

# Introduction to Data Management

## CSE 344

Unit 4: RDBMS Internals  
Logical and Physical Plans

Query Execution  
Query Optimization

(4 lectures)

# Introduction to Data Management

## CSE 344

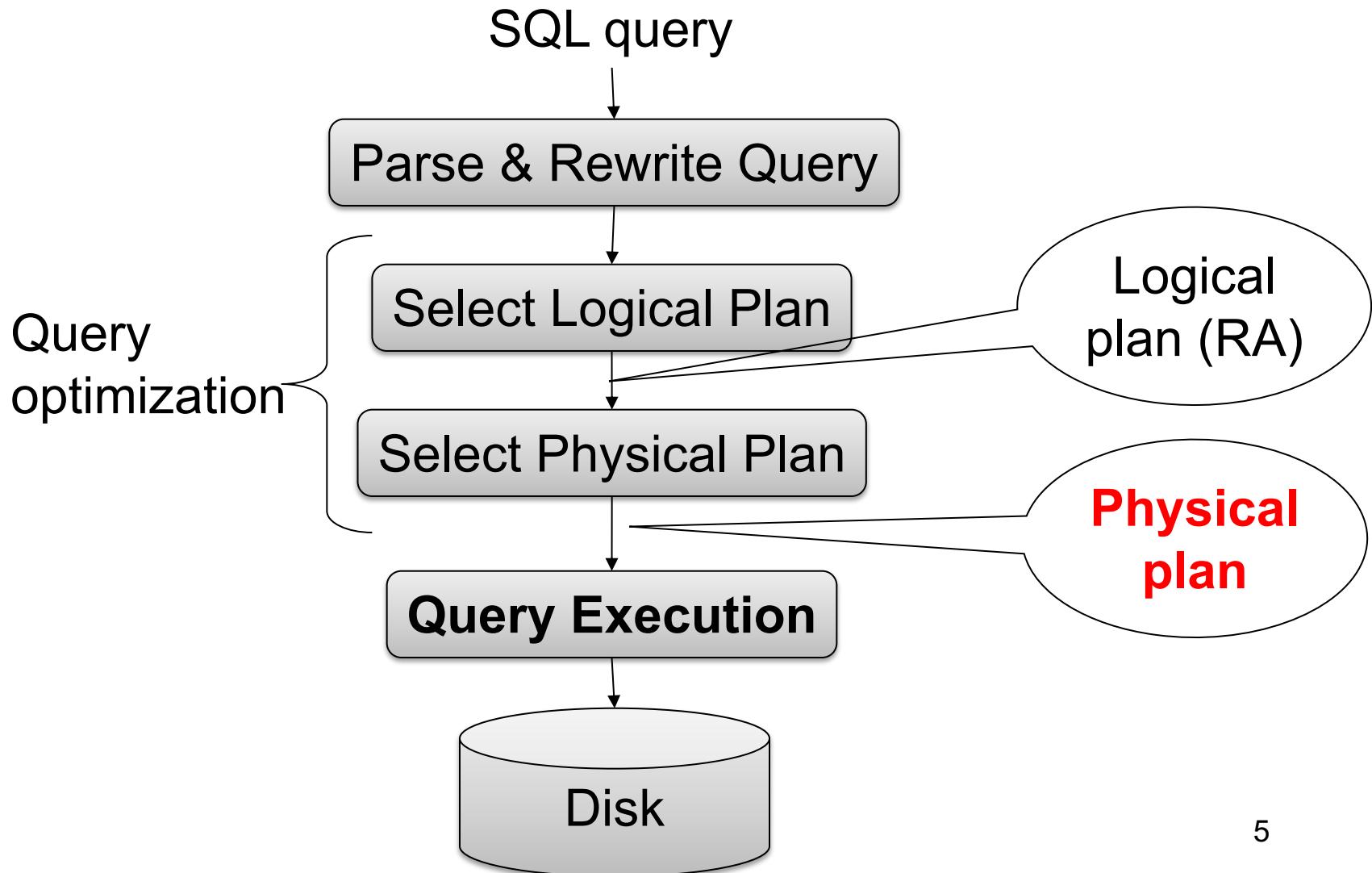
### Lecture 15: Introduction to Query Evaluation

# Class Overview

- Unit 1: Intro
- Unit 2: Relational Data Models and Query Languages
- Unit 3: Non-relational data
- Unit 4: RDMBS internals and query optimization
- Unit 5: Parallel query processing
- Unit 6: DBMS usability, conceptual design
- Unit 7: Transactions
- Unit 8: Advanced topics (time permitting)

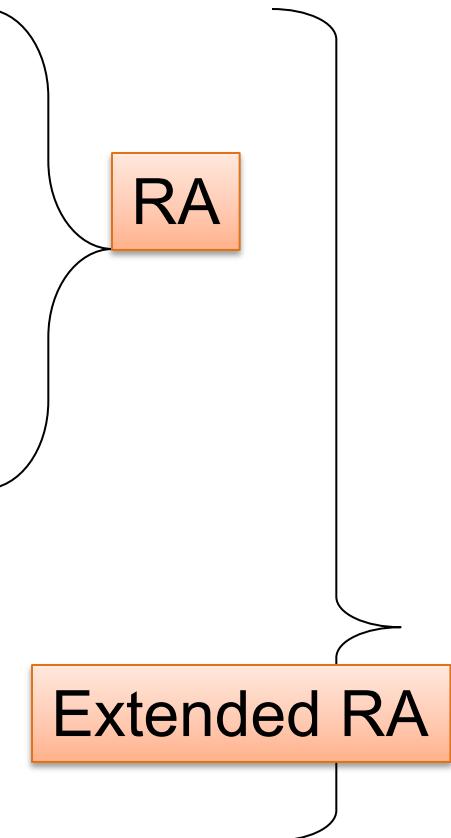
# From Logical RA Plans to Physical Plans

# Query Evaluation Steps Review



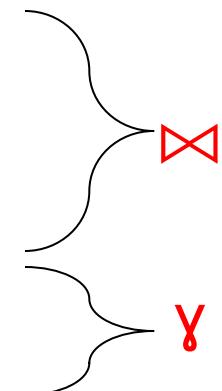
# Relational Algebra Operators

- Union  $\cup$ , intersection  $\cap$ , difference  $-$
- Selection  $\sigma$
- Projection  $\pi$
- Cartesian product  $\times$ , join  $\bowtie$
- (Rename  $\rho$ )
- Duplicate elimination  $\delta$
- Grouping and aggregation  $\gamma$
- Sorting  $\tau$



# Physical Operators

- For each operators above, several possible algorithms
- Main memory or external memory algorithms
- Examples:
  - Main memory hash join
  - External memory merge join
  - External memory partitioned hash join
  - Sort-based group by
  - Etc, etc



`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Main Memory Algorithms

Logical operator:

`Supplier ⚡sid=sid Supply`

Three algorithms:

1. Nested Loops
2. Hash-join
3. Merge-join

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# 1. Nested Loop Join

Logical operator:

`Supplier  $\bowtie_{\text{sid}=\text{sid}}$  Supply`

```
for x in Supplier do
    for y in Supply do
        if x.sid = y.sid
            then output(x,y)
```

`Supplier(sid, sname, scity, sstate)`

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# 1. Nested Loop Join

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If  $|R|=|S|=n$ ,  
what is the runtime?

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# 1. Nested Loop Join

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If  $|R|=|S|=n$ ,  
what is the runtime?

$O(n^2)$

# BRIEF Review of Hash Tables

Separate chaining:

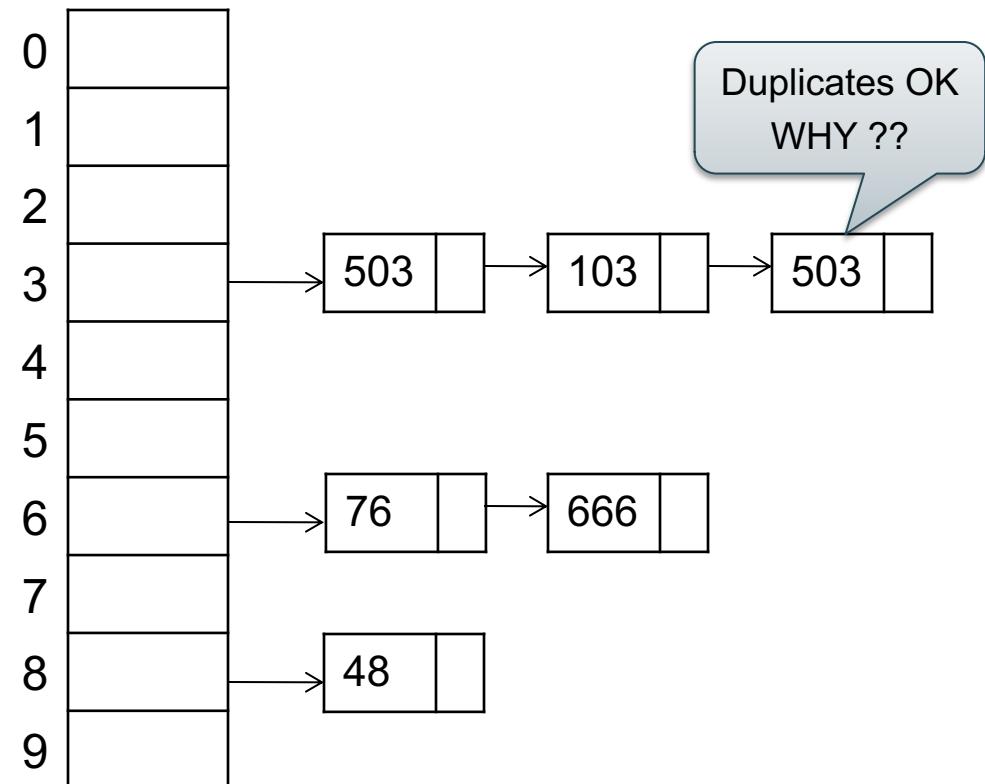
A (naïve) hash function:

$$h(x) = x \bmod 10$$

Operations:

$$\text{find}(103) = ??$$

$$\text{insert}(488) = ??$$



# BRIEF Review of Hash Tables

- $\text{insert}(k, v)$  = inserts a key  $k$  with value  $v$
- Many values for one key
  - Hence, duplicate  $k$ 's are OK
- $\text{find}(k)$  = returns the *list* of all values  $v$  associated to the key  $k$

**Supplier(sid, sname, scity, sstate)**

**Supply(sid, pno, quantity)**

## 2. Hash Join

Logical operator:

**Supplier  $\bowtie_{\text{sid}=\text{sid}}$  Supply**

```
for x in Supplier do
```

```
    insert(x.sid, x)
```

```
for y in Supply do
```

```
    x = find(y.sid);
```

```
    output(x,y);
```

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

## 2. Hash Join

Logical operator:

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If  $|R|=|S|=n$ ,  
what is the runtime?

$O(n)$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

## 2. Hash Join

Logical operator:

`Supplier  $\bowtie_{\text{sid}=\text{sid}}$  Supply`

Change join order

```
for y in Supply do  
    insert(y.sid, y)
```

```
for x in Supplier do  
    ????
```

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

## 2. Hash Join

Logical operator:

`Supplier  $\bowtie_{\text{sid}=\text{sid}}$  Supply`

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    for y in find(x.sid) do  
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If  $|R|=|S|=n$ ,  
what is the runtime?

$O(n)$

But can be  $O(n^2)$  **why?**

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## 2. Hash Join

Why would we change the order?

Logical operator:

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for y in Supply do  
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 $|\text{Supply}| \ll |\text{Supplier}|$

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```

sp

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`Supply(sid, pno, quantity)`

## 3. Merge Join

Logical operator:

`Supplier  $\bowtie_{\text{sid}=\text{sid}}$  Supply`

`Sort(Supplier); Sort(Supply);`

`x = Supplier.first();`

`y = Supply.first();`

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

### 3. Merge Join

Logical operator:

`Supplier  $\bowtie_{\text{sid}=\text{sid}}$  Supply`

`Sort(Supplier); Sort(Supply);`

`x = Supplier.first();`

`y = Supply.first();`

`while y != NULL do`

`case:`

`x.sid < y.sid: ???`

`x.sid = y.sid: ???`

`x.sid > y.sid: ???`

`Supplier(sid, sname, scity, sstate)`

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`x.sid < y.sid: x = x.next()`

`x.sid = y.sid: ???`

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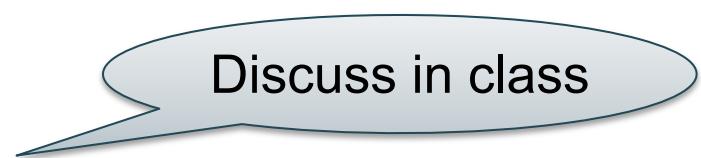
`x.sid = y.sid: output(x,y); y = y.next();`

`x.sid > y.sid: y = y.next();`

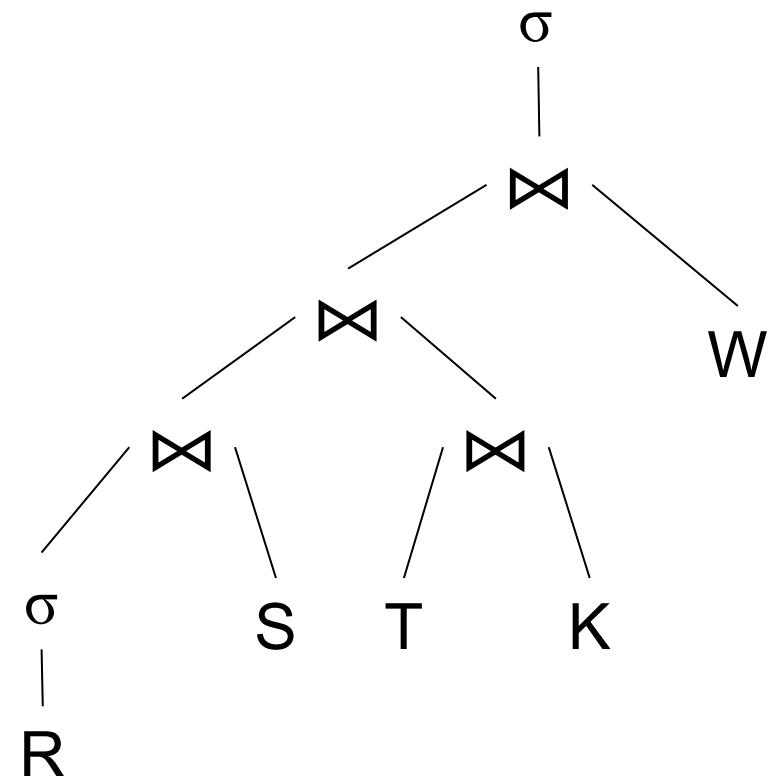
If  $|R|=|S|=n$ ,  
what is the runtime?

$O(n \log(n))$

# Main Memory Algorithms

- Join  $\bowtie$ :
    - Nested loop join
    - Hash join
    - Merge join
  - Selection  $\sigma$ 
    - “on-the-fly”
    - Index-based selection (next lecture)
  - Group by  $\gamma$ 
    - Hash-based
    - Merge-based
- 
- Discuss in class
- 
- Discuss in class

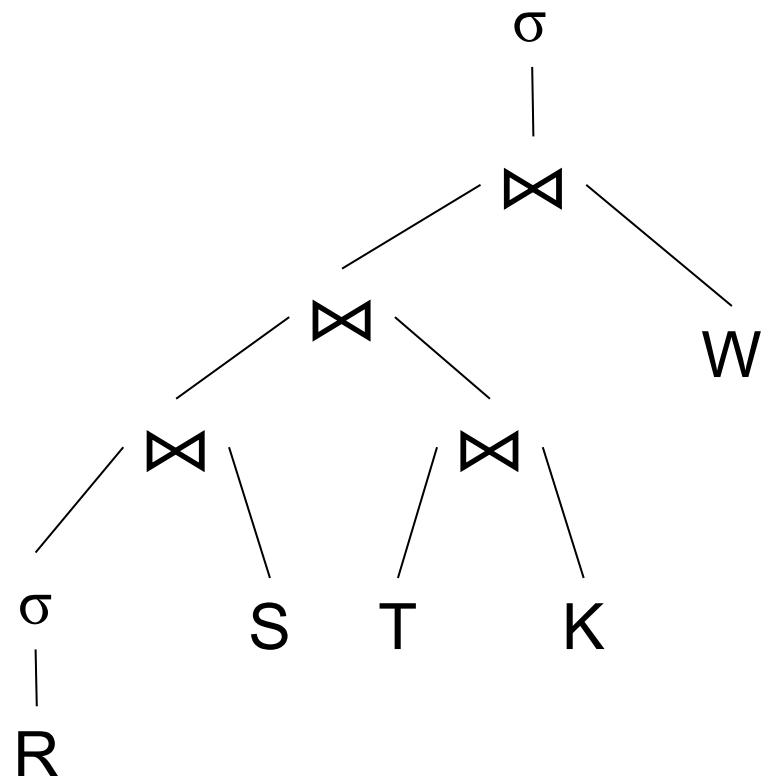
# How Do We Combine Them?



# How Do We Combine Them?

## The *Iterator Interface*

- `open()`
- `next()`
- `close()`



# Implementing Query Operators with the Iterator Interface

Example “on the fly” selection operator

```
interface Operator {
```

```
}
```

# Implementing Query Operators with the Iterator Interface

Example “on the fly” selection operator

```
interface Operator {  
  
    // initializes operator state  
    // and sets parameters  
    void open (...);  
  
}
```

# Implementing Query Operators with the Iterator Interface

Example “on the fly” selection operator

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    // initializes operator state  
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    void open (...);  
  
    // calls next() on its inputs  
    // processes an input tuple  
    // produces output tuple(s)  
    // returns null when done  
    Tuple next ();  
  
}
```

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    // cleans up (if any)  
    void close ();  
}
```

# Implementing Query Operators with the Iterator Interface

Example “on the fly” selection operator

```
interface Operator {  
  
    // initializes operator state  
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    void open (...);
```

```
class Select implements Operator {...  
    void open (Predicate p,  
              Operator c) {  
        this.p = p; this.c = c; c.open();  
    }  
}
```

```
// calls next() on its inputs  
// processes an input tuple  
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Tuple next ();
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// cleans up (if any)  
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    }  
    Tuple next () {  
        ...  
    }  
}
```

# Implementing Query Operators with the Iterator Interface

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    }  
    Tuple next () {  
        boolean found = false;  
        Tuple r = null;  
        while (!found) {  
            r = c.next();  
            if (r == null) break;  
            found = p(r);  
        }  
    }  
}
```

# Implementing Query Operators with the Iterator Interface

Example “on the fly” selection operator

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        }  
        return r;  
    }  
}
```

# Implementing Query Operators with the Iterator Interface

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        }  
        return r;  
    }  
    void close () { c.close(); }  
}
```

# Implementing Query Operators with the Iterator Interface

```
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    Tuple next ();  
  
    // cleans up (if any)  
    void close ();  
}
```

## Query plan execution

```
Operator q = parse("SELECT ...");  
q = optimize(q);  
  
q.open();  
while (true) {  
    Tuple t = q.next();  
    if (t == null) break;  
    else printOnScreen(t);  
}  
q.close();
```

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Pipelining

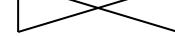
(On the fly)

$\Pi_{sname}$

(On the fly)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

(Nested loop)



$sid = sid$

Supplier  
(File scan)

Supply  
(File scan)

Discuss: open/next/close  
for nested loop join

`Supplier(sid, sname, scity, sstate)`

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# Pipelining

(On the fly)

$\Pi_{sname}$  **open()**

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$\bowtie$   
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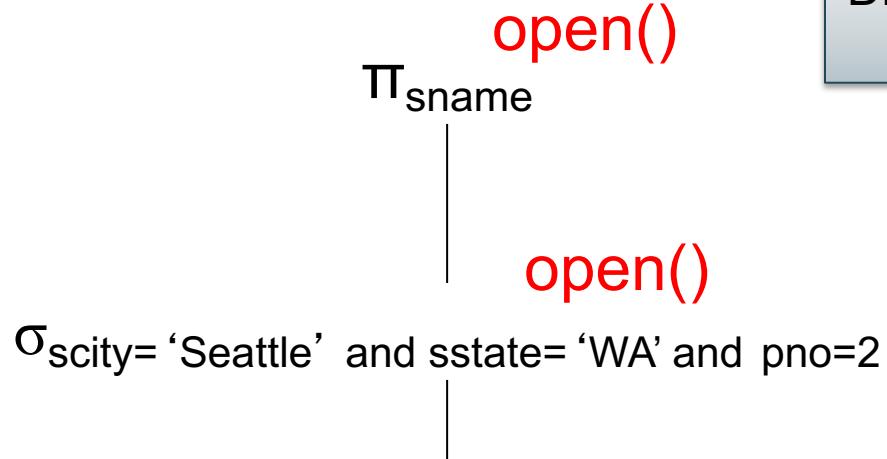
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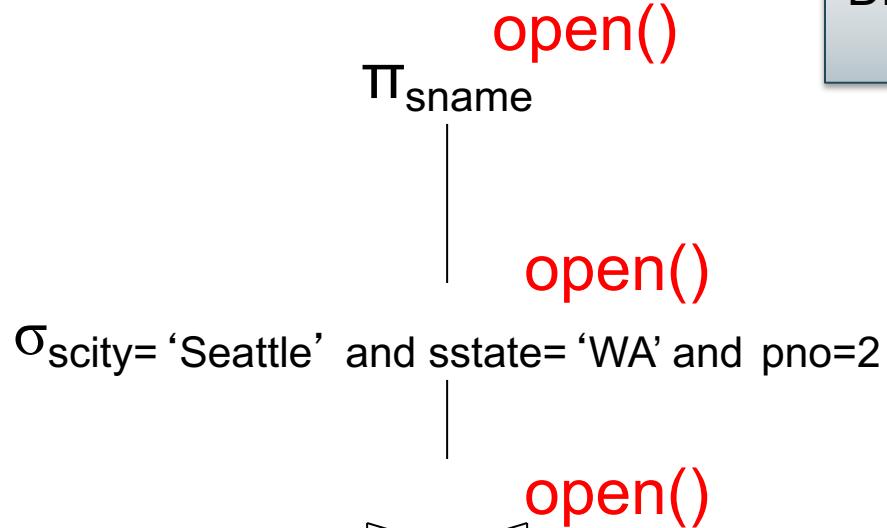
(On the fly)

(On the fly)

(Nested loop)

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(File scan)

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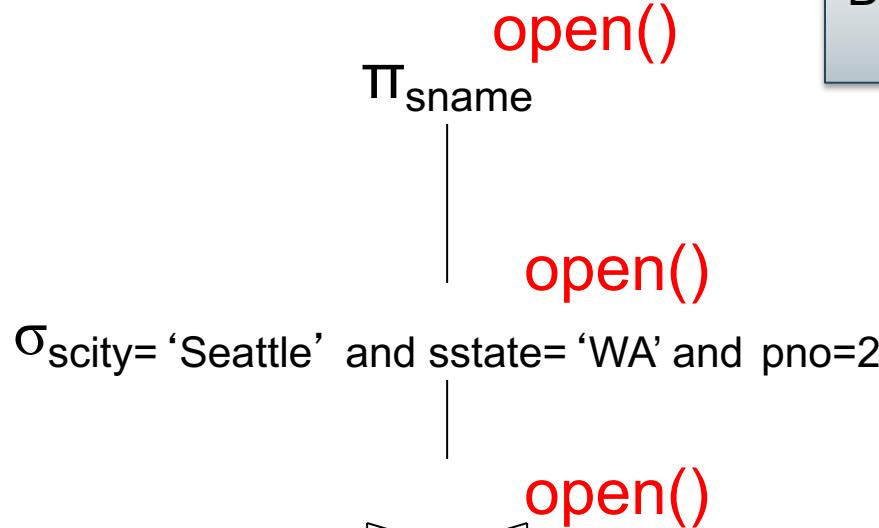
(On the fly)

(On the fly)

(Nested loop)

Supplier  
(File scan)

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Discuss: open/next/close  
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`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Pipelining

(On the fly)

$\Pi_{sname}$

next()

(On the fly)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

(Nested loop)



$sid = sid$

Supplier  
(File scan)

Supply  
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Discuss: open/next/close  
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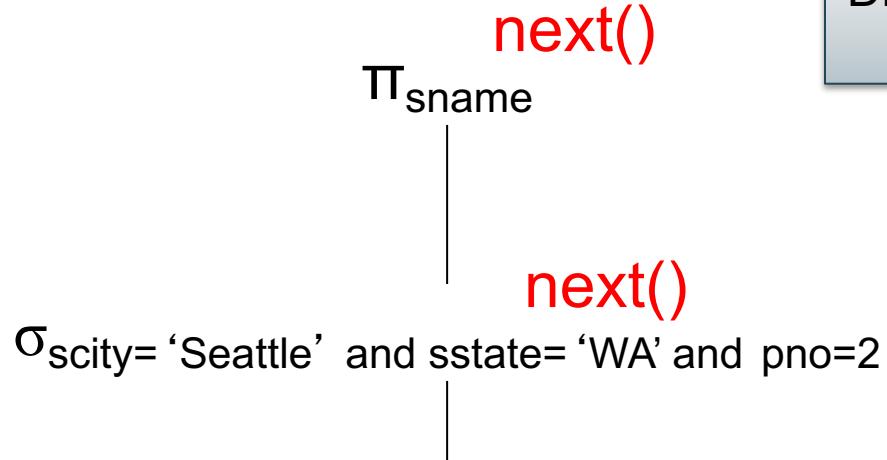
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Discuss: open/next/close  
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(On the fly)

(On the fly)

(Nested loop)

Supplier  
(File scan)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

$\pi_{sname}$

$\text{next}()$

$\text{next}()$

$\bowtie$

$\text{sid} = \text{sid}$

Discuss: open/next/close  
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# Pipelining

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Supplier  
(File scan)

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# Pipelining

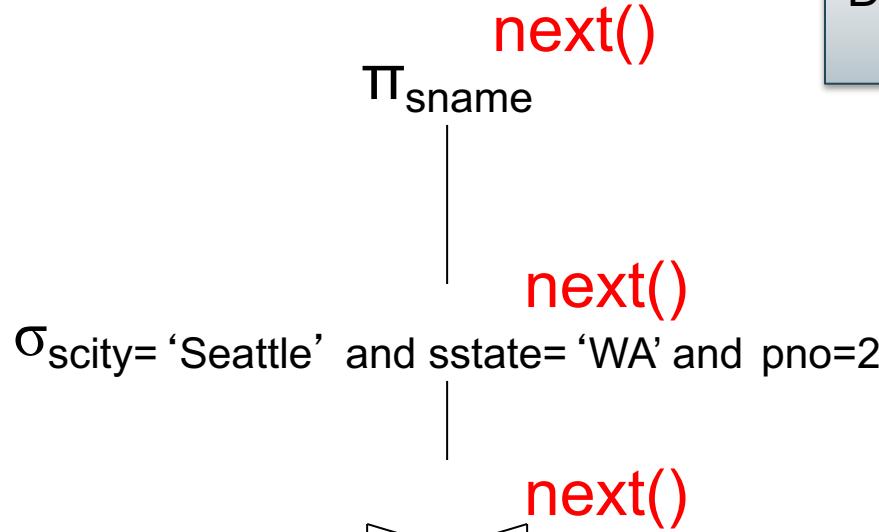
(On the fly)

(On the fly)

(Nested loop)

Supplier  
(File scan)

Supply  
(File scan)



Discuss: open/next/close  
for nested loop join

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Pipelining

(On the fly)

(On the fly)

(Nested loop)

next()

Supplier

(File scan)

next()

$\Pi_{sname}$

next()

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

next()

sid = sid

next()

next()

Supply

(File scan)

Discuss: open/next/close  
for nested loop join

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Pipelining

(On the fly)

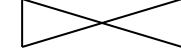
$\Pi_{sname}$

Discuss hash-join  
in class

(On the fly)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

(Hash Join)

  
 $sid = sid$

Supplier  
(File scan)

Supply  
(File scan)

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Pipelining

(On the fly)

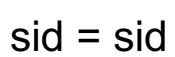
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Discuss hash-join  
in class

(On the fly)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

(Hash Join)



$sid = sid$

Supplier  
(File scan)

Supply  
(File scan)

Tuples from  
here are  
“blocked”

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Pipelining

(On the fly)

$\Pi_{sname}$

Discuss hash-join  
in class

(On the fly)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

(Hash Join)

Tuples from here are pipelined

Supplier  
(File scan)

$\bowtie$   
 $sid = sid$

Tuples from here are “blocked”

Supply  
(File scan)

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Blocked Execution

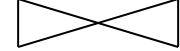
(On the fly)

$\Pi_{sname}$

(On the fly)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

(Merge Join)

  
sid = sid

Supplier  
(File scan)

Supply  
(File scan)

Discuss merge-join  
in class

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Blocked Execution

(On the fly)

$\Pi_{sname}$

Discuss merge-join  
in class

(On the fly)

$\sigma_{scity = \text{'Seattle'} \text{ and } sstate = \text{'WA'} \text{ and } pno = 2}$

(Merge Join)

$\bowtie$   
 $sid = sid$

Blocked

Blocked

Supplier  
(File scan)

Supply  
(File scan)

# Pipeline v.s. Blocking

- Pipeline
  - A tuple moves all the way through up the query plan
  - Advantages: speed
  - Disadvantage: need all hash at the same time in memory
- Blocking
  - The entire result of the subplan is computed (and stored to disk) before the first tuple is sent up the plan
  - Advantage: saves memory
  - Disadvantage: slower

# Introduction to Database Systems

## CSE 344

Lecture 16:  
Basics of Data Storage and Indexes

# Query Performance

To understand query performance and query optimization we need to understand:

- How is data organized on disk
- How to estimate query costs

We focus on **disk-based** DBMSs

# Hard Disk

- Disks are mechanical devices
- A block = unit of read/write
- Once in main memory we call it a page
- Read only at the rotation speed
- Consequence: sequential scan faster than random
  - **Fast**: read blocks 1,2,3,4,5,...
  - **Slow**: read blocks 2342, 11, 321,9, ...
- **Rule of thumb:**
  - Random read 1-2% of file  $\approx$  sequential scan entire file;
  - 1-2% decreases over time, because of increased density



# Data Storage

- DBMSs store data in **files**
- Most common organization is row-wise storage
- On disk, a file is split into **blocks**
- Each block contains a set of tuples

ID	fName	IName
10	Tom	Hanks
20	Amy	Hanks
...		

10	Tom	Hanks	block 1
20	Amy	Hanks	
50	...	...	block 2
200	...		
220			block 3
240			
420			
800			

In the example, we have **4 blocks** with 2 tuples each

ID	fName	IName
10	Tom	Hanks
20	Amy	Hanks
...		

# Data File Types

The data file can be one of:

- **Heap file**
  - Unsorted
- **Sequential file**
  - Sorted according to some attribute(s) called key

# Index

- An **additional** file, that allows fast access to records in the data file given a search key

# Index

- An **additional** file, that allows fast access to records in the data file given a search key
- The index contains (key, value) pairs:
  - Key = an attribute value (e.g., student ID or name)
  - Value = a pointer to the record OR the record itself

# Index

- An **additional** file, that allows fast access to records in the data file given a search key
- The index contains (key, value) pairs:
  - Key = an attribute value (e.g., student ID or name)
  - Value = a pointer to the record OR the record itself
- Could have many indexes for one table

Key = means here search key

# This Is Not A Key



Different keys:

- Primary key – uniquely identifies a tuple
- Key of the sequential file – how the data file is sorted, if at all
- Index key – how the index is organized



*This is not a pipe.*

CSE 414 - 2019sp



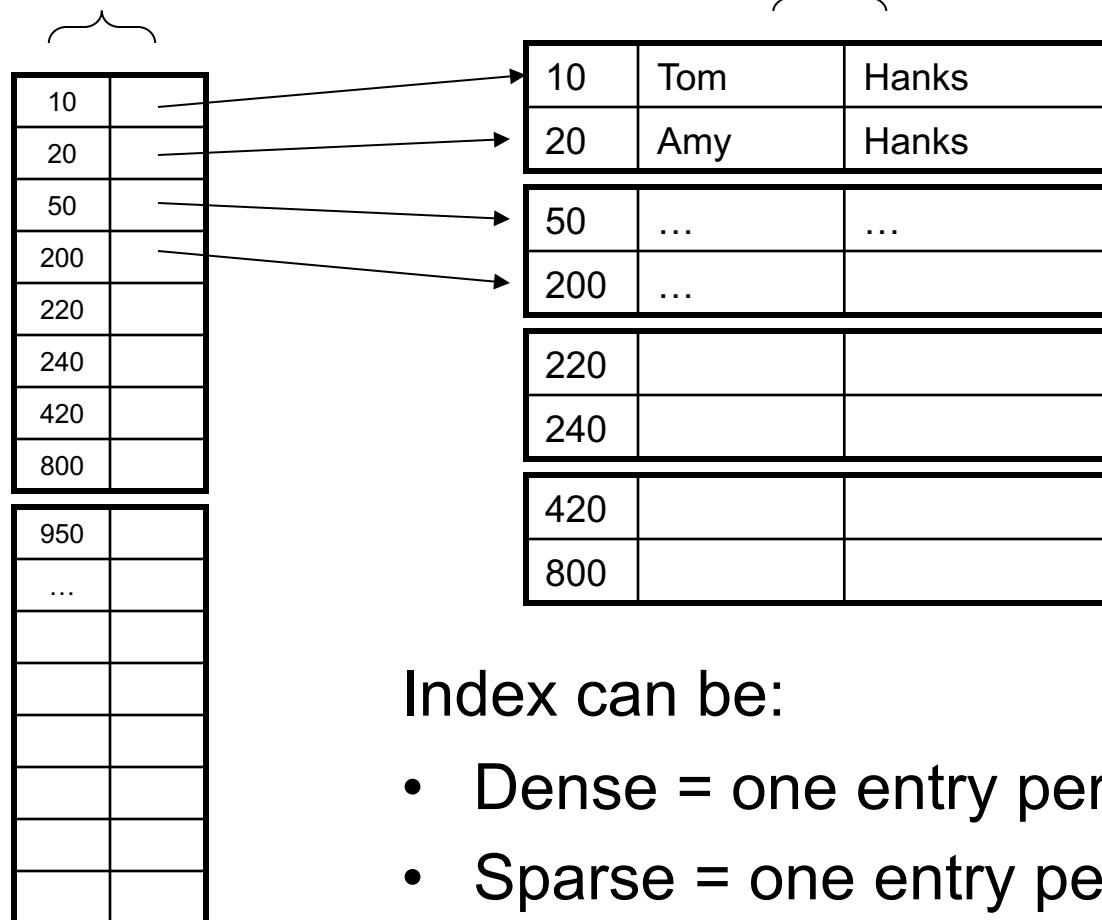
## Student

ID	fName	IName
10	Tom	Hanks
20	Amy	Hanks
...		

# Example 1: Index on ID

Index **Student\_ID** on **Student.ID**

Data File **Student**



Index can be:

- Dense = one entry per record
- Sparse = one entry per block

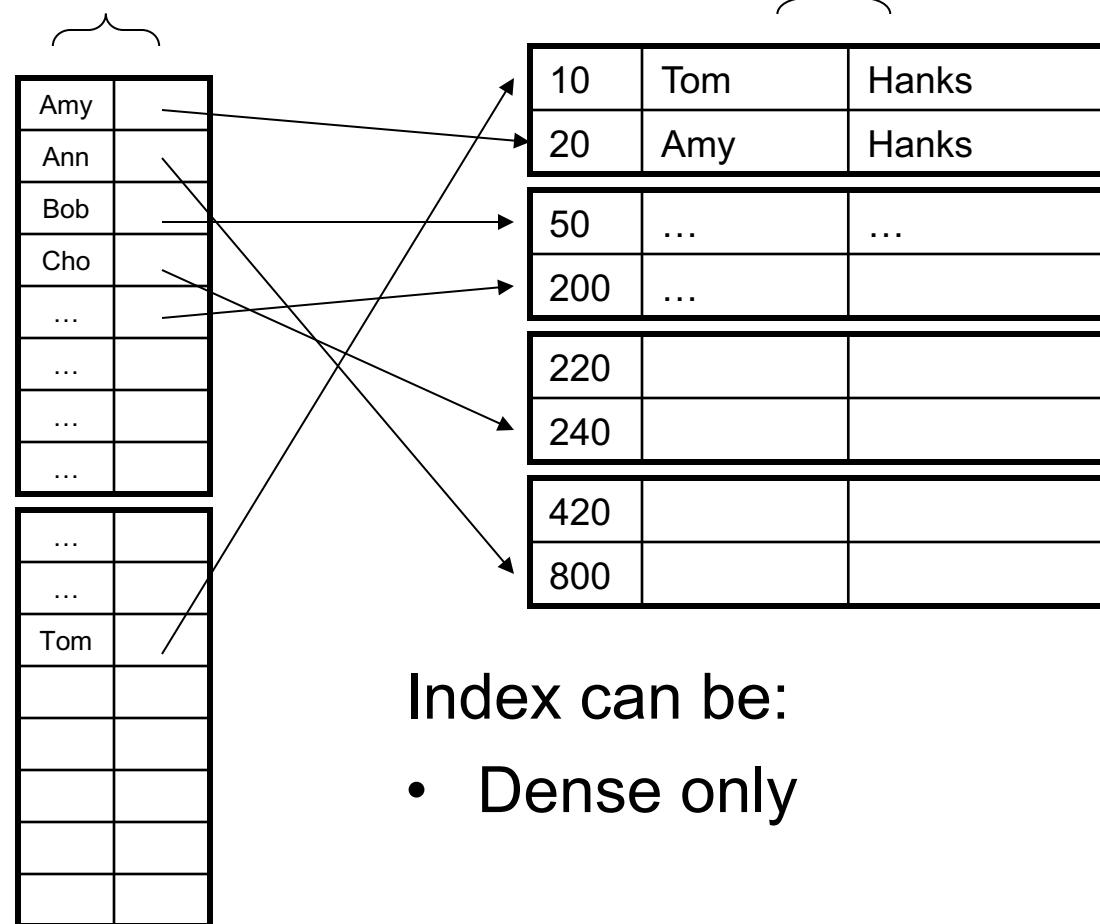
# Example 2:

## Index on fName

Index **Student\_fName**  
on **Student.fName**

Data File **Student**

ID	fName	IName
10	Tom	Hanks
20	Amy	Hanks
...		



Index can be:

- Dense only

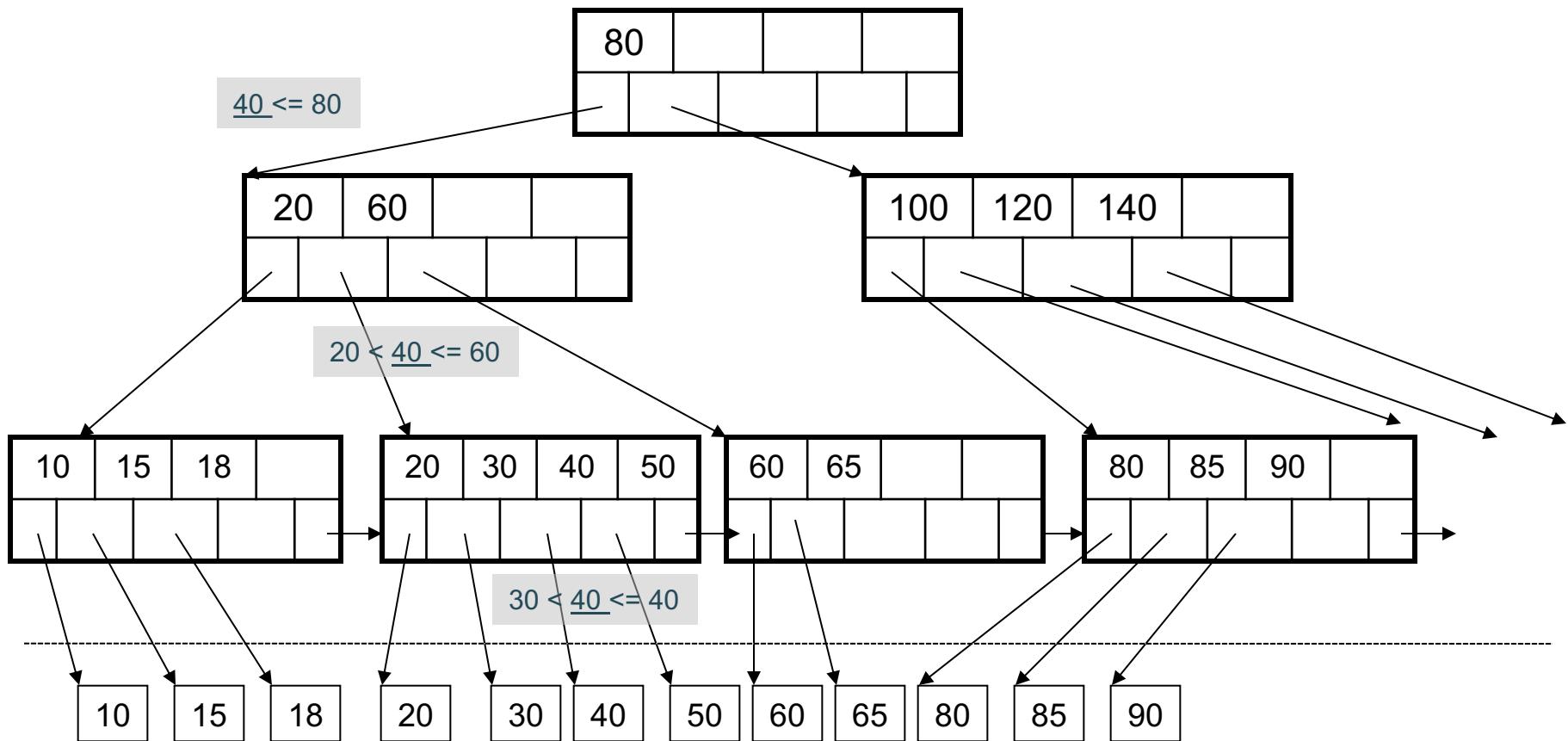
# Index Organization

- Hash table
- B+ trees – most common
  - They are search trees, but they are not binary instead have higher fan-out
  - Will discuss them briefly next
- Specialized indexes: bit maps, R-trees, inverted index; won't discuss

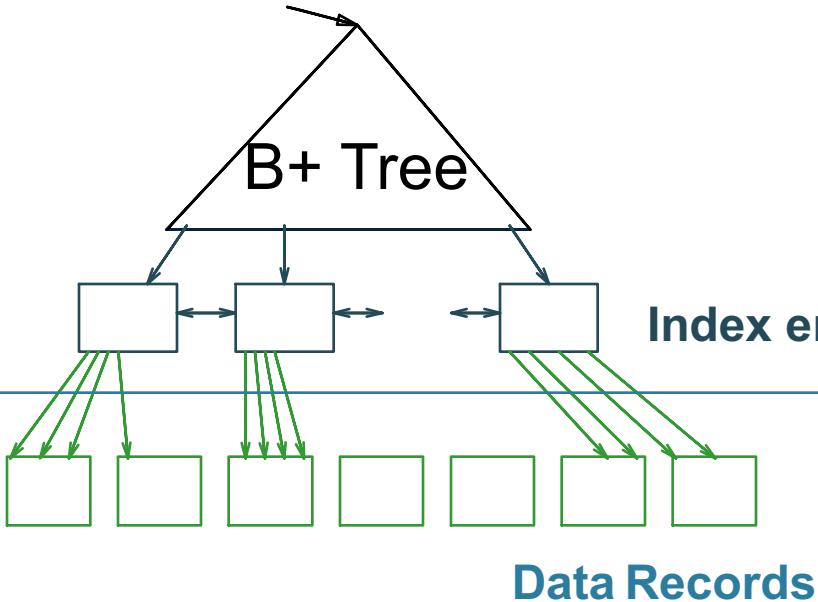
# B+ Tree Index by Example

$d = 2$

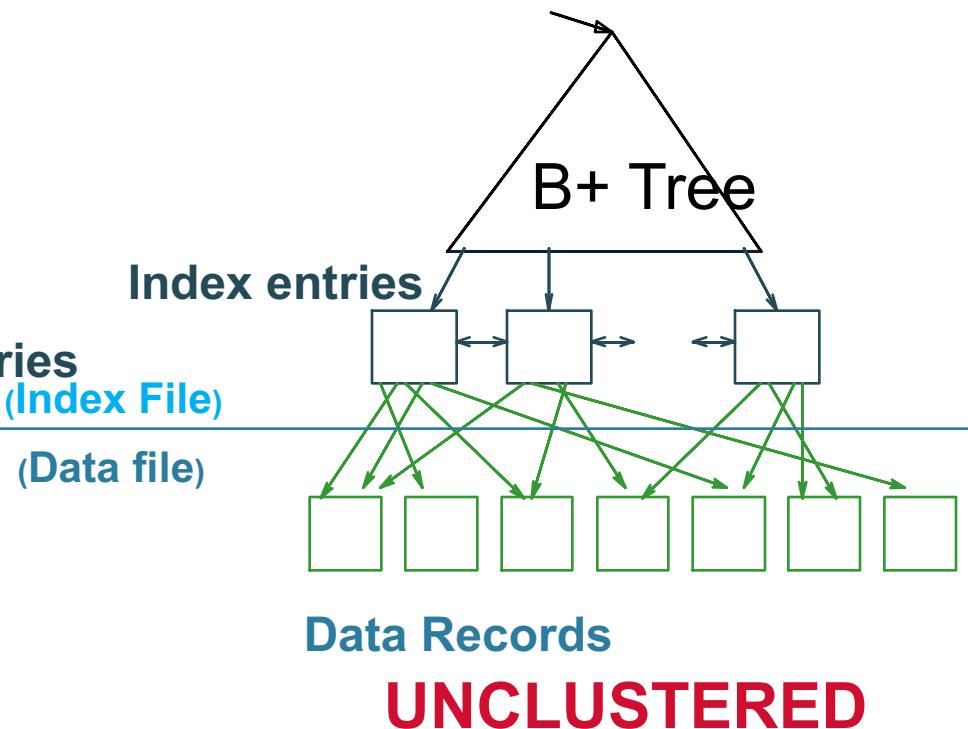
Find the key 40



# Clustered vs Unclustered



**CLUSTERED**



**UNCLUSTERED**

Every table can have **only one** clustered and **many** unclustered indexes  
Why?

# Index Classification

- **Clustered/unclustered**
  - Clustered = records close in index are close in data
    - Option 1: Data inside data file is sorted on disk
    - Option 2: Store data directly inside the index (no separate files)
  - Unclustered = records close in index may be far in data

# Index Classification

- **Clustered/unclustered**
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  - Unclustered = records close in index may be far in data
- **Primary/secondary**
  - Meaning 1:
    - Primary = is over attributes that include the primary key
    - Secondary = otherwise
  - Meaning 2: means the same as clustered/unclustered

# Index Classification

- **Clustered/unclustered**
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- **Primary/secondary**
  - Meaning 1:
    - Primary = is over attributes that include the primary key
    - Secondary = otherwise
  - Meaning 2: means the same as clustered/unclustered
- **Organization** B+ tree or Hash table

# Summary So Far

- Index = a file that enables direct access to records in another data file
  - B+ tree / Hash table
  - Clustered/unclustered
- Data resides on disk
  - Organized in blocks
  - Sequential reads are efficient
  - Random access less efficient
  - Random read 1-2% of data worse than sequential

# Main Memory Algorithms

- Selection  $\sigma$ 
  - “on-the-fly”
  - Index-based selection
- Join  $\bowtie$ :
  - Nested loop join
  - Hash join
  - Merge join
  - Index join

`Student(ID, fname, lname)`

`Takes(studentID, courseID)`

# Selection

```
SELECT *
FROM Takes y
WHERE y.courseID = 300
```

 $\sigma_{300}$ 

Takes

Logical plan

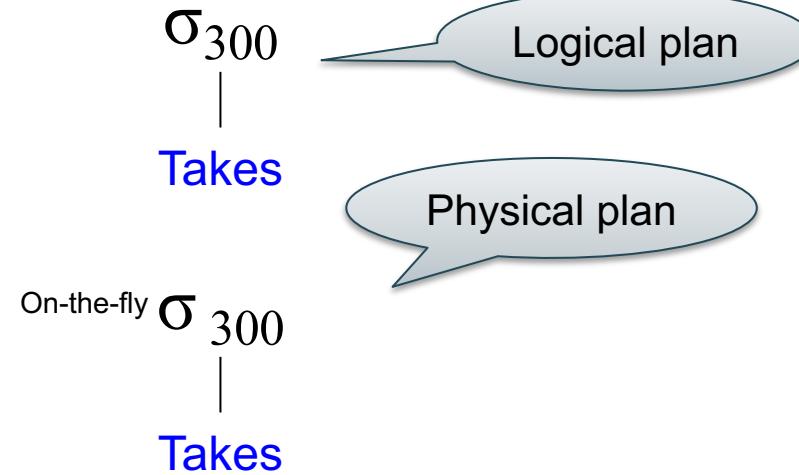
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`Takes(studentID, courseID)`

# Selection

```
SELECT *  
FROM Takes y  
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```

On-the-fly selection



Logical plan

Physical plan

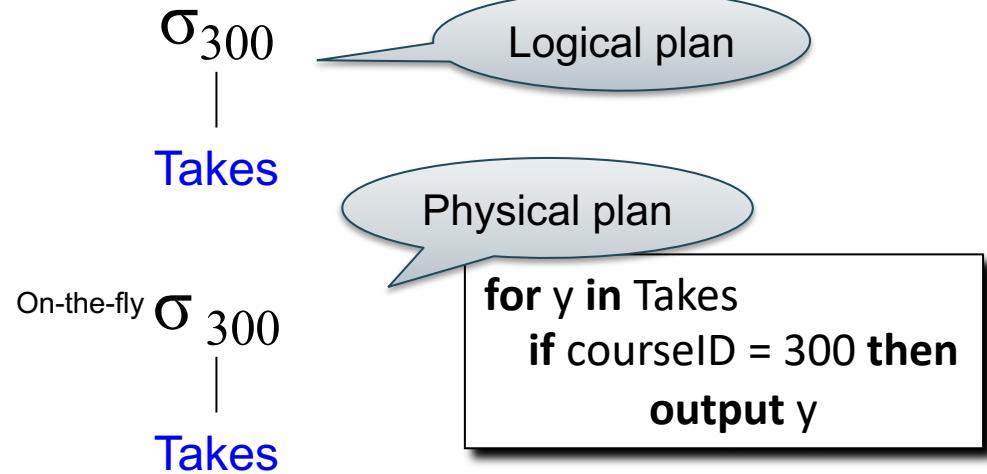
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# Selection

```
SELECT *
FROM Takes y
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```

On-the-fly selection



Student(ID, fname, lname)

Takes(studentID, courseID)

# Selection

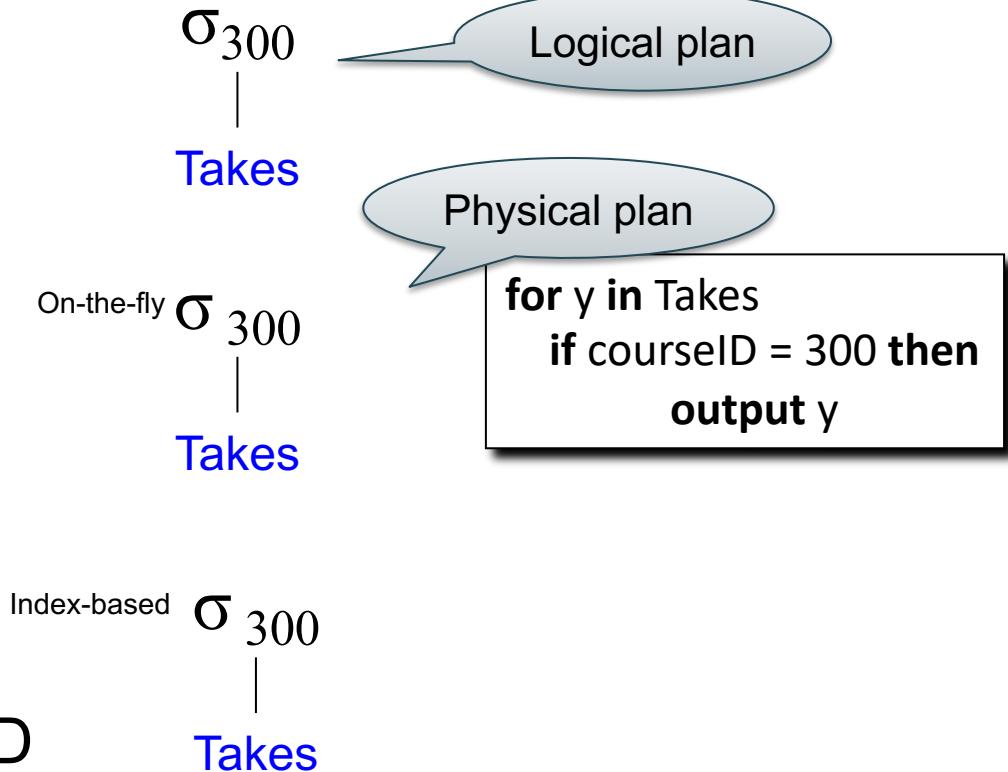
```
SELECT *
FROM Takes y
WHERE y.courseID = 300
```

On-the-fly selection

Index-based selection:

**Takes\_courseID =**

index on Takes.courseID



`Student(ID, fname, lname)`

`Takes(studentID, courseID)`

# Selection

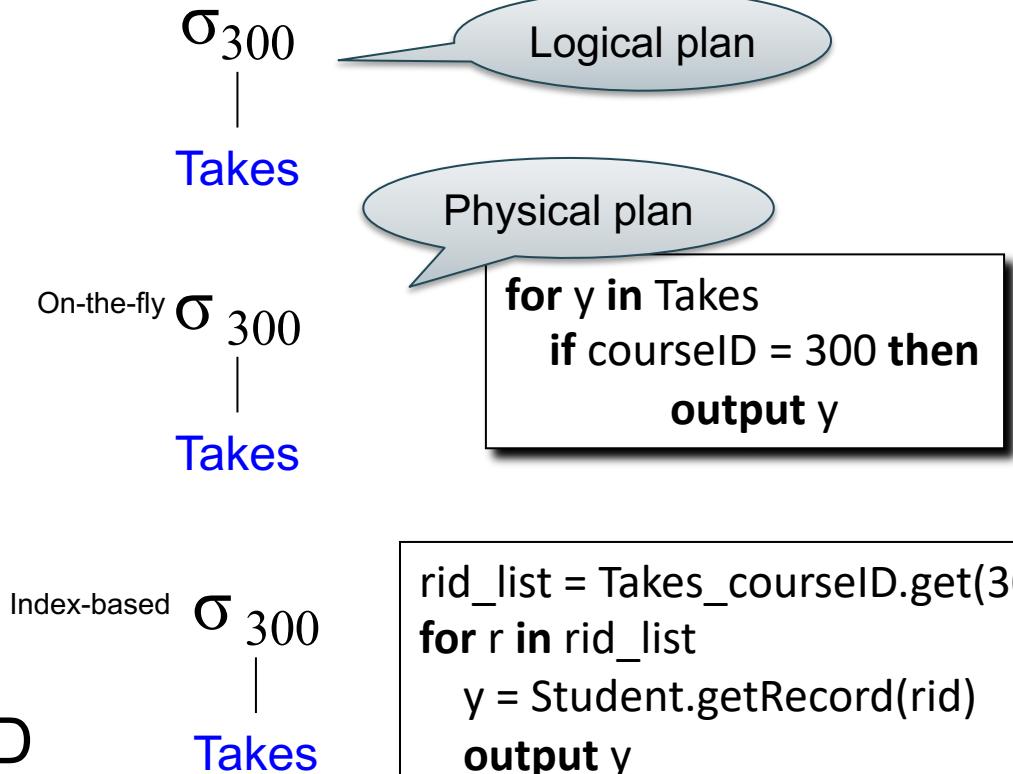
```
SELECT *
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WHERE y.courseID = 300
```

On-the-fly selection

Index-based selection:

**Takes\_courseID =**

index on `Takes.courseID`



`Student(ID, fname, lname)`

`Takes(studentID, courseID)`

# Selection

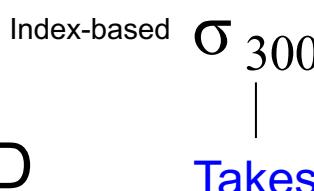
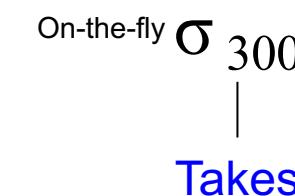
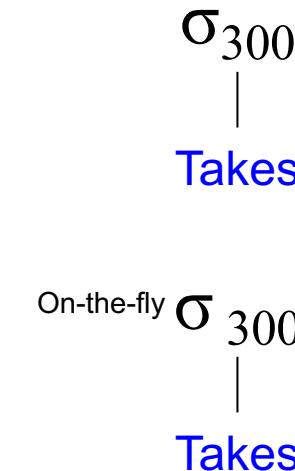
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SELECT *
FROM Takes y
WHERE y.courseID = 300
```

On-the-fly selection

Index-based selection:

**Takes\_courseID =**

index on `Takes.courseID`

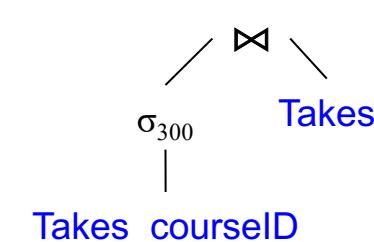


Logical plan

Physical plan

```
for y in Takes
  if courseID = 300 then
    output y
```

```
rid_list = Takes_courseID.get(300)
for r in rid_list
  y = Student.getRecord(rid)
  output y
```



SQL Server  
represents index-based  
selection as a join

Student(ID, fname, lname)

Takes(studentID, courseID)

# Discussion

Can the optimizer use the index Takes\_courseID to answer these queries?

```
SELECT *
FROM Takes y
WHERE y.courseID = 300 or y.courseID = 444
```

```
(SELECT *
FROM Takes y
WHERE y.courseID = 300)
UNION ALL
(SELECT *
FROM Takes Y
WHERE y.courseID = 444)
```

Student(ID, fname, lname)

Takes(studentID, courseID)

# Discussion

Can the optimizer use the index Takes\_courseID to answer these queries?

```
SELECT *
FROM Takes y
WHERE y.courseID = 300 or y.courseID = 444
```

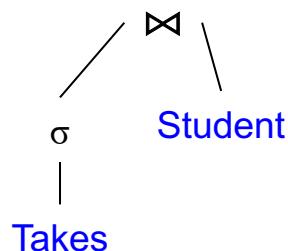
Probably not

```
(SELECT *
FROM Takes y
WHERE y.courseID = 300)
UNION ALL
(SELECT *
FROM Takes Y
WHERE y.courseID = 444)
```

Yes

Recall HW3!!

Student(ID, fname, lname)  
Takes(studentID, courseID)



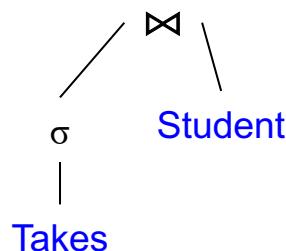
```
SELECT *
FROM Student x, Takes y
WHERE x.ID=y.studentID AND y.courseID = 300
```

# Join

Nested Loop Join:

```
for y in Takes
  if courseID = 300 then
    for x in Student
      if x.ID=y.studentID
        output *
```

Student(ID, fname, lname)  
Takes(studentID, courseID)



```
SELECT *
FROM Student x, Takes y
WHERE x.ID=y.studentID AND y.courseID = 300
```

# Join

Nested Loop Join:

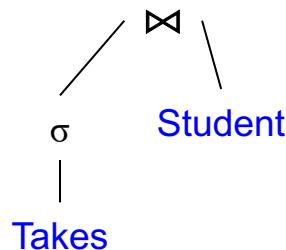
```
for y in Takes
  if courseID = 300 then
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      if x.ID=y.studentID
        output *
```

Index Join:

assume the database has these indexes

- **Takes\_courseID** = on Takes.courseID
- **Student\_ID** = on Student.ID

`Student(ID, fname, lname)`  
`Takes(studentID, courseID)`



```
SELECT *
FROM Student x, Takes y
WHERE x.ID=y.studentID AND y.courseID = 300
```

# Join

Nested Loop Join:

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  if courseID = 300 then
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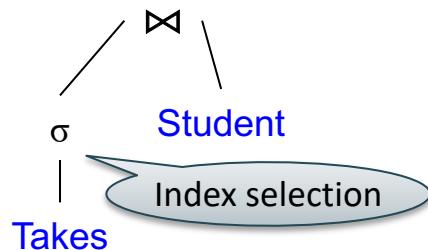
Index Join:

assume the database has these indexes

- **Takes\_courseID** = on `Takes.courseID`
- **Student\_ID** = on `Student.ID`

```
for y' in Takes_courseID.get(300)
  y = Takes.getRecord(y')
```

Student(ID, fname, lname)  
Takes(studentID, courseID)



```
SELECT *
FROM Student x, Takes y
WHERE x.ID=y.studentID AND y.courseID = 300
```

# Join

Nested Loop Join:

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for y in Takes
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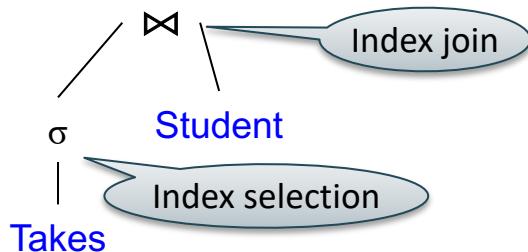
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assume the database has these indexes

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- **Student\_ID** = on Student.ID

```
for y' in Takes_courseID.get(300)
  y = Takes.getRecord(y')
```

Student(ID, fname, lname)  
Takes(studentID, courseID)



```
SELECT *
FROM Student x, Takes y
WHERE x.ID=y.studentID AND y.courseID = 300
```

# Join

Nested Loop Join:

```
for y in Takes
  if courseID = 300 then
    for x in Student
      if x.ID=y.studentID
        output *
```

Index Join:

assume the database has these indexes

- **Takes\_courseID** = on **Takes.courseID**
- **Student\_ID** = on **Student.ID**

```
for y' in Takes_courseID.get(300)
  y = Takes.getRecord(y')
  x' = Student_ID .get(y.studentID)
  x = Student.getRecord(x')
  output *
```

# Getting Practical: Creating Indexes in SQL

```
CREATE TABLE V(M int, N text, P int);
```

```
CREATE INDEX V1 ON V(N)
```

# Getting Practical: Creating Indexes in SQL

```
CREATE TABLE V(M int, N text, P int);
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```
CREATE INDEX V1 ON V(N)
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```
CREATE INDEX V2 ON V(P, M)
```

# Getting Practical: Creating Indexes in SQL

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CREATE INDEX V1 ON V(N)
```

```
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```

What does this mean?

# Getting Practical: Creating Indexes in SQL

```
CREATE TABLE V(M int, N text, P int);
```

yes

```
CREATE INDEX V1 ON V(N)
```

```
select *  
from V  
where P=55 and M=77
```

```
CREATE INDEX V2 ON V(P, M)
```

What does this mean?

# Getting Practical: Creating Indexes in SQL

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```
CREATE INDEX V2 ON V(P, M)
```

What does this mean?

```
select *  
from V  
where P=55
```

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```

```
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from V  
where P=55 and M=77
```

```
CREATE INDEX V2 ON V(P, M)
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What does this mean?

```
select *  
from V  
where P=55
```

yes

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```
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from V  
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```

yes

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```
CREATE INDEX V2 ON V(P, M)
```

What does this mean?

```
select *  
from V  
where P=55
```

yes

```
select *  
from V  
where M=77
```

no

# Getting Practical: Creating Indexes in SQL

```
CREATE TABLE V(M int, N text, P int);
```

yes

```
CREATE INDEX V1 ON V(N)
```

```
select *  
from V  
where P=55 and M=77
```

```
CREATE INDEX V2 ON V(P, M)
```

What does this mean?

```
CREATE INDEX V3 ON V(M, N)
```

```
select *  
from V  
where P=55
```

```
CREATE UNIQUE INDEX V4 ON V(N)
```

```
select *  
from V  
where M=77
```

```
CREATE CLUSTERED INDEX V5 ON V(N)
```

yes

no

Not supported  
in SQLite

# Which Indexes?

ID	fName	IName
10	Tom	Hanks
20	Amy	Hanks
...		

- How many indexes **could** we create?
- Which indexes **should** we create?

ID	fName	IName
10	Tom	Hanks
20	Amy	Hanks
...		

# Which Indexes?

- How many indexes **could** we create?
- Which indexes **should** we create?

This is called the ***Index Selection Problem***

(not to be confused with the **index selection** operator!)

# The Index Selection Problem 1

V(M, N, P);

Your workload is this

100000 queries:

```
SELECT *
FROM V
WHERE N=?
```

100 queries:

```
SELECT *
FROM V
WHERE P=?
```

# The Index Selection Problem 1

V(M, N, P);

Your workload is this

100000 queries:

```
SELECT *
FROM V
WHERE N=?
```

100 queries:

```
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FROM V
WHERE P=?
```

What indexes ?

# The Index Selection Problem 1

V(M, N, P);

Your workload is this

100000 queries:

```
SELECT *
FROM V
WHERE N=?
```

100 queries:

```
SELECT *
FROM V
WHERE P=?
```

A: V(N) and V(P) (hash tables or B-trees)

# The Index Selection Problem 2

V(M, N, P);

Your workload is this

100000 queries:

```
SELECT *  
FROM V  
WHERE N>? and N<?
```

100 queries:

```
SELECT *  
FROM V  
WHERE P=?
```

100000 queries:

```
INSERT INTO V  
VALUES (?, ?, ?)
```

What indexes ?

# The Index Selection Problem 2

$V(M, N, P)$ :

Your workload is this

100000 queries:

```
SELECT *  
FROM V  
WHERE N>? and N<?
```

100 queries:

```
SELECT *  
FROM V  
WHERE P=?
```

100000 queries:

```
INSERT INTO V  
VALUES (?, ?, ?)
```

A: definitely  $V(N)$  (must B-tree); unsure about  $V(P)$

# The Index Selection Problem 3

V(M, N, P);

Your workload is this

100000 queries: 1000000 queries: 100000 queries:

SELECT \*  
FROM V  
WHERE N=?

SELECT \*  
FROM V  
WHERE N=? and P>?

INSERT INTO V  
VALUES (?, ?, ?)

What indexes ?

# The Index Selection Problem 3

$V(M, N, P);$

Your workload is this

100000 queries: 1000000 queries: 100000 queries:

**SELECT \***  
**FROM V**  
**WHERE N=?**

**SELECT \***  
**FROM V**  
**WHERE N=? and P>?**

**INSERT INTO V  
VALUES (?, ?, ?)**

A:  $V(N, P)$

How does this index differ from:  
1. Two indexes  $V(N)$  and  $V(P)$ ?  
2. An index  $V(P, N)$ ?

# The Index Selection Problem 4

V(M, N, P);

Your workload is this

1000 queries:

```
SELECT *  
FROM V  
WHERE N>? and N<?
```

100000 queries:

```
SELECT *  
FROM V  
WHERE P>? and P<?
```

What indexes ?

# The Index Selection Problem 4

$V(M, N, P);$

Your workload is this

1000 queries:

```
SELECT *
FROM V
WHERE N>? and N<?
```

100000 queries:

```
SELECT *
FROM V
WHERE P>? and P<?
```

A:  $V(N)$  secondary,  $V(P)$  primary index

# Two typical kinds of queries

```
SELECT *
FROM Movie
WHERE year = ?
```

- Point queries
- Hash- or B<sup>+</sup>-tree index
- Clustered or not

```
SELECT *
FROM Movie
WHERE year >= ? AND
      year <= ?
```

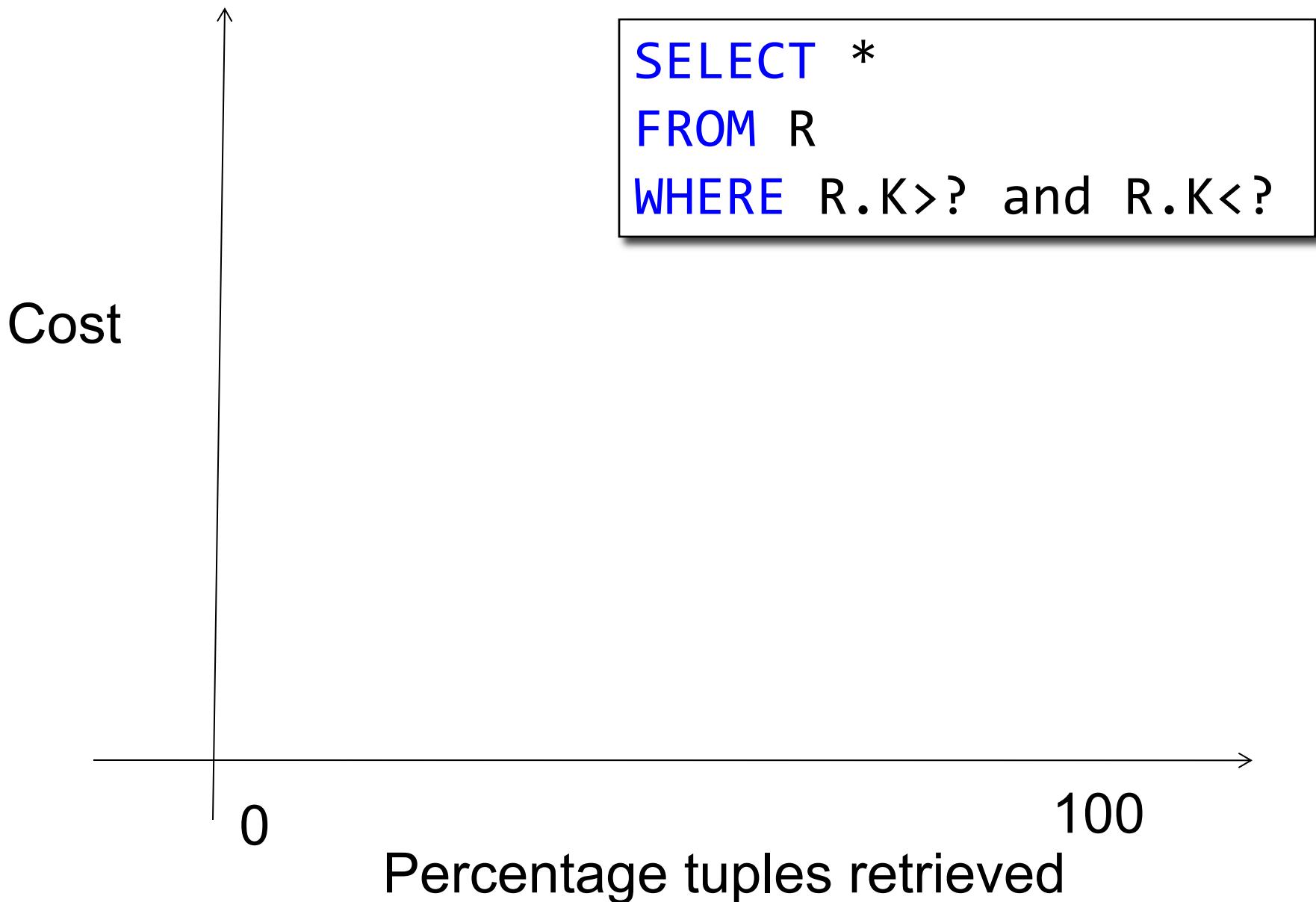
- Range queries
- B<sup>+</sup>-tree index
- Clustered

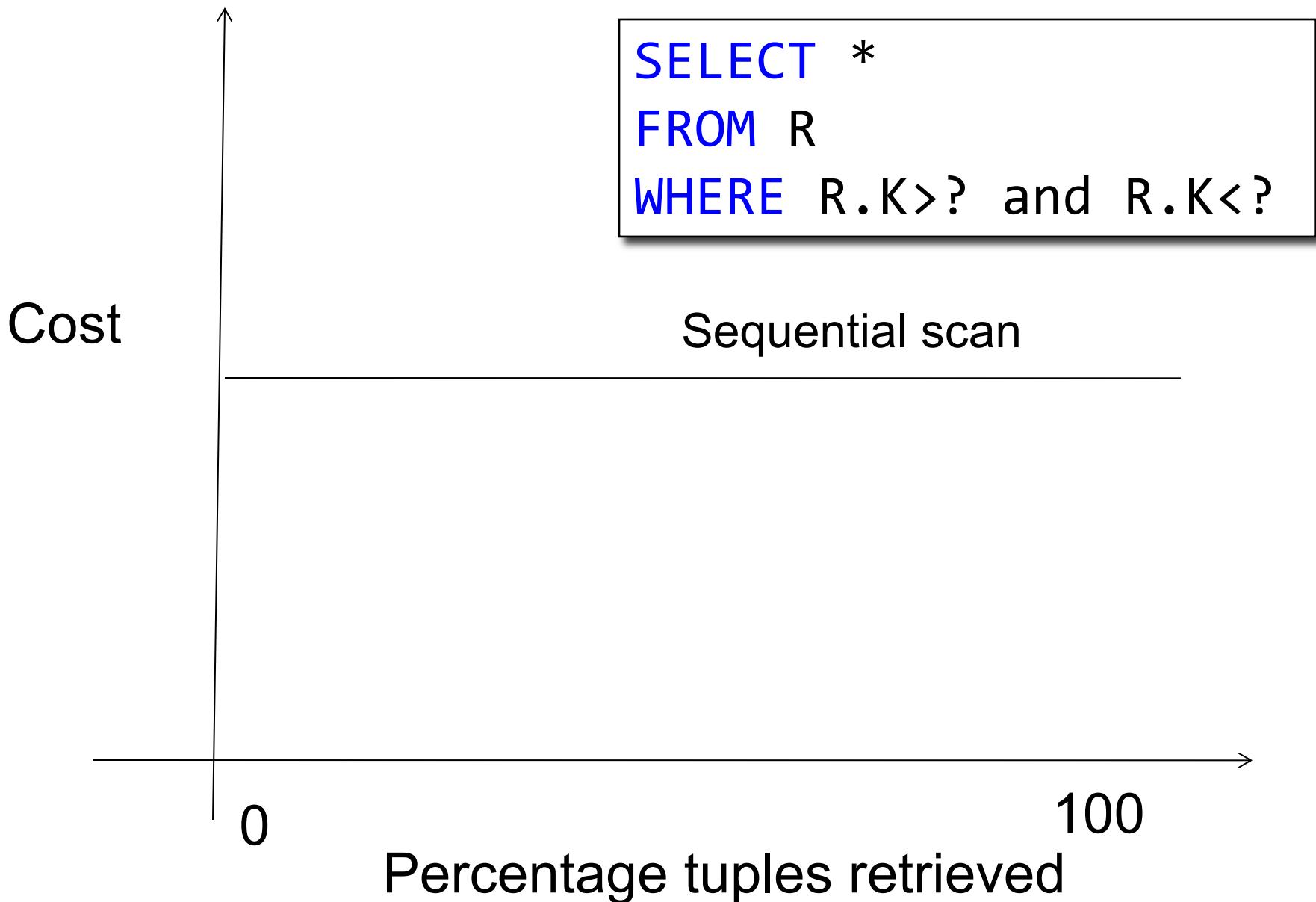
# To Cluster or Not

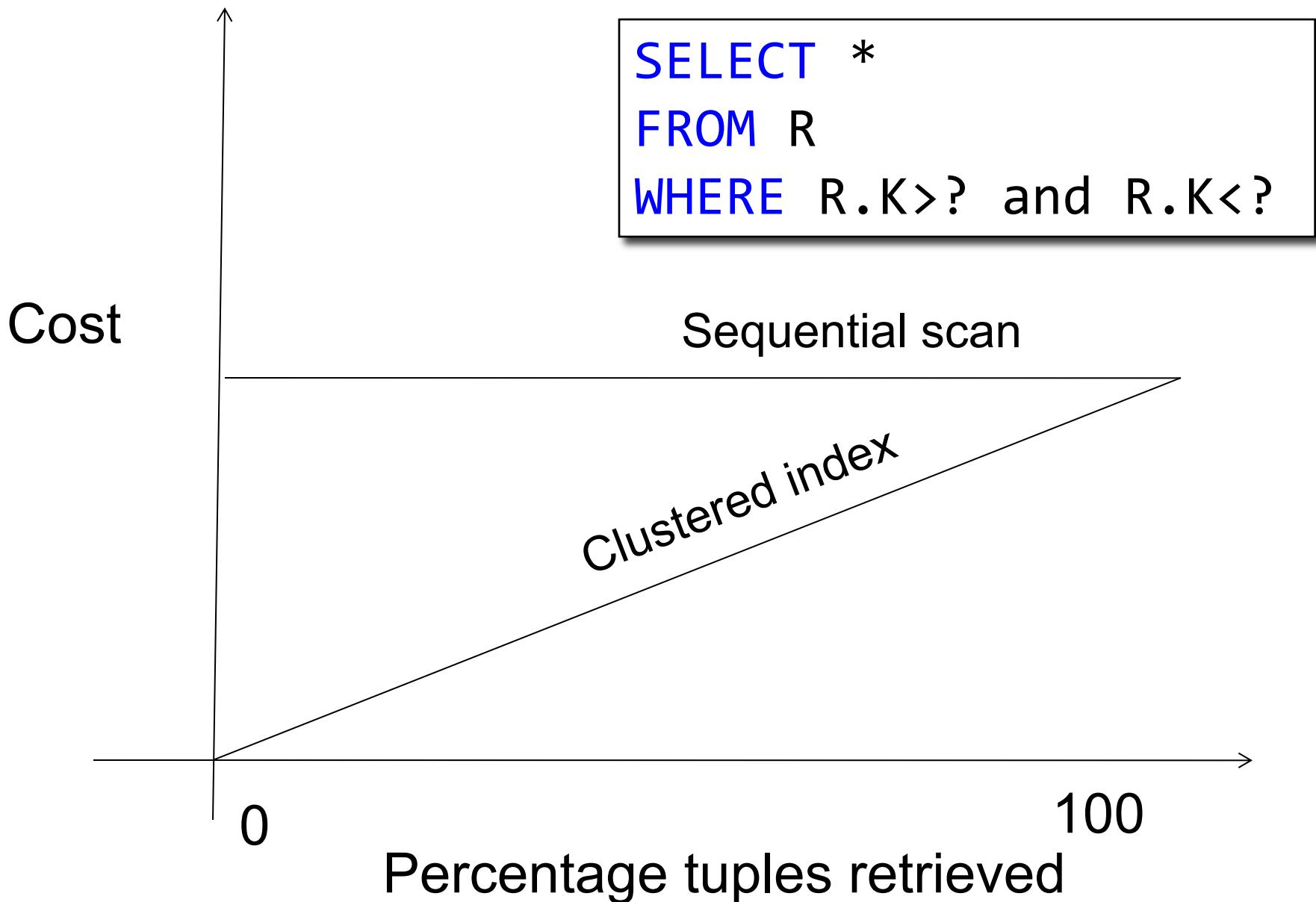
Remember:

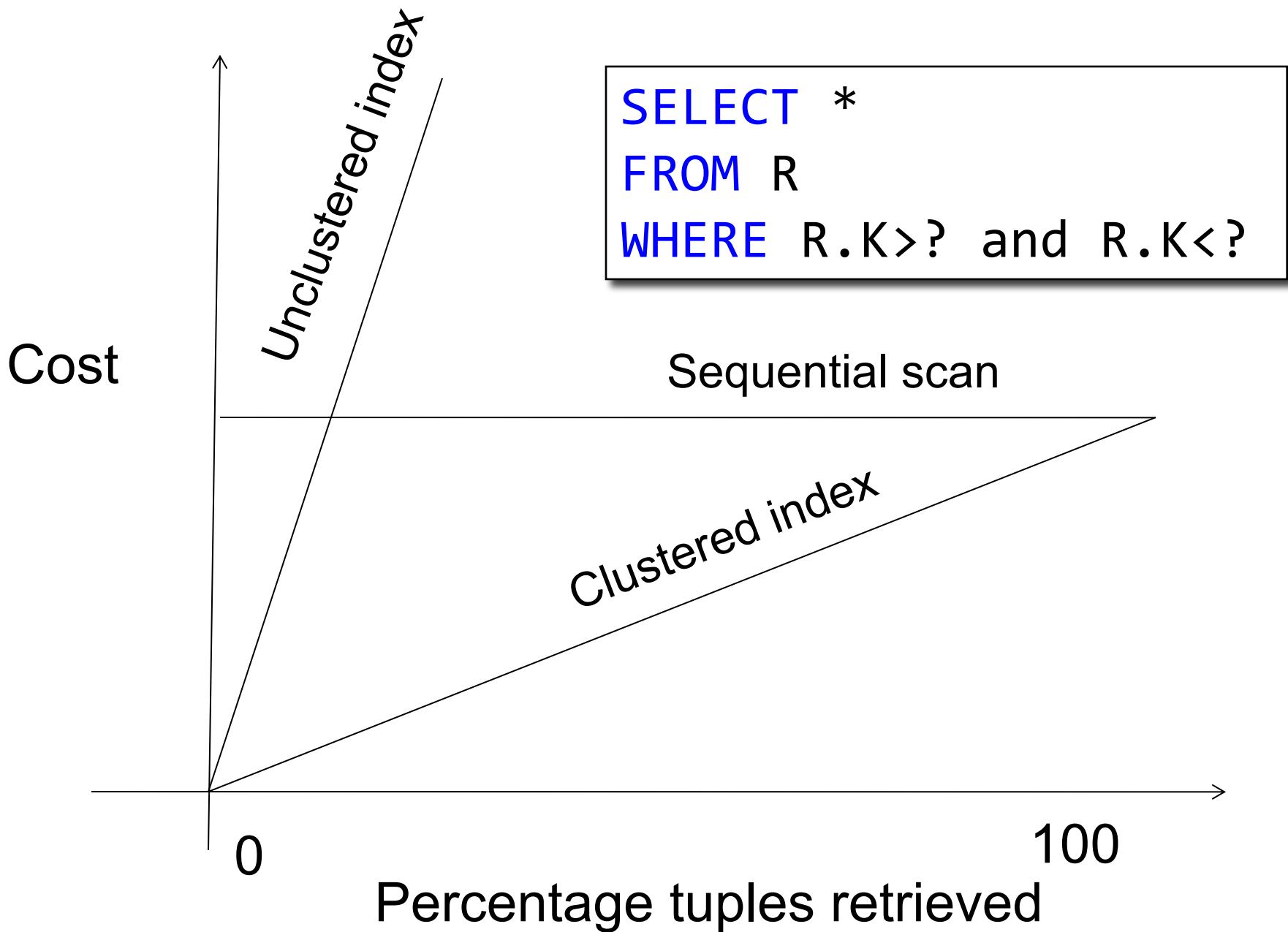
- **Rule of thumb:**  
Random reading 1-2% of file  $\approx$  sequential scan entire file;

Range queries benefit mostly from clustering because they may read more than 1-2%









# Summary of Physical Plan

More components of a physical plan:

- **Access path selection** for each relation
  - Scan the relation or use an index
- **Implementation choice** for each operator
  - Nested loop join, hash join, etc.
- **Scheduling decisions** for operators
  - Pipelined execution or intermediate materialization

# Introduction to Database Systems

## CSE 344

Lecture 17:  
Basics of Query Optimization and  
Query Cost Estimation

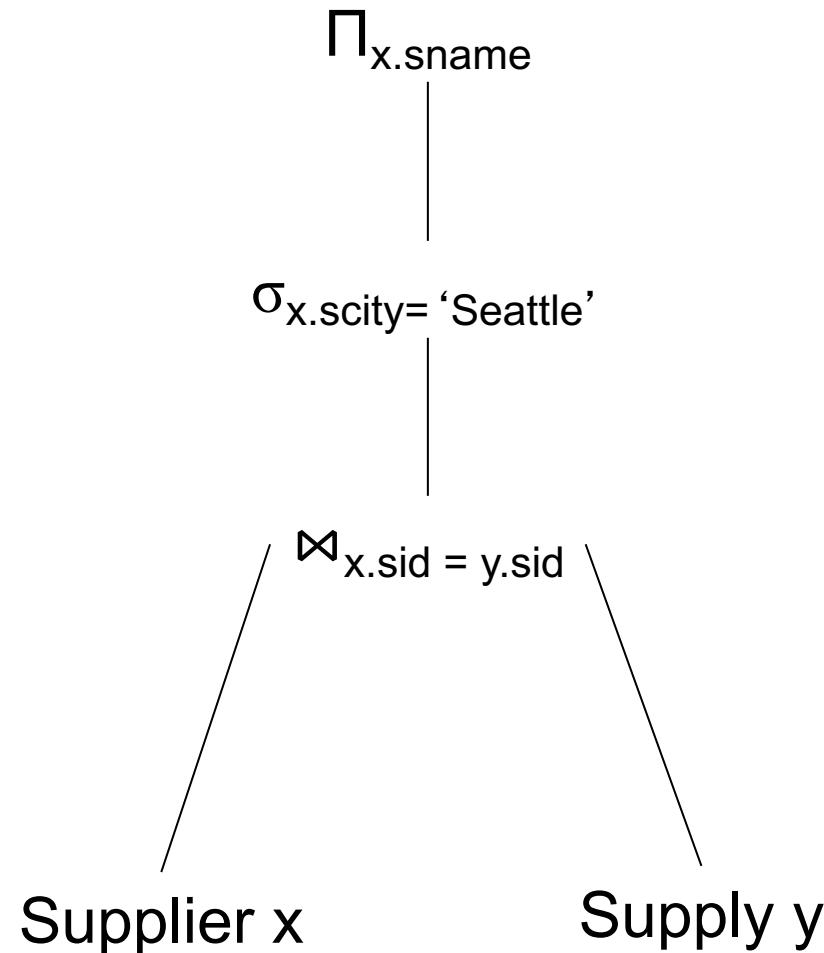
# Query Optimization

- Main idea: replace a query plan with another one that is equivalent, but cheaper
- Algebraic identities of the relational algebra
- Will discuss:
  1. Pushing selections down
  2. Join reorder

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

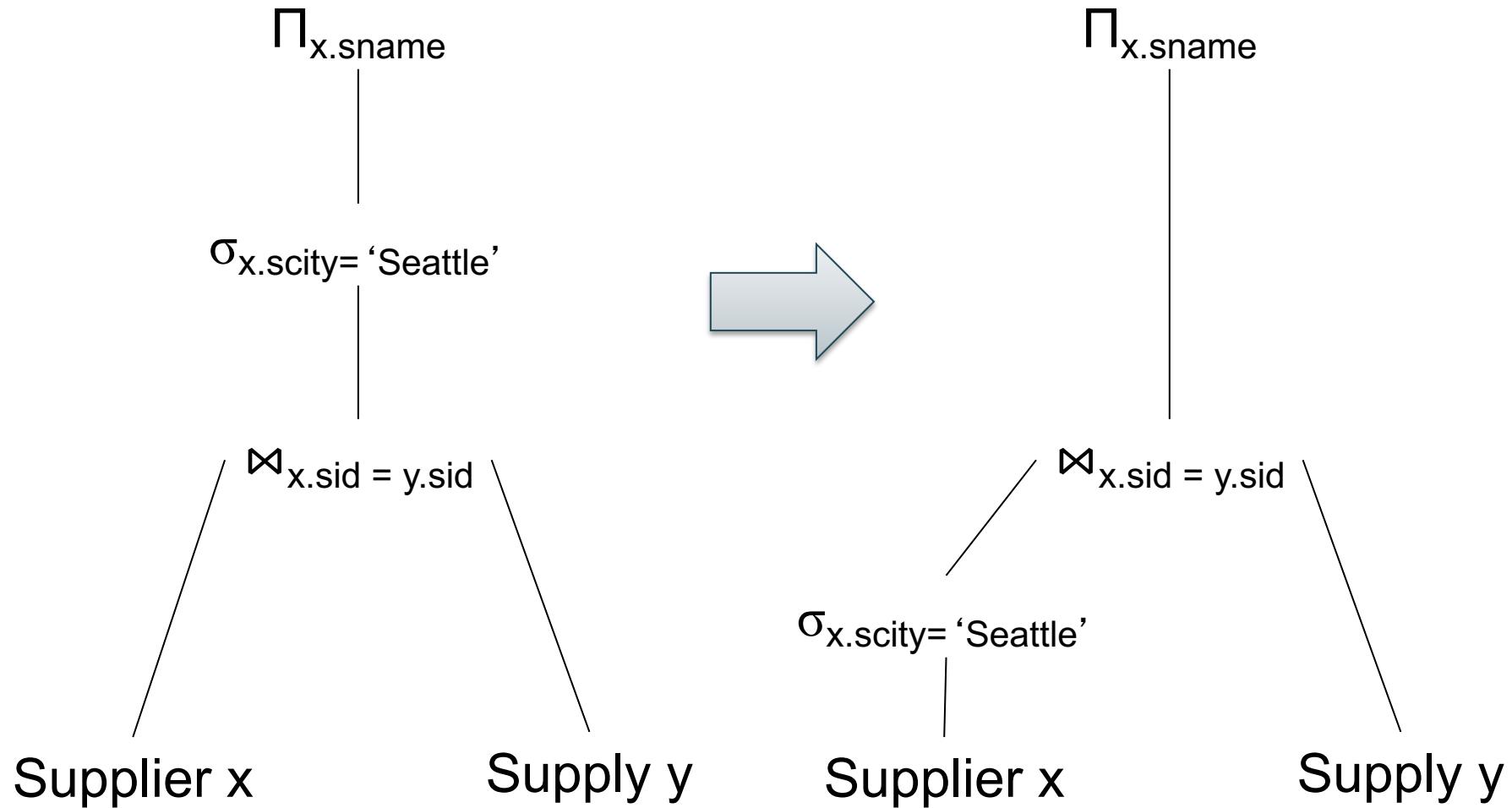
# Push Selections Down



`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

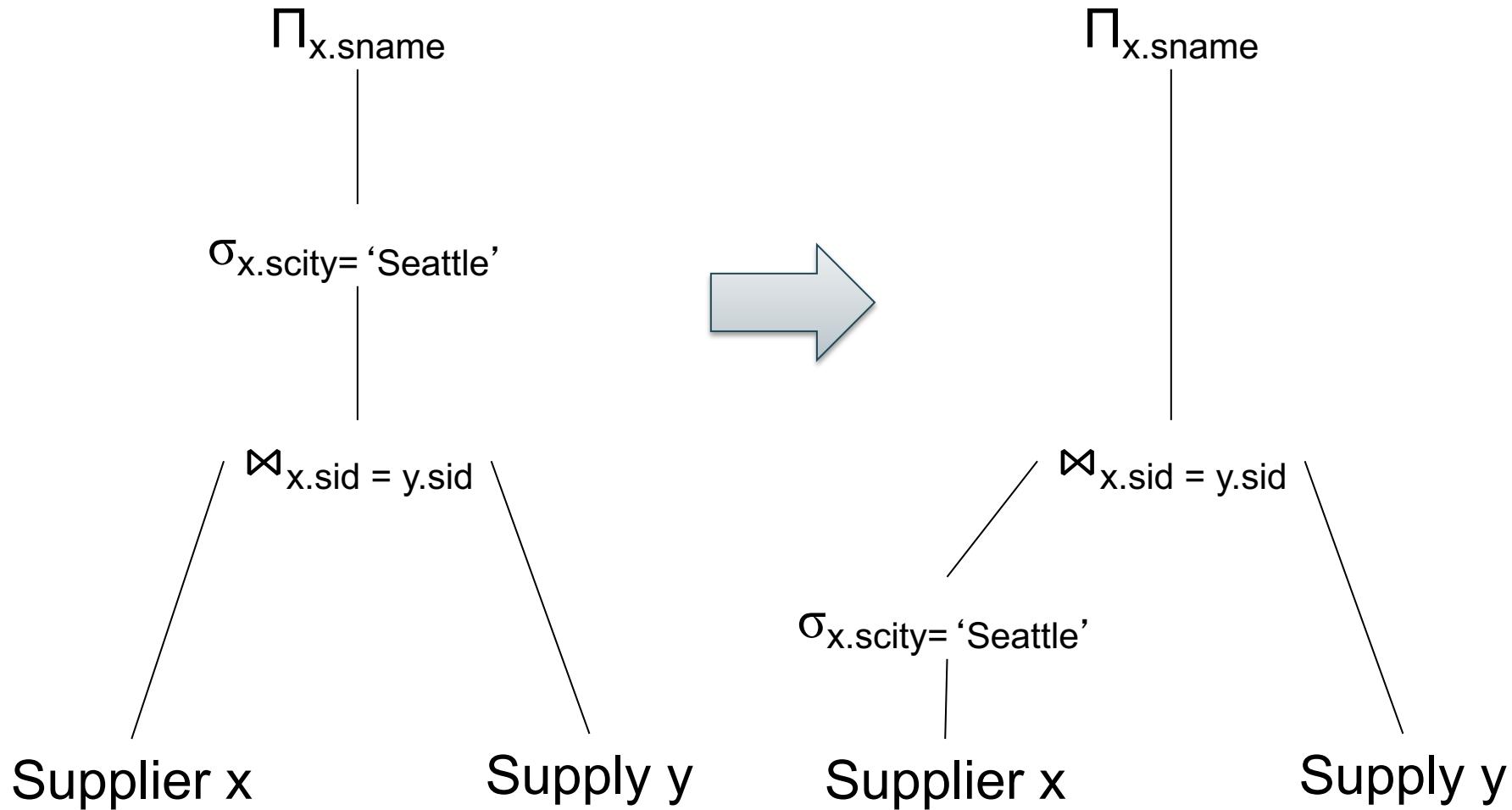
# Push Selections Down



`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Push Selections Down



$$\sigma_C(R \bowtie S) = \sigma_C(R) \bowtie S \quad \text{when } C \text{ refers only to } R$$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

# Push Selections Down

$\Pi_{x.sname}$

$\sigma_{x.scity = \text{'Seattle'} \text{ and } y.pno = 5}$

$\bowtie_{x.sid = y.sid}$

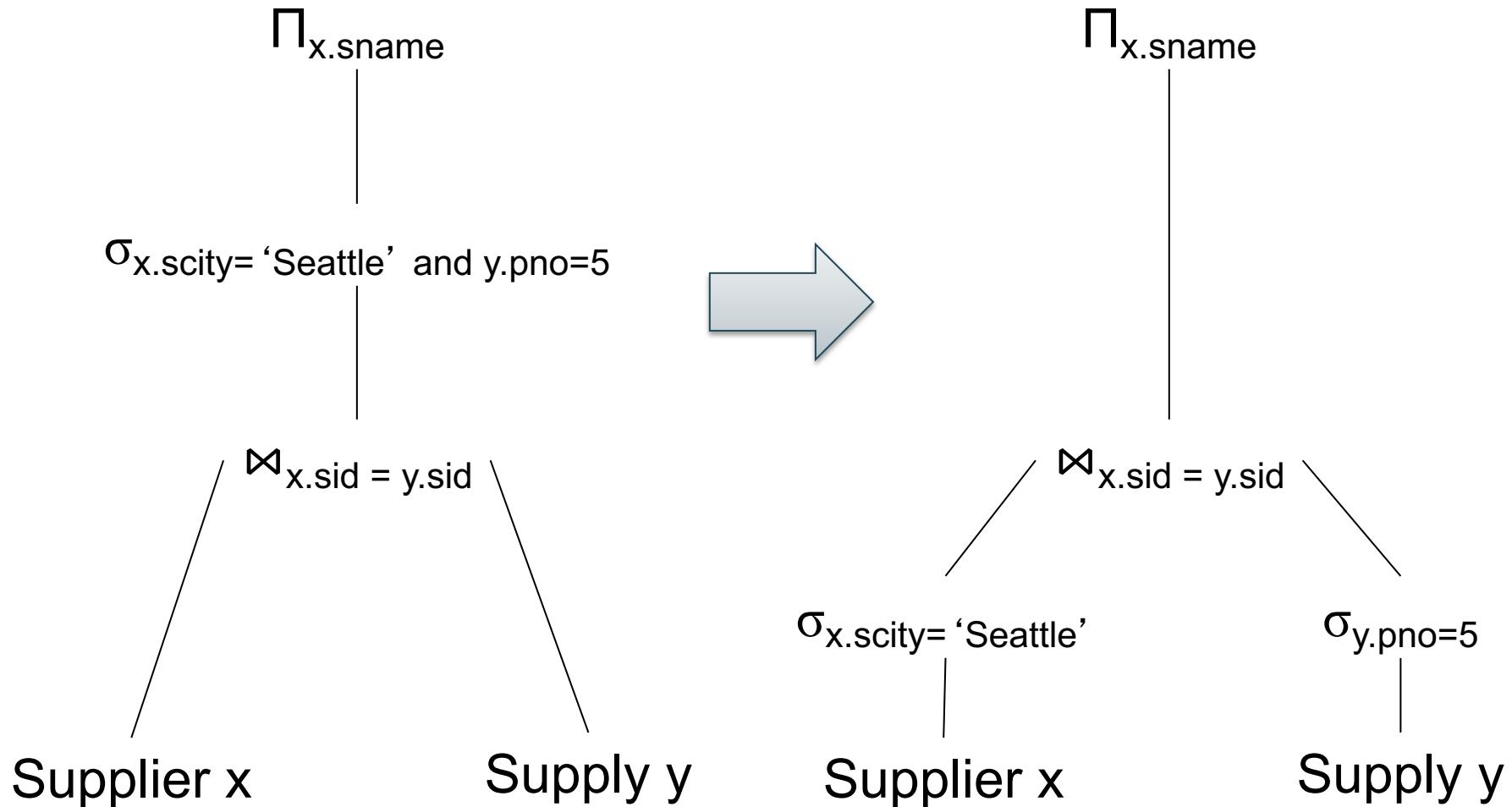
Supplier x

Supply y

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

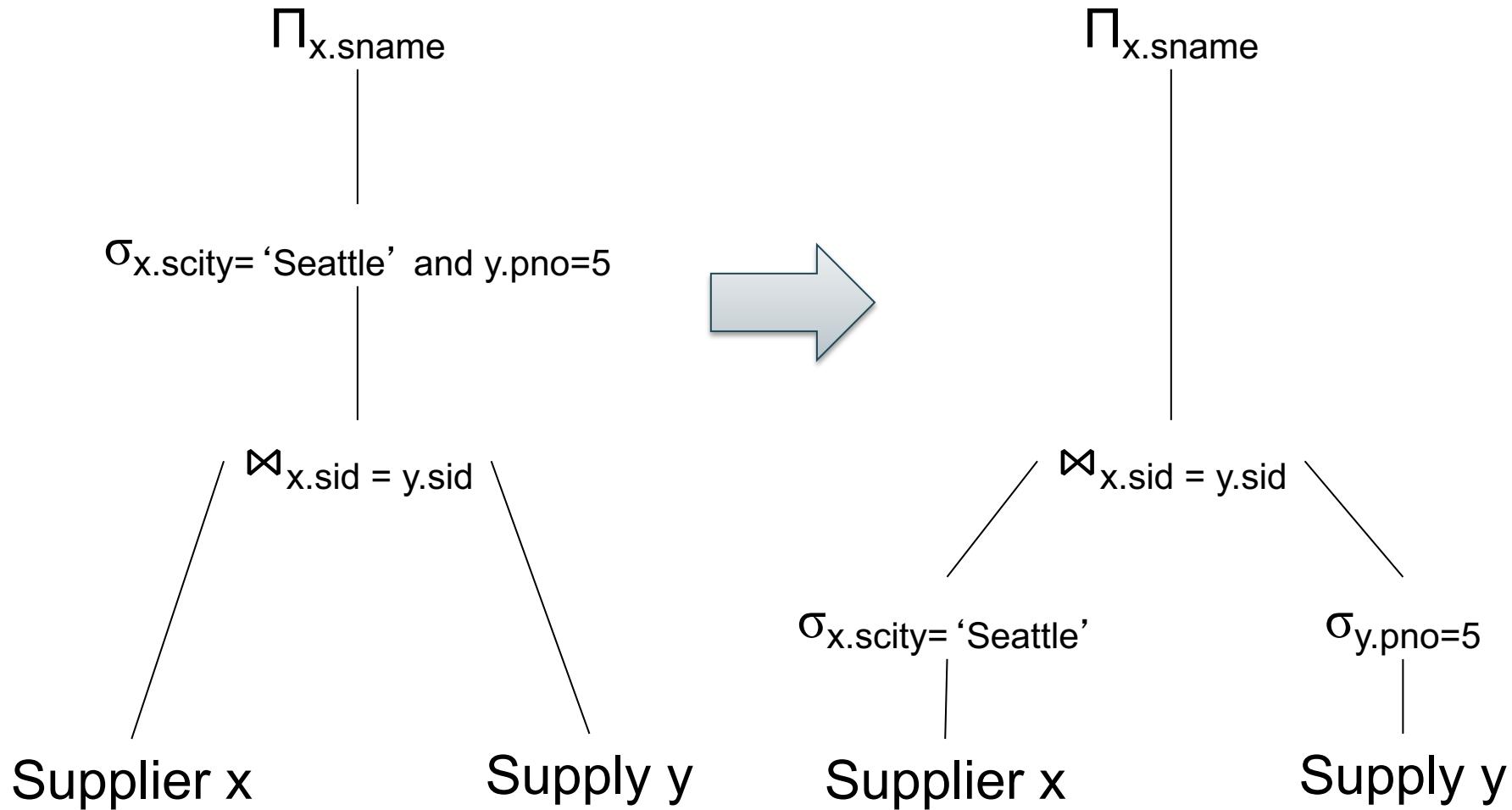
# Push Selections Down



$\text{Supplier}(\underline{\text{sid}}, \text{pname}, \text{scity}, \text{sstate})$

$\text{Supply}(\underline{\text{sid}}, \text{pno}, \text{quantity})$

# Push Selections Down



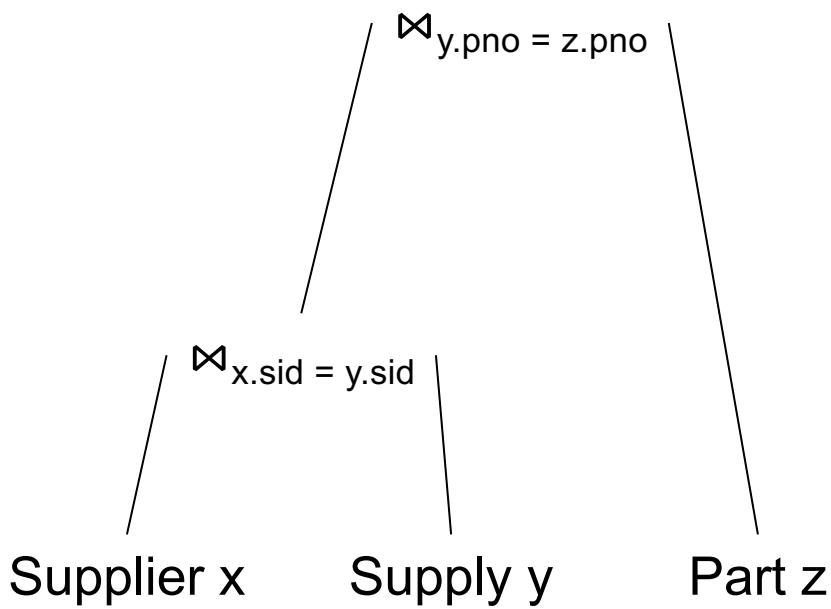
$$\sigma_{C_1 \text{ and } C_2}(R \bowtie S) = \sigma_{C_1}(\sigma_{C_2}(R \bowtie S)) = \sigma_{C_1}(R \bowtie \sigma_{C_2}(S)) = \sigma_{C_1}(R) \bowtie \sigma_{C_2}(S)$$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

# Join Reorder

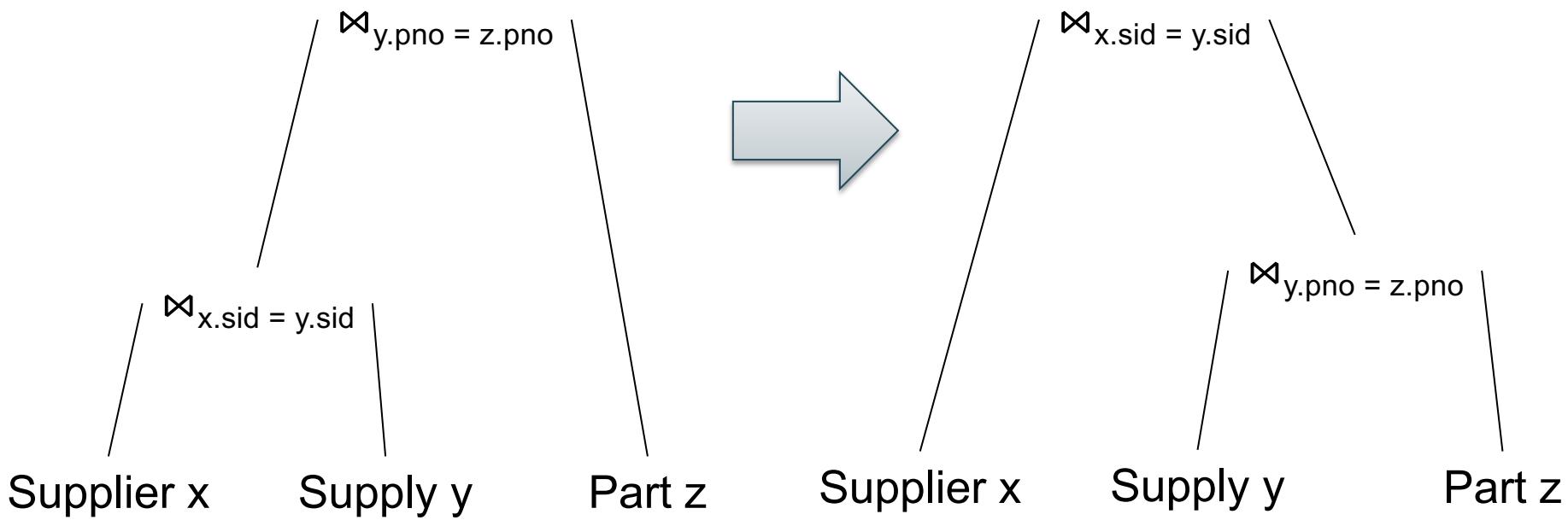


*Supplier*(sid, sname, scity, sstate)

*Supply*(sid, pno, quantity)

*Part*(pno, pname, pprice)

# Join Reorder

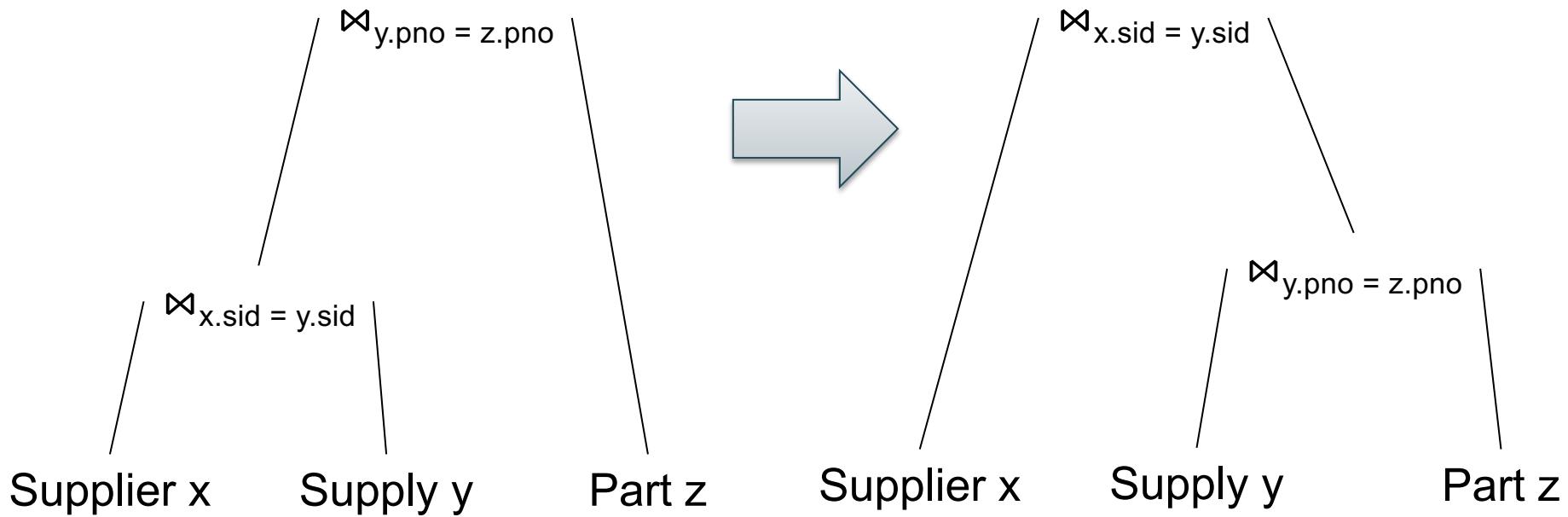


*Supplier*(sid, sname, scity, sstate)

*Supply*(sid, pno, quantity)

*Part*(pno, pname, pprice)

# Join Reorder



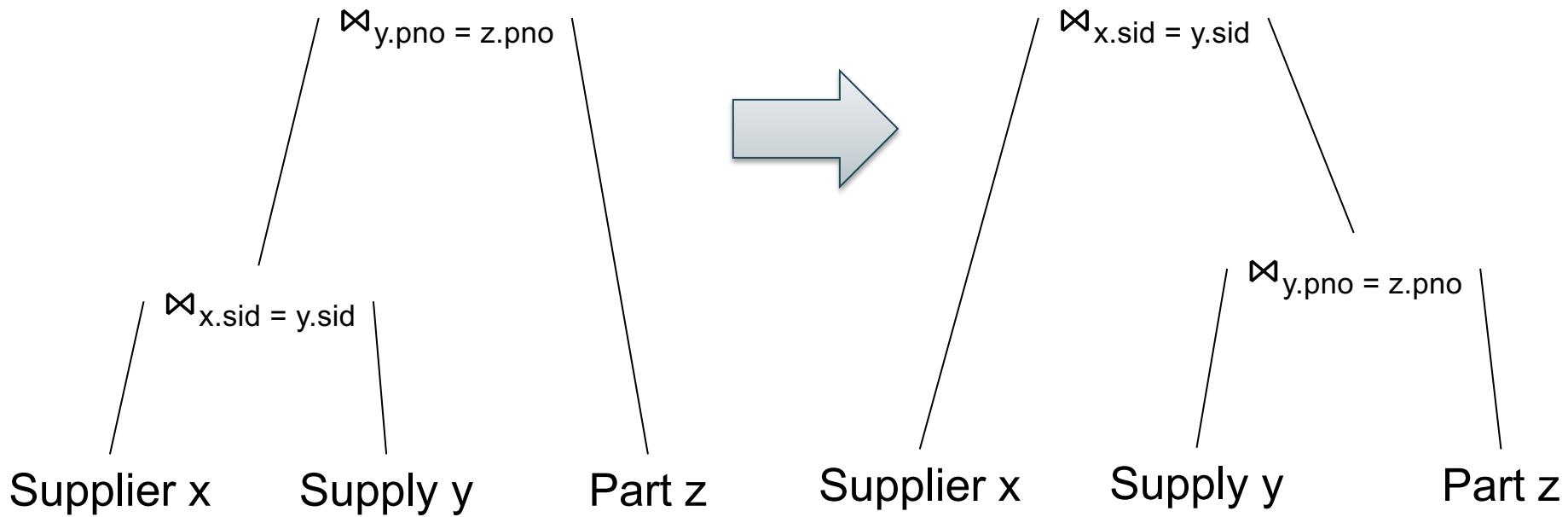
$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

*Supplier(sid, sname, scity, sstate)*

*Supply(sid, pno, quantity)*

*Part(pno, pname, pprice)*

# Join Reorder



$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

Also:

$$R \bowtie S = S \bowtie R$$

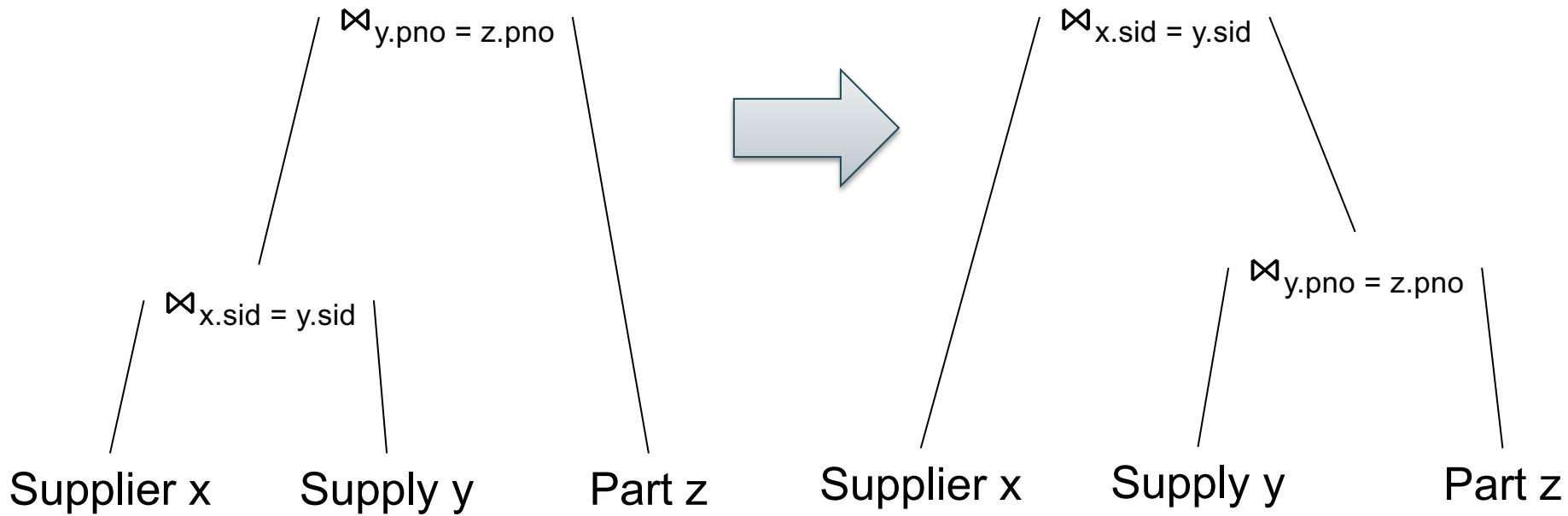
`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

# Join Reorder

When is one plan better than the other?



$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

Also:

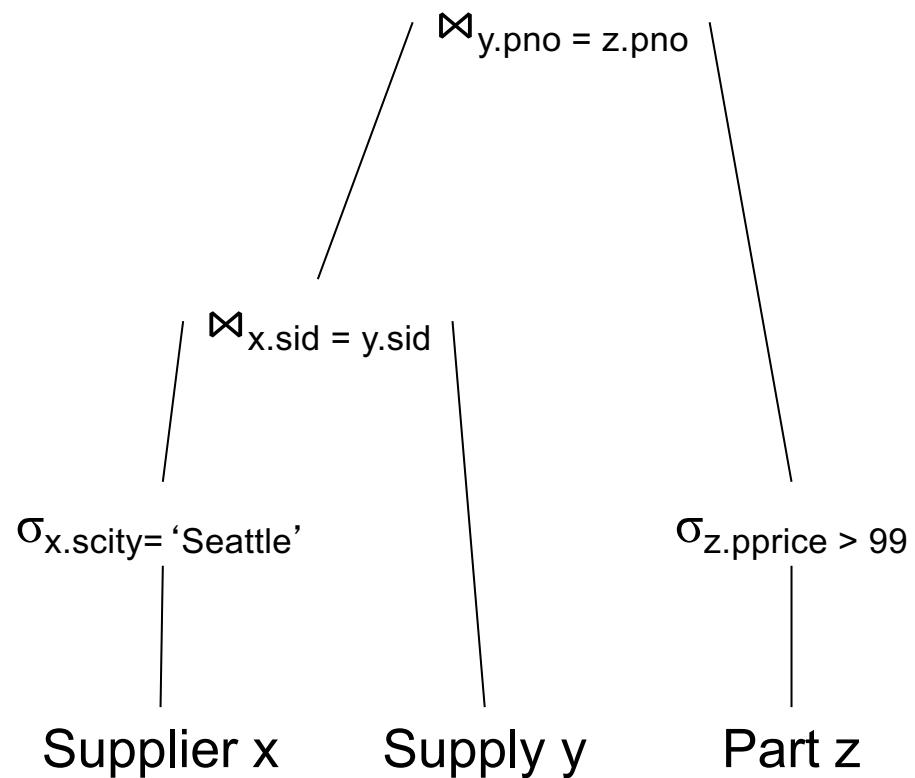
$$R \bowtie S = S \bowtie R$$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

# Join Reorder



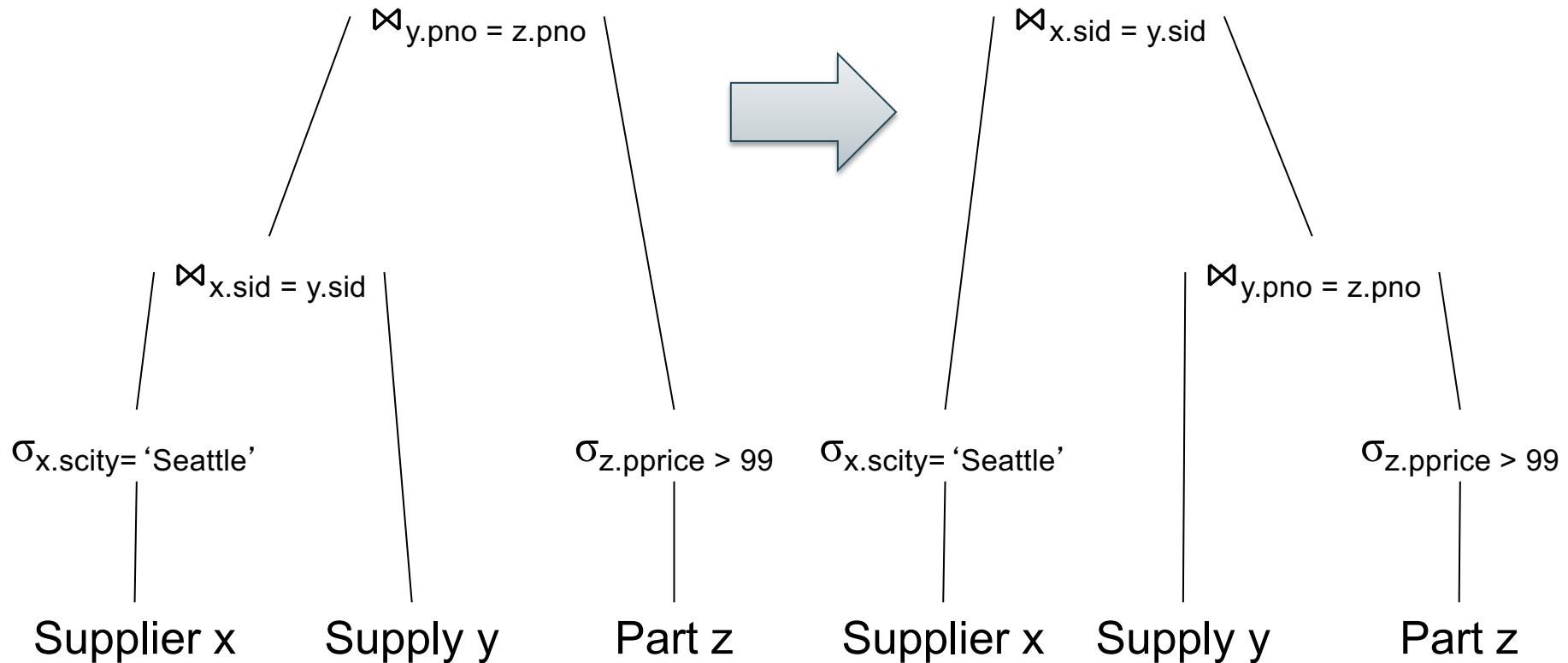
`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

# Join Reorder

When is one plan better than the other?



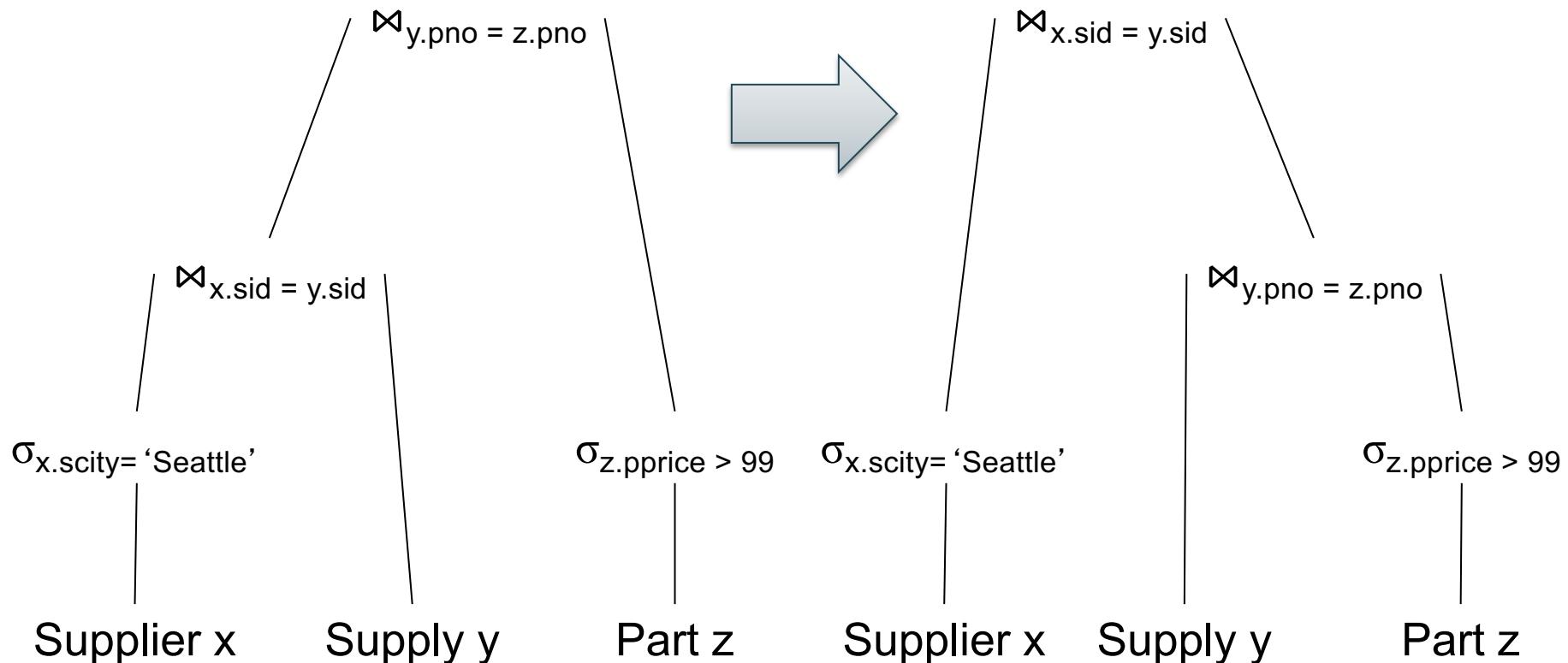
`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

# Join Reorder

When is one plan better than the other?



Lesson: need sizes of  $\sigma_{x.scity = 'Seattle'}$  (Supplier),  $\sigma_{z.pprice > 99}$  (Part)

# Size and Cost Estimation

Given statistics on the base tables:

- $B(R)$  = # of blocks (i.e., pages) for relation R
- $T(R)$  = # of tuples in relation R
- $V(R, A)$  = # of distinct values of attribute A

Size estimation: estimate the size of a logical subplan

Cost estimation: estimate the cost of a physical subplan

# Size Estimation

Problem: estimate the size of a query plan:  $|P|$

We consider plans with selections and joins

Worst case sizes:

- Size of a selection:  $|\sigma_C(R)| \leq |R|$
- Size of a join:  $|R \bowtie S| \leq |R| * |S|$

Estimate  $\approx f^* \text{worst-case}$

where  $f$  in  $(0,1)$  is called selectivity factor

R(A,B)

S(C,D)

# Estimating Size of a Selection

**Assumption 1:** uniform distribution of values

- $|\sigma_{A=v}(R)| \approx |T(R)| / V(R,A)$
- Selectivity factor:  $f_{A=v} = 1/V(R,A)$

**Assumption 2:** independence of attributes

- Selectivity factor:  $f_{A=v \text{ and } B=w} = f_{A=v} * f_{B=w}$
- $|\sigma_{A=v \text{ and } B=w}(R)| \approx |T(R)| / (V(R,A) * V(R,B))$

R(A,B)

S(C,D)

# Estimating Size of a Join

## **Assumption 3:** Inclusion assumption

if  $V(R,B) \leq V(S,C)$  then  $\Pi_B(R) \subseteq \Pi_C(S)$

- $|R \bowtie S| \approx |R| * |S| / V(S,C)$

In general:

- $|R \bowtie S| \approx |R| * |S| / \max(V(R,B), V(S,C))$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

## Example

```
SELECT *
FROM Supplier x, Supply y
WHERE x.sid = y.sid
```

$T(\text{Supplier}) = 100,000$

$T(\text{Supply}) = 3,000,000$

$V(\text{Supply}, \text{sid}) = 60,000$

$V(\text{Supply}, \text{pno}) = 25,000$

$T(\text{Part}) = 50,000$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

## Example

```
SELECT *
FROM Supplier x, Supply y
WHERE x.sid = y.sid
```

$T(\text{Supplier}) = 100,000$

$T(\text{Supply}) = 3,000,000$

$V(\text{Supply}, \text{sid}) = 60,000$

$V(\text{Supply}, \text{pno}) = 25,000$

$T(\text{Part}) = 50,000$

$$|Q| = T(\text{Supplier}) * T(\text{Supply}) / \max(V(\text{Supplier}, \text{sid}), V(\text{Supply}, \text{sid}))$$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

## Example

```
SELECT *
FROM Supplier x, Supply y
WHERE x.sid = y.sid
```

$T(\text{Supplier}) = 100,000$

$T(\text{Supply}) = 3,000,000$

$V(\text{Supply}, \text{sid}) = 60,000$

$V(\text{Supply}, \text{pno}) = 25,000$

$T(\text{Part}) = 50,000$

$$\begin{aligned}|Q| &= T(\text{Supplier}) * T(\text{Supply}) / \max(V(\text{Supplier}, \text{sid}), V(\text{Supply}, \text{sid})) \\&= 100,000 * 3,000,000 / 100,000\end{aligned}$$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

## Example

```
SELECT *
FROM Supplier x, Supply y
WHERE x.sid = y.sid
```

$T(\text{Supplier}) = 100,000$

$T(\text{Supply}) = 3,000,000$

$V(\text{Supply}, \text{sid}) = 60,000$

$V(\text{Supply}, \text{pno}) = 25,000$

$T(\text{Part}) = 50,000$

$$\begin{aligned} |Q| &= T(\text{Supplier}) * T(\text{Supply}) / \max(V(\text{Supplier}, \text{sid}), V(\text{Supply}, \text{sid})) \\ &= 100,000 * 3,000,000 / 100,000 \\ &= 3,000,000 \end{aligned}$$

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

## Example

```
SELECT *
FROM Supplier x, Supply y
WHERE x.sid = y.sid
```

$T(\text{Supplier}) = 100,000$

$T(\text{Supply}) = 3,000,000$

$V(\text{Supply}, \text{sid}) = 60,000$

$V(\text{Supply}, \text{pno}) = 25,000$

$T(\text{Part}) = 50,000$

$$\begin{aligned}|Q| &= T(\text{Supplier}) * T(\text{Supply}) / \max(V(\text{Supplier}, \text{sid}), V(\text{Supply}, \text{sid})) \\&= 100,000 * 3,000,000 / 100,000 \\&= 3,000,000\end{aligned}$$

This is obvious!! Why?

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

## Example

```
SELECT *
FROM Supplier x, Supply y, Part z
WHERE x.sid = y.sid and y.pno = z.pno
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
      and z.price = 30
```

$T(\text{Supplier}) = 100,000$

$V(\text{Supplier}, \text{city}) = 2000$

$V(\text{Supplier}, \text{state}) = 50$

$T(\text{Supply}) = 3,000,000$

$V(\text{Supply}, \text{sid}) = 60,000$

$V(\text{Supply}, \text{pno}) = 25,000$

$T(\text{Part}) = 50,000$

$V(\text{Part}, \text{price}) = 5000$

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

Part(pno, pname, pprice)

## Example

```
SELECT *
FROM Supplier x, Supply y, Part z
WHERE x.sid = y.sid and y.pno = z.pno
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
      and z.price = 30
```

T(Supplier) = 100,000

V(Supplier,city) = 2000

V(Supplier,state) = 50

T(Supply) = 3,000,000

V(Supply,sid) = 60,000

V(Supply,pno) = 25,000

T(Part) = 50,000

V(Part,price) = 5000

Q = T(Supply) / V(Supplier,city)\*V(Supplier,state),V(Part,price)

`Supplier(sid, sname, scity, sstate)`

`Supply(sid, pno, quantity)`

`Part(pno, pname, pprice)`

## Example

```
SELECT *
FROM Supplier x, Supply y, Part z
WHERE x.sid = y.sid and y.pno = z.pno
and x.scity = 'Seattle'
and x.sstate = 'WA'
and z.price = 30
```

$T(\text{Supplier}) = 100,000$

$V(\text{Supplier}, \text{city}) = 2000$

$V(\text{Supplier}, \text{state}) = 50$

$T(\text{Supply}) = 3,000,000$

$V(\text{Supply}, \text{sid}) = 60,000$

$V(\text{Supply}, \text{pno}) = 25,000$

$T(\text{Part}) = 50,000$

$V(\text{Part}, \text{price}) = 5000$

$$\begin{aligned} Q &= T(\text{Supply}) / V(\text{Supplier}, \text{city}) * V(\text{Supplier}, \text{state}), V(\text{Part}, \text{price}) \\ &= 3,000,000 / (2000 * 50 * 5000) < 1 \end{aligned}$$

# Optimization

- The optimizer considers several plans
- For each plan, it estimates costs
- Then chooses the cheapest plan

Cost estimation: we will consider only the I/O cost.

# I/O Cost of Physical Operators

# Cost Parameters

Given statistics on the base tables:

- $B(R)$  = # of blocks (i.e., pages) for relation R
- $T(R)$  = # of tuples in relation R
- $V(R, A)$  = # of distinct values of attribute A

# I/O Cost of Selection

- Sequential scan for relation R costs  $\mathbf{B(R)}$
- Index-based selection
  - Estimate selectivity factor  $f$
  - Clustered index:  $f^*\mathbf{B(R)}$
  - Unclustered index  $f^*\mathbf{T(R)}$

Note: we ignore I/O cost for index pages

# Example

$B(R) = 2000$   
 $T(R) = 100,000$   
 $V(R, A) = 20$

cost of  $\sigma_{A=v}(R) = ?$

- Table scan:
- Index based selection:

# Example

$B(R) = 2000$   
 $T(R) = 100,000$   
 $V(R, A) = 20$

cost of  $\sigma_{A=v}(R) = ?$

- Table scan:  $B(R) = 2,000$  I/Os
- Index based selection:

# Example

$B(R) = 2000$   
 $T(R) = 100,000$   
 $V(R, A) = 20$

cost of  $\sigma_{A=v}(R) = ?$

- Table scan:  $B(R) = 2,000$  I/Os
- Index based selection:
  - If index is unclustered:  $T(R) * 1/V(R,A) = 5,000$  I/Os

# Example

$$\begin{aligned}B(R) &= 2000 \\T(R) &= 100,000 \\V(R, A) &= 20\end{aligned}$$

$$\text{cost of } \sigma_{A=v}(R) = ?$$

- Table scan:  $B(R) = 2,000$  I/Os
- Index based selection:
  - If index is unclustered:  $T(R) * 1/V(R,A) = 5,000$  I/Os
  - If index is clustered:  $B(R) * 1/V(R,A) = 100$  I/Os

# Example

$$\begin{aligned}B(R) &= 2000 \\T(R) &= 100,000 \\V(R, A) &= 20\end{aligned}$$

$$\text{cost of } \sigma_{A=v}(R) = ?$$

- Table scan:  $B(R) = 2,000$  I/Os
- Index based selection:
  - If index is unclustered:  $T(R) * 1/V(R,A) = 5,000$  I/Os
  - If index is clustered:  $B(R) * 1/V(R,A) = 100$  I/Os

Lesson: Don't build unclustered indexes when  $V(R,A)$  is small !

# NOT COVERED

CSE 414, Spring 2019:

- We will not cover the I/O cost of a join
- **Skip slides until “Cost of a query plan”**
- Study the size estimate of the logical plan.

# I/O Cost of a Join

- Nested loop join
- Hash join
- Sort-merge join
- Index-join

Read: sections 15.2, 15.3, 15.6

# Join Example

Patient(pid, name, address)

Insurance(pid, provider, policy\_nb)

Patient  $\bowtie$  Insurance

Two tuples  
per page

Patient

1	'Bob'	'Seattle'
2	'Ela'	'Everett'

3	'Jill'	'Kent'
4	'Joe'	'Seattle'

Insurance

2	'Blue'	123
4	'Prem'	432

4	'Prem'	343
3	'GrpH'	554

# Nested Loop Joins

- Tuple-based nested loop  $R \bowtie S$
- R is the outer relation, S is the inner relation

```
for each tuple t1 in R do  
  for each tuple t2 in S do  
    if t1 and t2 join then output (t1,t2)
```

What is the Cost?

# Nested Loop Joins

- Tuple-based nested loop  $R \bowtie S$
- R is the outer relation, S is the inner relation

```
for each tuple  $t_1$  in R do  
  for each tuple  $t_2$  in S do  
    if  $t_1$  and  $t_2$  join then output  $(t_1, t_2)$ 
```

- Cost:  $B(R) + T(R) B(S)$
- Multiple-pass since S is read many times

What is the Cost?

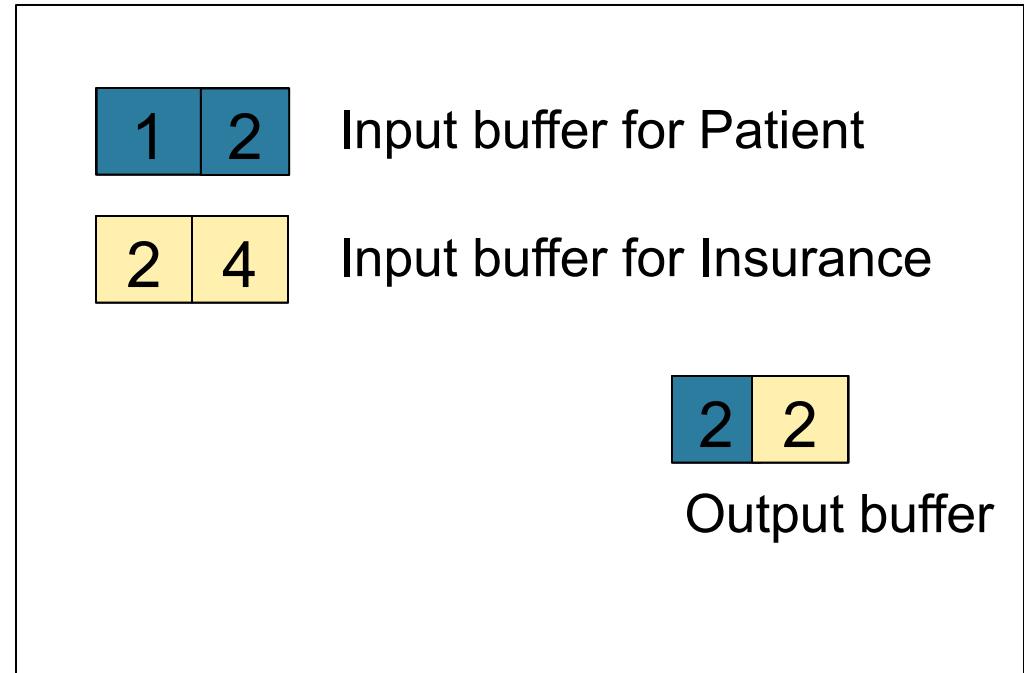
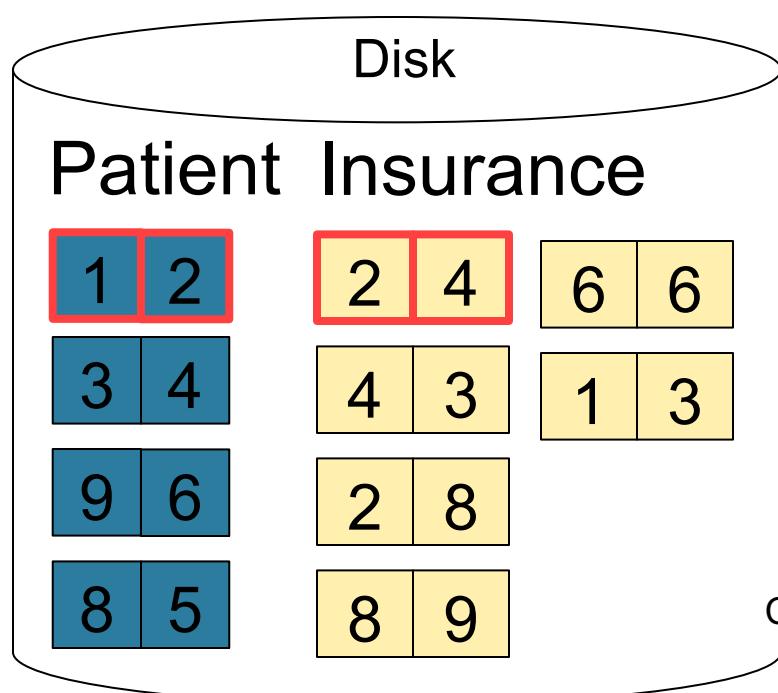
# Page-at-a-time Refinement

```
for each page of tuples r in R do  
  for each page of tuples s in S do  
    for all pairs of tuples t1 in r, t2 in s  
      if t1 and t2 join then output (t1,t2)
```

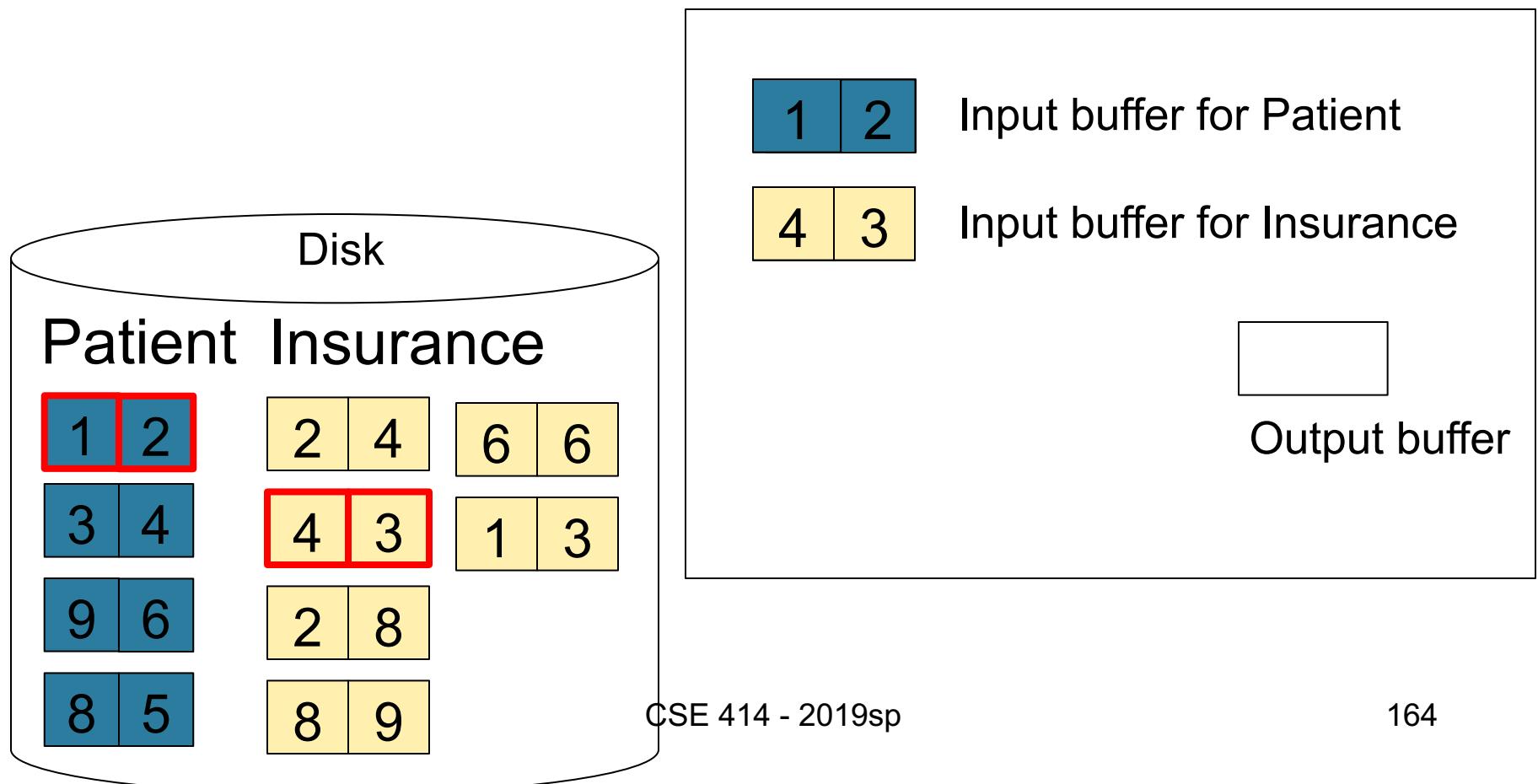
- Cost:  $B(R) + B(R)B(S)$

What is the Cost?

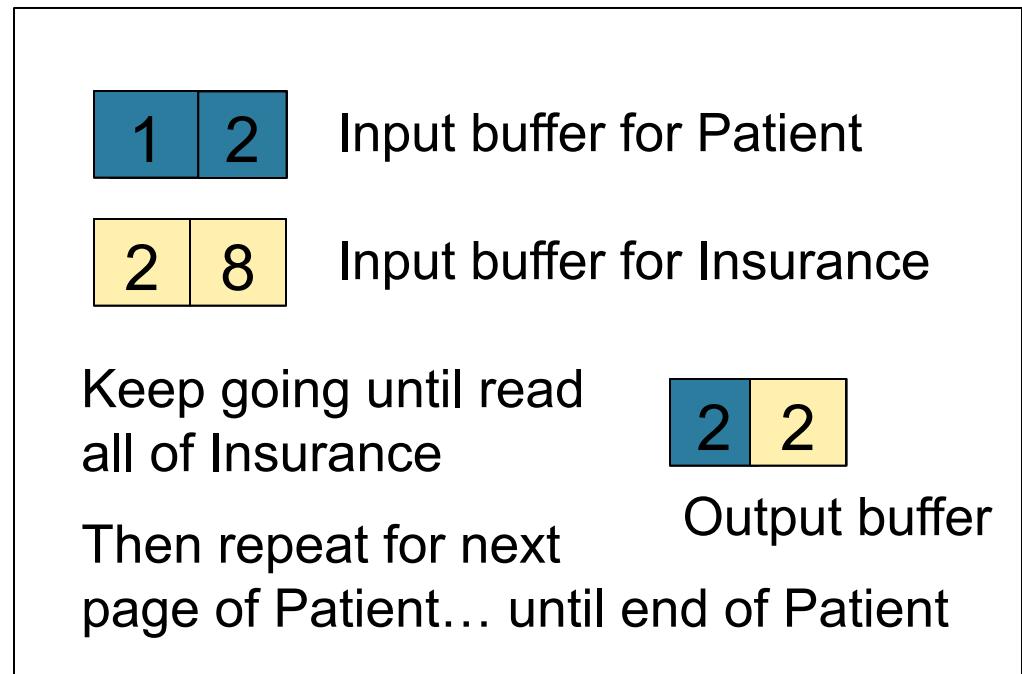
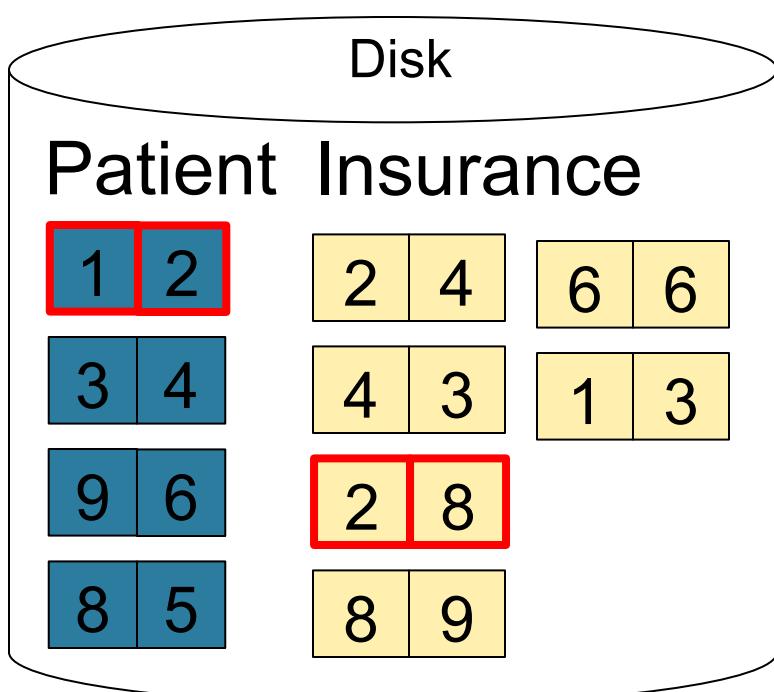
# Page-at-a-time Refinement



# Page-at-a-time Refinement



# Page-at-a-time Refinement



Cost:  $B(R) + B(R)B(S)$

# Block-Nested-Loop Refinement

```
for each group of M-1 pages r in R do
    for each page of tuples s in S do
        for all pairs of tuples t1 in r, t2 in s
            if t1 and t2 join then output (t1,t2)
```

- Cost:  $B(R) + B(R)B(S)/(M-1)$

What is the Cost?

# Hash Join

Hash join:  $R \bowtie S$

- Scan R, build buckets in main memory
- Then scan S and join
- Cost:  $B(R) + B(S)$
- Which relation to build the hash table on?

# Hash Join

Hash join:  $R \bowtie S$

- Scan R, build buckets in main memory
- Then scan S and join
- Cost:  $B(R) + B(S)$
- Which relation to build the hash table on?
- One-pass algorithm when  $B(R) \leq M$ 
  - $M$  = number of memory pages available

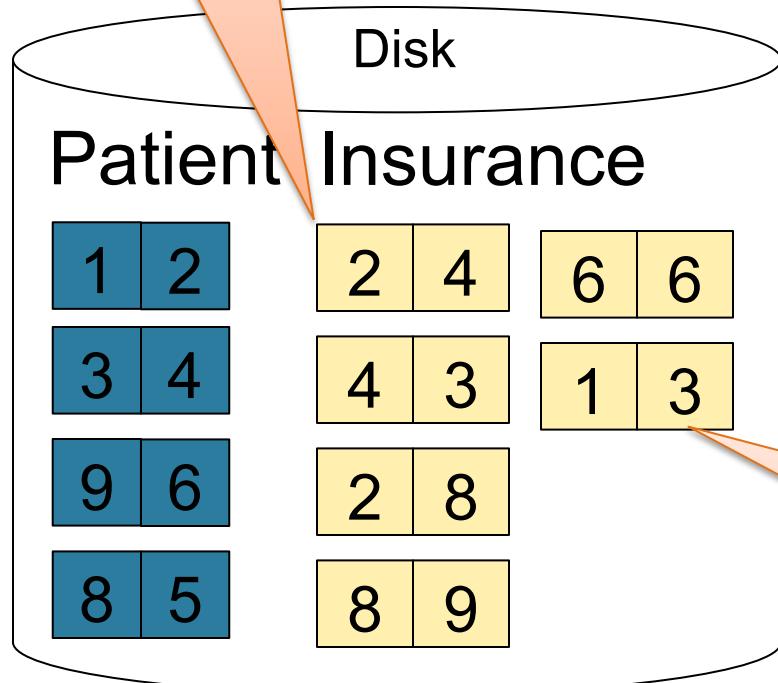
# Hash Join Example

Patient  $\bowtie$  Insurance

Some large-enough #

Memory M = 21 pages

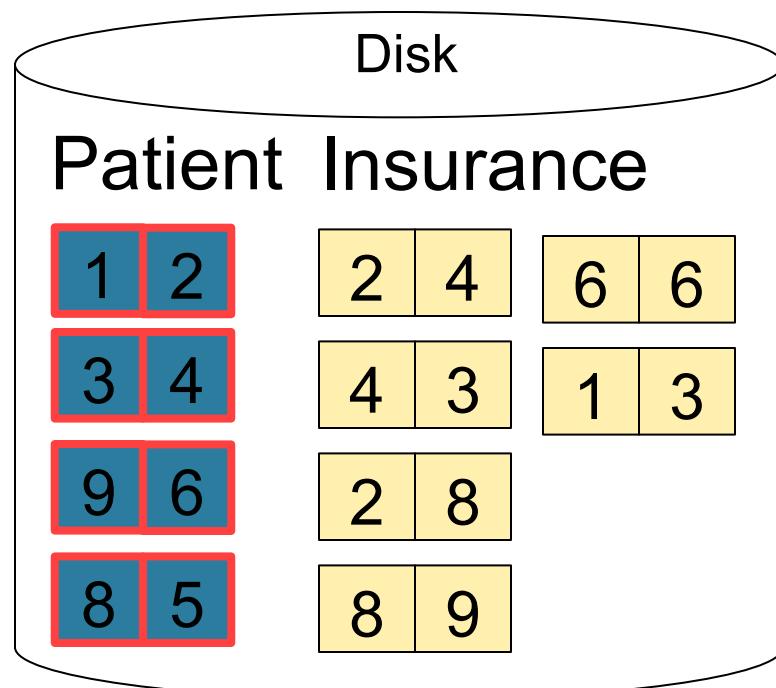
Showing pid only



# Hash Join Example

Step 1: Scan Patient and **build** hash table in memory

Can be done in  
method open()



Memory M = 21 pages

Hash h: pid % 5

5		1	6	2		3	8	4	9
---	--	---	---	---	--	---	---	---	---

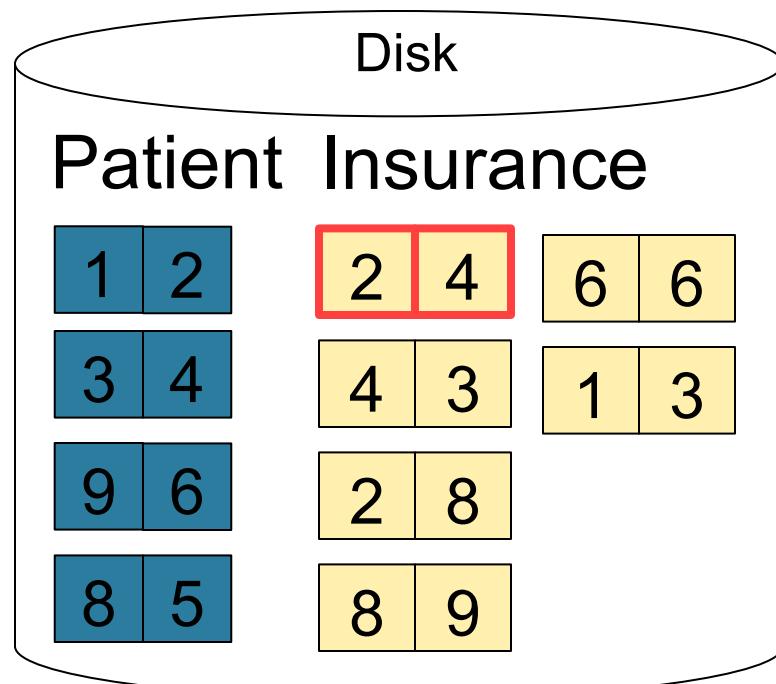


Input buffer

# Hash Join Example

Step 2: Scan Insurance and **probe** into hash table

Done during  
calls to next()



Memory M = 21 pages

Hash h: pid % 5

5		1	6	2		3	8	4	9
---	--	---	---	---	--	---	---	---	---

2	4
---	---

Input buffer

2	2
---	---

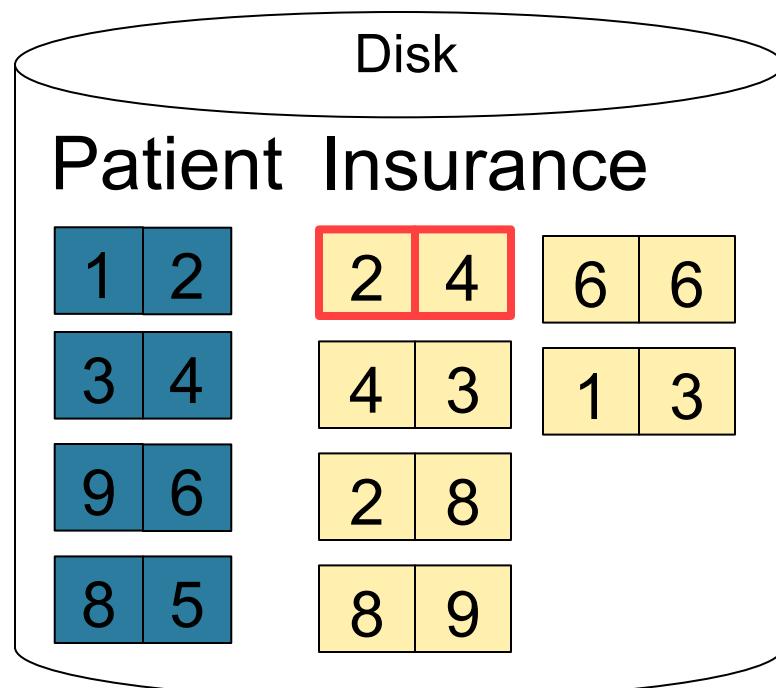
Output buffer

Write to disk or  
pass to next  
operator

# Hash Join Example

Step 2: Scan Insurance and **probe** into hash table

Done during  
calls to next()



Memory M = 21 pages

Hash h: pid % 5

5		1	6	2		3	8	4	9
---	--	---	---	---	--	---	---	---	---

2	4
---	---

Input buffer

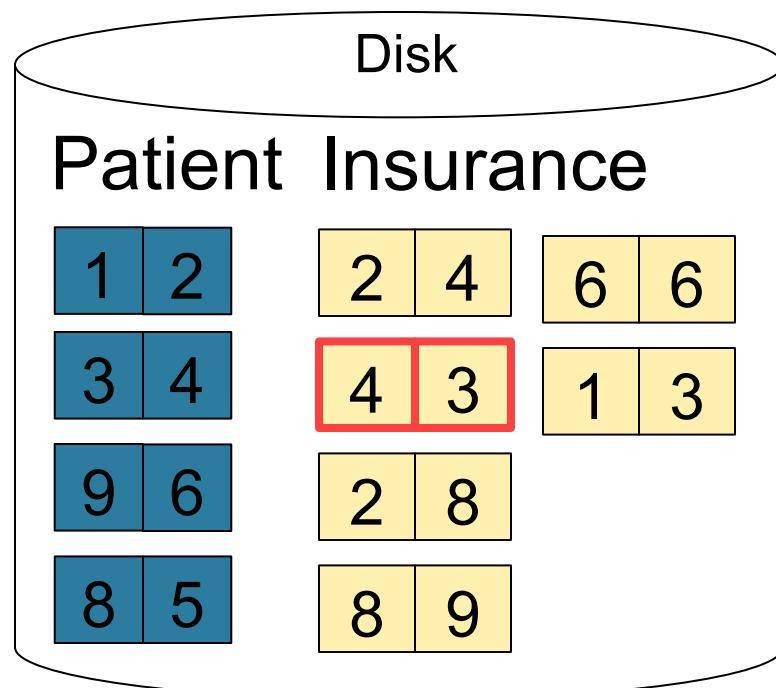
4	4
---	---

Output buffer

# Hash Join Example

Step 2: Scan Insurance and **probe** into hash table

Done during  
calls to next()



Memory M = 21 pages

Hash h: pid % 5

5		1	6	2		3	8	4	9
---	--	---	---	---	--	---	---	---	---

4	3
---	---

Input buffer

4	4
---	---

Output buffer

Keep going until read all of Insurance

Cost:  $B(R) + B(S)$

# Sort-Merge Join

Sort-merge join:  $R \bowtie S$

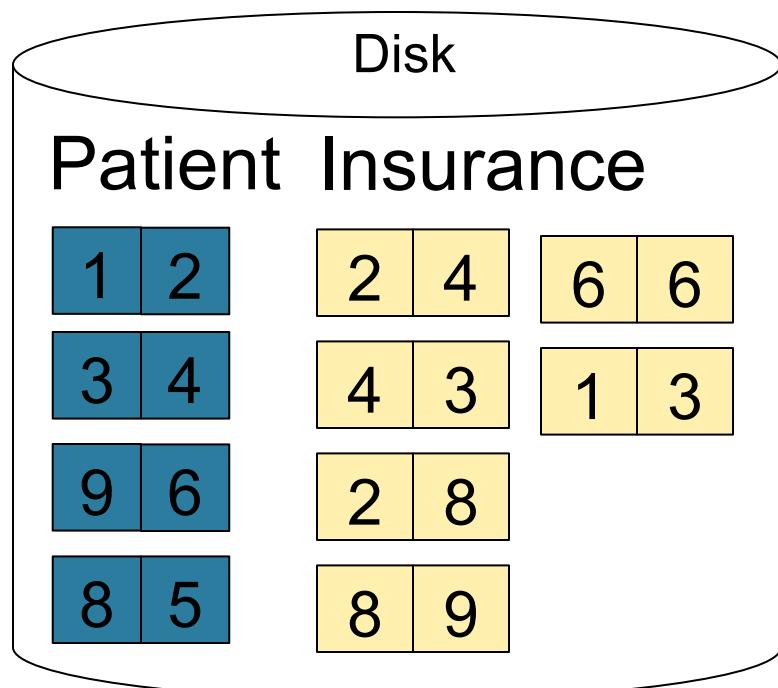
- Scan R and sort in main memory
  - Scan S and sort in main memory
  - Merge R and S
- 
- Cost:  $B(R) + B(S)$
  - One pass algorithm when  $B(S) + B(R) \leq M$
  - Typically, this is NOT a one pass algorithm

# Sort-Merge Join Example

Step 1: Scan Patient and **sort** in memory

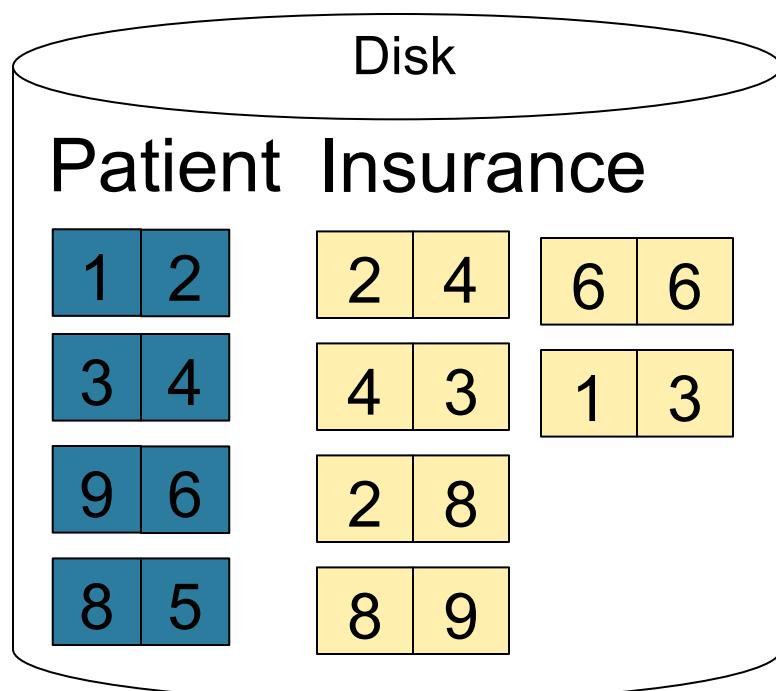
Memory M = 21 pages

1	2	3	4	5	6	8	9
---	---	---	---	---	---	---	---

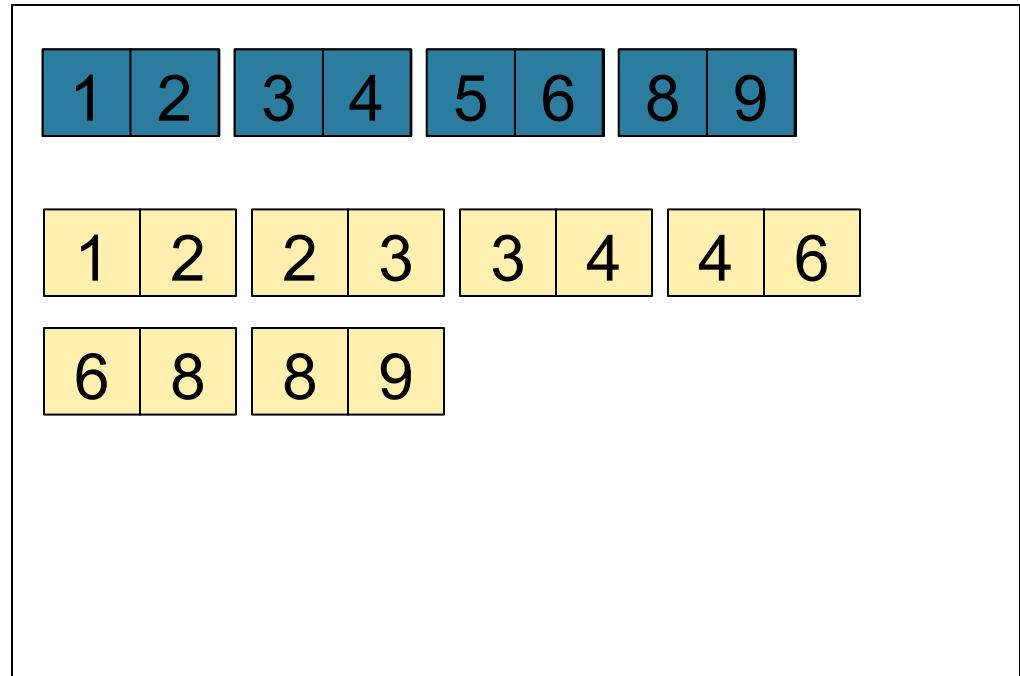


# Sort-Merge Join Example

Step 2: Scan Insurance and **sort** in memory

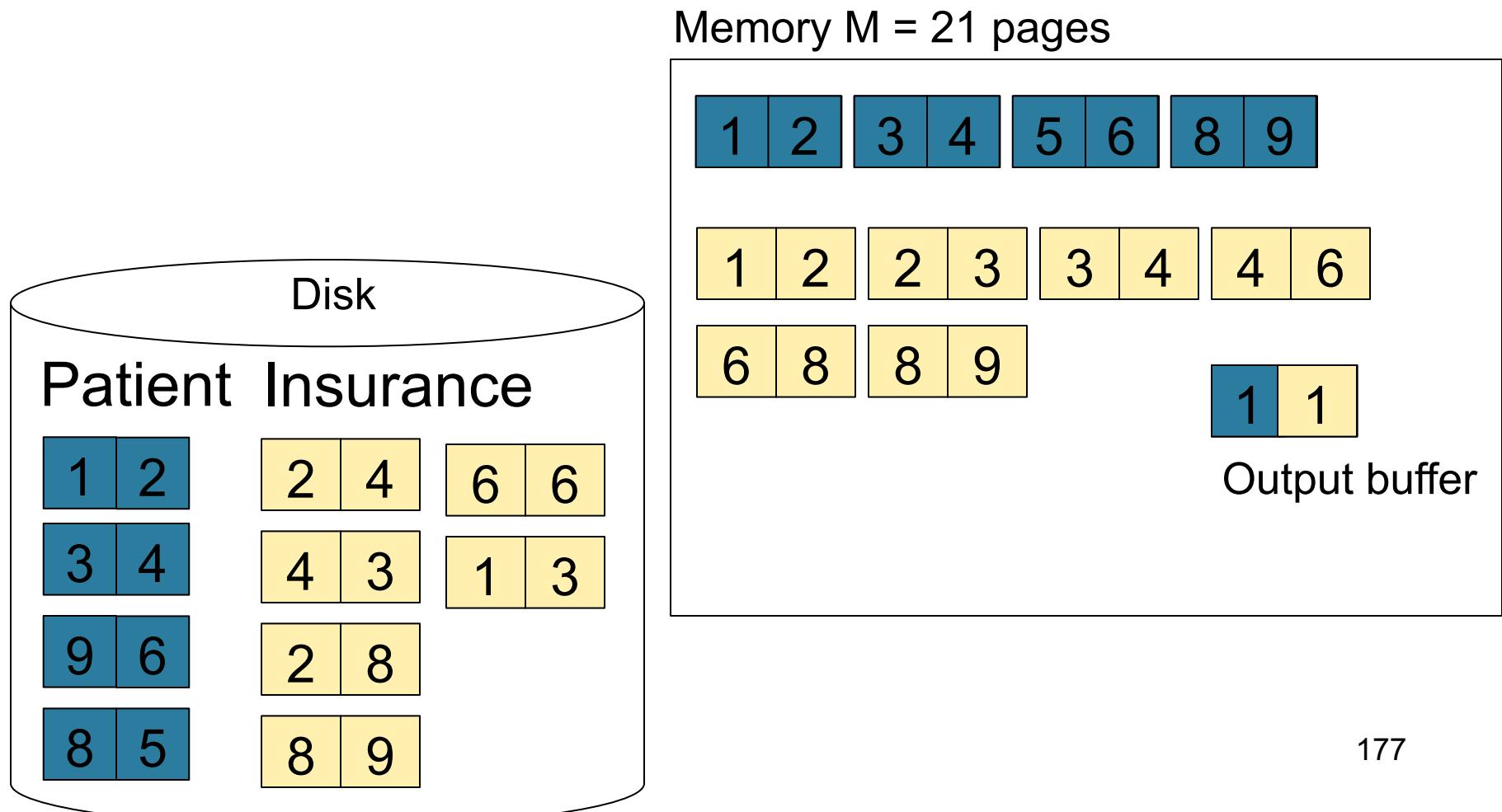


Memory M = 21 pages



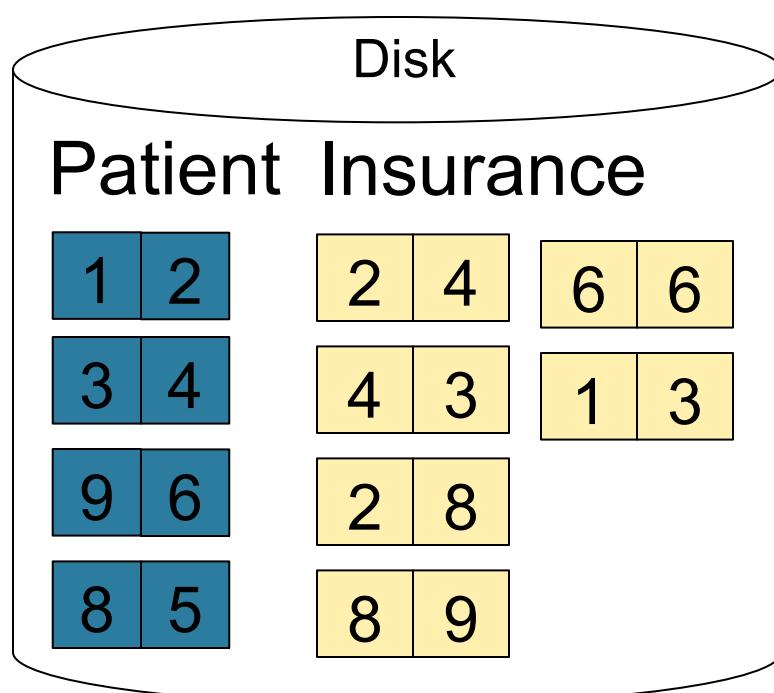
# Sort-Merge Join Example

Step 3: Merge Patient and Insurance

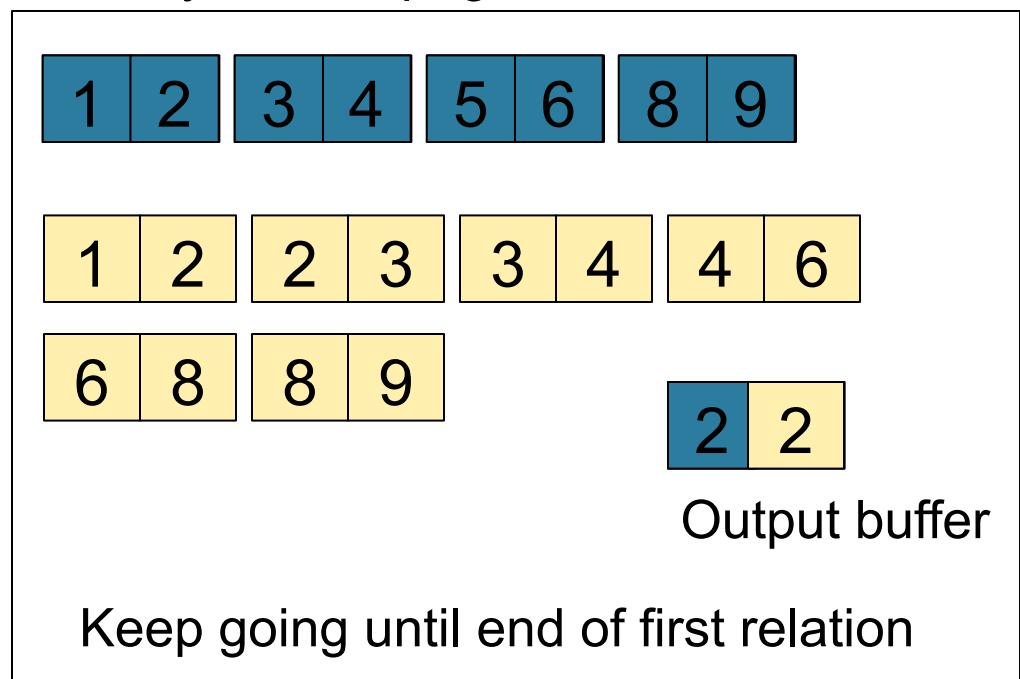


# Sort-Merge Join Example

## Step 3: Merge Patient and Insurance



Memory M = 21 pages



# Index Join

$R \bowtie S$

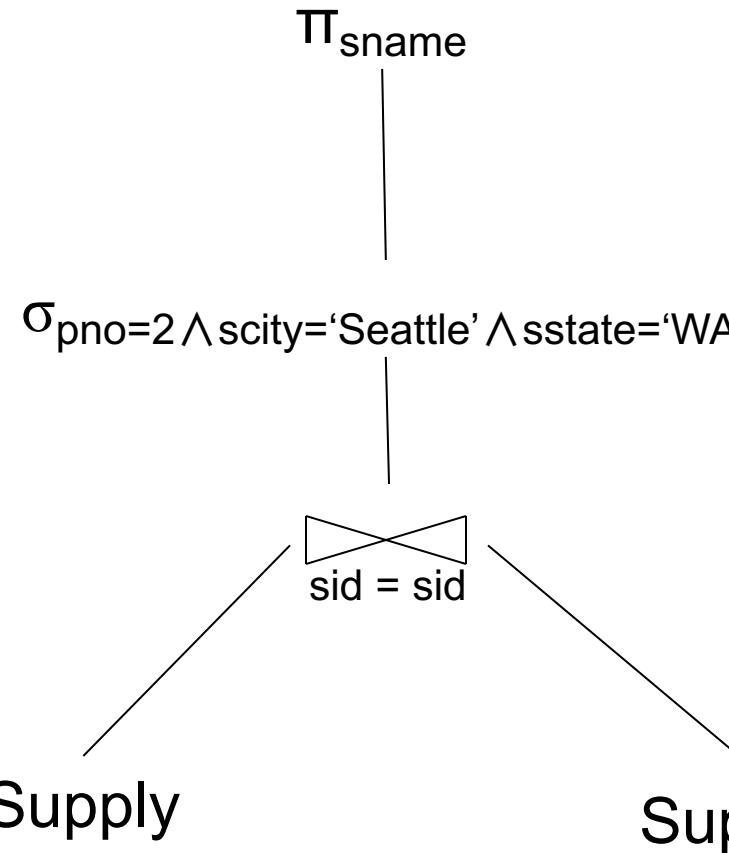
- Assume S has an index on the join attribute
- Iterate over R, for each tuple fetch corresponding tuple(s) from S
- **Cost:**
  - If index on S is clustered:  
 $B(R) + T(R) * (B(S) * 1/V(S,a))$
  - If index on S is unclustered:  
 $B(R) + T(R) * (T(S) * 1/V(S,a))$

# Cost of Query Plans Example

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Logical Query Plan 1



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
and y.pno = 2
and x.scity = 'Seattle'
and x.sstate = 'WA'
```

T(Supply) = 10000  
B(Supply) = 100  
V(Supply, pno) = 2500

T(Supplier) = 1000  
B(Supplier) = 100  
V(Supplier, scity) = 20  
V(Supplier, state) = 10

M=11

Supplier(sid, sname, scity, sstate)

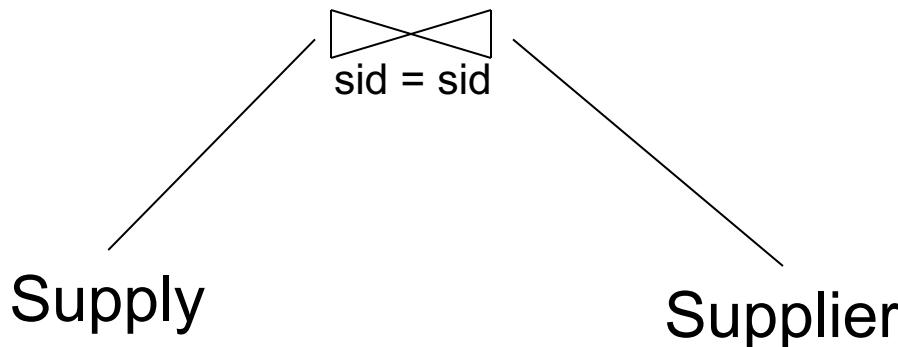
Supply(sid, pno, quantity)

# Logical Query Plan 1

$\Pi_{\text{sname}}$

$\sigma_{\text{pno}=2 \wedge \text{scity}=\text{'Seattle'} \wedge \text{sstate}=\text{'WA'}}$

$T = 10000$



```
SELECT sname  
FROM Supplier x, Supply y  
WHERE x.sid = y.sid  
and y.pno = 2  
and x.scity = 'Seattle'  
and x.sstate = 'WA'
```

$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, \text{pno}) = 2500$

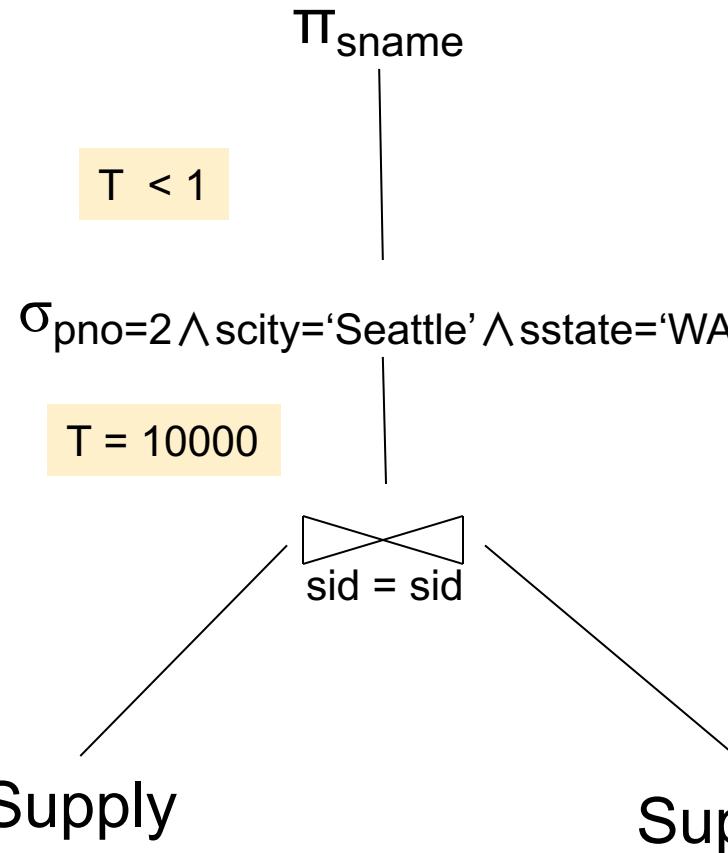
$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Logical Query Plan 1



$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, \text{pno}) = 2500$

$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

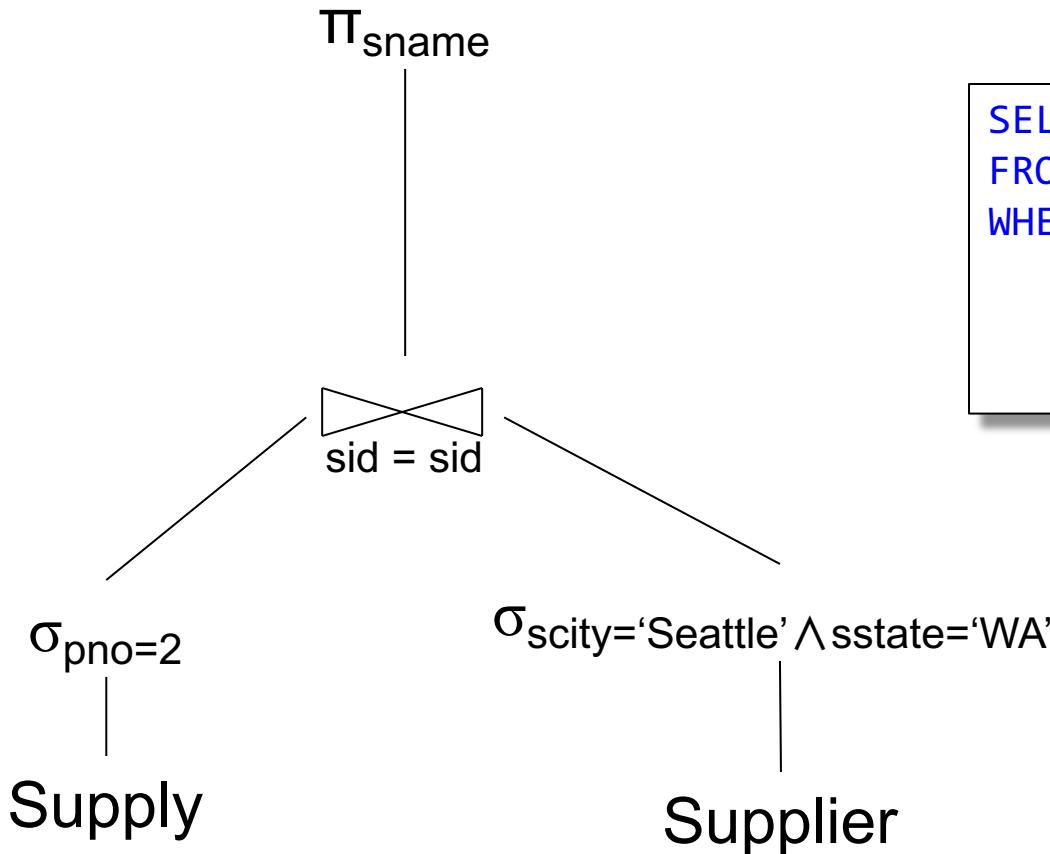
```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
and y.pno = 2
and x.scity = 'Seattle'
and x.sstate = 'WA'
```

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Logical Query Plan 2



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
and y.pno = 2
and x.scity = 'Seattle'
and x.sstate = 'WA'
```

T(Supply) = 10000  
B(Supply) = 100  
V(Supply, pno) = 2500

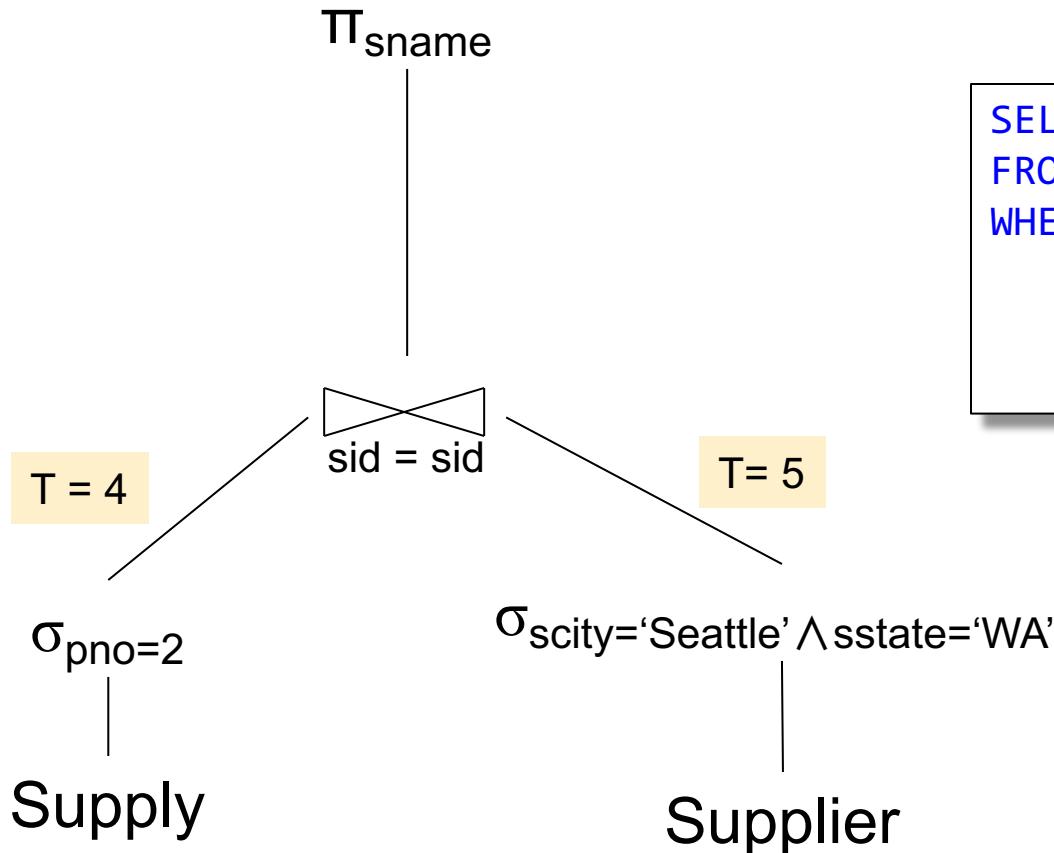
T(Supplier) = 1000  
B(Supplier) = 100  
V(Supplier, scity) = 20  
V(Supplier, state) = 10

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Logical Query Plan 2



$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, \text{pno}) = 2500$

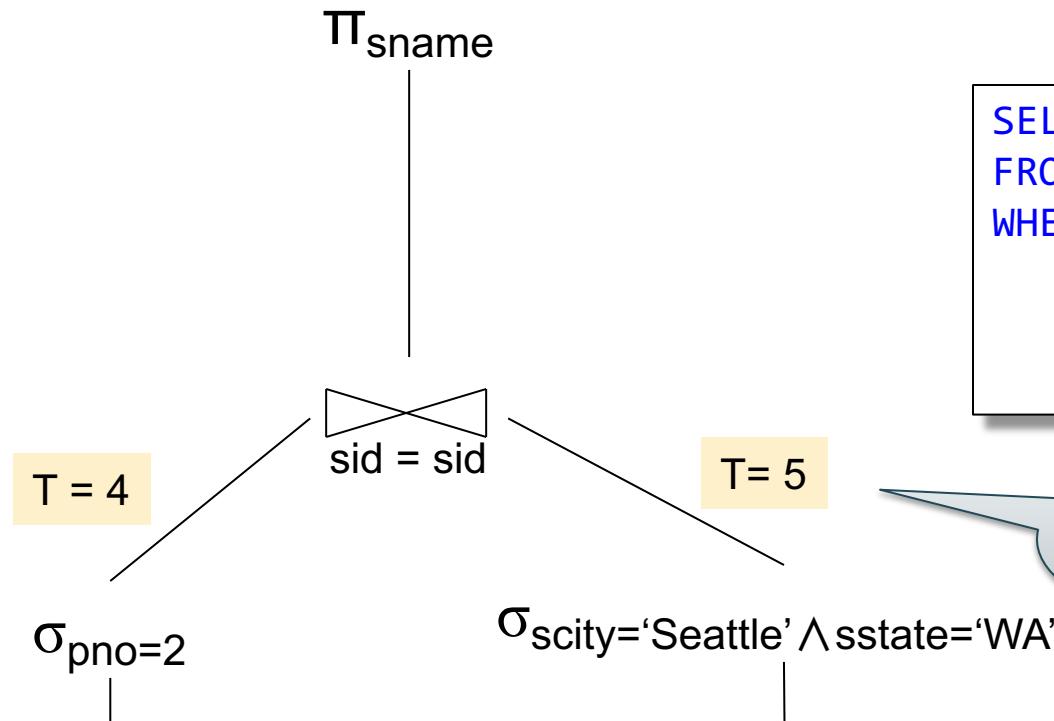
$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

$M=11$

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Logical Query Plan 2



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
and y.pno = 2
and x.scity = 'Seattle'
and x.sstate = 'WA'
```

Very wrong!  
Why?

$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, \text{pno}) = 2500$

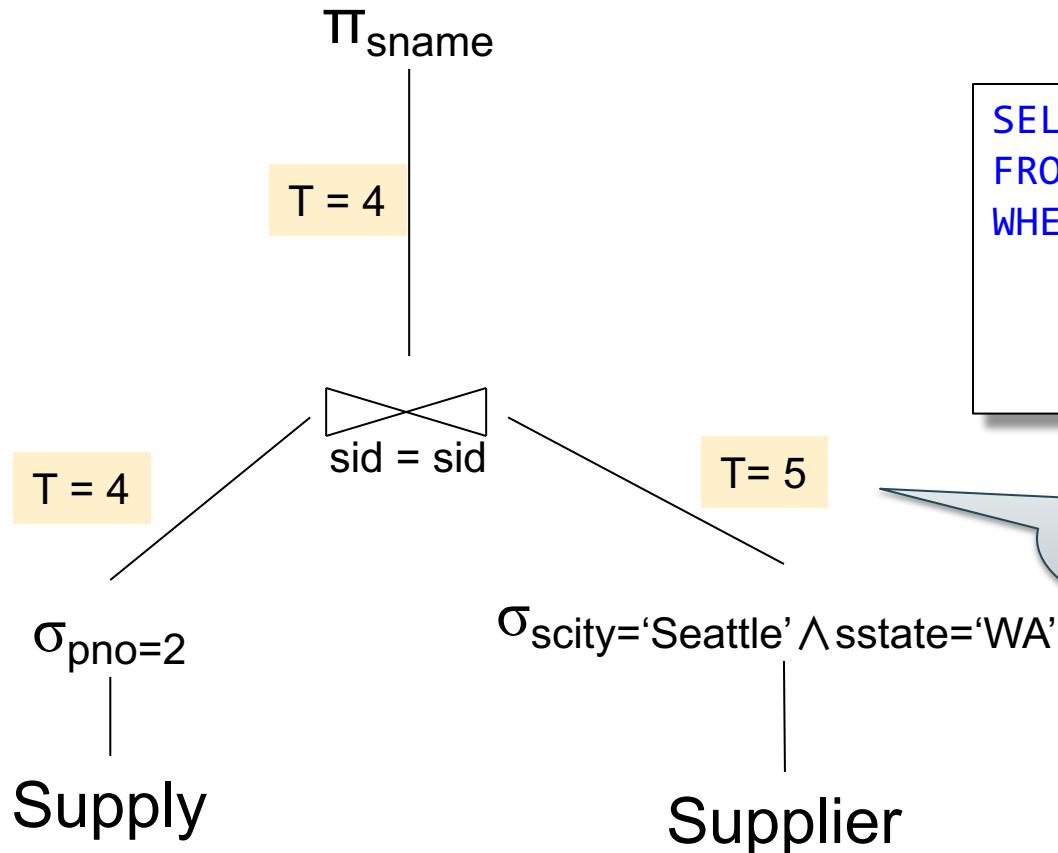
$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Logical Query Plan 2



`SELECT sname  
FROM Supplier x, Supply y  
WHERE x.sid = y.sid  
and y.pno = 2  
and x.scity = 'Seattle'  
and x.sstate = 'WA'`

Very wrong!  
Why?

$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, \text{pno}) = 2500$

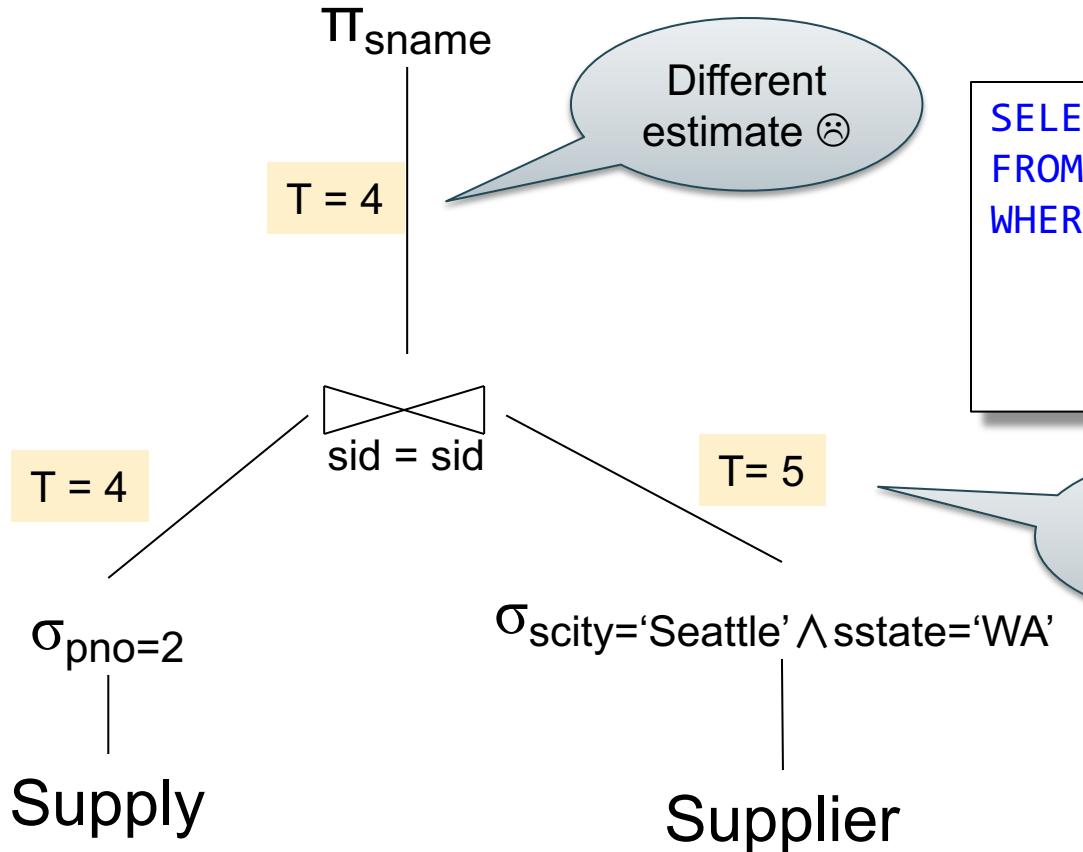
$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Logical Query Plan 2



$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, pno) = 2500$

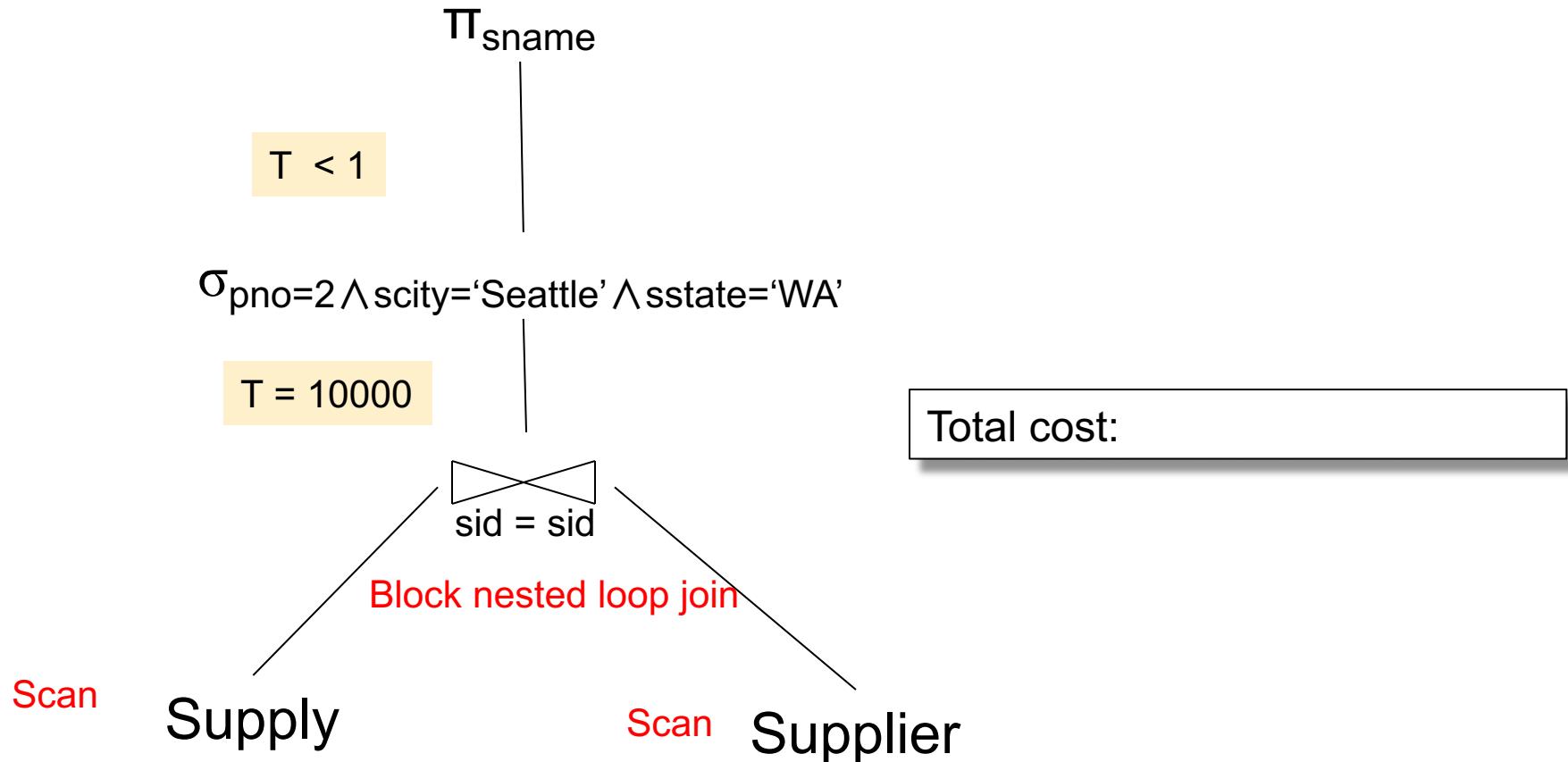
$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Physical Plan 1



$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, \text{pno}) = 2500$

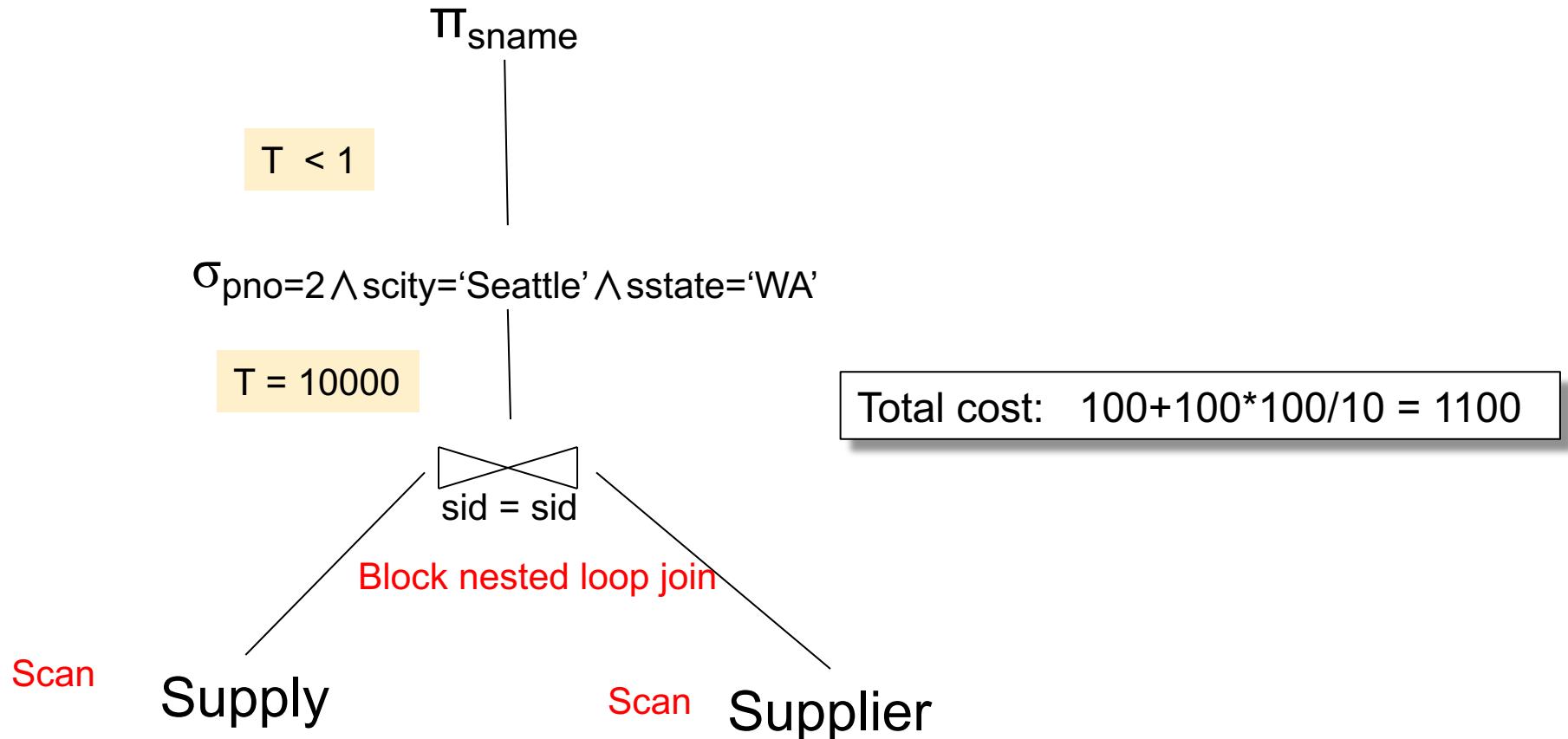
$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Physical Plan 1



$T(\text{Supply}) = 10000$   
 $B(\text{Supply}) = 100$   
 $V(\text{Supply}, \text{pno}) = 2500$

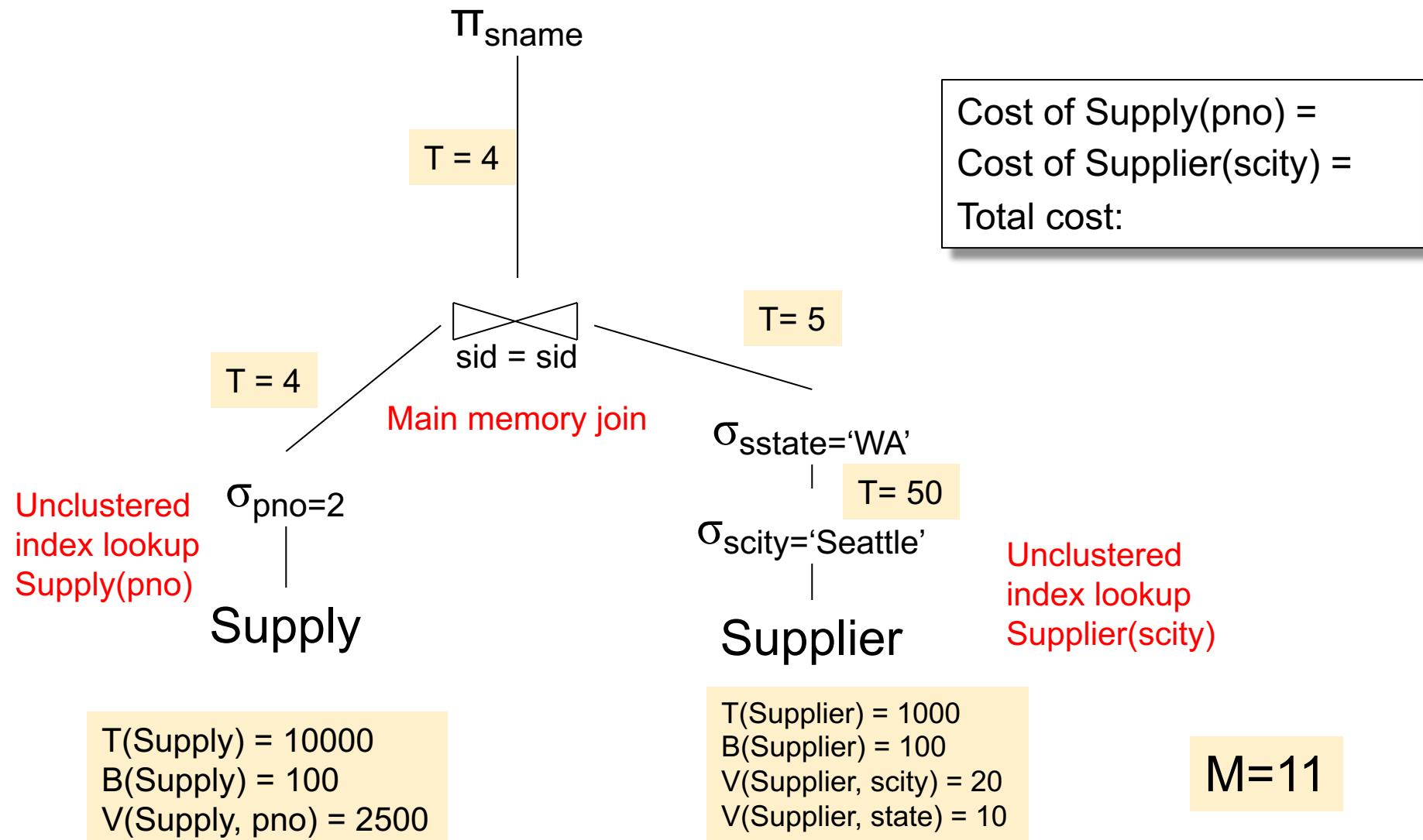
$T(\text{Supplier}) = 1000$   
 $B(\text{Supplier}) = 100$   
 $V(\text{Supplier}, \text{scity}) = 20$   
 $V(\text{Supplier}, \text{state}) = 10$

M=11

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

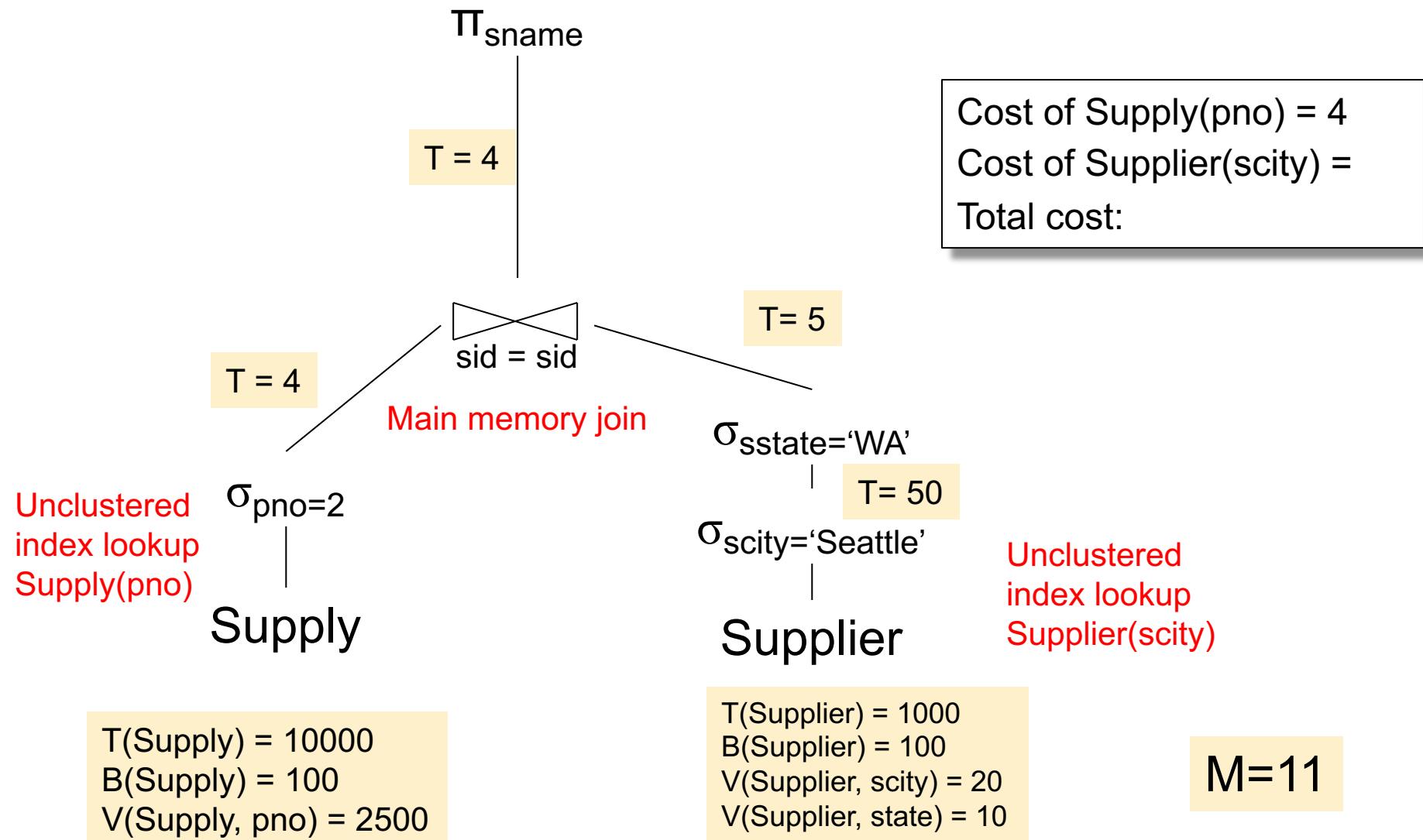
# Physical Plan 2



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

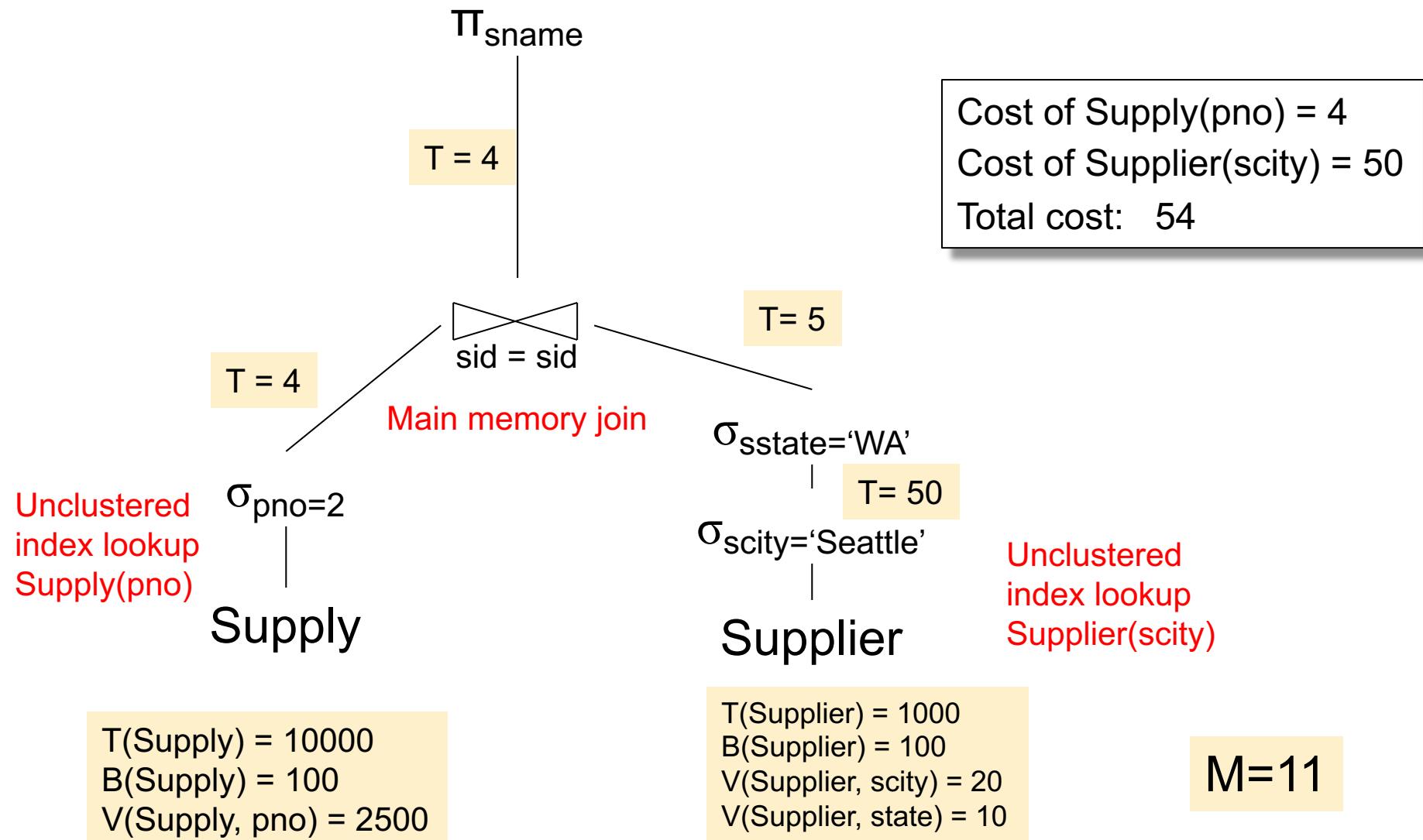
# Physical Plan 2



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

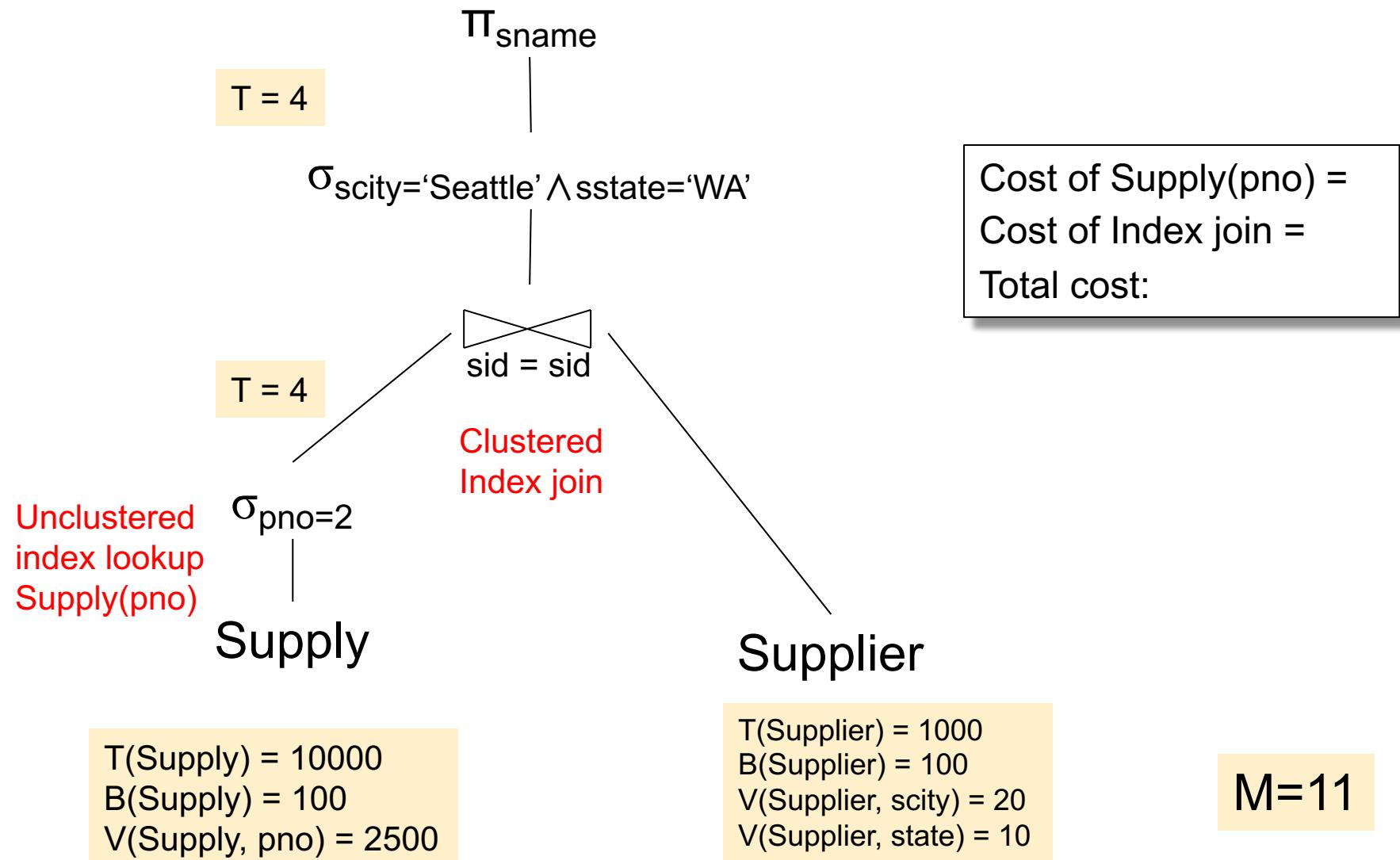
# Physical Plan 2



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

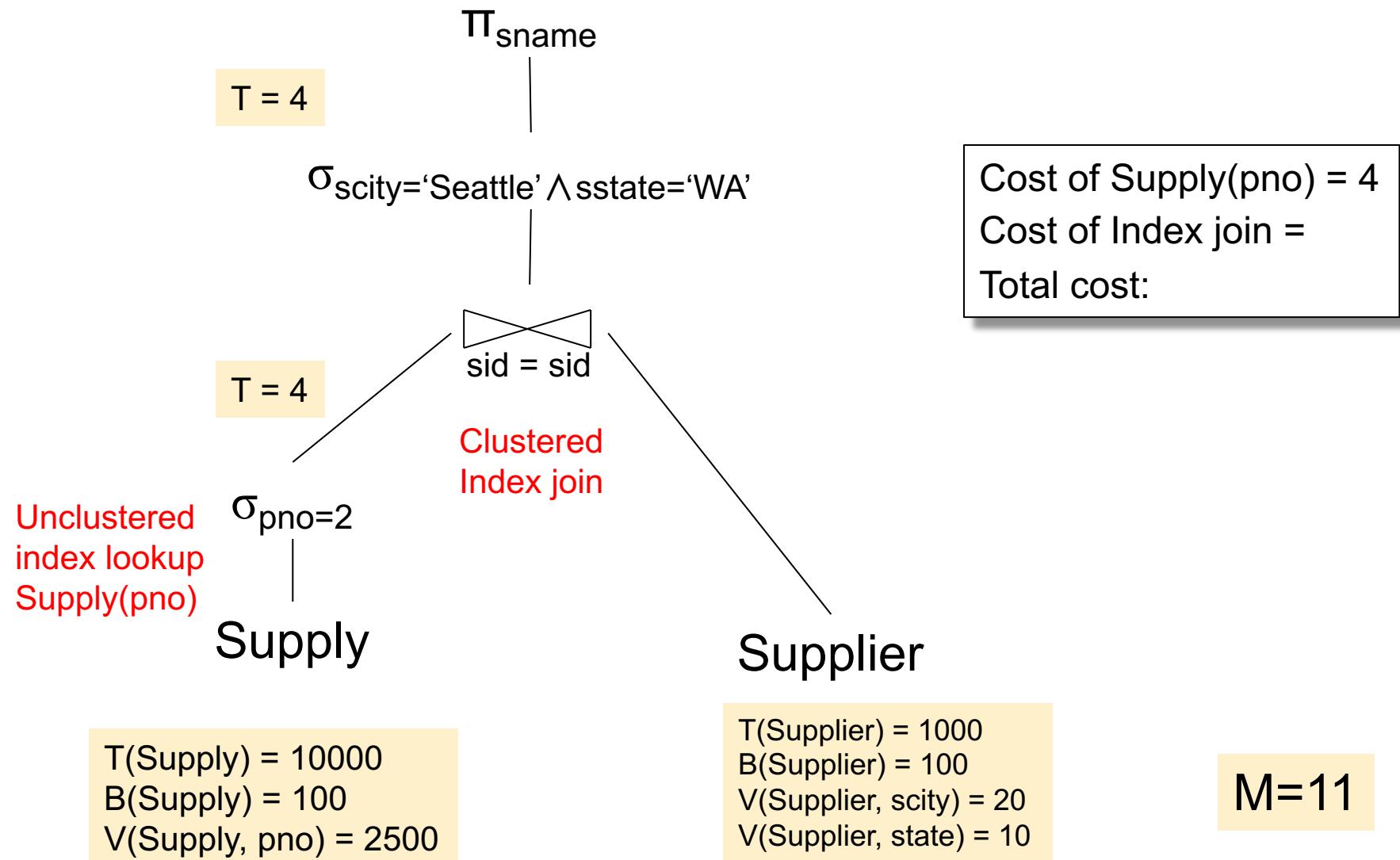
# Physical Plan 3



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

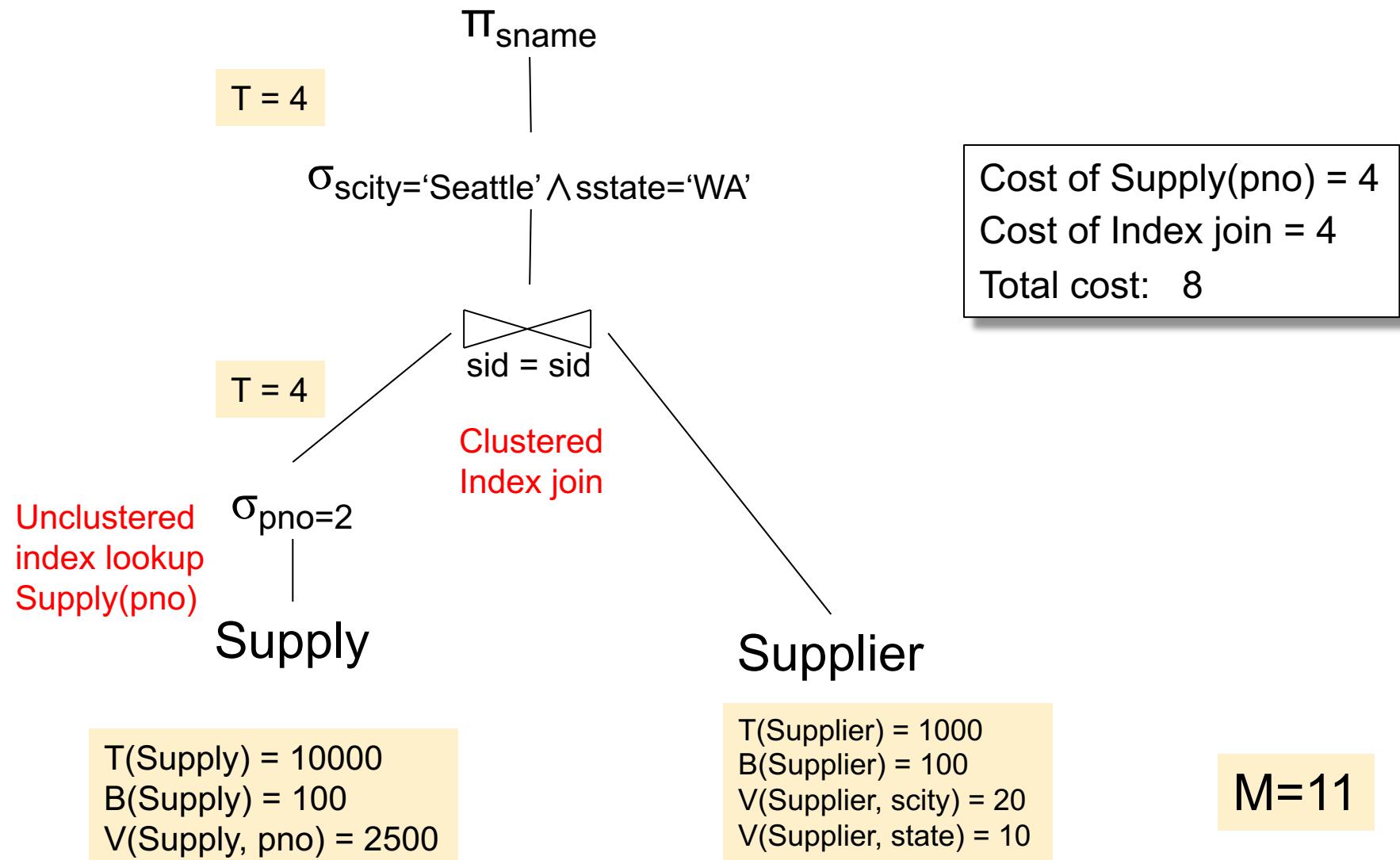
# Physical Plan 3



Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

# Physical Plan 3



# Query Optimizer Summary

- Input: A logical query plan
- Output: A good physical query plan
- Basic query optimization algorithm
  - Enumerate alternative plans (logical and physical)
  - Compute estimated cost of each plan
  - Choose plan with lowest cost
- This is called cost-based optimization