

# Database Systems

## CSE 414

Lectures 9: Relational Algebra  
(part 2) and Query Evaluation  
(Ch. 5.2 & 16.3 (skim 16.3.2))

# Announcements

- Should have used SQL / Azure now
  - let us know if you had any setup problems
- WQ3 is due on Sunday
- HW3 is due one week from Tuesday
- HW1 grades *should* be posted tonight

# Join Summary

- **Theta-join:**  $R \bowtie_{\theta} S = \sigma_{\theta}(R \times S)$ 
  - Join of R and S with a join condition  $\theta$
  - Cross-product followed by selection  $\theta$
- **Equijoin:**  $R \bowtie_{\theta} S = \sigma_{\theta}(R \times S)$ 
  - Join condition  $\theta$  consists only of equalities
- **Natural join:**  $R \bowtie S = \pi_A(\sigma_{\theta}(R \times S))$ 
  - Equijoin
  - Equality on **all** fields with same name in R and in S
  - Projection  $\pi_A$  drops all redundant attributes

# So Which Join Is It ?

When we write  $R \bowtie S$  we usually mean an equijoin, but we often omit the equality predicate when it is clear from the context

# More Joins

- **Outer join**
  - Include tuples with no matches in the output
  - Use NULL values for missing attributes
  - Does not eliminate duplicate columns
- Variants
  - Left outer join
  - Right outer join
  - Full outer join

# Outer Join Example

AnonPatient P

age	zip	disease
54	98125	heart
20	98120	flu
33	98120	lung

AnonJob J

job	age	zip
lawyer	54	98125
cashier	20	98120

$P \bowtie J$

P.age	P.zip	disease	job	J.age	J.zip
54	98125	heart	lawyer	54	98125
20	98120	flu	cashier	20	98120
33	98120	lung	null	null	null

# More Examples

Supplier(sno, sname, scity, sstate)

Part(pno, pname, psize, pcolor)

Supply(sno, pno, qty, price)

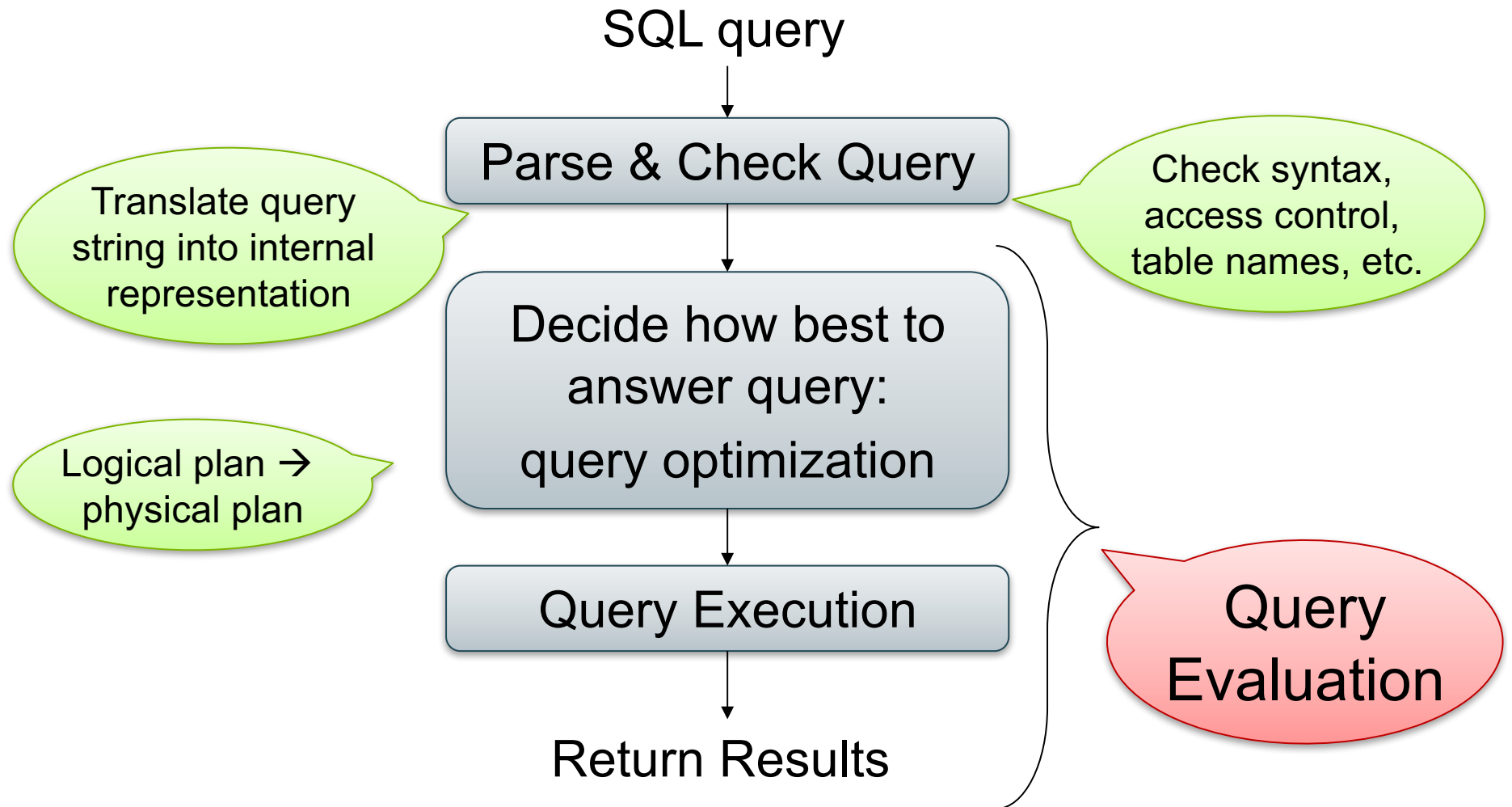
Name of supplier of parts with size greater than 10

$\pi_{\text{sname}}(\text{Supplier} \bowtie \text{Supply} \bowtie (\sigma_{\text{psize} > 10}(\text{Part})))$

Name of supplier of red parts or parts with size greater than 10

$\pi_{\text{sname}}(\text{Supplier} \bowtie \text{Supply} \bowtie (\sigma_{\text{psize} > 10}(\text{Part}) \cup \sigma_{\text{pcolor} = \text{'red'}}(\text{Part})))$

# Query Evaluation Steps

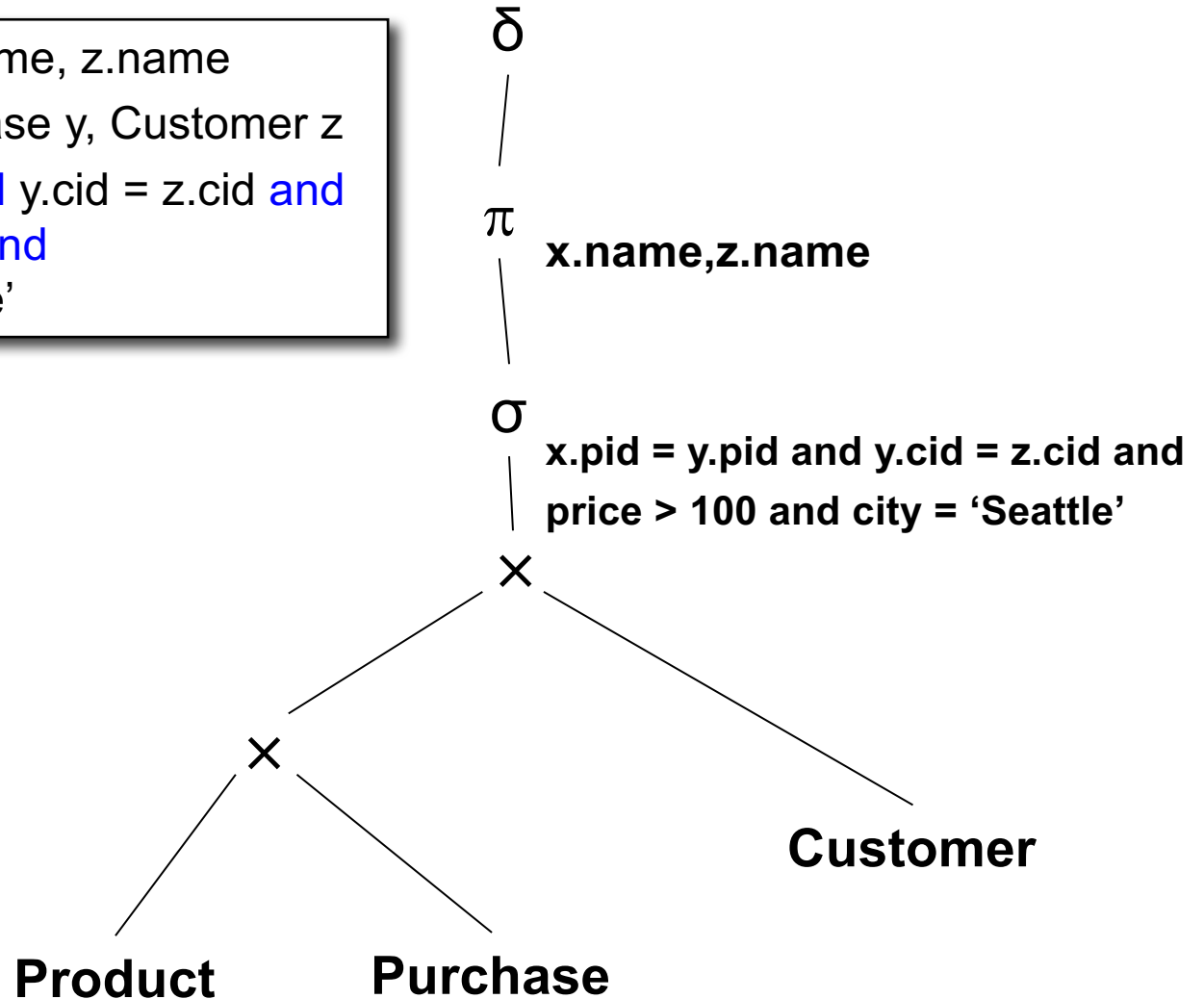




Product(pid, name, price)  
Purchase(pid, cid, store)  
Customer(cid, name, city)

# From SQL to RA

```
SELECT DISTINCT x.name, z.name  
FROM Product x, Purchase y, Customer z  
WHERE x.pid = y.pid and y.cid = z.cid and  
      x.price > 100 and  
      z.city = 'Seattle'
```

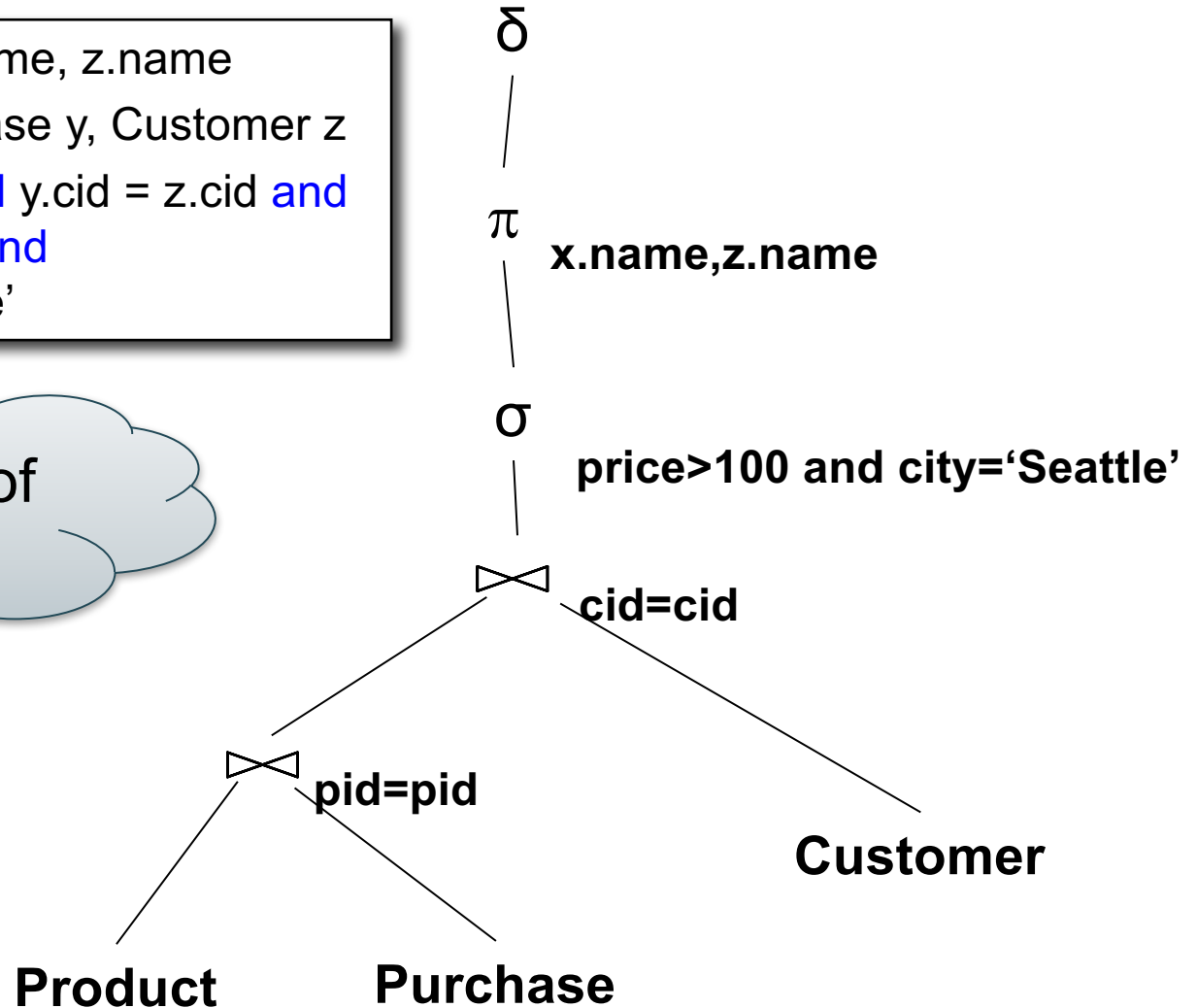


Product(pid, name, price)  
Purchase(pid, cid, store)  
Customer(cid, name, city)

# From SQL to RA

```
SELECT DISTINCT x.name, z.name  
FROM Product x, Purchase y, Customer z  
WHERE x.pid = y.pid and y.cid = z.cid and  
       x.price > 100 and  
       z.city = 'Seattle'
```

Can you think of  
another plan?

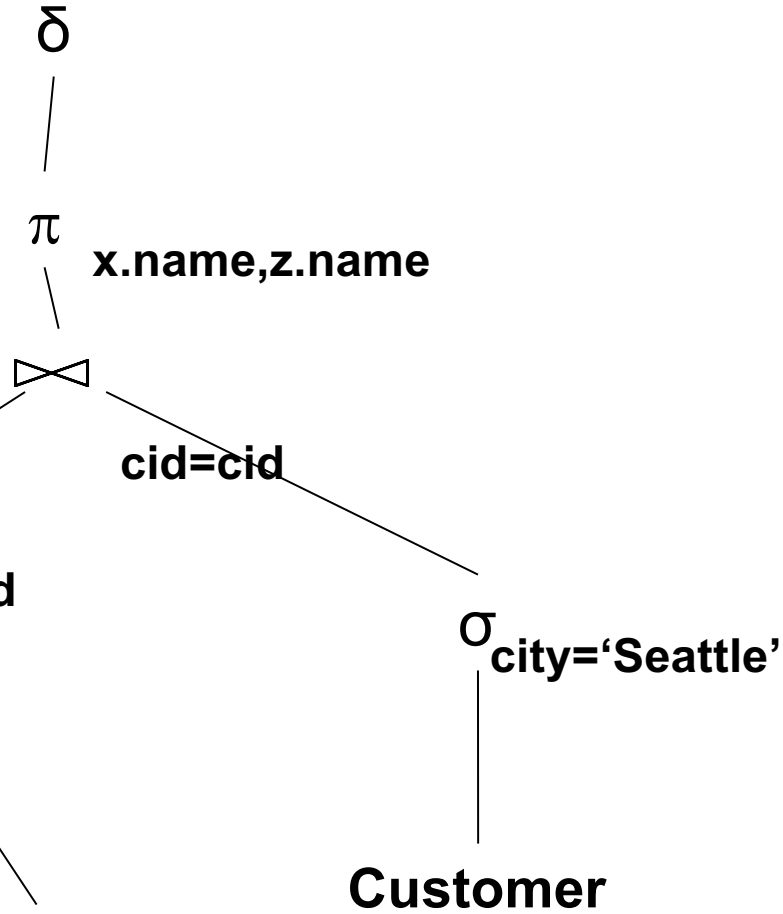


Product(pid, name, price)  
Purchase(pid, cid, store)  
Customer(cid, name, city)

# From SQL to RA

```
SELECT DISTINCT x.name, z.name  
FROM Product x, Purchase y, Customer z  
WHERE x.pid = y.pid and y.cid = z.cid and  
x.price > 100 and  
z.city = 'Seattle'
```

Can you think of another plan?



Push selections down the query plan!

Query optimization: find an equivalent optimal plan

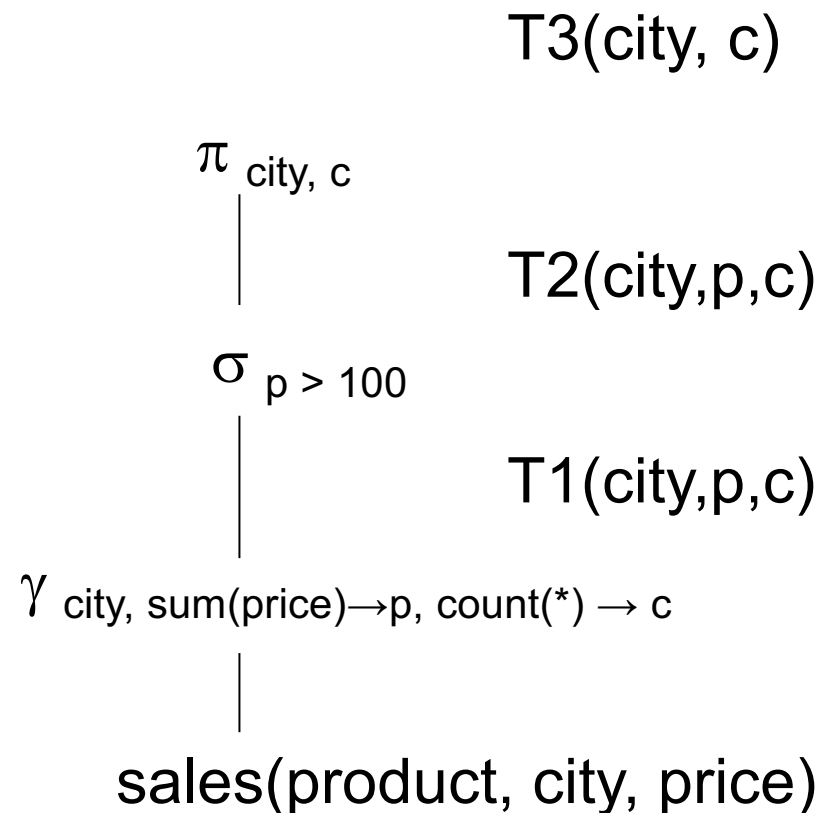
# Extended RA: Operators on Bags

- Duplicate elimination  $\delta$
- Grouping & aggregation  $\gamma$
- Sorting  $\tau$

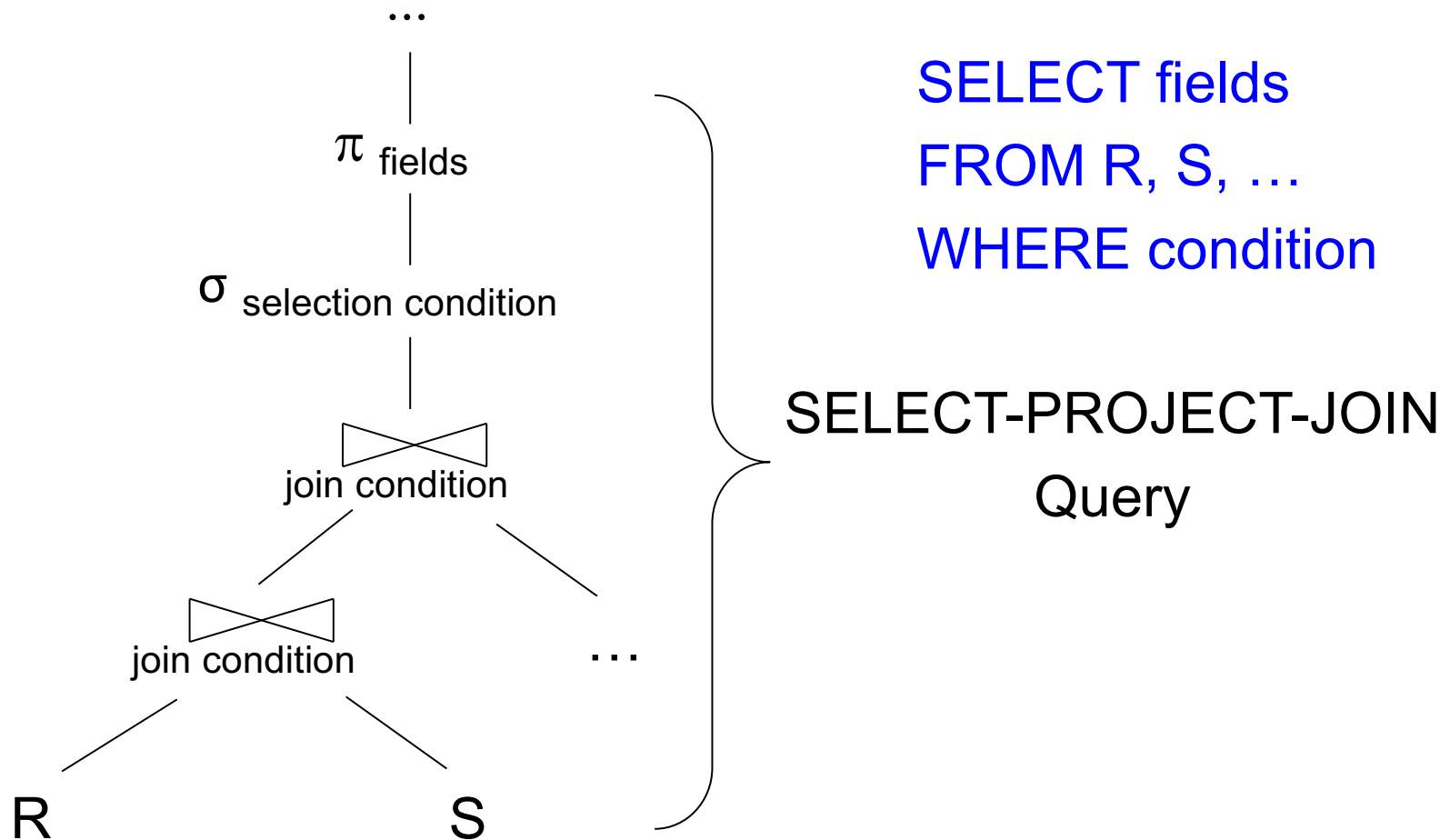
# Logical Query Plan

```
SELECT city, count(*)  
FROM sales  
GROUP BY city  
HAVING sum(price) > 100
```

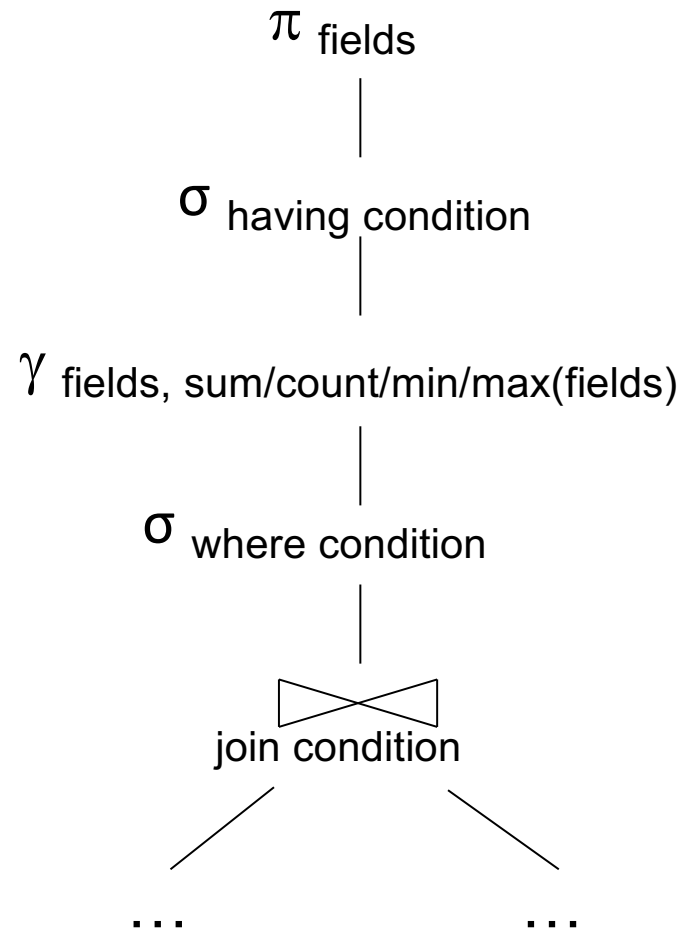
T1, T2, T3 = temporary tables



# Typical Plan for Block (1/2)



# Typical Plan for Block (2/2)



SELECT fields  
FROM R, S, ...  
WHERE condition  
GROUP BY fields  
HAVING condition

Supplier(sno,sname,scity,sstate)  
Part(pno,pname,psize,pcolor)  
Supply(sno,pno,price)

# How about Subqueries?

```
SELECT Q.sno  
FROM Supplier Q  
WHERE Q.sstate = 'WA'  
and not exists  
  (SELECT *  
   FROM Supply P  
   WHERE P.sno = Q.sno  
   and P.price > 100)
```

Correlation !



Supplier(sno,sname,scity,sstate)  
Part(pno,pname,psize,pcolor)  
Supply(sno,pno,price)

# How about Subqueries?

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
    and not exists
    (SELECT *
     FROM Supply P
     WHERE P.sno = Q.sno
        and P.price > 100)
```

De-Correlation

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
    and Q.sno not in
    (SELECT P.sno
     FROM Supply P
     WHERE P.price > 100)
```

Supplier(sno,sname,scity,sstate)  
Part(pno,pname,psize,pcolor)  
Supply(sno,pno,price)

# How about Subqueries?

Un-nesting

```
(SELECT Q.sno  
FROM Supplier Q  
WHERE Q.sstate = 'WA')  
EXCEPT  
(SELECT P.sno  
FROM Supply P  
WHERE P.price > 100)
```

EXCEPT = set difference

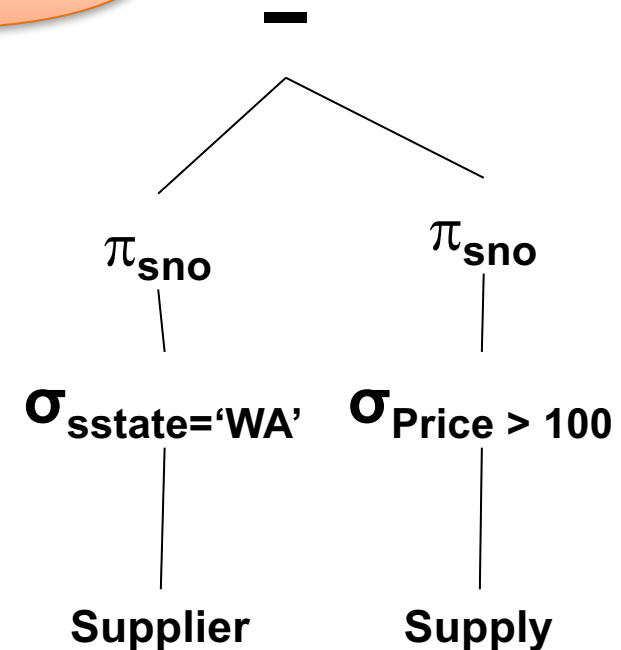
```
SELECT Q.sno  
FROM Supplier Q  
WHERE Q.sstate = 'WA'  
and Q.sno not in  
(SELECT P.sno  
FROM Supply P  
WHERE P.price > 100)
```

Supplier(sno,sname,scity,sstate)  
Part(pno,pname,psize,pcolor)  
Supply(sno,pno,price)

# How about Subqueries?

```
(SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA')
EXCEPT
(SELECT P.sno
FROM Supply P
WHERE P.price > 100)
```

Finally...



# From Logical Plans to Physical Plans

# Physical Operators

Each of the logical operators may have one or more implementations = physical operators

Will discuss several basic physical operators, with a focus on join

Product(pid, name, price)  
Purchase(pid, cid, store)

# Main Memory Algorithms

Logical operator:

Product(pid, name, price)  $\bowtie_{pid=pid}$  Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join  $O(??)$
2. Merge join  $O(??)$
3. Hash join  $O(??)$

(note that pid is a key)

Product(pid, name, price)  
Purchase(pid, cid, store)

# Main Memory Algorithms

Logical operator:

Product(pid, name, price)  $\bowtie_{pid=pid}$  Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join  $O(n^2)$  
2. Merge join  $O(??)$
3. Hash join  $O(??)$

Product(pid, name, price)  
Purchase(pid, cid, store)

# Main Memory Algorithms

Logical operator:

Product(pid, name, price)  $\bowtie_{pid=pid}$  Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join  $O(n^2)$
2. Merge join  $O(n \log n)$
3. Hash join  $O(??)$

sort both –  $O(n \log n)$   
merge –  $O(n)$



Product(pid, name, price)  
Purchase(pid, cid, store)

# Main Memory Algorithms

Logical operator:

Product(pid, name, price)  $\bowtie_{pid=pid}$  Purchase(pid, cid, store)

Propose three physical operators for the join, assuming the tables are in main memory:

1. Nested Loop Join  $O(n^2)$
2. Merge join  $O(n \log n)$
3. Hash join  $O(n) \dots O(n^2)$

add n to hash –  $O(n)$ ?  
lookup n in hash –  $O(n)$ ?

# BRIEF Review of Hash Tables

Separate chaining:

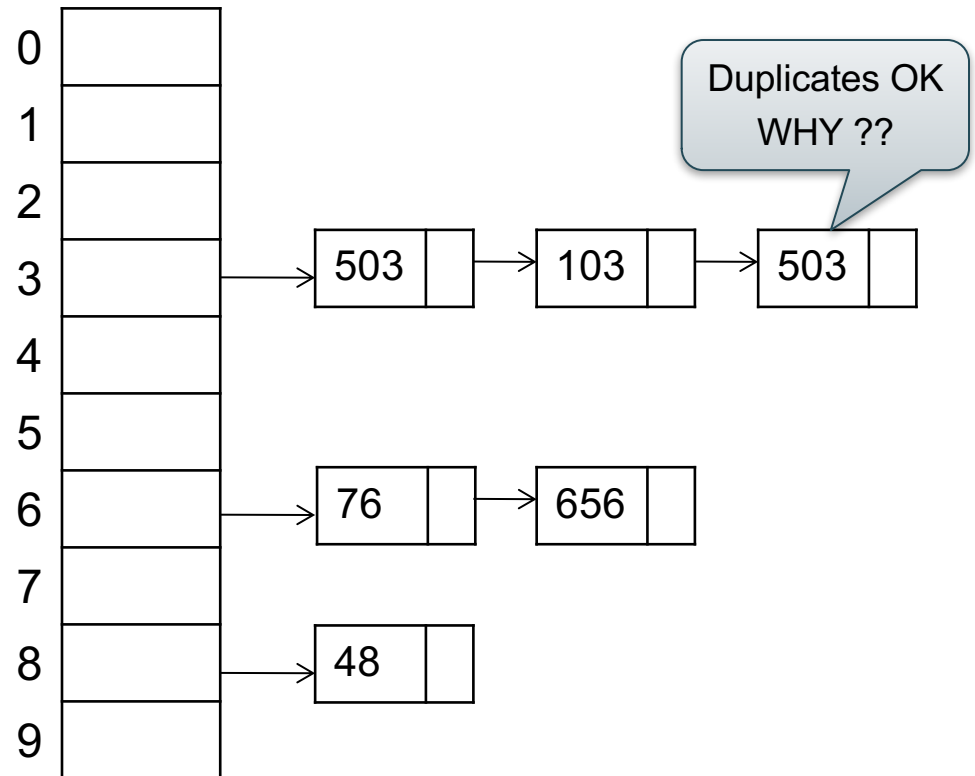
A (naïve) hash function:

$$h(x) = x \bmod 10$$

Operations:

$$\text{find}(103) = ??$$

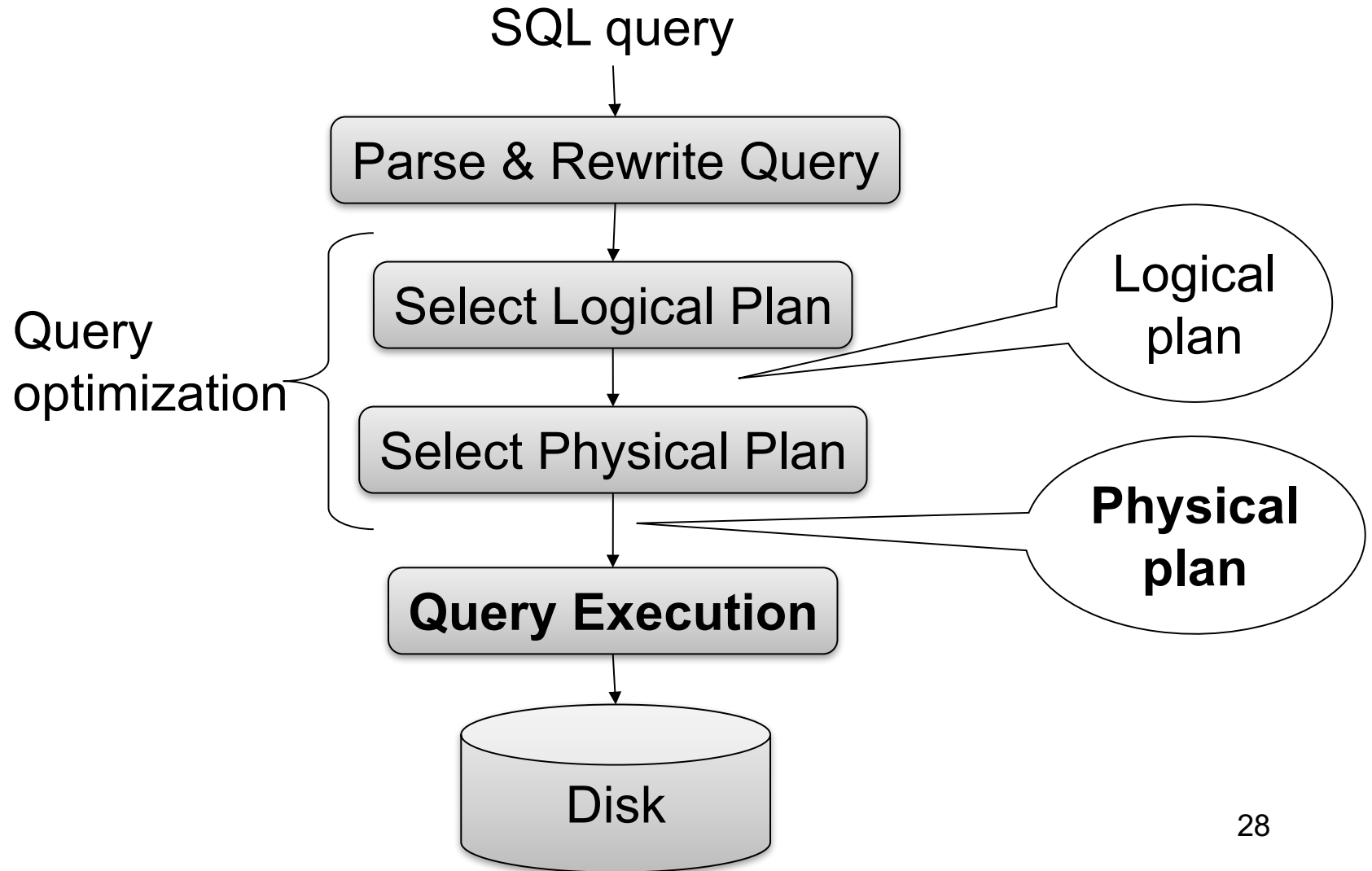
$$\text{insert}(488) = ??$$



# BRIEF Review of Hash Tables

- $\text{insert}(k, v)$  = inserts a key  $k$  with value  $v$
- Many values for one key
  - Hence, duplicate  $k$ 's are OK
- $\text{find}(k)$  = returns the *list* of all values  $v$  associated to the key  $k$

# Query Evaluation Steps Review



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Relational Algebra

```
SELECT sname  
FROM Supplier x, Supply y  
WHERE x.sid = y.sid  
      and y.pno = 2  
      and x.scity = 'Seattle'  
      and x.sstate = 'WA'
```

Give a relational algebra expression for this query

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Relational Algebra

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

$\pi_{\text{sname}}(\sigma_{\text{scity}='Seattle' \wedge \text{sstate}='WA' \wedge \text{pno}=2}(\text{Supplier} \bowtie_{\text{sid}=\text{sid}} \text{Supply}))$

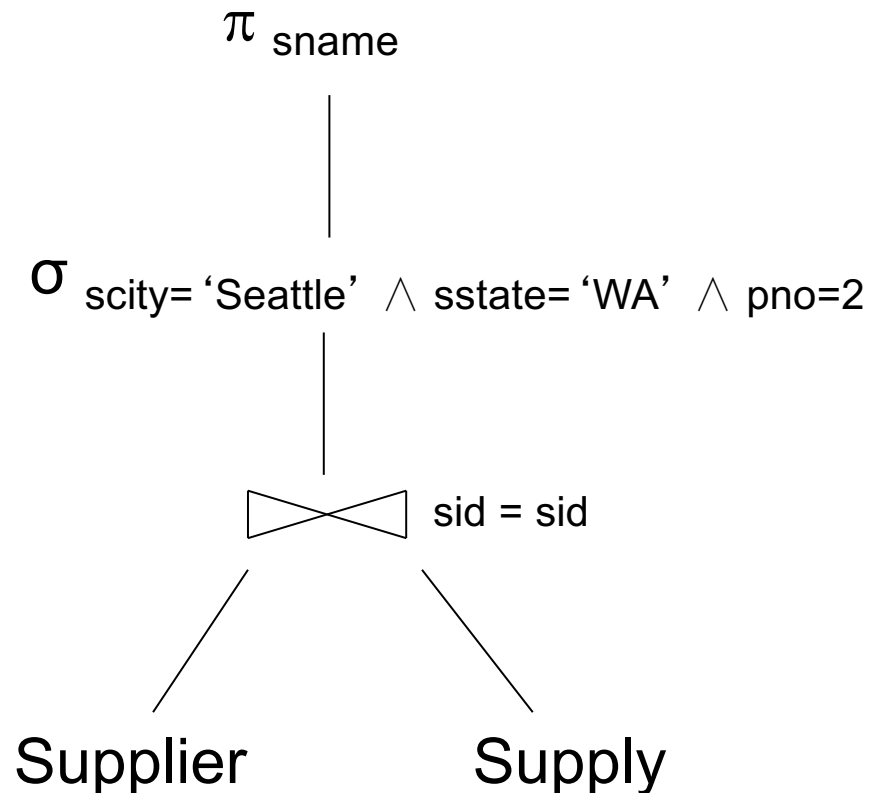
Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Relational Algebra

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Relational algebra expression is also called the “logical query plan”



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Physical Query Plan 1

(On the fly)

$\pi$  sname

(On the fly)

$\sigma$  scity='Seattle'  $\wedge$  sstate='WA'  $\wedge$  pno=2

(Nested loop)

sid = sid

Supplier

(File scan)

Supply

(File scan)

A physical query plan is a logical query plan annotated with physical implementation details

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Physical Query Plan 2

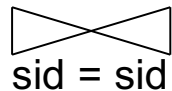
(On the fly)

$\pi$  sname

(On the fly)

$\sigma$  scity='Seattle'  $\wedge$  sstate='WA'  $\wedge$  pno=2

(Hash join)



Supplier

(File scan)

Supply

(File scan)

Same logical query plan  
Different physical plan

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Physical Query Plan 3

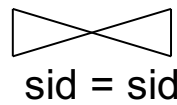
Different but equivalent logical query plan; different physical plan

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

(On the fly)

$\pi_{\text{sname}}$

(Sort-merge join)



(Scan & write to T1)

(Scan & write to T2)

$\sigma_{\text{scity}='Seattle' \wedge \text{sstate}='WA'}$

$\sigma_{\text{pno}=2}$

Supplier  
(File scan)

Supply  
(File scan)

# Query Optimization Problem

- For each SQL query... many logical plans
- For each logical plan... many physical plans
- How do find a fast physical plan?
  - Will discuss in a few lectures