

Ray Tracing

Reading

Foley *et al.*, 16.12

Optional:

- Glassner, An introduction to Ray Tracing, Academic Press, Chapter 1.
- T. Whitted. "An improved illumination model for shaded display". *Communications of the ACM* 23(6), 343-349, 1980.

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Geometric optics

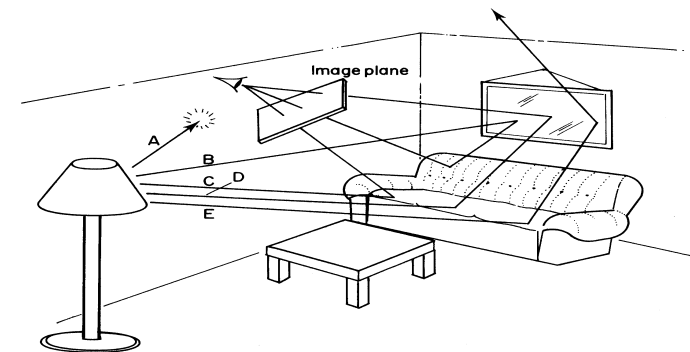
We will take the view of **geometric optics**

- Light is a flow of photons with wavelengths. We'll call these flows "light rays."
- Light rays travel in straight lines in free space.
- Light rays do not interfere with each other as they cross.
- Light rays obey the laws of reflection and refraction.
- Light rays travel from the light sources to the eye, but the physics is invariant under path reversal (reciprocity).

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Forward Ray Tracing

- Rays emanate from light sources and bounce around in the scene.
- Rays that pass through the projection plane and enter the eye contribute to the final image.

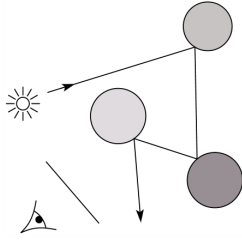


- What's wrong with this method?

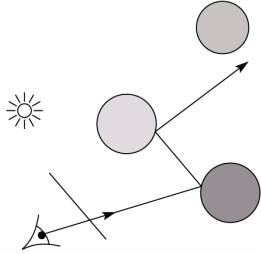
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Eye vs. Light

- Starting at the light (a.k.a. forward ray tracing, photon tracing)



- Starting at the eye (a.k.a. backward ray tracing)

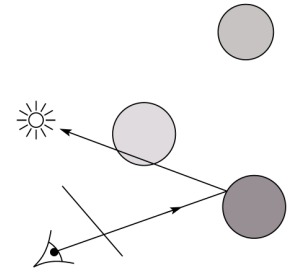


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Hybrid methods

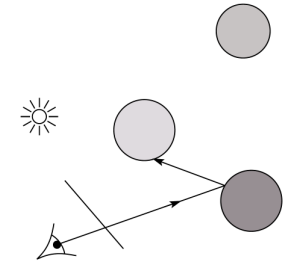
Local illumination

- Cast one ray, shade according to light



Appel (1968)

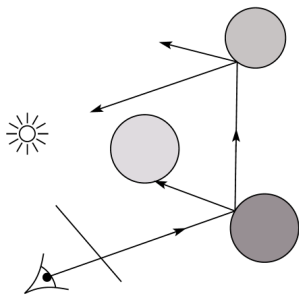
- Cast one eye ray & one ray to light



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Whitted (1980)

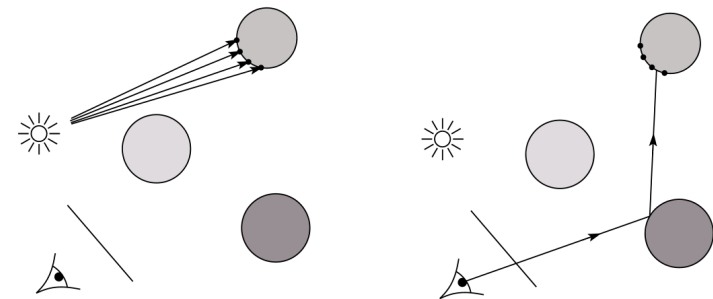
Eye ray tracing and rays to light & recursive ray tracing



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Heckbert (1990)

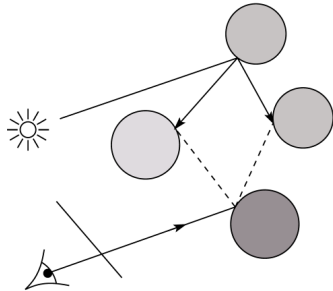
Ray tracing & light ray tracing & light storage on surface



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Veach (1995)

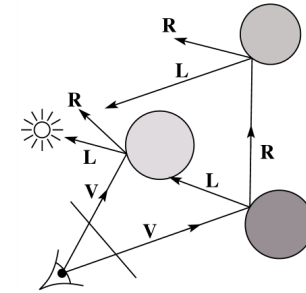
- Eye ray tracing & light ray tracing & path connection



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Whitted ray-tracing algorithm

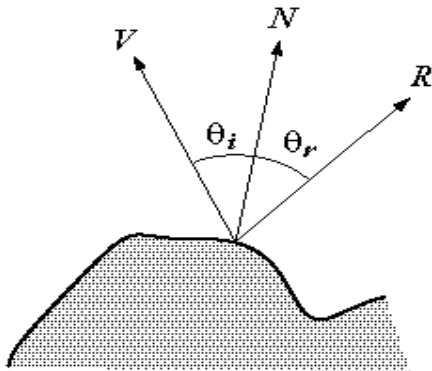
1. For each pixel, trace a **primary ray** to the first visible surface
2. For each intersection trace **secondary rays**:
 - **Shadow rays** in directions L_i to light sources
 - **Reflected ray** in direction R
 - **Refracted ray (transmitted ray)** in direction T



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Reflection

- Reflected light from objects behaves like specular reflection from light sources
 - Reflectivity is just specular color
 - Reflected light comes from direction of perfect specular reflection

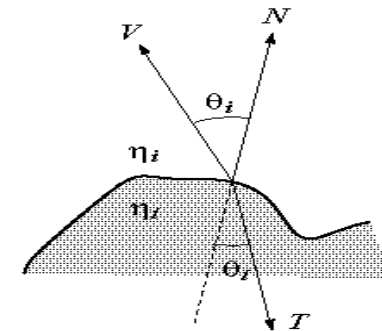


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Refraction

- Amount to transmit determined by transparency coefficient, which we store explicitly
- T comes from Snell's law

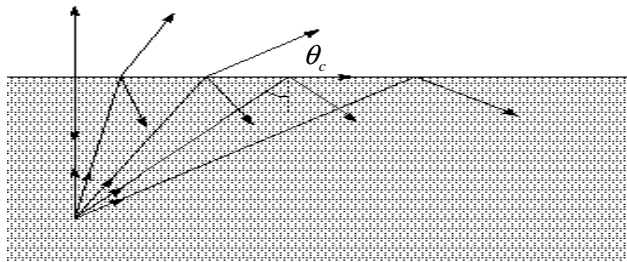
$$\eta_i \sin(\theta_i) = \eta_t \sin(\theta_t)$$



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Total Internal Reflection

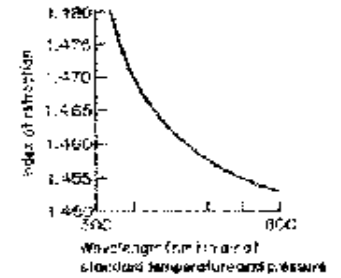
- When passing from a dense medium to a less dense medium, light is bent further away from the surface normal
- Eventually, it can bend right past the surface!
- The θ_i that causes θ_t to exceed 90 degrees is called the **critical angle (θ_c)**. For θ_i greater than the critical angle, no light is transmitted.
- A check for TIR falls out of the construction of T



Index of Refraction

- Real-world index of refraction is a complicated physical property of the material

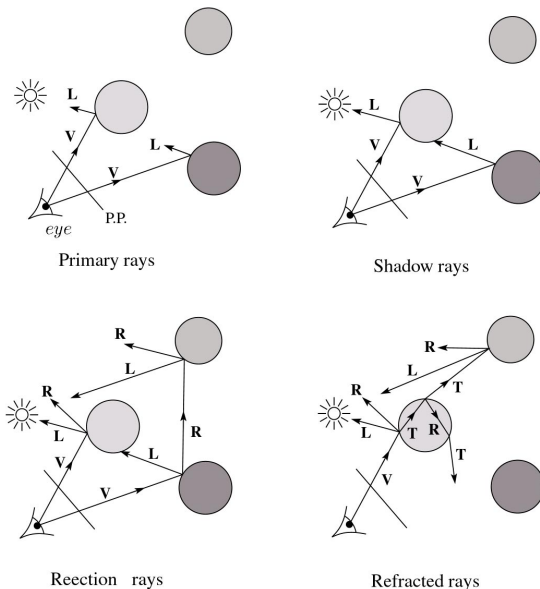
Medium	Index of refraction
Vacuum	1
Air	1.0003
Water	1.33
Fused quartz	1.46
Glass, crown	1.52
Glass, dense flint	1.66
Diamond	2.42



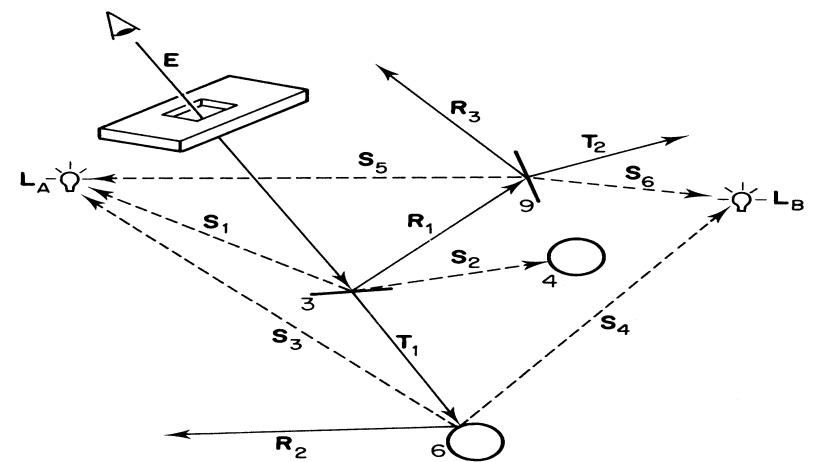
Index of refraction variation for fused quartz

- IOR also varies with wavelength, and even temperature!
- How can we account for wavelength dependence when ray tracing?

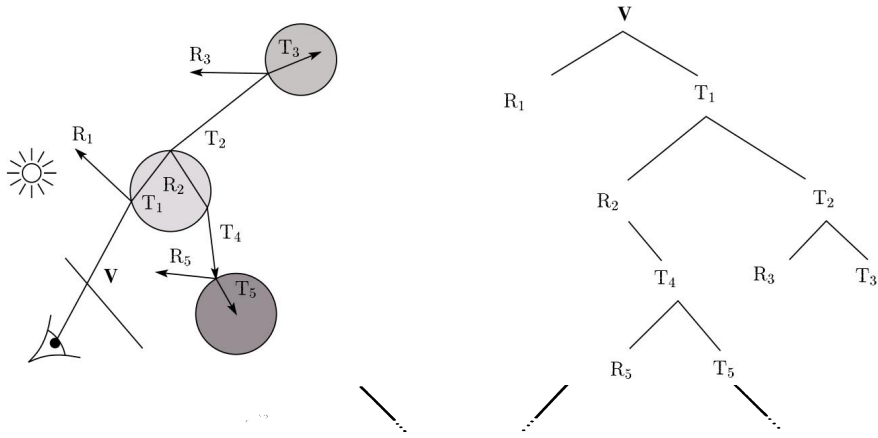
Stages of Whitted ray-tracing



Example of Ray Tracing



The Ray Tree



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Shading

If $I(P_0, \mathbf{u})$ is the intensity seen from point P along direction \mathbf{u}

$$I(P_0, \mathbf{u}) = I_{direct} + I_{reflected} + I_{transmitted}$$

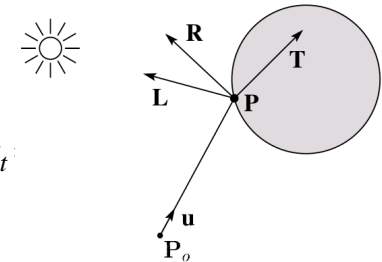
where

$$I_{direct} = \text{Shade}(\mathbf{N}, \mathbf{L}, \mathbf{u}, \mathbf{R}) \text{ (e.g. Phong shading model)}$$

$$I_{reflected} = k_r I(P, \mathbf{R})$$

$$I_{transmitted} = k_t I(P, \mathbf{T})$$

Typically, we set $k_r = k_s$ and k_t



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Parts of a Ray Tracer

- What major components make up the core of a ray tracer?
 - Outer loop sends primary rays into the scene
 - Trace arbitrary ray and compute its color contribution as it travels through the scene
 - Shading model

$$I = k_e + k_a I_a + \sum_i f(d_i) I_{li} \left[k_d (\mathbf{N} \cdot \mathbf{L}_i)_+ + k_s (\mathbf{V} \cdot \mathbf{R})_+^{n_s} \right]$$

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Outer Loop

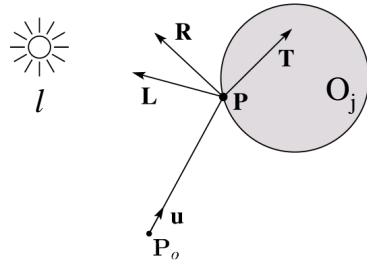
```

void traceImage (scene)
{
    for each pixel (i,j) in the image {
        p = pixelToWorld(i,j)
        c = COP
        d = (p - c) / ||p - c||
        I(i,j) = traceRay (scene, c, d)
    }
}
    
```

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Trace Pseudocode

```
color traceRay(point P0, direction u )
{
    (P, Oi) = intersect( P0, u);
    I = 0
    for each light source l {
        (P', LightObj) = intersect(P, dir(P, l))
        if LightObj = l {
            I = I + I(l)
        }
    }
    I = I + Obj.Kr * traceRay(P, R)
    I = I + Obj.Kt * traceRay(P, T)
    return I
}
```



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Controlling Tree Depth

- Ideally, we'd spawn child rays at every object intersection forever, getting a "perfect" color for the primary ray.
- In practice, we need heuristics for bounding the depth of the tree (i.e., recursion depth)
- ?

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Ray-object intersection

```
color traceRay(point P0, direction u )
{
    (P, Oi) = intersect( P0, u);
    I = 0
    for each light source l {
        (P', LightObj) = intersect(P, dir(P, l))
        if LightObj = l {
            I = I + I(l)
        }
    }
    I = I + Obj.Kr * traceRay(P, R)
    I = I + Obj.Kt * traceRay(P, T)
    return I
}
```

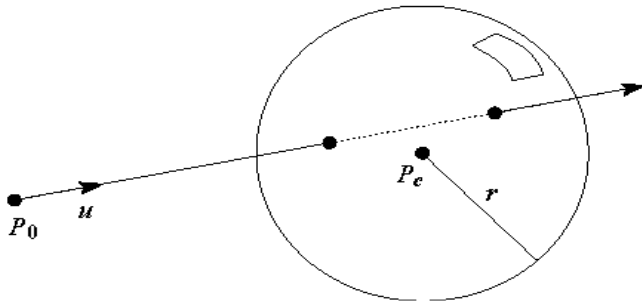
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Ray-Object Intersection

- Must define different intersection routine for each primitive
- The bottleneck of the ray tracer, so make it fast!
- Most general formulation: find all roots of a function of one variable
- In practice, many optimized intersection tests exist (see Glassner)

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Ray-Sphere Intersection



- Given a sphere centered at $P_c = [0,0,0]$ with radius r and a ray $P(t) = P_0 + tu$, find the intersection(s) of $P(t)$ with the sphere.

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Object hierarchies and ray intersection

How do we intersect with primitives transformed with affine transformations?

$$\mathbf{v}' = \begin{bmatrix} v_x \\ v_y \\ v_z \\ 0 \end{bmatrix} \mathbf{X}^{-1}$$

$$P' = \begin{bmatrix} P_x \\ P_y \\ P_z \\ 1 \end{bmatrix} \mathbf{X}^{-1}$$

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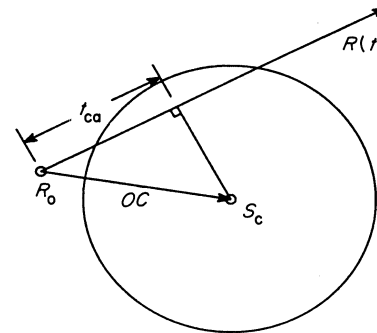
Numerical Error

- Floating-point roundoff can add up in a ray tracer, and create unwanted artifacts
 - Example: intersection point calculated to be ever-so-slightly *inside* the intersecting object. How does this affect child rays?
- Solutions:
 - Perturb child rays
 - Use global ray epsilon

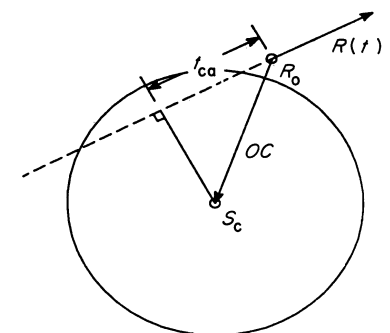
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Fast Failure

- We can greatly speed up ray-object intersection by identifying cheap tests that guarantee failure
- Example: if origin of ray is outside sphere and ray points away from sphere, fail immediately.



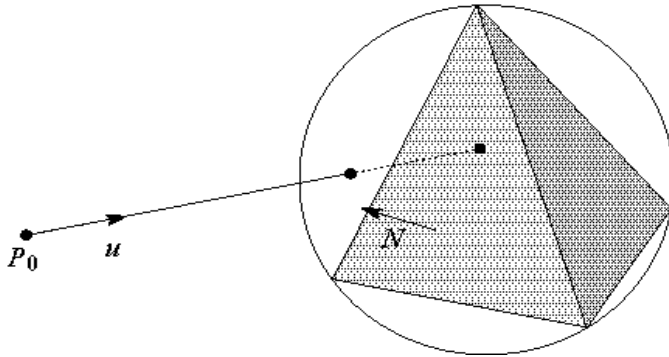
$t_{ca} > 0$, so the ray points toward the sphere



$t_{ca} < 0$, so the ray points away from the sphere

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Ray-PolyMesh Intersection



1. Use bounding sphere for fast failure
2. Test only front-facing polygons
3. Intersect ray with each polygon's supporting plane
4. Use a point-in-polygon test
5. Intersection point is smallest t

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Goodies

- There are some advanced ray tracing feature that self-respecting ray tracers shouldn't be caught without:
 - Acceleration techniques
 - Antialiasing
 - CSG
 - Distribution ray tracing

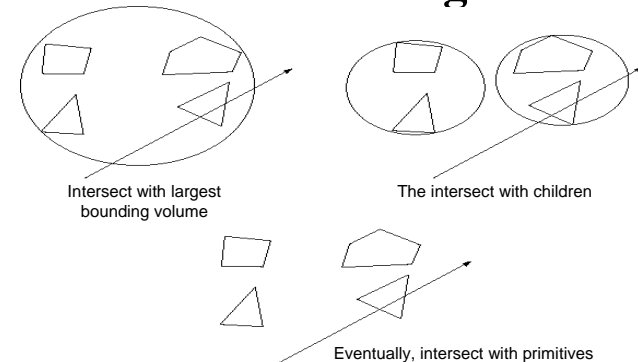
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Acceleration Techniques

- Problem: ray-object intersection is very expensive
 - make intersection tests faster
 - do fewer tests

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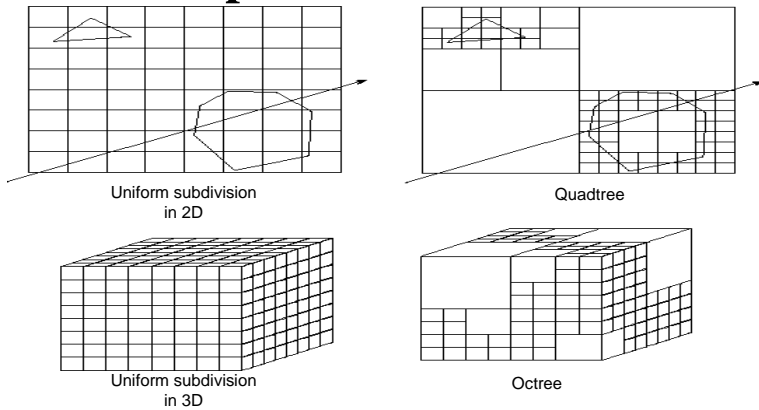
Hierarchical Bounding Volumes



- Arrange scene into a tree
 - Interior nodes contain primitives with very simple intersection tests (e.g., spheres). Each node's volume contains all objects in subtree
 - Leaf nodes contain original geometry
- Like BSP trees, the potential benefits are big but the hierarchy is hard to build

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Spatial Subdivision



- Divide up space and record what objects are in each cell
- Trace ray through **voxel** array

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Antialiasing

- So far, we have traced one ray through each pixel in the final image. Is this an adequate description of the contents of the pixel?

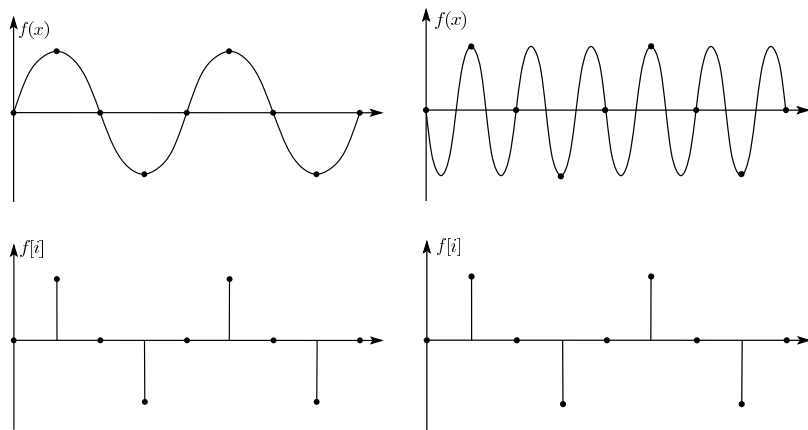


- This quantization through inadequate sampling is a form of **aliasing**. Aliasing is visible as “jaggies” in the ray-traced image.
- We really need to colour the pixel based on the *average*



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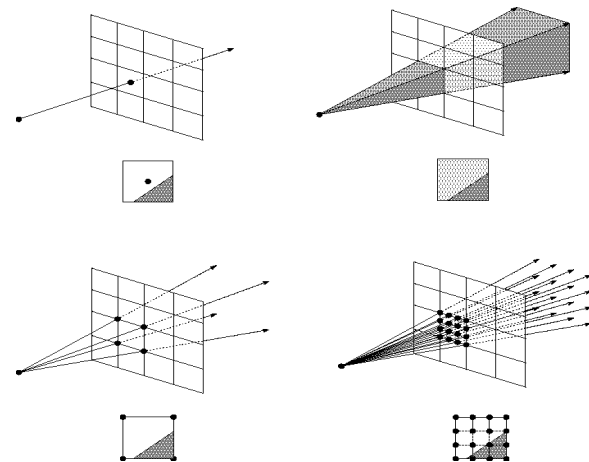
Aliasing



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Supersampling

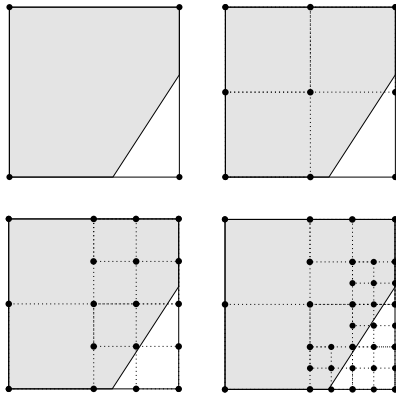
- We can approximate the average colour of a pixel's area by firing multiple rays and averaging the result.



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Adaptive Sampling

- Uniform supersampling can be wasteful if large parts of the pixel don't change much.
- So we can subdivide regions of the pixel's area only when the image changes in that area:

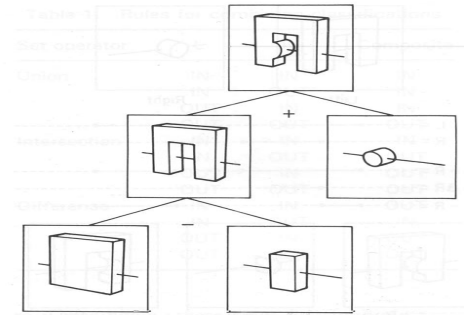


- How do we decide when to subdivide?

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CSG

- CSG (constructive solid geometry) is an incredibly powerful way to create complex scenes from simple primitives.

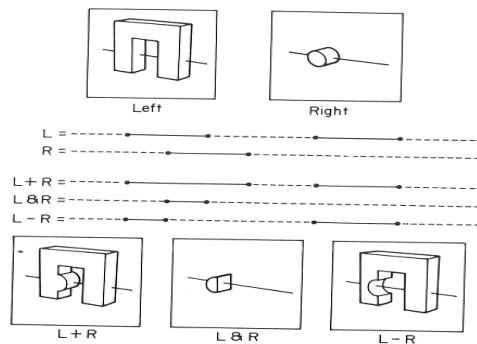


- CSG is a modeling technique; basically, we only need to modify ray-object intersection.

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CSG Implementation

- CSG intersections can be analyzed using "Roth diagrams".
 - Maintain description of *all intersections* of ray with primitive
 - Functions to combine Roth diagrams under CSG operations

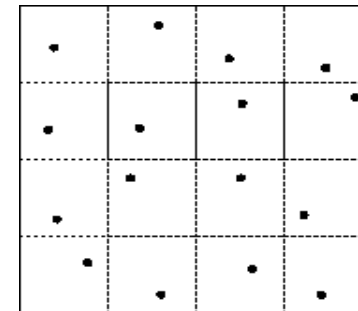


- An elegant and extremely slow system

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Distribution Ray Tracing

- Usually known as "distributed ray tracing", but it has nothing to do with distributed computing
- General idea: instead of firing one ray, fire multiple rays in a jittered grid



- Distributing over different dimensions gives different effects
- Example: what if we distribute rays over pixel area?

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Noise



- **Noise** can be thought of as randomness added to the signal.
- The eye is relatively insensitive to noise.

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DRT pseudocode

traceImage() looks basically the same, except now each pixel records the average color of jittered sub-pixel rays.

```

function traceImage (scene):
  for each pixel (i, j) in image do
    I(i, j) ← 0
    for each sub-pixel id in (i,j) do
      s ← pixelToWorld(jitter(i, j, id))
      p ← COP
      d ← (s - p).normalize()
      I(i, j) ← I(i, j) + traceRay(scene, p, d, id)
    end for
    I(i, j) ← I(i, j)/numSubPixels
  end for
end function
  
```

- A typical choice is numSubPixels = 4*4.

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DRT pseudocode (cont'd)

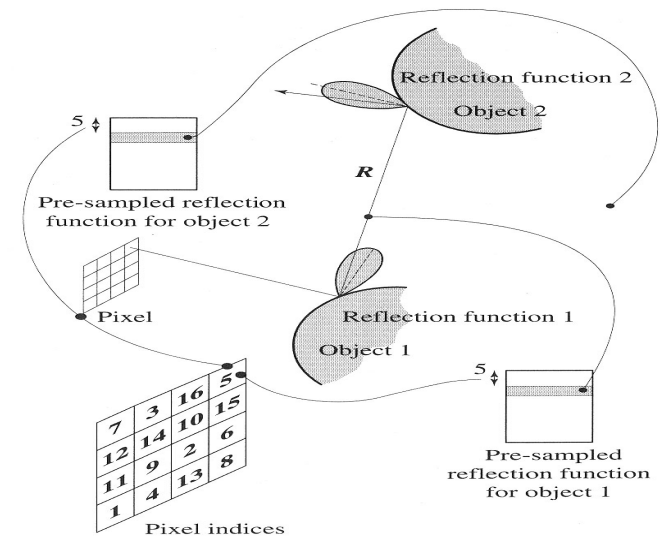
• Now consider *traceRay()*, modified to handle (only) opaque glossy surfaces:

```

function traceRay(scene, p, d, id):
  (q, N, material) ← intersect (scene, p, d)
  I ← shade(...)
  R ← jitteredReflectDirection(N, -d, id)
  I ← I + material.kr * traceRay(scene, q, R, id)
  return I
end function
  
```

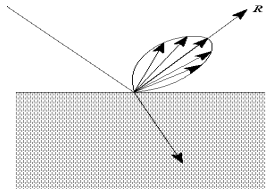
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Pre-sampling glossy reflections

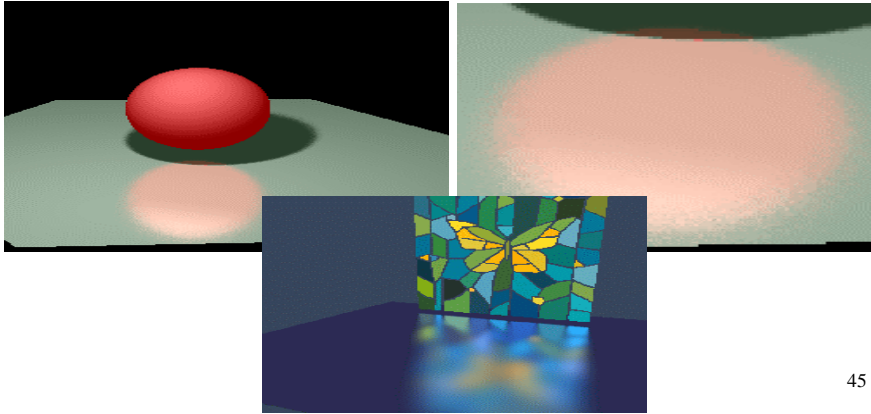


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Distributing Reflections



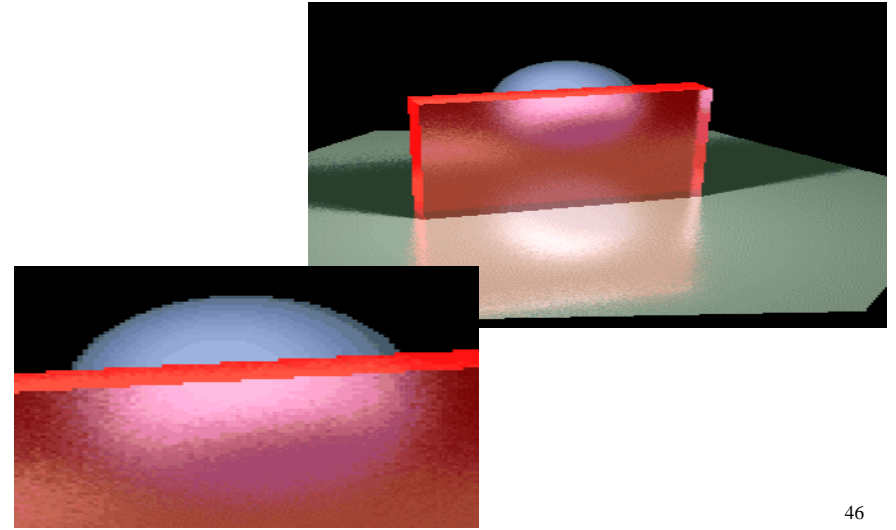
- Distributing rays over reflection direction gives:



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Distributing Refractions

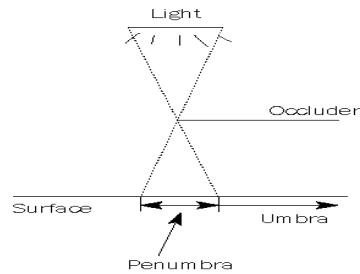
- Distributing rays over transmission direction gives:



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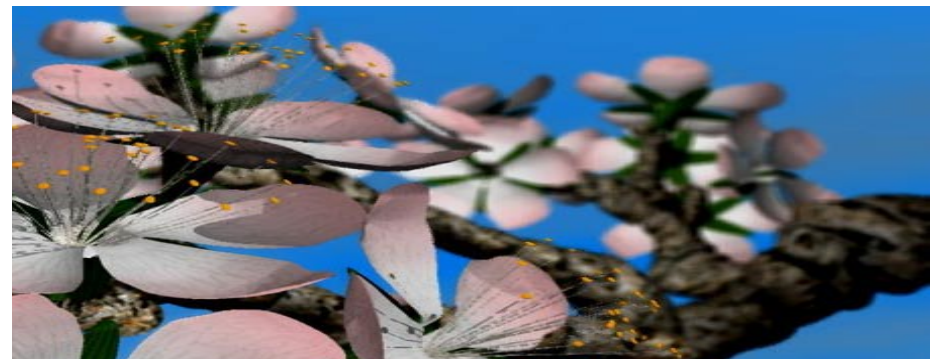
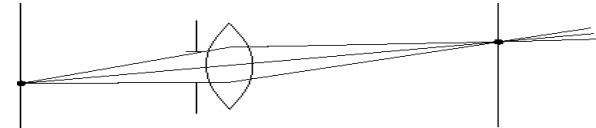
Distributing Over Light Area

- Distributing over light area gives:



Distributing Over Aperature

- We can fake distribution through a lens by choosing a point on a finite aperture and tracing through the “in-focus point”.



Distributing Over Time

- We can endow models with velocity vectors and distribute rays over *time*. this gives:

