

# Summary of Topics for Midterm

# Asymptotics

- Relationship between polynomial, exponential, logarithmic time
- Big-Oh notation

$\Theta$   
 $\Omega$

$$f = O(g(n))$$
$$f \leq c \cdot g \quad \text{if } n \text{ is enough}$$

# Basic Proof Ideas

- Direct Proofs
- Proof by Contradiction (*stable matching*)
- Pigeon hole principle
- Induction / Strong Induction

# Graphs

- Relationship between degree and number of edges
- Cycles, trees → *natv look for induction*
- Graph search (BFS, DFS)
- Algorithms for finding Connected Components →
- Algorithm for coloring (bipartite graphs)
- Directed graphs (topological sort)

# Greedy Algorithms

Techniques:

Greedy stays ahead, structural, exchange arguments

Problems

- Interval Scheduling
- Interval Partitioning
- Minimum Spanning Trees and Cycle/Cut Properties
- Union Find Data Structure

ALG     A  
OPT     0

$A \neq 0 \Rightarrow \exists e \in 0, e \notin A$   
 $f \in A, f \notin 0$

swap you get  
smaller ~~opt~~  
contradicts optimality.

# Divide and Conquer Algorithms

- Recurrences (Master Theorem)
- Binary Search, Merge-sort
- Approximation the Root of a Function
- Finding Closest Points
- Integer Multiplication