

# Introduction to Database Systems

## CSE 444

### Lectures 6-7: Database Design

# Outline

- Design theory: 3.1-3.4
  - [Old edition: 3.4-3.6]

# Schema Refinements = Normal Forms

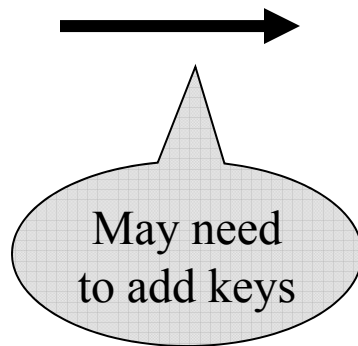
- 1st Normal Form = all tables are flat
- 2nd Normal Form = obsolete
- Boyce Codd Normal Form = will study
- 3rd Normal Form = see book

# First Normal Form (1NF)

- A database schema is in First Normal Form if all tables are flat

Student

Name	GPA	Courses			
Alice	3.8	<table border="1"><tr><td>Math</td></tr><tr><td>DB</td></tr><tr><td>OS</td></tr></table>	Math	DB	OS
Math					
DB					
OS					
Bob	3.7	<table border="1"><tr><td>DB</td></tr><tr><td>OS</td></tr></table>	DB	OS	
DB					
OS					
Carol	3.9	<table border="1"><tr><td>Math</td></tr><tr><td>OS</td></tr></table>	Math	OS	
Math					
OS					



Student

Name	GPA
Alice	3.8
Bob	3.7
Carol	3.9

Takes

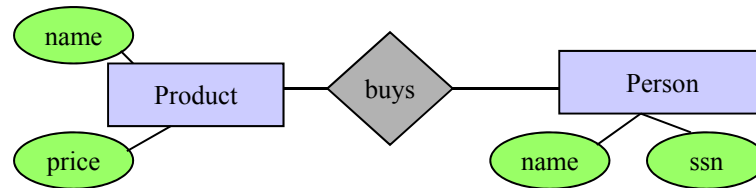
Student	Course
Alice	Math
Carol	Math
Alice	DB
Bob	DB
Alice	OS
Carol	OS

Course

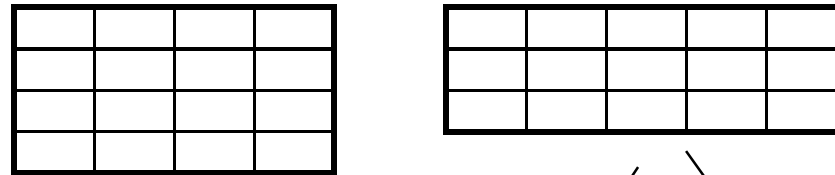
Course
Math
DB
OS

# Relational Schema Design

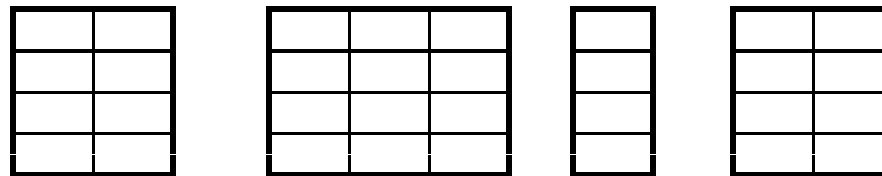
Conceptual Model:



Relational Model:  
plus FD's



Normalization:  
Eliminates anomalies



# Data Anomalies

When a database is poorly designed we get anomalies:

**Redundancy**: data is repeated

**Updated anomalies**: need to change in several places

**Delete anomalies**: may lose data when we don't want

# Relational Schema Design

Recall set attributes (persons with several phones):

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

Primary key is thus (SSN,PhoneNumber)

The above is in 1NF, but what is the problem with this schema?

# Relational Schema Design

Recall set attributes (persons with several phones):

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

## Anomalies:

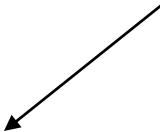
- Redundancy = repeat data
- Update anomalies = what if Fred moves to “Bellevue”?
- Deletion anomalies = what if Joe deletes his phone number?  
(what if Joe had only one phone #)



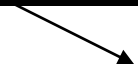
# Relation Decomposition

Break the relation into two:

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield



Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield



<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121

Anomalies have gone:

- No more repeated data
- Easy to move Fred to “Bellevue” (how ?)
- Easy to delete all Joe’s phone numbers (how ?)

# Relational Schema Design (or Logical Design)

Main idea:

- Start with some relational schema
- Find out its **functional dependencies**
  - They come from the application domain knowledge!
- Use them to design a better relational schema

# Functional Dependencies

- A form of constraint
  - Hence, part of the schema
- Finding them is part of the database design
- Use them to normalize the relations

# Functional Dependencies (FDs)

## Definition:

If two tuples agree on the attributes

$$A_1, A_2, \dots, A_n$$

then they must also agree on the attributes

$$B_1, B_2, \dots, B_m$$

## Formally:

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

# When Does an FD Hold

Definition:  $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$  holds in R if:

$\forall t, t' \in R,$

$(t.A_1 = t'.A_1 \wedge \dots \wedge t.A_m = t'.A_m \Rightarrow t.B_1 = t'.B_1 \wedge \dots \wedge t.B_n = t'.B_n)$

R	$A_1$	...	$A_m$		$B_1$	...	$B_n$		
t									
t'									



if t, t' agree here



then t, t' agree here

# Example

An FD holds, or does not hold on an instance:

<b>EmpID</b>	<b>Name</b>	<b>Phone</b>	<b>Position</b>
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

EmpID → Name, Phone, Position

Position → Phone

but not Phone → Position

# Example

<b>EmpID</b>	<b>Name</b>	<b>Phone</b>	<b>Position</b>
E0045	Smith	1234	Clerk
E3542	Mike	9876 ←	Salesrep
E1111	Smith	9876 ←	Salesrep
E9999	Mary	1234	Lawyer

Position → Phone

# Example

<b>EmpID</b>	<b>Name</b>	<b>Phone</b>	<b>Position</b>
E0045	Smith	1234 →	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234 →	Lawyer

But not Phone → Position



# Example

FD's are constraints:

- On some instances they hold
- On others they don't

$name \rightarrow color$   
 $category \rightarrow department$   
 $color, category \rightarrow price$

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99

Does this instance satisfy all the FDs ?

# Example

name → color  
category → department  
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Black	Toys	99
Gizmo	Stationary	Green	Office-sup.	59

What about this one ?

# An Interesting Observation

If all these FDs are true:

name  $\rightarrow$  color  
category  $\rightarrow$  department  
color, category  $\rightarrow$  price

Then this FD also holds:

name, category  $\rightarrow$  price

Why ??

# Goal: Find ALL Functional Dependencies

- Anomalies occur when certain “bad” FDs hold
- We know some of the FDs
- Need to find *all* FDs
- Then look for the bad ones

# Armstrong's Rules (1/3)

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

Is equivalent to

$$\begin{array}{l} A_1, A_2, \dots, A_n \rightarrow B_1 \\ A_1, A_2, \dots, A_n \rightarrow B_2 \\ \dots \dots \dots \\ A_1, A_2, \dots, A_n \rightarrow B_m \end{array}$$

**Splitting rule  
and  
Combing rule**

	A1	...	Am		B1	...	Bm	

# Armstrong's Rules (2/3)

$$A_1, A_2, \dots, A_n \rightarrow A_i$$

Trivial Rule

where  $i = 1, 2, \dots, n$

Why ?

	$A_1$	...	$A_m$	

# Armstrong's Rules (3/3)

## Transitive Rule

If

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

and

$$B_1, B_2, \dots, B_m \rightarrow C_1, C_2, \dots, C_p$$

then

$$A_1, A_2, \dots, A_n \rightarrow C_1, C_2, \dots, C_p$$

Why ?

# Armstrong's Rules (3/3)

## Illustration

	$A_1$	...	$A_m$		$B_1$	...	$B_m$		$C_1$	...	$C_p$	



# Example (continued)

Start from the following FDs:

1. name  $\rightarrow$  color
2. category  $\rightarrow$  department
3. color, category  $\rightarrow$  price

Infer the following FDs:

Inferred FD	Which Rule did we apply ?
4. name, category $\rightarrow$ name	
5. name, category $\rightarrow$ color	
6. name, category $\rightarrow$ category	
7. name, category $\rightarrow$ color, category	
8. name, category $\rightarrow$ price	

# Example (continued)

Answers:

1. name  $\rightarrow$  color
2. category  $\rightarrow$  department
3. color, category  $\rightarrow$  price

Inferred FD	Which Rule did we apply ?
4. name, category $\rightarrow$ name	Trivial rule
5. name, category $\rightarrow$ color	Transitivity on 4, 1
6. name, category $\rightarrow$ category	Trivial rule
7. name, category $\rightarrow$ color, category	Split/combine on 5, 6
8. name, category $\rightarrow$ price	Transitivity on 3, 7

THIS IS TOO HARD ! Let's see an easier way.

# Closure of a set of Attributes

**Given** a set of attributes  $A_1, \dots, A_n$

The **closure**,  $\{A_1, \dots, A_n\}^+$  = the set of attributes  $B$   
s.t.  $A_1, \dots, A_n \rightarrow B$

Example:

$\text{name} \rightarrow \text{color}$   
 $\text{category} \rightarrow \text{department}$   
 $\text{color, category} \rightarrow \text{price}$

Closures:

$\text{name}^+ = \{\text{name}, \text{color}\}$

$\{\text{name}, \text{category}\}^+ = \{\text{name}, \text{category}, \text{color}, \text{department}, \text{price}\}$

$\text{color}^+ = \{\text{color}\}$

# Closure Algorithm

$X = \{A_1, \dots, A_n\}$ .

**Repeat until**  $X$  doesn't change **do:**  
**if**  $B_1, \dots, B_n \rightarrow C$  is a FD **and**  
 $B_1, \dots, B_n$  are all in  $X$   
**then** add  $C$  to  $X$ .

Example:

$\text{name} \rightarrow \text{color}$   
 $\text{category} \rightarrow \text{department}$   
 $\text{color, category} \rightarrow \text{price}$

$\{\text{name, category}\}^+ =$   
 $\{\text{name, category, color, department, price}\}$

Hence:  $\text{name, category} \rightarrow \text{color, department, price}$

# Example

In class:

$R(A,B,C,D,E,F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute  $\{A,B\}^+$   $X = \{A, B, \}$

Compute  $\{A, F\}^+$   $X = \{A, F, \}$

# Example

In class:

$R(A, B, C, D, E, F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute  $\{A, B\}^+$   $X = \{A, B, C, D, E\}$

Compute  $\{A, F\}^+$   $X = \{A, F, \quad \}$

# Example

In class:

$R(A,B,C,D,E,F)$

A, B	→	C
A, D	→	E
B	→	D
A, F	→	B

Compute  $\{A,B\}^+$   $X = \{A, B, C, D, E\}$

Compute  $\{A, F\}^+$   $X = \{A, F, B, C, D, E\}$

# Why Do We Need Closure

- With closure we can find all FD's easily
- To check if  $X \rightarrow A$ 
  - Compute  $X^+$
  - Check if  $A \in X^+$



# Using Closure to Infer ALL FDs

Example: 
$$\begin{array}{l} A, B \rightarrow C \\ A, D \rightarrow B \\ B \rightarrow D \end{array}$$

Step 1: Compute  $X^+$ , for every  $X$ :

$$\begin{array}{l} A^+ = A, \quad B^+ = BD, \quad C^+ = C, \quad D^+ = D \\ AB^+ = ABCD, \quad AC^+ = AC, \quad AD^+ = ABCD, \\ \quad \quad \quad BC^+ = BCD, \quad BD^+ = BD, \quad CD^+ = CD \\ ABC^+ = ABD^+ = ACD^+ = ABCD \text{ (no need to compute— why ?)} \\ BCD^+ = BCD, \quad ABCD^+ = ABCD \end{array}$$

Step 2: Enumerate all FD's  $X \rightarrow Y$ , s.t.  $Y \subseteq X^+$  and  $X \cap Y = \emptyset$ :

$$AB \rightarrow CD, \quad AD \rightarrow BC, \quad BC \rightarrow D, \quad ABC \rightarrow D, \quad ABD \rightarrow C, \quad ACD \rightarrow B$$

# Another Example

- Enrollment(student, major, course, room, time)  
student → major  
major, course → room  
course → time

What else can we infer ? [in class, or at home]

# Keys

- A **superkey** is a set of attributes  $A_1, \dots, A_n$  s.t. for any other attribute  $B$ , we have  $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
  - I.e. set of attributes which is a superkey and for which no subset is a superkey

# Computing (Super)Keys

- Compute  $X^+$  for all sets  $X$
- If  $X^+ =$  all attributes, then  $X$  is a superkey
- List only the minimal  $X$ 's to get the keys

# Example

Product(name, price, category, color)

name, category → price  
category → color

What is the key ?

# Example

Product(name, price, category, color)

name, category $\rightarrow$ price category $\rightarrow$ color
--

What is the key ?

$(\text{name, category})^+ = \{ \text{name, category, price, color} \}$

Hence (name, category) is a key

# Examples of Keys

Enrollment(student, address, course, room, time)

student → address

room, time → course

student, course → room, time

(find keys at home)

# Eliminating Anomalies

Main idea:

- $X \rightarrow A$  is OK if  $X$  is a (super)key
- $X \rightarrow A$  is not OK otherwise



# Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

SSN  $\rightarrow$  Name, City

What is the key?

{SSN, PhoneNumber}

Hence SSN  $\rightarrow$  Name, City  
is a “bad” dependency

# Key or Keys ?

Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more keys

# Key or Keys ?

Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more keys

$\boxed{\begin{array}{l} AB \rightarrow C \\ BC \rightarrow A \end{array}}$       or       $\boxed{\begin{array}{l} A \rightarrow BC \\ B \rightarrow AC \end{array}}$

what are the keys here ?

Can you design FDs such that there are *three* keys ?

# Boyce-Codd Normal Form

A simple condition for removing anomalies from relations:

A relation  $R$  is in BCNF if:

If  $A_1, \dots, A_n \rightarrow B$  is a non-trivial dependency in  $R$ ,  
then  $\{A_1, \dots, A_n\}$  is a superkey for  $R$

In other words: there are no “bad” FDs

Equivalently:

for all  $X$ , either  $(X^+ = X)$  or  $(X^+ = \text{all attributes})$

# BCNF Decomposition Algorithm

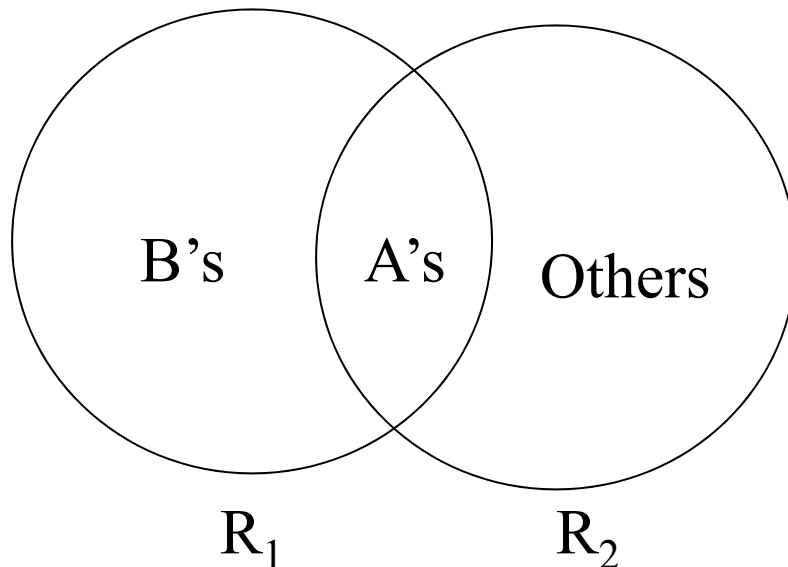
**repeat**

choose  $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$  that violates BCNF

split  $R$  into  $R_1(A_1, \dots, A_m, B_1, \dots, B_n)$  and  $R_2(A_1, \dots, A_m, [\text{others}])$

continue with both  $R_1$  and  $R_2$

**until** no more violations



Is there a  
2-attribute  
relation that is  
not in BCNF ?

In practice, we have  
a better algorithm (coming up)

# Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

SSN → Name, City

What is the key?

{SSN, PhoneNumber} use SSN → Name, City  
to split

# Example

Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

SSN → Name, City

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

Let's check anomalies:

- Redundancy ?
- Update ?
- Delete ?

# Example Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

FD1: SSN  $\rightarrow$  name, age

FD2: age  $\rightarrow$  hairColor

Decompose in BCNF (in class):



# Example Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

FD1: SSN  $\rightarrow$  name, age

FD2: age  $\rightarrow$  hairColor

Decompose in BCNF (in class): What is the key?

{SSN, phoneNumber}

But how to decompose?

Person(SSN, name, age)

Phone(SSN, hairColor, phoneNumber)

Or

Person(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Or ....

# BCNF Decomposition Algorithm

BCNF\_Decompose(R)

find  $X$  s.t.:  $X \neq X^+ \neq$  [all attributes]

**if** (not found) **then** “R is in BCNF”

**let**  $Y = X^+ - X$

**let**  $Z =$  [all attributes]  $- X^+$

decompose R into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$

continue to decompose recursively  $R_1$  and  $R_2$

Find  $X$  s.t.:  $X \neq X^+ \neq$  [all attributes]

## Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN  $\rightarrow$  name, age

age  $\rightarrow$  hairColor

Iteration 1: Person

SSN<sup>+</sup> = SSN, name, age, hairColor

Decompose into: P(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Iteration 2: P

age<sup>+</sup> = age, hairColor

Decompose: People(SSN, name, age)

Hair(age, hairColor)

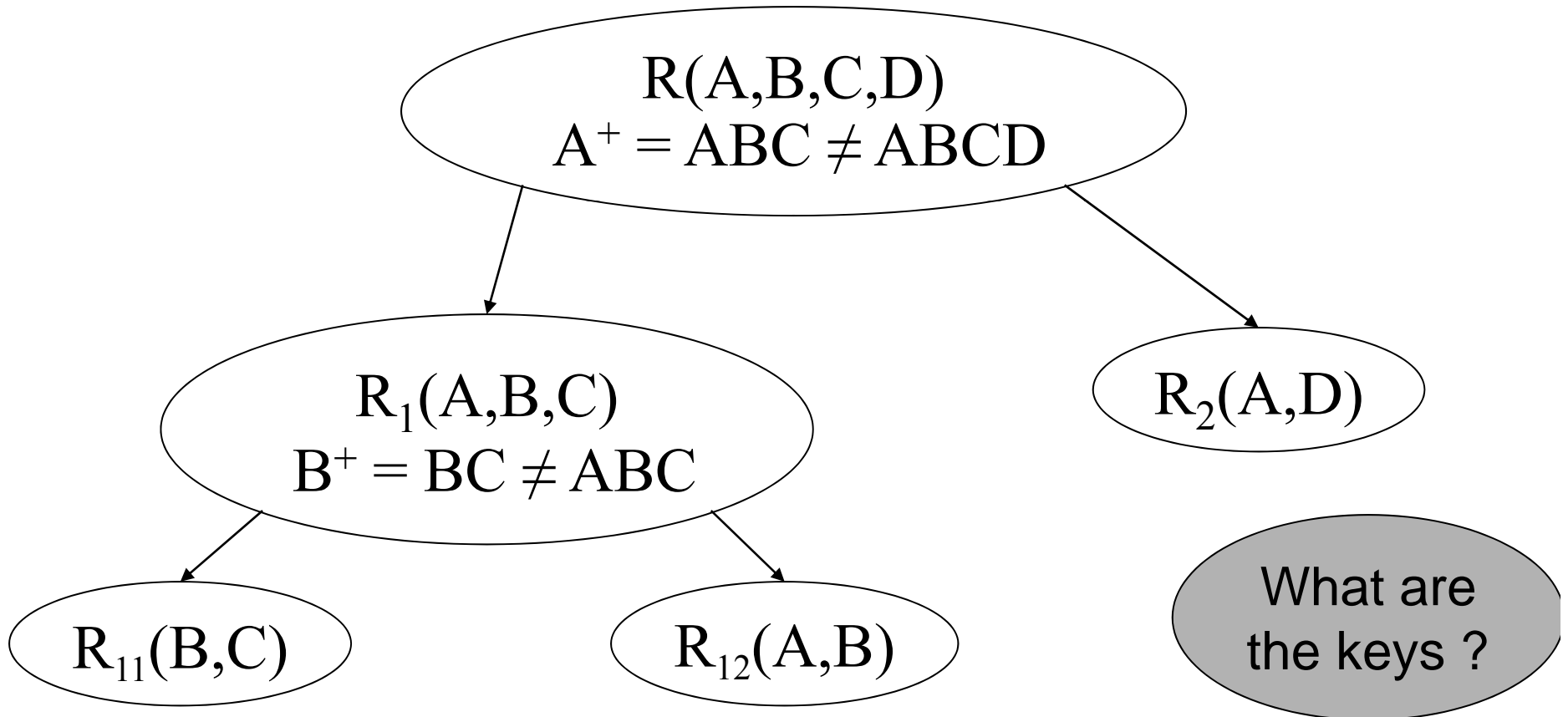
Phone(SSN, phoneNumber)

What are  
the keys ?

R(A,B,C,D)

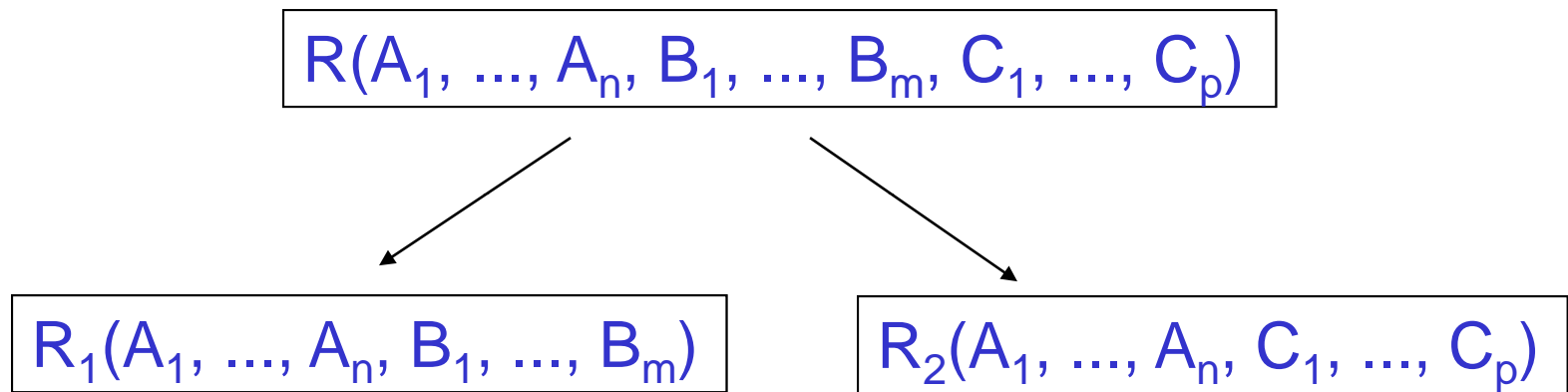
A → B  
B → C

# Example



What happens if in R we first pick B+ ? Or AB+ ?

# Decompositions in General

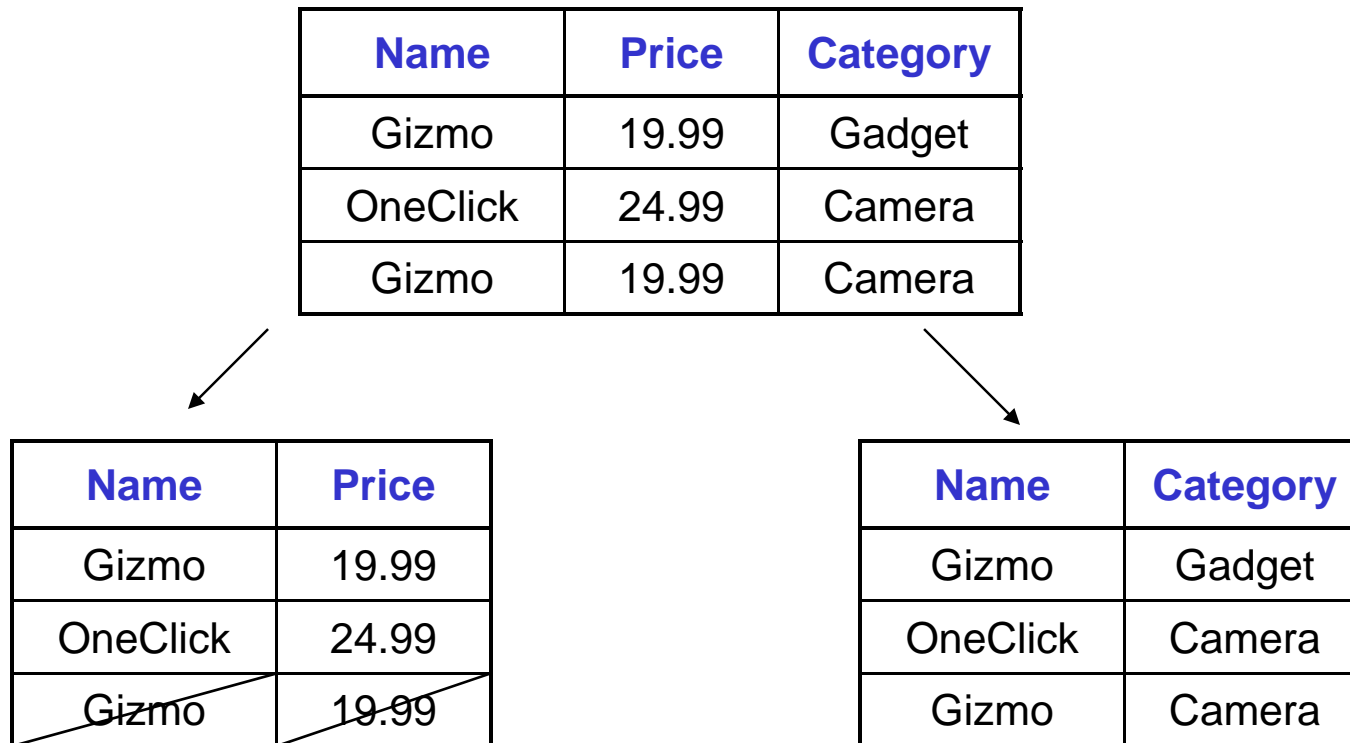


$R_1$  = projection of  $R$  on  $A_1, \dots, A_n, B_1, \dots, B_m$

$R_2$  = projection of  $R$  on  $A_1, \dots, A_n, C_1, \dots, C_p$

# Theory of Decomposition

- Sometimes it is correct:



Lossless decomposition

# Incorrect Decomposition

- Sometimes it is not:

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
Gizmo	19.99	Camera

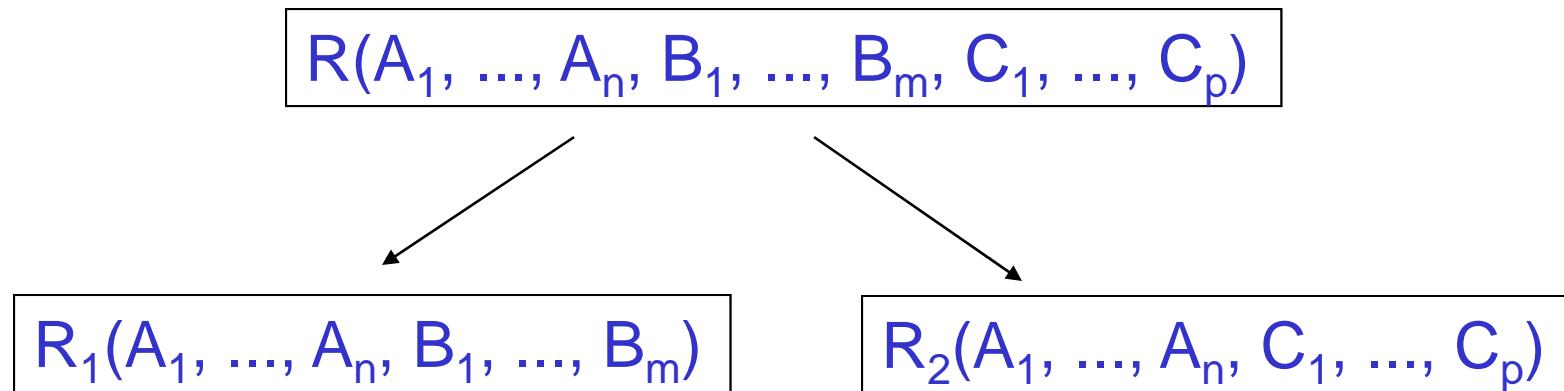
What's incorrect ??

Name	Category
Gizmo	Gadget
OneClick	Camera
Gizmo	Camera

Price	Category
19.99	Gadget
24.99	Camera
19.99	Camera

Lossy decomposition

# Decompositions in General



If  $A_1, \dots, A_n \rightarrow B_1, \dots, B_m$   
Then the decomposition is lossless

Note: don't need  $A_1, \dots, A_n \rightarrow C_1, \dots, C_p$

BCNF decomposition is always lossless. WHY ?



# Optional

- The following four slides are optional
- The content will not be on any exam
- But please take a look because they motivate the need for 3NF
- It's good to know at least why 3NF exists

# General Decomposition Goals

1. Elimination of anomalies
2. Recoverability of information
  - Can we get the original relation back?
3. Preservation of dependencies
  - Want to enforce FDs without performing joins

Sometimes cannot decomposed into BCNF without losing ability to check some FDs

# BCNF and Dependencies

Unit	Company	Product

FD's:  $\text{Unit} \rightarrow \text{Company}$ ;  $\text{Company, Product} \rightarrow \text{Unit}$

So, there is a BCNF violation, and we decompose.

# BCNF and Dependencies

Unit	Company	Product

FD's:  $\text{Unit} \rightarrow \text{Company}$ ;  $\text{Company, Product} \rightarrow \text{Unit}$

So, there is a BCNF violation, and we decompose.

Unit	Company

$\text{Unit} \rightarrow \text{Company}$

Unit	Product

No FDs

In BCNF we lose the FD:  $\text{Company, Product} \rightarrow \text{Unit}$

# 3NF Motivation

A relation R is in 3rd normal form if :

Whenever there is a nontrivial dep.  $A_1, A_2, \dots, A_n \rightarrow B$  for R,  
then  $\{A_1, A_2, \dots, A_n\}$  is a super-key for R,  
or B is part of a key.

## Tradeoffs

BCNF = no anomalies, but may lose some FDs

3NF = keeps all FDs, but may have some anomalies