Introduction to Database Systems CSE 414

Lecture 8: Relational Algebra

Announcements

- HW3 is out due Friday
 - git pull upstream master
 - Make sure you have email from Microsoft
 Azure and log in
- Web quiz 2 due tonight

Relational Algebra

Relational Algebra

- Set-at-a-time algebra, which manipulates relations
- In SQL we say <u>what</u> we want
- In RA we can express <u>how</u> to get it
- Every DBMS implementation converts a SQL query to RA in order to execute it
- An RA expression is called a <u>query plan</u>

Why study another relational query language?

- RA is how SQL is implemented in DBMS
 - We will see more of this in a few weeks

RA opens up opportunities for query optimization

Basics

- Relations and attributes
- Functions that are applied to relations
 - Return relations

$$R2 = \sigma (R1)$$

Can be composed together

$$R3 = \pi (\sigma (R1))$$

- Often displayed using a tree rather than linearly
- Use Greek symbols: σ , π , δ , etc

Sets v.s. Bags

- Sets: {a,b,c}, {a,d,e,f}, { }, . . .
- Bags: {a, a, b, c}, {b, b, b, b, b}, . . .

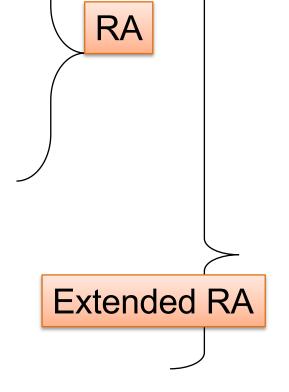
Relational Algebra has two flavors:

- Set semantics = standard Relational Algebra
- Bag semantics = extended Relational Algebra

DB systems implement bag semantics (Why?)

Relational Algebra Operators

- Union ∪, intersection ∩, difference -
- Selection σ
- Projection π
- Cartesian product X, join ⋈
- (Rename ρ)
- Duplicate elimination δ
- Grouping and aggregation y
- Sorting τ



All operators take in 1 or more relations as inputs and return another relation

Union and Difference

R1 U R2 R1 – R2

Only make sense if R1, R2 have the same schema

What do they mean over bags?

What about Intersection?

Derived operator using minus

$$R1 \cap R2 = R1 - (R1 - R2)$$

Derived using join

$$R1 \cap R2 = R1 \bowtie R2$$

Selection

Returns all tuples which satisfy a condition

$$\sigma_{\rm c}(R)$$

- Examples
 - $-\sigma_{\text{Salary} > 40000}$ (Employee)
 - $-\sigma_{\text{name = "Smith"}}$ (Employee)
- The condition c can be =, <, <=, >, >=, <> combined with AND, OR, NOT

Employee

SSN	Name	Salary
1234545	John	20000
5423341	Smith	60000
4352342	Fred	50000

$\sigma_{\text{Salary} > 40000}$ (Employee)

SSN	Name	Salary
5423341	Smith	60000
4352342	Fred	50000

Projection

Eliminates columns

$$\pi_{A1,...,An}(R)$$

- Example: project social-security number and names:
 - $-\pi_{SSN, Name}$ (Employee) \rightarrow Answer(SSN, Name)

Different semantics over sets or bags! Why?

Employee

SSN	Name	Salary
1234545	John	20000
5423341	John	60000
4352342	John	20000

π _{Name,Salary} (Employee)

Name	Salary
John	20000
John	60000
John	20000

Name	Salary
John	20000
John	60000

Bag semantics

Set semantics

Which is more efficient?

Composing RA Operators

Patient

no	name	zip	disease
1	p1	98125	flu
2	p2	98125	heart
3	р3	98120	lung
4	p4	98120	heart

$\pi_{zip,disease}(Patient)$

zip	disease
98125	flu
98125	heart
98120	lung
98120	heart

 $\sigma_{disease='heart'}(Patient)$

no	name	zip	disease
2	p2	98125	heart
4	p4	98120	heart

$$\pi_{zip,disease}(\sigma_{disease='heart'}(Patient))$$

zip	disease
98125	heart
98120	heart

Cartesian Product

Each tuple in R1 with each tuple in R2

· Rare in practice; mainly used to express joins

Cross-Product Example

Employee

Name	SSN
John	99999999
Tony	77777777

Dependent

EmpSSN	DepName
99999999	Emily
77777777	Joe

Employee X Dependent

Name	SSN	EmpSSN	DepName
John	99999999	99999999	Emily
John	99999999	77777777	Joe
Tony	77777777	99999999	Emily
Tony	77777777	77777777	Joe

Renaming

Changes the schema, not the instance

- Example:
 - Given Employee(Name, SSN)
 - $-\rho_{N,S}(Employee) \rightarrow Answer(N,S)$

Natural Join

 $R1 \bowtie R2$

• Meaning: R1 \bowtie R2 = $\Pi_A(\sigma_\theta(R1 \times R2))$

Where:

- Selection σ_{θ} checks equality of all common attributes (i.e., attributes with same names)
- Projection Π_A eliminates duplicate common attributes

Natural Join Example

R

Α	В
Х	Υ
Х	Z
Υ	Z
Z	V

S

В	С
Z	U
V	W
Z	V

 $R\bowtie S=$

$$\Pi_{ABC}(\sigma_{R.B=S.B}(R \times S))$$

Α	В	С
X	Z	U
X	Z	V
Υ	Z	U
Υ	Z	V
Z	V	W

Natural Join Example 2

AnonPatient P

age	zip	disease
54	98125	heart
20	98120	flu

Voters V

name	age	zip
Alice	54	98125
Bob	20	98120

$P \bowtie V$

age	zip	disease	name
54	98125	heart	Alice
20	98120	flu	Bob

Natural Join

Given schemas R(A, B, C, D), S(A, C, E),
 what is the schema of R ⋈ S?

• Given R(A, B, C), S(D, E), what is R \bowtie S?

• Given R(A, B), S(A, B), what is $R \bowtie S$?

AnonPatient (age, zip, disease)
Voters (name, age, zip)

Theta Join

A join that involves a predicate

$$R1 \bowtie_{\theta} R2 = \sigma_{\theta} (R1 X R2)$$

- Here θ can be any condition
- No projection in this case!
- For our voters/patients example:

Equijoin

A theta join where θ is an equality predicate

$$R1 \bowtie_{\theta} R2 = \sigma_{\theta} (R1 \times R2)$$

- By far the most used variant of join in practice
- What is the relationship with natural join?

Equijoin Example

AnonPatient P

age	zip	disease
54	98125	heart
20	98120	flu

Voters V

name	age	zip
p1	54	98125
p2	20	98120

$$P\bowtie_{P.age=V.age}V$$

P.age	P.zip	P.disease	V.name	V.age	V.zip
54	98125	heart	p1	54	98125
20	98120	flu	p2	20	98120

Join Summary

- Theta-join: $R \bowtie_{\theta} S = \sigma_{\theta} (R \times S)$
 - Join of R and S with a join condition θ
 - Cross-product followed by selection θ
 - No projection
- Equijoin: $R \bowtie_{\theta} S = \sigma_{\theta} (R \times S)$
 - Join condition θ consists only of equalities
 - No projection
- Natural join: $R \bowtie S = \pi_A (\sigma_\theta (R \times S))$
 - Equality on all fields with same name in R and in S
 - Projection π_A drops all redundant attributes

So Which Join Is It?

When we write $R \bowtie S$ we usually mean an equijoin, but we often omit the equality predicate when it is clear from the context

More Joins

Outer join

- Include tuples with no matches in the output
- Use NULL values for missing attributes
- Does not eliminate duplicate columns

Variants

- Left outer join
- Right outer join
- Full outer join

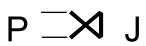
Outer Join Example

AnonPatient P

age	zip	disease
54	98125	heart
20	98120	flu
33	98120	lung

AnnonJob J

job	age	zip
lawyer	54	98125
cashier	20	98120



P.age	P.zip	P.diseas e	J.job	J.age	J.zip
54	98125	heart	lawyer	54	98125
20	98120	flu	cashier	20	98120
33	98120	lung	null	null	null

Some Examples

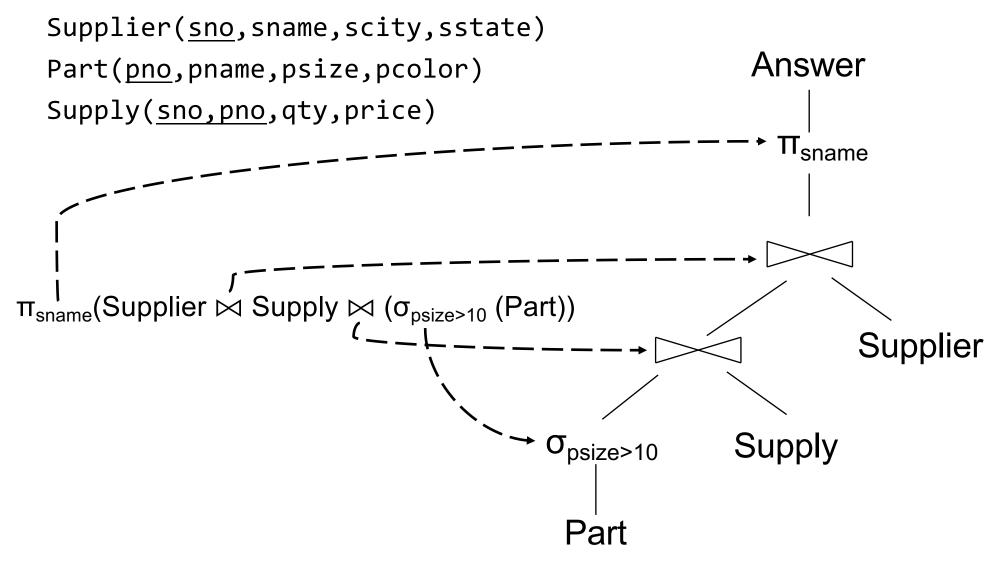
```
Supplier(sno,sname,scity,sstate)
Part(pno,pname,psize,pcolor)
Supply(sno,pno,qty,price)
```

Using symbols:

```
\pi_{\text{sname}}(\text{Supplier} \bowtie (\text{Supply} \bowtie (\sigma_{\text{psize}>10} (\text{Part})))
```

Can be represented as trees as well

Representing RA Queries as Trees



Some Examples

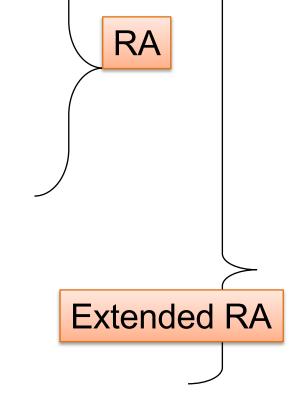
```
Supplier(sno,sname,scity,sstate)
Part(pno,pname,psize,pcolor)
Supply(sno,pno,qty,price)
```

Name of supplier of parts with size greater than 10 $\pi_{\text{sname}}(\text{Supplier} \bowtie (\text{Supply} \bowtie (\sigma_{\text{psize}>10} (\text{Part})))$

Name of supplier of red parts or parts with size greater than 10 $\pi_{\text{sname}}(\text{Supplier}\bowtie(\text{Supply}\bowtie(\sigma_{\text{psize}>10}\lor_{\text{pcolor='red'}}(\text{Part}))))$ $\pi_{\text{sname}}(\text{Supplier}\bowtie(\text{Supply}\bowtie(\sigma_{\text{psize}>10}(\text{Part})\cup\sigma_{\text{pcolor='red'}}(\text{Part}))))$

Relational Algebra Operators

- Union ∪, intersection ∩, difference -
- Selection σ
- Projection π
- Cartesian product X, join ⋈
- (Rename ρ)
- Duplicate elimination δ
- Grouping and aggregation γ
- Sorting τ



All operators take in 1 or more relations as inputs and return another relation

Extended RA: Operators on Bags

- Duplicate elimination δ
- Grouping γ
 - Takes in relation and a list of grouping operations (e.g., aggregates). Returns a new relation.
- Sorting τ
 - Takes in a relation, a list of attributes to sort on, and an order. Returns a new relation.

Grouping

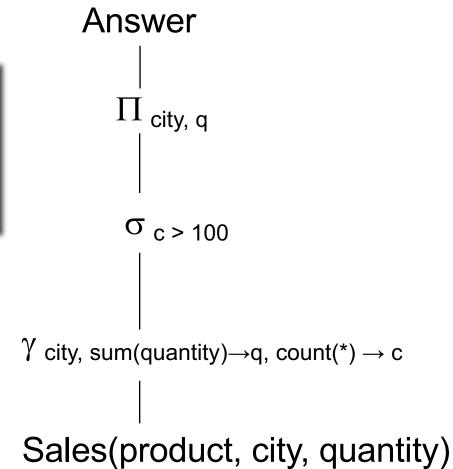
Specify groups and aggregates

```
\gamma_{A1,...,An, sum/max(B1)...}(R)
```

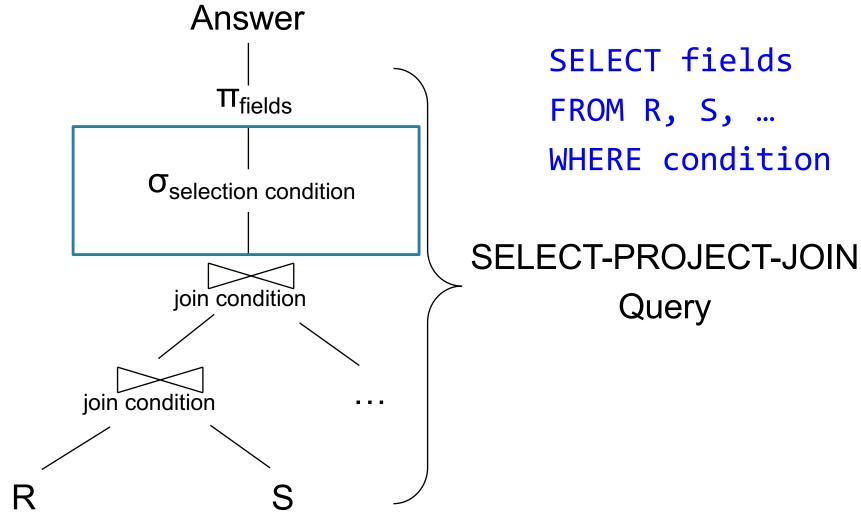
- Example: project social-security number and names:
- Output is like project: only output is attributes in the subscript
- Can also rename:
 _{A, count(B) → count}(R)

Using Extended RA Operators

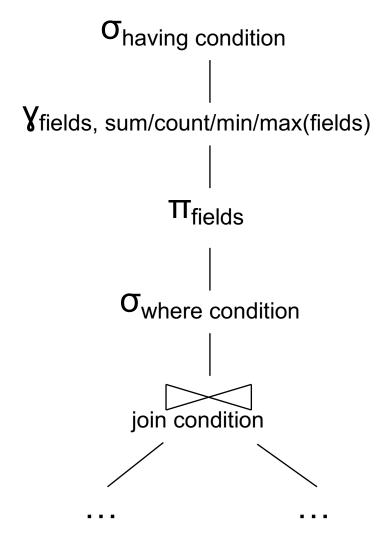
```
SELECT city, sum(quantity)
FROM Sales
GROUP BY city
HAVING count(*) > 100
```



Typical Plan for a Query (1/2)



Typical Plan for a Query (1/2)



SELECT fields
FROM R, S, ...
WHERE condition
GROUP BY fields
HAVING condition

How about Subqueries?

Return all suppliers in WA that sell no products greater than \$100

How about Subqueries?

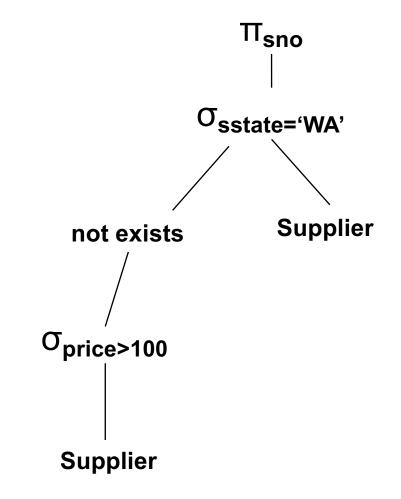
```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
and not exists
(SELECT *
   FROM Supply P
   WHERE P.sno = Q.sno
        and P.price > 100)
```

Return all suppliers in WA that sell no products greater than \$100

How about Subqueries?

Option 1: create nested plans

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
  and not exists
  (SELECT *
    FROM Supply P
    WHERE P.sno = Q.sno
        and P.price > 100)
```



How about Subqueries?

```
SELECT Q.sno
FROM Supplier Q.
WHERE Q.sstate = 'WA'
and not exists
(SELECT *
FROM Supply P
WHERE P.sno = Q.sno
and P.price > 100)
```

How about Subqueries?

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
and not exists
(SELECT *
   FROM Supply P
   WHERE P.sno = Q.sno
        and P.price > 100)
```

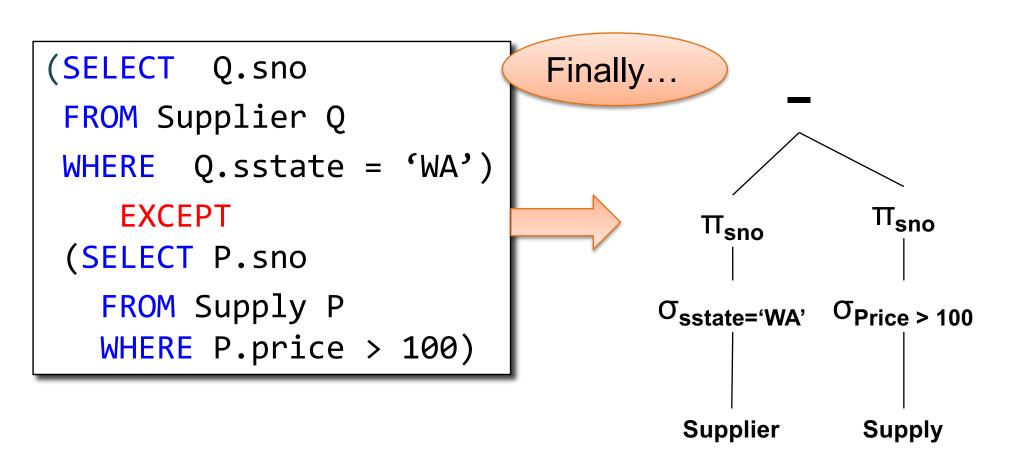
De-Correlation

```
SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA'
and Q.sno not in
  (SELECT P.sno
   FROM Supply P
   WHERE P.price > 100)
```

How about Subqueries?

```
Un-nesting
(SELECT Q.sno
FROM Supplier Q
                             SELECT Q.sno
WHERE Q.sstate = 'WA')
                             FROM Supplier Q
    EXCEPT
                             WHERE Q.sstate = 'WA'
 (SELECT P.sno
                                and Q.sno not in
   FROM Supply P
                                (SELECT P.sno
  WHERE P.price > 100)
                                 FROM Supply P
  EXCEPT = set difference
                                 WHERE P.price > 100)
```

How about Subqueries?



Summary of RA and SQL

- SQL = a declarative language where we say <u>what</u> data we want to retrieve
- RA = an algebra where we say <u>how</u> we want to retrieve the data
- Theorem: SQL and RA can express exactly the same class of queries

Summary of RA and SQL

- SQL (and RA) cannot express ALL queries that we could write in, say, Java
- Example:
 - Parent(p,c): find all descendants of 'Alice'
 - No RA query can compute this!
 - This is called a recursive query
- Next lecture: Datalog is an extension that can compute recursive queries

Class Overview

- Unit 1: Intro
- Unit 2: Relational Data Models and Query Languages
 - Data models, SQL, Relational Algebra, Datalog
- Unit 3: Non-relational data
- Unit 4: RDMBS internals and query optimization
- Unit 5: Parallel query processing
- Unit 6: DBMS usability, conceptual design
- Unit 7: Transactions

What is Datalog?

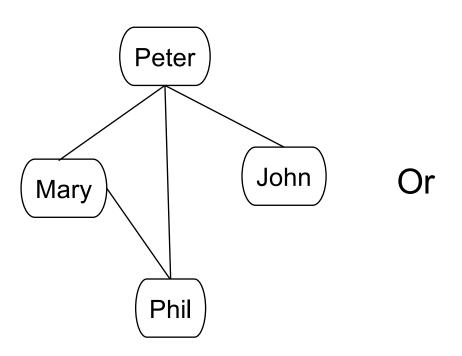
- Another query language for relational model
 - Designed in the 80's
 - Simple, concise, elegant
 - Extends relational queries with <u>recursion</u>
- Today is a hot topic:
 - Souffle (we will use in HW4)
 - Eve http://witheve.com/
 - Differential datalog
 https://github.com/frankmcsherry/differential-dataflow
 - Beyond databases in many research projects:
 network protocols, static program analysis



- Open-source implementation of Datalog DBMS
- Under active development
- Commercial implementations are available
 - More difficult to set up and use
- "sqlite" of Datalog
 - Set-based rather than bag-based
- Install in your VM
 - Run sudo yum install souffle in terminal
 - More details in upcoming HW4

Why bother with *yet* another relational query language?

Example: storing FB friends



Person1	Person2	is_friend
Peter	John	1
John	Mary	0
Mary	Phil	1
Phil	Peter	1

As a graph

As a relation

We will learn the tradeoffs of different data models later this quarter

Compute your friends graph

p1	p2	isFriend
Peter	John	1
John	Mary	0
Mary	Phil	1
Phil	Peter	1

Friends(p1, p2, isFriend)

```
SELECT f.p2
FROM Friends as f
WHERE f.p1 = 'me' AND f.isFriend = 1
```

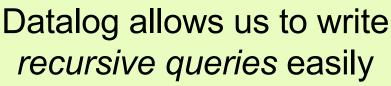
My own friends

```
SELECT f1.p2
FROM Friends as f1,
    (SELECT f.p2
    FROM Friends as f
    WHERE f.p1 = 'me' AND
    f.isFriend = 1) as f2
WHERE f1.p1 = f2.p2 AND
    f1.isFriend = 1
```

My FoF

My FoFoF... My FoFoFoF...

CSE 414 - When does it end???





Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

Datalog: Facts and Rules

Facts = tuples in the database Rules = queries Table declaration .decl Actor(id:number, fname:symbol, lname:symbol) .decl Casts(id:number, mid:number) .decl Movie(id:number, name:symbol, year:number) Types in Souffle: Actor(344759, 'Douglas', 'Fowley'). number symbol (aka varchar) Casts(344759, 29851). Casts(355713, 29000). Movie(7909, 'A Night in Armour', 1910). Insert data Movie(29000, 'Arizona', 1940). Movie(29445, 'Ave Maria', 1940).

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').

Casts(344759, 29851).

Casts(355713, 29000).

Movie(7909, 'A Night in Armour', 1910).

Movie(29000, 'Arizona', 1940).

Movie(29445, 'Ave Maria', 1940).
```

Q1(y) :- Movie(x,y,z), z=1940.

Datalog: Facts and Rules

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```
Actor(344759, 'Douglas', 'Fowley').
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Q1(y) :- Movie(x,y,z), z=1940.

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(x,y,z), z=1940.
```

SQL

```
SELECT name
FROM Movie
WHERE year = 1940
```

Datalog: Facts and Rules

Facts = tuples in the database

```
Actor(344759, 'Douglas', 'Fowley').

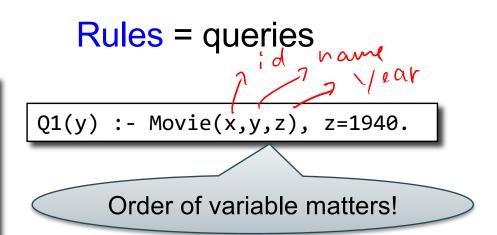
Casts(344759, 29851).

Casts(355713, 29000).

Movie(7909, 'A Night in Armour', 1910).

Movie(29000, 'Arizona', 1940).

Movie(29445, 'Ave Maria', 1940).
```



Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(iDontCare,y,z), z=1940.
```

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(_,y,z), z=1940.
_ = "don't care" variables
```

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(x,y,z), z=1940.
```

```
Q2(f,1) :- Actor(z,f,1), Casts(z,k),
Movie(x,y,1940).
```

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(x,y,z), z=1940.
```

```
Q2(f,1) :- Actor(z,f,1), Casts(z,x),
Movie(x,y,1940).
```

Find Actors who acted in Movies made in 1940

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(x,y,z), z=1940.
```

```
Q2(f,1) :- Actor(z,f,1), Casts(z,x),
Movie(x,y,1940).
```

```
Q3(f,l) :- Actor(z,f,l), Casts(z,x1), Movie(x1,y1,1910), Casts(z,x2), Movie(x2,y2,1940).
```

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(x,y,z), z=1940.
```

```
Q3(f,1) :- Actor(z,f,1), Casts(z,x1), Movie(x1,y1,1910), Casts(z,x2), Movie(x2,y2,1940).
```

Find Actors who acted in a Movie in 1940 and in one in 1910

Datalog: Facts and Rules

Facts = tuples in the database

Rules = queries

```
Actor(344759, 'Douglas', 'Fowley').
Casts(344759, 29851).
Casts(355713, 29000).
Movie(7909, 'A Night in Armour', 1910).
Movie(29000, 'Arizona', 1940).
Movie(29445, 'Ave Maria', 1940).
```

```
Q1(y) :- Movie(x,y,z), z=1940.
```

```
Q2(f,1) :- Actor(z,f,1), Casts(z,x), Movie(x,y,1940).
```

```
Q3(f,l) :- Actor(z,f,l), Casts(z,x1), Movie(x1,y1,1910), Casts(z,x2), Movie(x2,y2,1940).
```

Extensional Database Predicates = EDB = Actor, Casts, Movie
Intensional Database Predicates = IDB = Q1, Q2, Q3

CSE 414 - Autumn 2018