CSE/EE 461 – Lecture 4

Error Detection and Correction

Last Time

- Different media have different properties that affect higher layer protocols.
- We abstract media into a simple model of a link
- To send messages over a link we must frame them

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L4.2

This Lecture

- Error detection and correction
- Focus: How do we detect and correct messages that are garbled during transmission?



• The responsibility for doing this cuts across the different layers

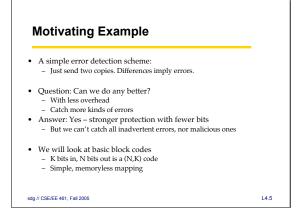
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Errors and Redundancy

- Noise can flip some of the bits we receive
 - We must be able to detect when this occurs!
 - Why?
 - Who needs to detect it? (links, routers, OSs, or apps?)
- Basic approach: add redundant data
 - Error detection codes allow errors to be recognizedError correction codes allow errors to be repaired too

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L4.4



Detection vs. Correction

- Two strategies to correct errors:
 - Detect and retransmit, or Automatic Repeat reQuest. (ARQ)
 Error correcting codes, or Forward Error Correction (FEC)
- Satellites, real-time media tend to use error correction
- Retransmissions typically at higher levels (Network+)
- Question: Which should we choose?

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Retransmissions vs. FEC

- The better option depends on the kind of errors and the cost of recovery
- Example: Message with 1000 bits, Prob(bit error) 0.001
 Case 1: random errors
 - Case 2: bursts of 1000 errors
 - Case 3: real-time application (teleconference)

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The Hamming Distance

- Errors must not turn one valid codeword into another valid codeword, or we cannot detect/correct them.
- <u>Hamming distance</u> of a code is the smallest number of bit differences that turn any one codeword into another e.g. code 000 for 0, 111 for 1, Hamming distance is 3
- For code with distance d+1:
 d errors can be detected, e.g, 001, 010, 110, 101, 011
- For code with distance 2d+1:
 d errors can be corrected, e.g., 001 → 000

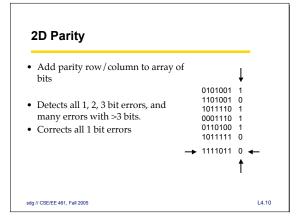
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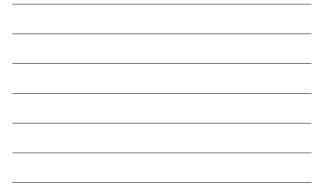
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Parity

- Start with n bits and add another so that the total number of 1s is even (even parity)
 - e.g. 0110010 → 01100101
 Easy to compute as XOR of all input bits
- Will detect an odd number of bit errors
 But not an even number
- Does not correct any errors

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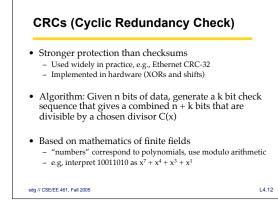




Checksums

- Used in Internet protocols (IP, ICMP, TCP, UDP)
- Basic Idea: Add up the data and send it along with sum
- Algorithm:
 - checksum is the 1s complement of the 1s complement sum of the data interpreted 16 bits at a time (for 16-bit TCP/UDP checksum)
- 1s complement: flip all bits to make number negative
 Consequence: adding requires carryout to be added back

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How is C(x) Chosen?

- Mathematical properties:
 - All 1-bit errors if non-zero x^k and x^0 terms
 - All 2-bit errors if $C(\boldsymbol{x})$ has a factor with at least three terms
 - Any odd number of errors if C(x) has (x + 1) as a factor
 - Any burst error < k bits

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Reed-Solomon / BCH Codes Developed to protect data on magnetic disks Used for CDs and cable modems too Property: 2t redundant bits can correct <= t errors Mathematics somewhat more involved ...

L4.14

Key Concepts

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- Redundant bits are added to messages to protect against transmission errors.
- Two recovery strategies are retransmissions (ARQ) and error correcting codes (FEC)
- The Hamming distance tells us how much error can safely be tolerated.