

Announcements

- Project 2 artifact winners
- Project 3
 - demo session at the end of class

Photometric Stereo

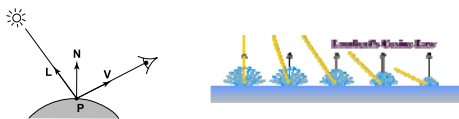


Merle Norman Cosmetics, Los Angeles

Readings

- Forsyth and Ponce, section 5.4
 - online: <http://www.cs.berkeley.edu/~daf/bookpages/bdf/chap05-final.pdf>

Diffuse reflection



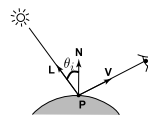
$$R_e = k_d \mathbf{N} \cdot \mathbf{L} R_i$$

image intensity of P $\rightarrow I = k_d \mathbf{N} \cdot \mathbf{L}$

Simplifying assumptions

- $I = R_e$: camera response function f is the identity function:
 - can always achieve this in practice by solving for f and applying f^{-1} to each pixel in the image
- $R_i = 1$: light source intensity is 1
 - can achieve this by dividing each pixel in the image by R_i

Shape from shading



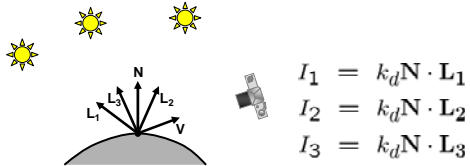
Suppose $k_d = 1$

$$\begin{aligned} I &= k_d \mathbf{N} \cdot \mathbf{L} \\ &= \mathbf{N} \cdot \mathbf{L} \\ &= \cos \theta_i \end{aligned}$$

You can directly measure angle between normal and light source

- Not quite enough information to compute surface shape
- But can be if you add some additional info, for example
 - assume a few of the normals are known (e.g., along silhouette)
 - constraints on neighboring normals—"integrability"
 - smoothness
- Hard to get it to work well in practice
 - plus, how many real objects have constant albedo?

Photometric stereo



Can write this as a matrix equation:

$$\begin{bmatrix} I_1 & I_2 & I_3 \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} \mathbf{L}_1 & \mathbf{L}_2 & \mathbf{L}_3 \end{bmatrix}$$

Solving the equations

$$\underbrace{\begin{bmatrix} I_1 & I_2 & I_3 \end{bmatrix}}_{\mathbf{I}_{1 \times 3}} = k_d \mathbf{N}^T \underbrace{\begin{bmatrix} \mathbf{L}_1 & \mathbf{L}_2 & \mathbf{L}_3 \end{bmatrix}}_{\mathbf{L}_{3 \times 3}}$$

$$\mathbf{G} = \mathbf{I} \mathbf{L}^{-1}$$

$$k_d = \|\mathbf{G}\|$$

$$\mathbf{N} = \frac{1}{k_d} \mathbf{G}$$

More than three lights

Get better results by using more lights

$$\begin{bmatrix} I_1 & \dots & I_n \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} \mathbf{L}_1 & \dots & \mathbf{L}_n \end{bmatrix}$$

Least squares solution:

$$\begin{aligned} \mathbf{I} &= \mathbf{G} \mathbf{L} \\ \mathbf{I} \mathbf{L}^T &= \mathbf{G} \mathbf{L} \mathbf{L}^T \\ \mathbf{G} &= (\mathbf{I} \mathbf{L}^T) (\mathbf{L} \mathbf{L}^T)^{-1} \end{aligned}$$

Solve for \mathbf{N} , k_d as before

What's the size of $\mathbf{L} \mathbf{L}^T$?

Computing light source directions

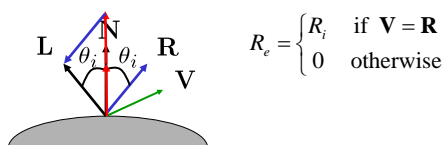
Trick: place a chrome sphere in the scene



- the location of the highlight tells you where the light source is

Recall the rule for specular reflection

For a perfect mirror, light is reflected about \mathbf{N}



$$R_e = \begin{cases} R_i & \text{if } \mathbf{V} = \mathbf{R} \\ 0 & \text{otherwise} \end{cases}$$

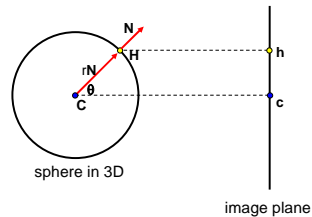
We see a highlight when $\mathbf{V} = \mathbf{R}$

- then \mathbf{L} is given as follows:

$$\mathbf{L} = 2(\mathbf{N} \cdot \mathbf{R})\mathbf{N} - \mathbf{R}$$

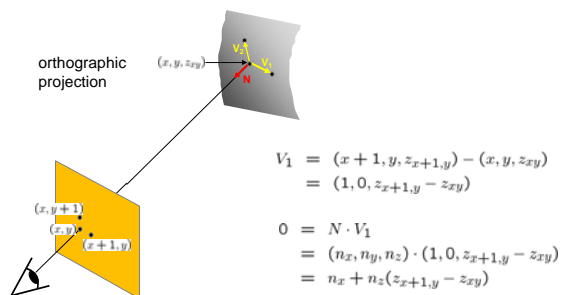
Computing the light source direction

Chrome sphere that has a highlight at position \mathbf{h} in the image



Can compute θ (and hence \mathbf{N}) from this figure
Now just reflect \mathbf{V} about \mathbf{N} to obtain \mathbf{L}

Depth from normals



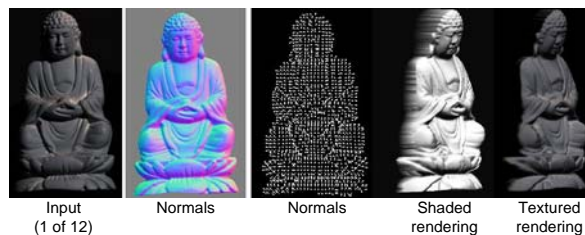
$$\begin{aligned} \mathbf{V}_1 &= (x+1, y, z_{x+1,y}) - (x, y, z_{xy}) \\ &= (1, 0, z_{x+1,y} - z_{xy}) \end{aligned}$$

$$\begin{aligned} 0 &= \mathbf{N} \cdot \mathbf{V}_1 \\ &= (n_x, n_y, n_z) \cdot (1, 0, z_{x+1,y} - z_{xy}) \\ &= n_x + n_z(z_{x+1,y} - z_{xy}) \end{aligned}$$

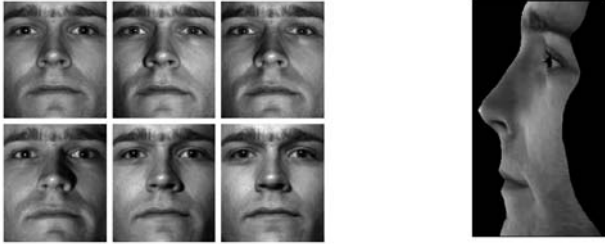
Get a similar equation for \mathbf{V}_2

- Each normal gives us two linear constraints on z
- compute z values by solving a matrix equation

Results...



Results...



from Athos Georghiades
<http://cvc.yale.edu/people/Athos.html>

Limitations

Big problems

- doesn't work for shiny things, semi-translucent things
- shadows, inter-reflections

Smaller problems

- camera and lights have to be distant
 - measure light source directions, intensities
 - camera response function

Trick for handling shadows

Weight each equation by the pixel brightness:

$$I_i(I_i) = I_i[k_d \mathbf{N} \cdot \mathbf{L}_i]$$

Gives weighted least-squares matrix equation:

$$\begin{bmatrix} I_1^2 & \dots & I_n^2 \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} I_1 \mathbf{L}_1 & \dots & I_n \mathbf{L}_n \end{bmatrix}$$

Solve for \mathbf{N} , k_d as before