

Image Filtering, Part 2: Resampling



Images by [Pawan Sinha](#)

Today's readings

- [Forsyth & Ponce](#), chapters 8.1-8.2
– <http://www.cs.washington.edu/education/courses/490cv/02w/readings/book-7-revised-a-indx.pdf>

Announcements

Photoshop help sessions for project 1

- Today after class (228)
- Thursday at 6pm (228)

Demo sessions next Thursday 12-2:30

- [signup online](#)

Image Scaling

This image is too big to fit on the screen. How can we reduce it?

How to generate a half-sized version?



Image sub-sampling



1/8

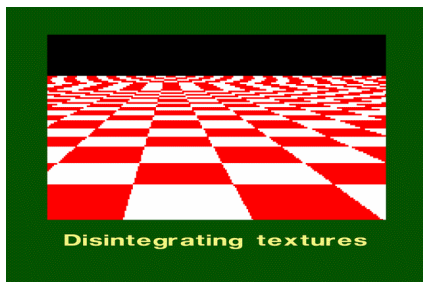
1/4

Throw away every other row and column to create a 1/2 size image

Why does this look so cruffy?

- Called **nearest-neighbor** sampling

Even worse for synthetic images



Sampling and the Nyquist rate

Aliasing can arise when you sample a continuous signal or image

- Demo applet
http://www.cs.brown.edu/exploratories/freeSoftware/repository/edu/brown/cs/exploratories/applets/nyquist/nyquist_limit_java_plugin.html
- occurs when your sampling rate is not high enough to capture the amount of detail in your image
- formally, the image contains structure at different scales
 - called "frequencies" in the Fourier domain
- the sampling rate must be high enough to capture the highest frequency in the image

To avoid aliasing:

- sampling rate $> 2 * \text{max frequency in the image}$
 - i.e., need more than two samples per period
- This minimum sampling rate is called the **Nyquist rate**

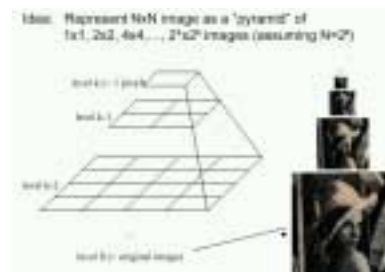
Subsampling with Gaussian pre-filtering



Solution: filter the image, *then* subsample

- Filter size should double for each $\frac{1}{2}$ size reduction. Why?
- How can we speed this up?

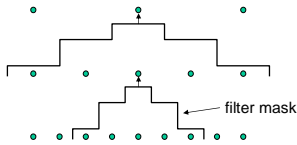
Some times we want many resolutions



Known as a **Gaussian Pyramid** [Burt and Adelson, 1983]

- In computer graphics, a *mip map* [Williams, 1983]
 - A precursor to *wavelet transform*
- Gaussian Pyramids have all sorts of applications in computer vision
- We'll talk about these later in the course

Gaussian pyramid construction



Repeat

- Filter
- Subsample

Until minimum resolution reached

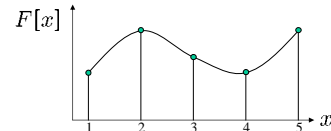
- can specify desired number of levels (e.g., 3-level pyramid)

The whole pyramid is only 4/3 the size of the original image!

Image resampling

So far, we considered only power-of-two subsampling

- What about arbitrary scale reduction?
- How can we increase the size of the image?



d = 1 in this example

Recall how a digital image is formed

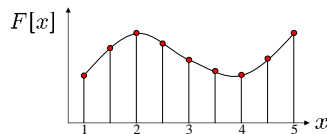
$$F[x, y] = \text{quantize}\{f(xd, yd)\}$$

- It is a discrete point-sampling of a continuous function
- If we could somehow reconstruct the original function, any new image could be generated, at any resolution and scale

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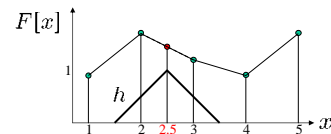
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Image resampling

So what to do if we don't know f

- Answer: guess an approximation \tilde{f}
- Can be done in a principled way: filtering



d = 1 in this example

Image reconstruction

- Convert F to a continuous function

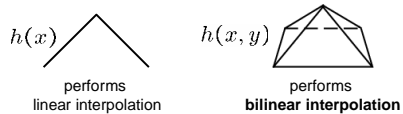
$$f_F(x) = F\left(\frac{x}{d}\right) \text{ when } \frac{x}{d} \text{ is an integer, } 0 \text{ otherwise}$$

- Reconstruct by cross-correlation:

$$\tilde{f} = h \otimes f_F$$

Resampling filters

What does the 2D version of this hat function look like?



Better filters give better resampled images

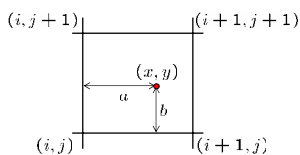
- Bicubic is common choice
 - fit 3rd degree polynomial surface to pixels in neighborhood
 - can also be implemented by a convolution or cross-correlation

Subsampling with bilinear pre-filtering



Bilinear interpolation

A common method for resampling images



$$F(x, y) = (1 - a)(1 - b) F(i, j) + a(1 - b) F(i + 1, j) + ab F(i + 1, j + 1) + (1 - a)b F(i, j + 1)$$

Things to take away from this lecture

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- An image as a function
- Digital vs. continuous images
- Image transformation: range vs. domain
- Types of noise
- LSI filters
 - cross-correlation and convolution
 - properties of LSI filters
 - mean, Gaussian, bilinear filters
- Median filtering
- Image scaling
- Image resampling
- Aliasing
- Gaussian pyramids
- Bilinear interpolation