Announcements

- Photos right now
- Project 3 questions
- · Midterms back at the end of class

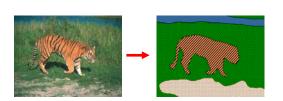
Image Segmentation



Today's Readings

- Shapiro, pp. 279-289
 - http://www.dai.ed.ac.uk/HIPR2/morops.htm
 - Dilation, erosion, opening, closing

From images to objects



What Defines an Object?

- Subjective problem, but has been well-studied
- Gestalt Laws seek to formalize this
 - proximity, similarity, continuation, closure, common fate
 - see $\underline{\text{notes}}$ by Steve Joordens, U. Toronto

Image Segmentation

We will consider different methods

Already covered:

Intelligent Scissors (contour-based, manual)

Today—automatic methods:

- K-means clustering (color-based)
- Normalized Cuts (region-based)

Image histograms

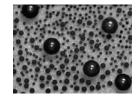


How many "orange" pixels are in this image?

- This type of question answered by looking at the histogram
- A histogram counts the number of occurrences of each color
 - Given an image $\ F[x,y] o RGB$
 - The histogram is $H_F[c] = |\{(x,y) \mid F[x,y] = c\}|$
 - » i.e., for each color value c (x-axis), plot # of pixels with that color (y-axis)
 - What is the dimension of the histogram of an NxN RGB image?

What do histograms look like?

Photoshop demo



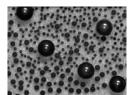


How Many Modes Are There?

• Easy to see, hard to compute

Histogram-based segmentation

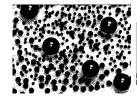
- Break the image into K regions (segments)
- Solve this by reducing the number of colors to K and mapping each pixel to the closest color
 - photoshop demo

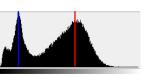




Histogram-based segmentation

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 - photoshop demo



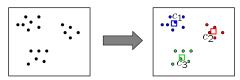


Here's what it looks like if we use two colors

Clustering

How to choose the representative colors?

• This is a clustering problem!



Objective

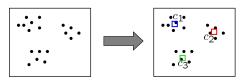
· Each point should be as close as possible to a cluster center - Minimize sum squared distance of each point to closest center

$$\sum_{\text{clusters } i} \quad \sum_{\text{points p in cluster } i} \|p - c_i\|^2$$

Break it down into subproblems

Suppose I tell you the cluster centers ci

- Q: how to determine which points to associate with each c;?
- A: for each point p, choose closest c_{i}



Suppose I tell you the points in each cluster

- Q: how to determine the cluster centers?
 A: choose c_i to be the mean of all points in the cluster

K-means clustering

K-means clustering algorithm

- 1. Randomly initialize the cluster centers, $c_1, ..., c_K$
- 2. Given cluster centers, determine points in each cluster
 - For each point p, find the closest c_i . Put p into cluster i
- 3. Given points in each cluster, solve for ci
- Set c_i to be the mean of points in cluster i
- 4. If c, have changed, repeat Step 2

Java demo: http://home.dei.polimi.it/matteucc/Clustering/tutorial_html/AppletKM.html

Properties

- Will always converge to some solution
- Can be a "local minimum"

• does not always find the global minimum of objective function:
$$\sum_{\text{clusters } i} \sum_{\text{p oints p in cluster } i} ||p-c_i||^2$$

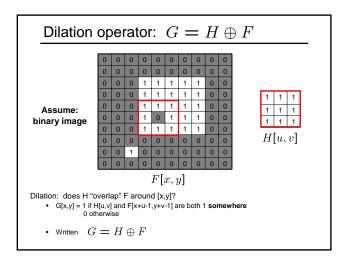
Cleaning up the result

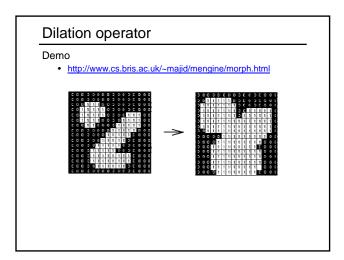
Problem:

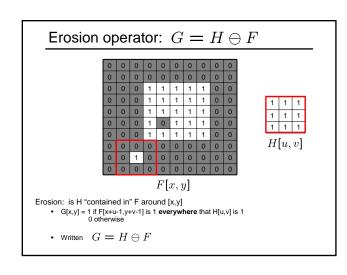
- Histogram-based segmentation can produce messy regions
 - segments do not have to be connected
 - may contain holes

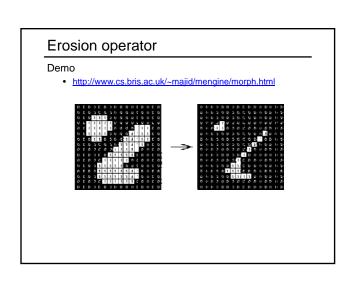
How can these be fixed?

photoshop demo









Nested dilations and erosions

What does this operation do?

$$G = H \ominus (H \oplus F)$$

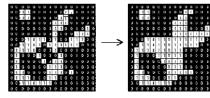


• this is called a **closing** operation

Nested dilations and erosions

What does this operation do?

$$G = H \ominus (H \oplus F)$$



• this is called a closing operation

Is this the same thing as the following?

$$G = H \oplus (H \ominus F)$$

Nested dilations and erosions

What does this operation do?

$$G = H \oplus (H \ominus F)$$

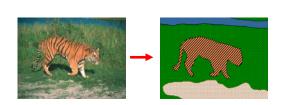
- this is called an **opening** operation
- http://www.dai.ed.ac.uk/HIPR2/open.htm

You can clean up binary pictures by applying combinations of dilations and erosions

Dilations, erosions, opening, and closing operations are known as **morphological operations**

• see http://www.dai.ed.ac.uk/HIPR2/morops.htm

Graph-based segmentation?



Images as graphs





Fully-connected graph

- · node for every pixel
- link between every pair of pixels, p,q
- cost cpq for each link

Segmentation by Graph Cuts

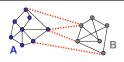




Break Graph into Segments

- · Delete links that cross between segments
- · Easiest to break links that have low cost (low similarity)
 - similar pixels should be in the same segments
 - dissimilar pixels should be in different segments

Cuts in a graph



Link Cut

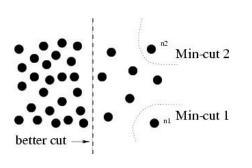
- set of links whose removal makes a graph disconnected
- · cost of a cut:

$$cut(A,B) = \sum_{p \in A, q \in B} c_{p,q}$$

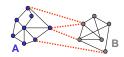
Find minimum cut

- gives you a segmentation fast algorithms exist for doing this

But min cut is not always the best cut...



Cuts in a graph



Normalized Cut

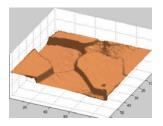
- a cut penalizes large segments
- fix by normalizing for size of segments

$$Ncut(A,B) = \frac{cut(A,B)}{volume(A)} + \frac{cut(A,B)}{volume(B)}$$

• volume(A) = sum of costs of all edges that touch A

Interpretation as a Dynamical System





Treat the links as springs and shake the system

• elasticity proportional to cost

• vibration "modes" correspond to segments

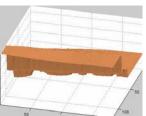
- can compute these by solving an eigenvector problem

- for more details, see

* J. Shi and J. Malik, Normalized Cuts and Image Segmentation, CVPR, 1997

Interpretation as a Dynamical System





Color Image Segmentation