations

- a, b, c elements of Σ
- w, x, y, z elements of  $\Sigma^*$
- A, B, C elements of N
- X, Y, Z elements of  $N \cup \Sigma$
- $\alpha$ ,  $\beta$ ,  $\gamma$  elements of  $(N \cup \Sigma)^*$
- $A \rightarrow \alpha$  or  $A ::= \alpha$  if  $\langle A, \alpha \rangle$  in P



### Derivation Relations (1)

- $\alpha A \gamma => \alpha \beta \gamma$  iff  $A := \beta$  in P
  - derives
- A =>\* w if there is a chain of productions starting with A that generates w
  - transitive closure



### Derivation Relations (2)

- $\mathsf{w} \mathsf{A} \gamma = \mathsf{I}_{\mathsf{Im}} \mathsf{w} \beta \gamma$  iff  $\mathsf{A} ::= \beta$  in  $\mathsf{P}$ 
  - derives leftmost
- $\alpha A w = >_{rm} \alpha \beta w \text{ iff } A ::= \beta \text{ in } P$ 
  - derives rightmost
- We will only be interested in leftmost and rightmost derivations – not random orderings

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#### Languages

- For A in N,  $L(A) = \{ w \mid A = > * w \}$
- If S is the start symbol of grammar G, define L(G) = L(S)
  - Nonterminal on left of first rule is taken to be the start symbol if one is not specified explicitly



#### Reduced Grammars

• Grammar G is reduced iff for every production  $A ::= \alpha$  in G there is a derivation

$$S = > * x A z = > x \alpha z = > * xyz$$

- i.e., no production is useless
- Convention: we will use only reduced grammars



#### **Ambiguity**

- Grammar G is unambiguous iff every w in L(G) has a unique leftmost (or rightmost) derivation
  - Fact: unique leftmost or unique rightmost implies the other
- A grammar without this property is ambiguous
  - Note that other grammars that generate the same language may be unambiguous
- We want unambiguous grammars for parsing



# Example: Ambiguous Grammar for Arithmetic Expressions

```
expr ::= expr + expr | expr - expr
| expr * expr | expr | expr | expr | int
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

- Exercise: show that this is ambiguous
  - How? Show two different leftmost or rightmost derivations for the same string
  - Equivalently: show two different parse trees for the same string



### Example (cont)

 Give a leftmost derivation of 2+3\*4 and show the parse tree



### Example (cont)

 Give a different leftmost derivation of 2+3\*4 and show the parse tree



#### Another example

• Give two different derivations of 5+6+7



### What's going on here?

- The grammar has no notion of precedence or associatively
- Solution
  - Create a non-terminal for each level of precedence
  - Isolate the corresponding part of the grammar
  - Force the parser to recognize higher precedence subexpressions first
  - Use left- or right-recursion for left- or rightassociative operators (non-associative operators are not recursive)

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#### Classic Expression Grammar

```
expr::= expr + term | expr - term | term
term ::= term * factor | term | factor | factor
factor ::= int | ( expr )
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7
```

expr::= expr + term | expr - term | term

term ::= term \* factor | term | factor | factor

factor ::= int | ( expr )

*int* ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7



Check: Derive 2 + 3 \* 4

```
expr ::= expr + term | expr - term | term
term ::= term * factor | term | factor | factor
factor ::= int | ( expr )
```

*int* ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7



#### Check: Derive 5 + 6 + 7

 Note interaction between left- vs right-recursive rules and resulting associativity

expr ::= expr + term | expr - term | term

term ::= term \* factor | term | factor | factor

factor ::= int | ( expr )

*int* ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7



## Check: Derive 5 + (6 + 7)



#### **Another Classic Example**

Grammar for conditional statements

```
ifStmt ::= if ( cond ) stmt
| if ( cond ) stmt else stmt
```

- Exercise: show that this is ambiguous
  - How?



#### One Derivation

if ( cond ) if ( cond ) stmt else stmt

```
ifStmt ::= if ( cond ) stmt
| if ( cond ) stmt else stmt
```



#### **Another Derivation**

if ( cond ) if ( cond ) stmt else stmt



### Solving "if" Ambiguity

- Fix the grammar to separate if statements with else clause and if statements with no else
  - Done in Java reference grammar
  - Adds lots of non-terminals
- Change the language
  - But it'd better be ok to do this
- Use some ad-hoc rule in parser
  - "else matches closest unpaired if"

# Resolving Ambiguity with Grammar (1)

```
Stmt ::= MatchedStmt | UnmatchedStmt

MatchedStmt ::= ... |

if ( Expr ) MatchedStmt else MatchedStmt

UnmatchedStmt ::= if ( Expr ) Stmt |

if ( Expr ) MatchedStmt else UnmatchedStmt
```

- formal, no additional rules beyond syntax
- sometimes obscures original grammar



```
Stmt ::= MatchedStmt | UnmatchedStmt

MatchedStmt ::= ... |

if ( Expr ) MatchedStmt else MatchedStmt

UnmatchedStmt ::= if ( Expr ) Stmt |

if ( Expr ) MatchedStmt else UnmatchedStmt
```

if ( cond ) if ( cond ) stmt else stmt

# Resolving Ambiguity with Grammar (2)

If you can (re-)design the language, avoid the problem entirely

```
Stmt ::= ... |

if Expr then Stmt end |

if Expr then Stmt else Stmt end
```

- formal, clear, elegant
- allows sequence of Stmts in then and else branches, no { , } needed
- extra end required for every if
  - (But maybe this is a good idea anyway?)



#### Parser Tools and Operators

- Most parser tools can cope with ambiguous grammars
  - Makes life simpler if used with discipline
- Typically one can specify operator precedence & associativity
  - Allows simpler, ambiguous grammar with fewer nonterminals as basis for generated parser, without creating problems



# Parser Tools and Ambiguous Grammars

- Possible rules for resolving other problems
  - Earlier productions in the grammar preferred to later ones
  - Longest match used if there is a choice
- Parser tools normally allow for this
  - But be sure that what the tool does is really what you want



#### **Coming Attractions**

- Next topic: LR parsing
  - Continue reading ch. 3