

CSE 473: Artificial Intelligence

Spring 2014

Search

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With slides from

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Announcements

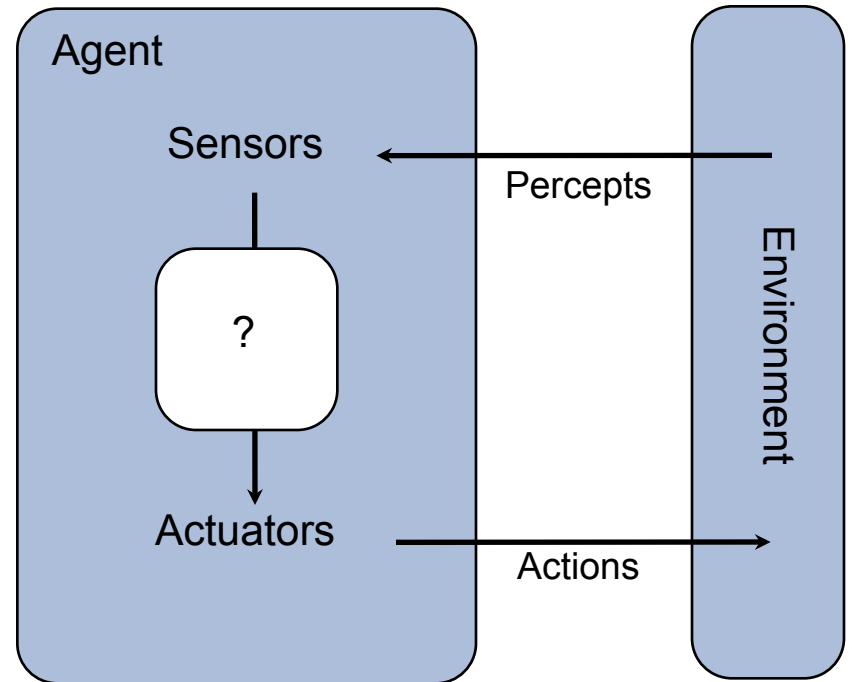
- Project 0: Python Tutorial
 - Online, but not graded
- Project 1: Search
 - On the web by tomorrow.
 - Start early and ask questions. **It's longer than most!**

Outline

- Agents that Plan Ahead
- Search Problems
- Uninformed Search Methods (part review for some)
 - Depth-First Search
 - Breadth-First Search
 - Uniform-Cost Search
- Heuristic Search Methods (new for all)
 - Best First / Greedy Search

Review: Rational Agents

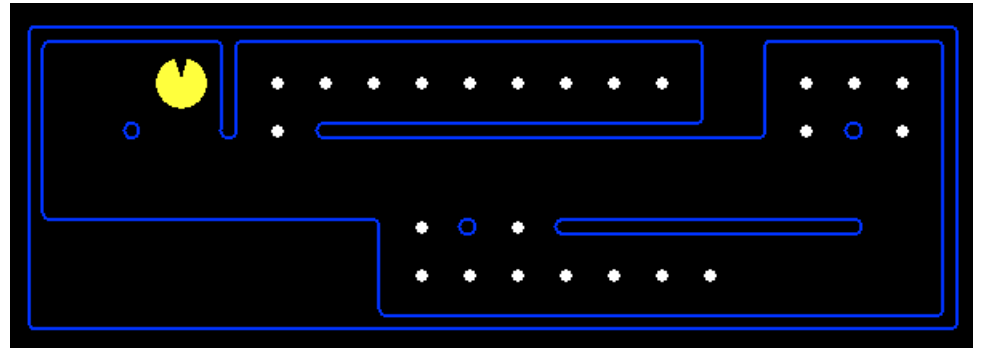
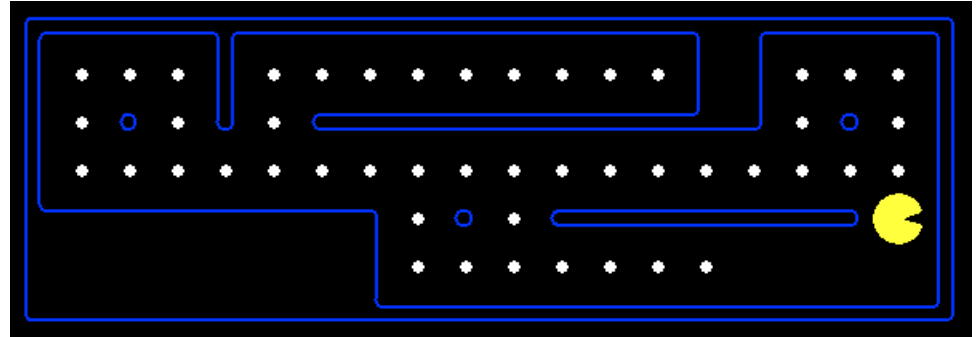
- An agent is an entity that perceives and acts.
- A rational agent selects actions that maximize its utility function.
- Characteristics of the percepts, environment, and action space dictate techniques for selecting rational actions.



Search -- the environment is:
fully observable, single agent, deterministic, episodic,
discrete

Reflex Agents

- Reflex agents:
 - Choose action based on current percept (and maybe memory)
 - Do not consider the future consequences of their actions
 - **Act on how the world IS**
- Can a reflex agent be rational?
- Can a non-rational agent achieve goals?

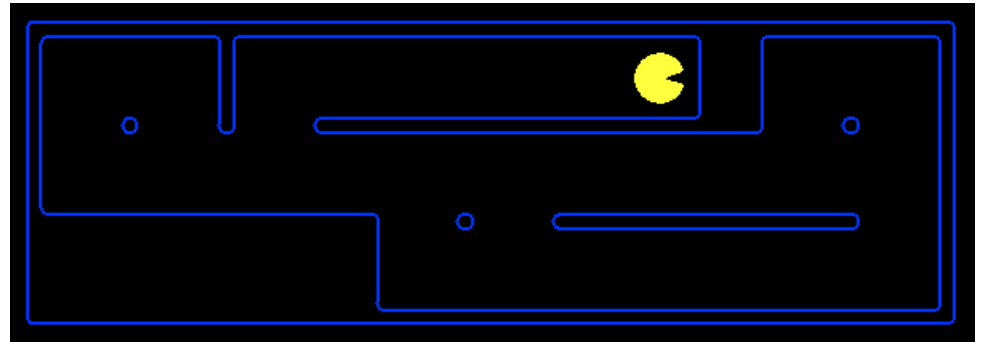
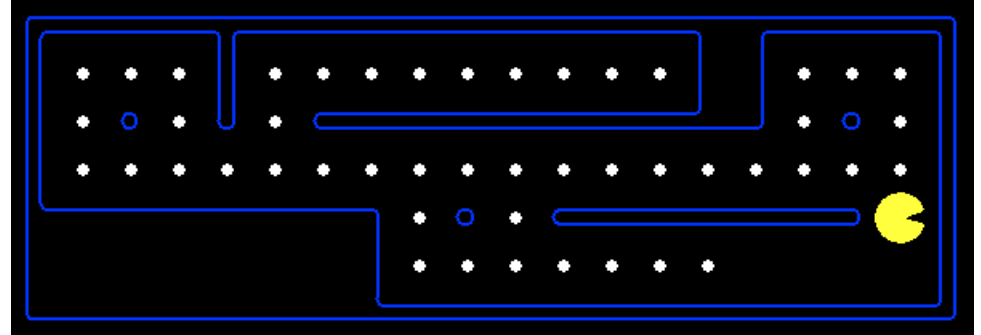


Famous Reflex Agents



Goal Based Agents

- Goal-based agents:
 - Plan ahead
 - Ask “what if”
 - Decisions based on (hypothesized) consequences of actions
 - Must have a model of how the world evolves in response to actions
 - Act on how the world **WOULD BE**



Search thru a Problem Space / State Space

- Input:

- Set of states
- Operators [and costs]
- Start state
- Goal state [test]

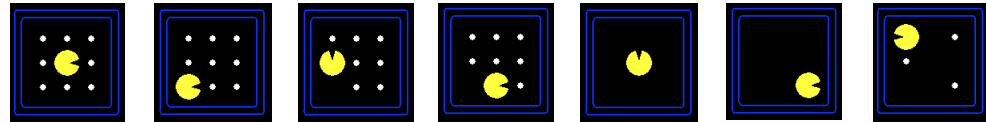
- Output:

- Path: start \Rightarrow a state satisfying goal test
- [May require shortest path]
- [Sometimes just need state passing test]

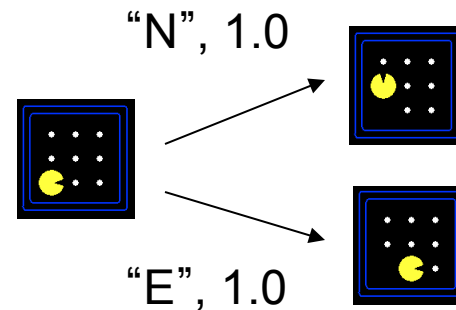
Example: Simplified Pac-Man

- **Input:**

- A state space



- A successor function



- A start state

- A goal test

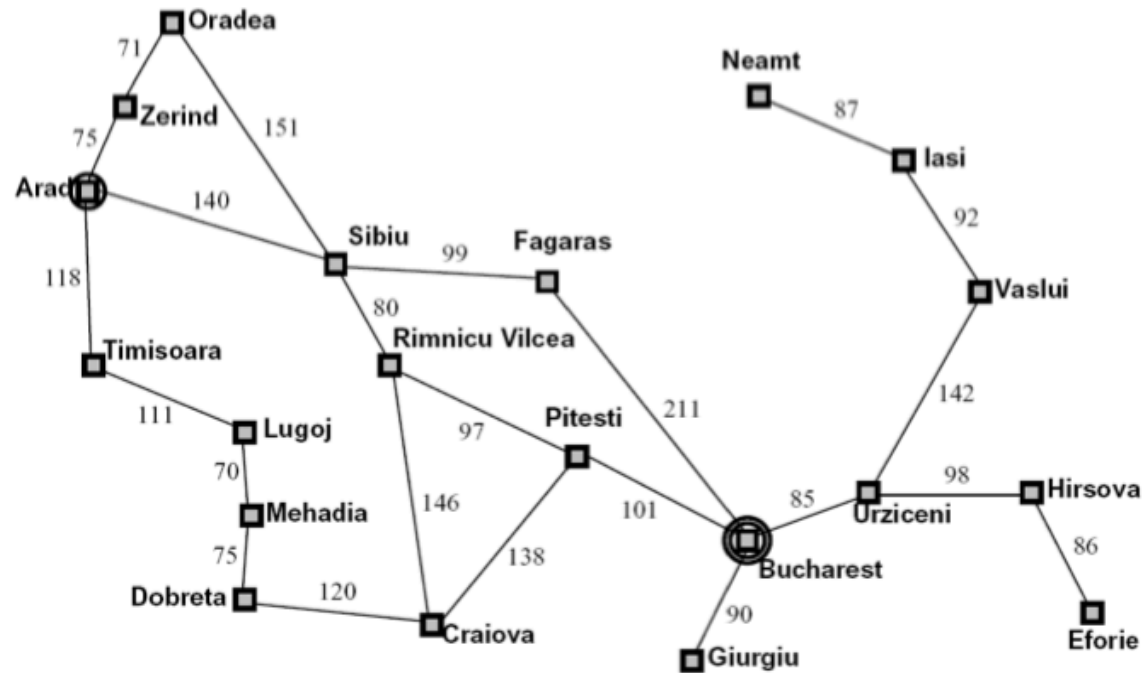
- **Output:**

Ex: Route Planning: Romania → Bucharest

Input:

- Set of states
- Operators [and costs]
- Start state
- Goal state (test)

Output:



Example: N Queens

- **Input:**
 - Set of states
 - Operators [and costs]
 - Start state
 - Goal state (test)
- **Output**

		Q	
Q			
			Q
	Q		



Algebraic Simplification

■ Input:

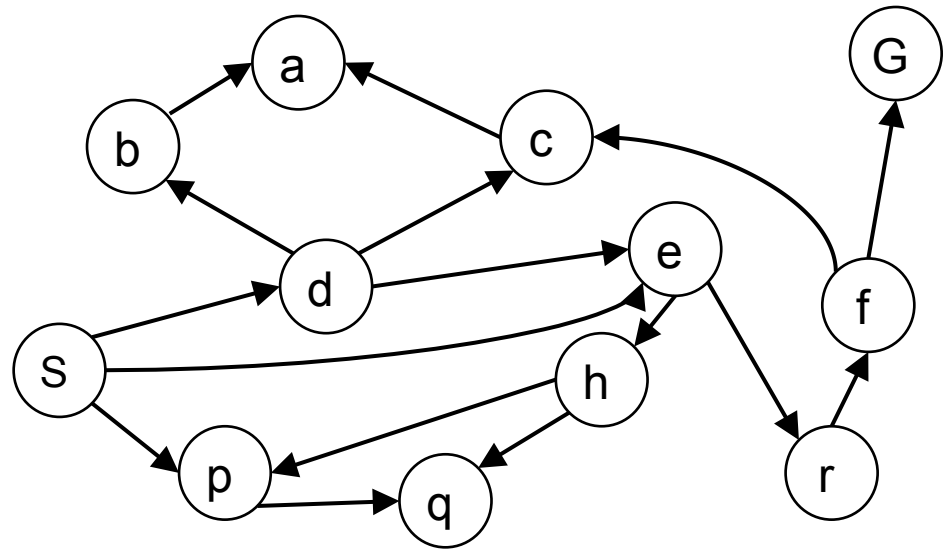
- Set of states
- Operators [and costs]
- Start state
- Goal state (test)

$$\begin{aligned} \partial_r^2 u &= - \left[E' - \frac{l(l+1)}{r^2} - r^2 \right] u(r) \\ e^{-2s} (\partial_s^2 - \partial_s) u(s) &= - [E' - l(l+1)e^{-2s} - e^{2s}] u(s) \\ e^{-2s} \left[e^{\frac{1}{2}s} \left(e^{-\frac{1}{2}s} u(s) \right)'' - \frac{1}{4} u \right] &= - [E' - l(l+1)e^{-2s} - e^{2s}] u(s) \\ e^{-2s} \left[e^{\frac{1}{2}s} \left(e^{-\frac{1}{2}s} u(s) \right)'' \right] &= - \left[E' - \left(l + \frac{1}{2} \right)^2 e^{-2s} - e^{2s} \right] u(s) \\ v'' &= -e^{2s} \left[E' - \left(l + \frac{1}{2} \right)^2 e^{-2s} - e^{2s} \right] v \end{aligned}$$

■ Output:

State Space Graphs

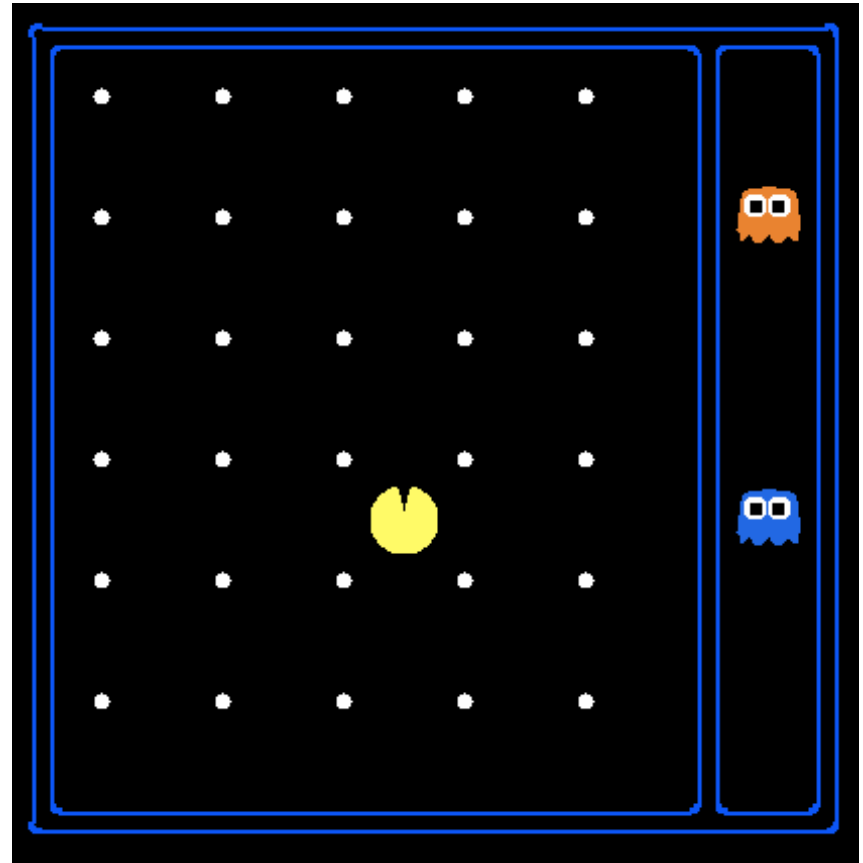
- State space graph:
 - Each node is a state
 - The successor function is represented by arcs
 - Edges may be labeled with costs
- We can rarely build this graph in memory (so we don't)



Ridiculously tiny search graph
for a tiny search problem

State Space Sizes?

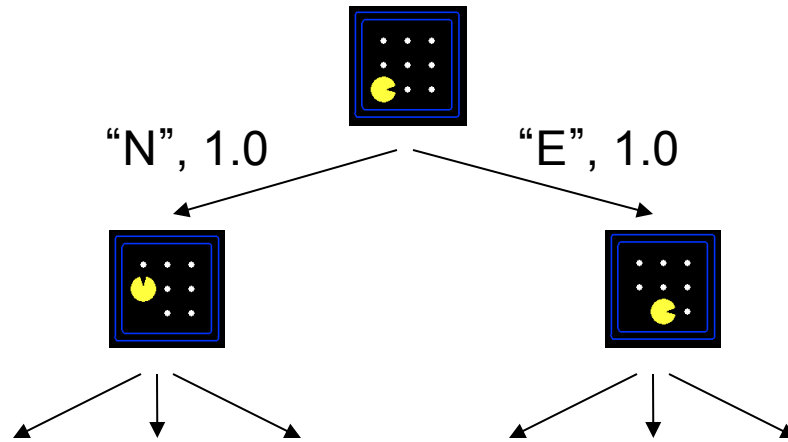
- Search Problem:
Eat all of the food
- Pacman positions:
 $10 \times 12 = 120$
- Pacman facing:
up, down, left, right
- Food Count: 30
- Ghost positions: 12



Search Strategies

- **Blind Search**
 - Depth first search
 - Breadth first search
 - Iterative deepening search
 - Uniform cost search
- **Informed Search**
- **Constraint Satisfaction**
- **Adversary Search**

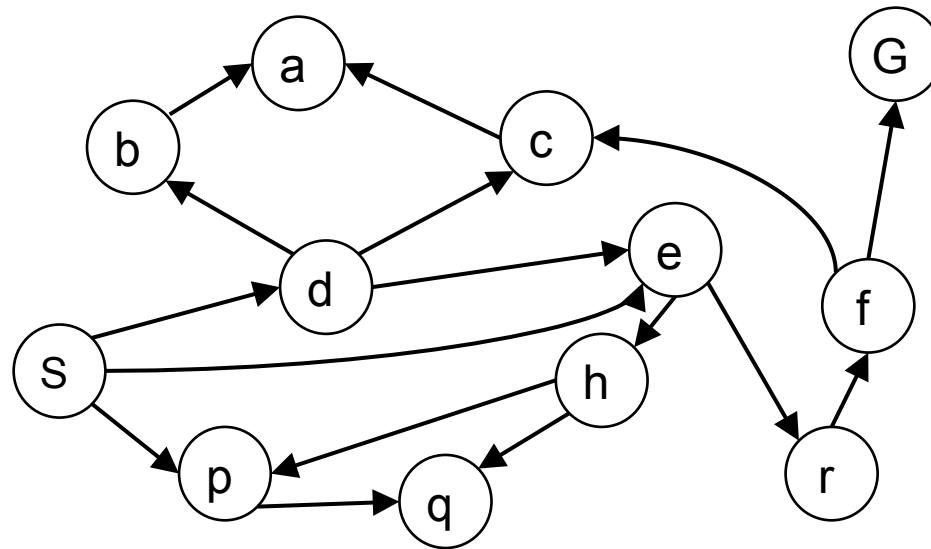
Search Trees



- A search tree:
 - Start state at the root node
 - Children correspond to successors
 - Nodes contain states, correspond to PLANS to those states
 - Edges are labeled with actions and costs
 - For most problems, we can never actually build the whole tree

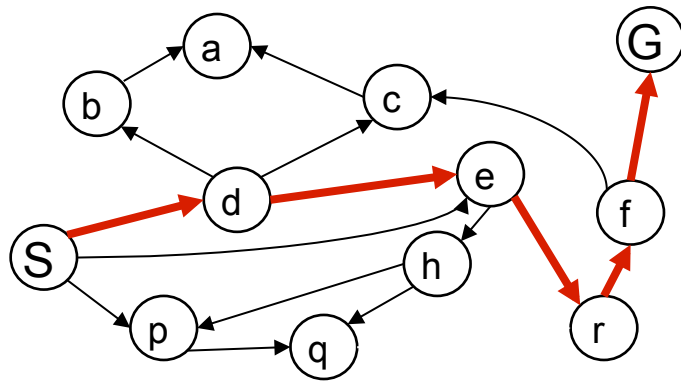
Example: Tree Search

State Graph:



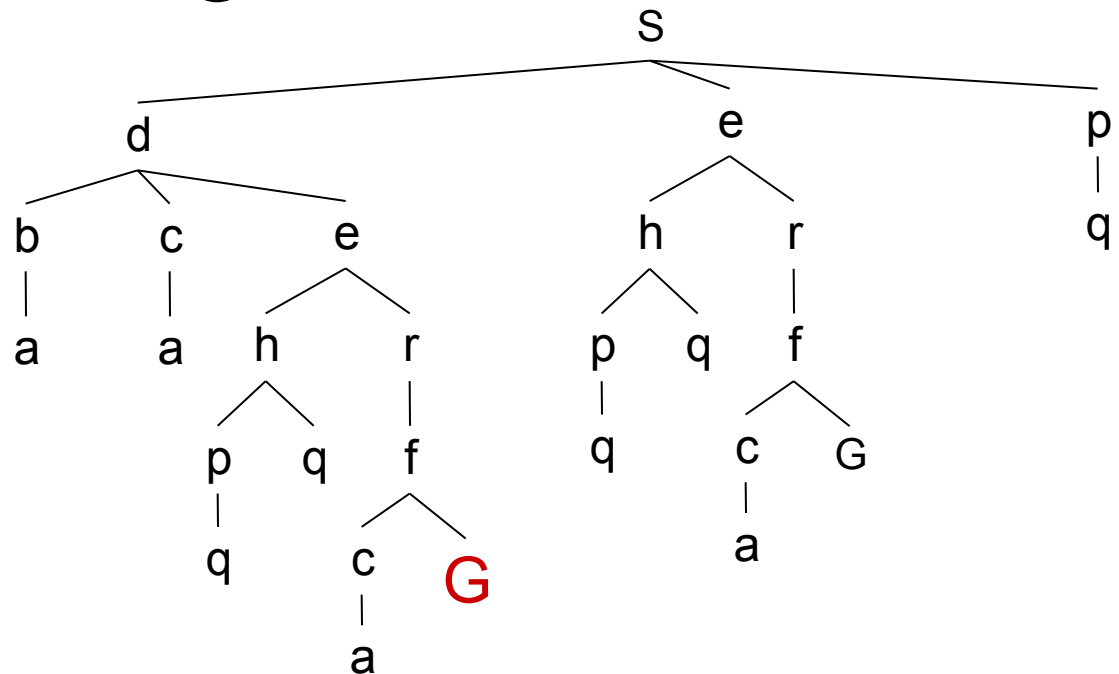
What is the search tree?

State Graphs vs. Search Trees



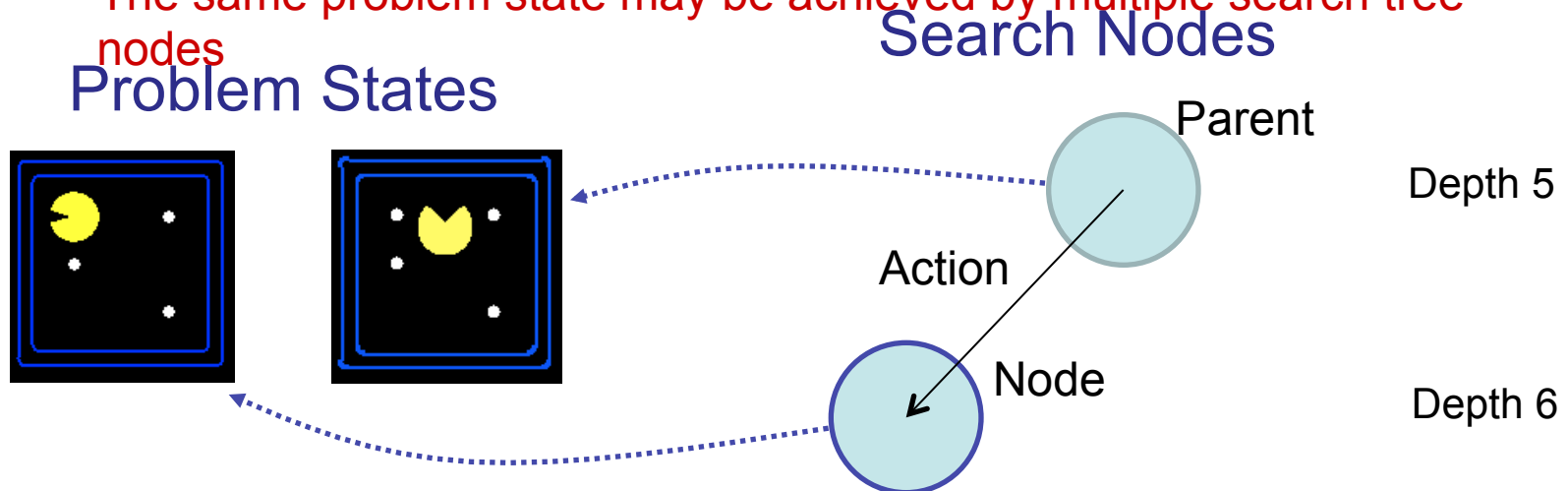
Each NODE in the search tree is an entire PATH in the problem graph.

We construct both on demand – and we construct as little as possible.



States vs. Nodes

- Nodes in state space graphs are problem states
 - Represent an abstracted state of the world
 - Have successors, can be goal / non-goal, have multiple predecessors
- Nodes in search trees are plans
 - Represent a plan (sequence of actions) which results in the node's state
 - Have a **problem state** and one parent, a path length, a depth & a cost
 - **The same problem state may be achieved by multiple search tree nodes**



Building Search Trees



■ Search:

- Expand out possible plans
- Maintain a **fringe** of unexpanded plans
- Try to expand as few tree nodes as possible

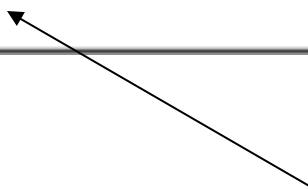
General Tree Search

```
function TREE-SEARCH(problem, strategy) returns a solution, or failure
  initialize the search tree using the initial state of problem
  loop do
    if there are no candidates for expansion then return failure
    choose a leaf node for expansion according to strategy
    if the node contains a goal state then return the corresponding solution
    else expand the node and add the resulting nodes to the search tree
  end
```

- Important ideas:

- Fringe
- Expansion
- Exploration strategy

Detailed pseudocode is
in the book!

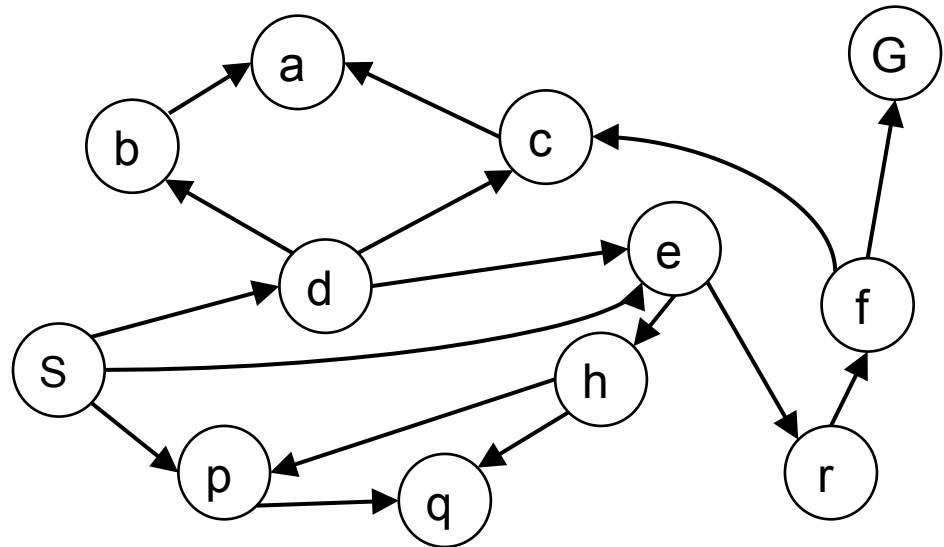


- Main question: which fringe nodes to explore?

Review: Depth First Search

Strategy: expand deepest node first

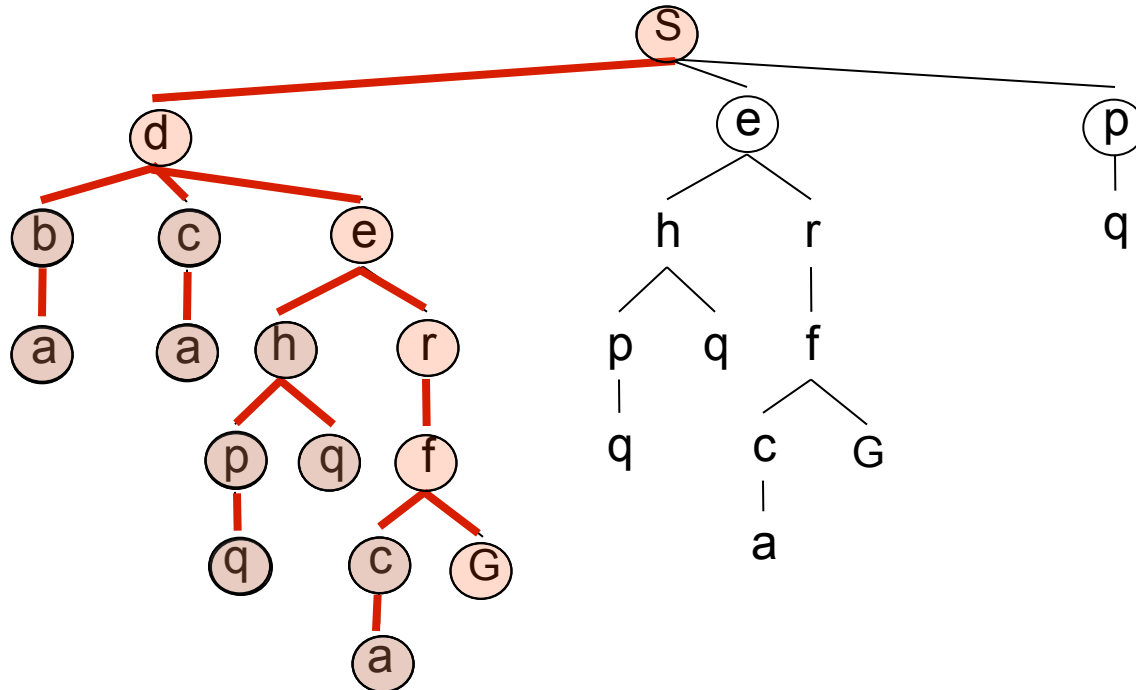
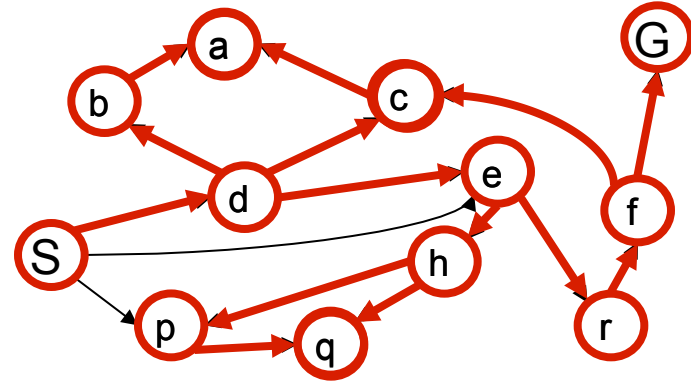
Implementation:
Fringe is a LIFO queue (a stack)



Review: Depth First Search

Expansion ordering:

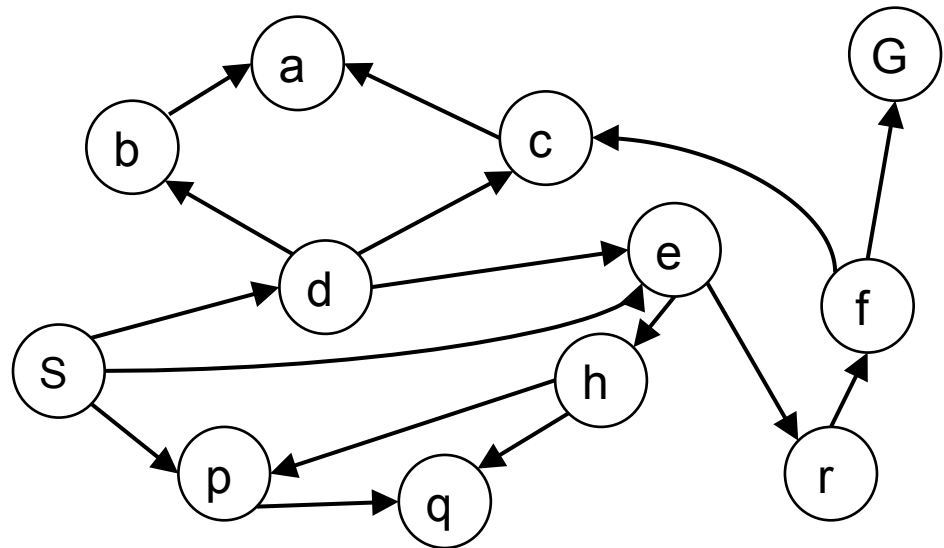
(d,b,a,c,a,e,h,p,q,q,r,f,c,a,G)



Review: Breadth First Search

Strategy: expand shallowest node first

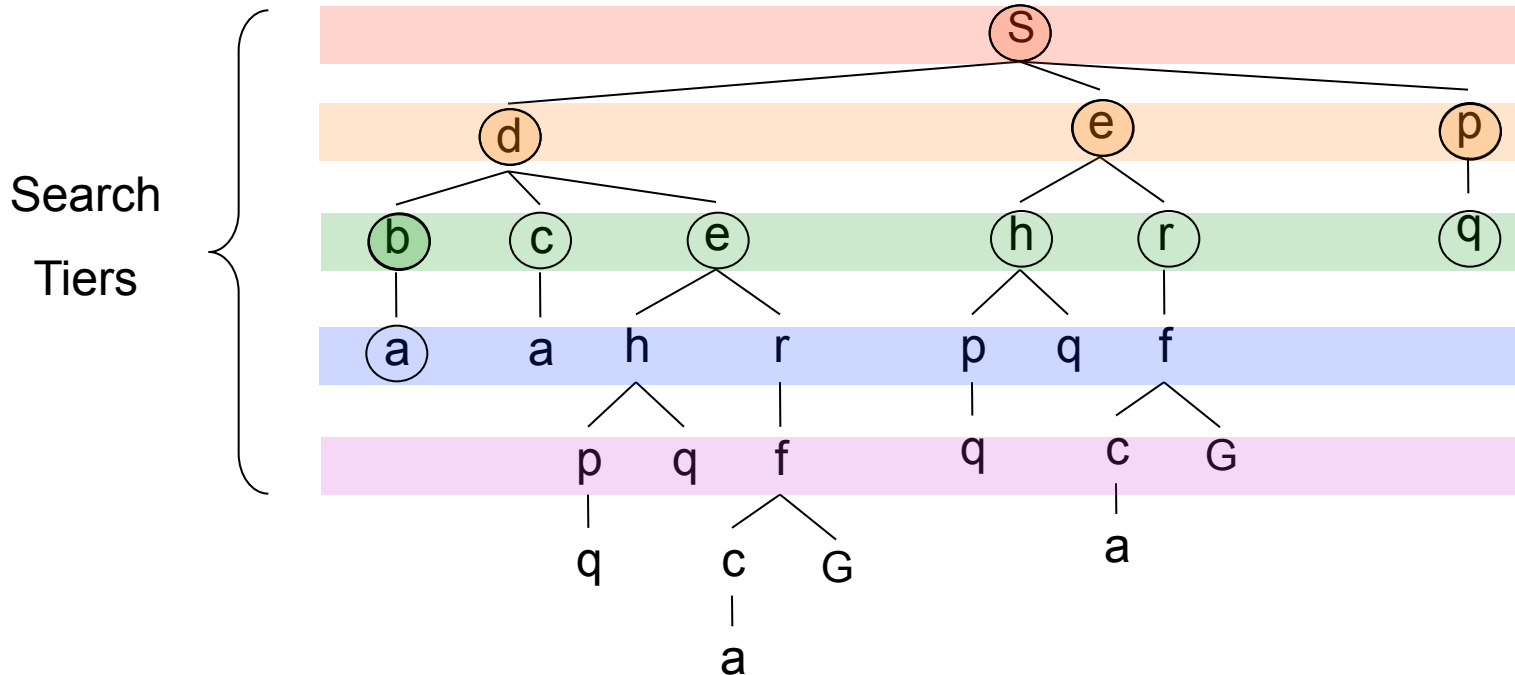
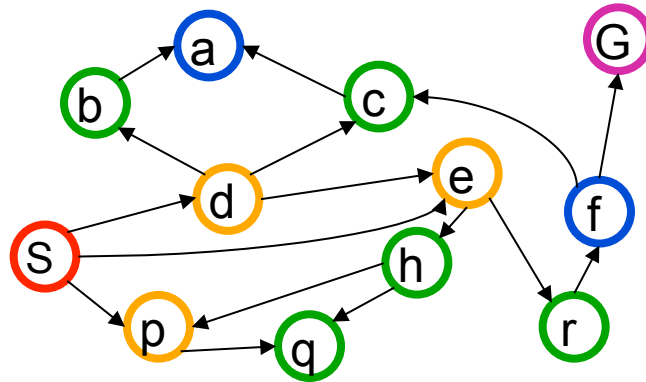
Implementation: Fringe is a FIFO queue



Review: Breadth First Search

Expansion order:

(S,d,e,p,b,c,e,h,r,q,a,a
,h,r,p,q,f,p,q,f,q,c,G)



Search Algorithm Properties

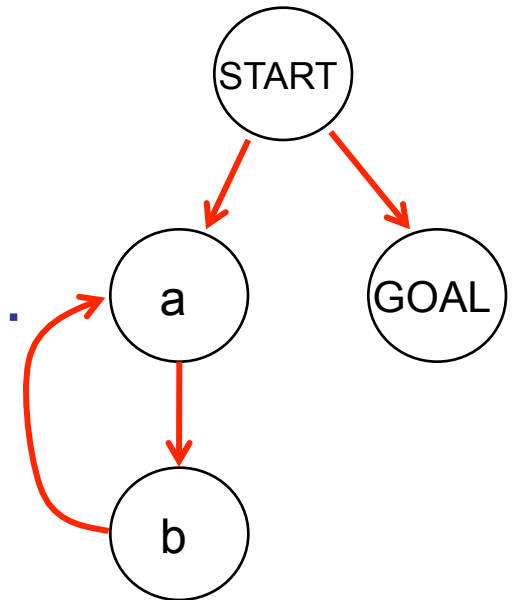
- **Complete?** Guaranteed to find a solution if one exists?
- **Optimal?** Guaranteed to find the least cost path?
- **Time complexity?**
- **Space complexity?**

Variables:

n	Number of states in the problem
b	The maximum branching factor B (the maximum number of successors for a state)
C^*	Cost of least cost solution
d	Depth of the shallowest solution
m	Max depth of the search tree

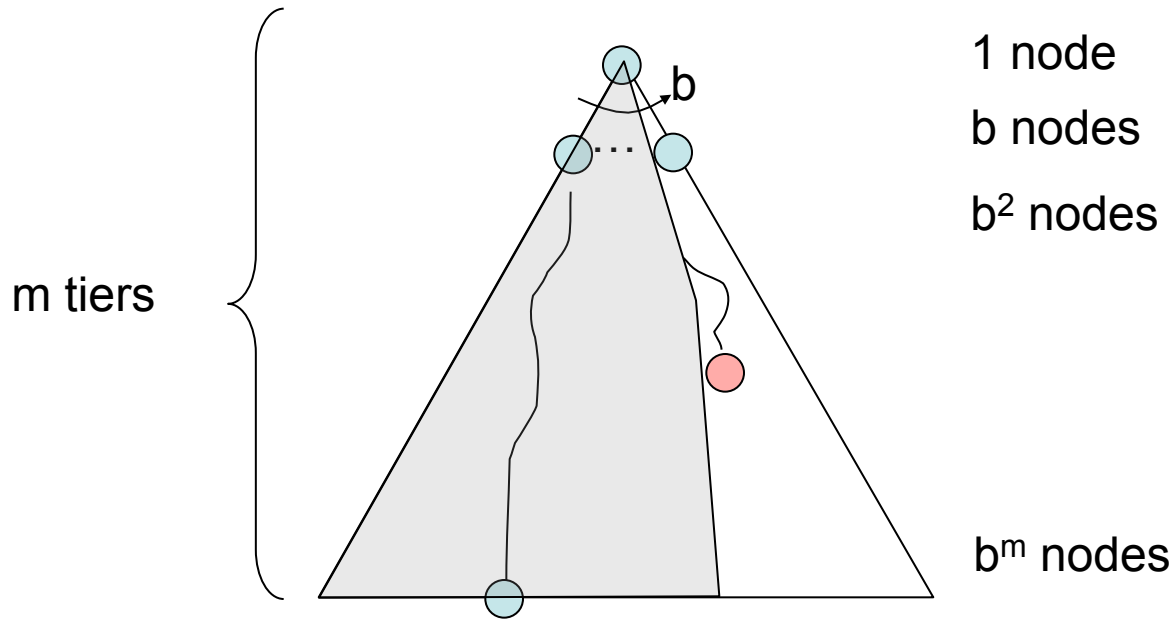
DFS

Algorithm		Complete	Optimal	Time	Space
DFS	Depth First Search	No	No	Infinite	Infinite



- Infinite paths make DFS incomplete...
 - How can we fix this?
 - Check new nodes against path from S
- Infinite search spaces still a problem

DFS

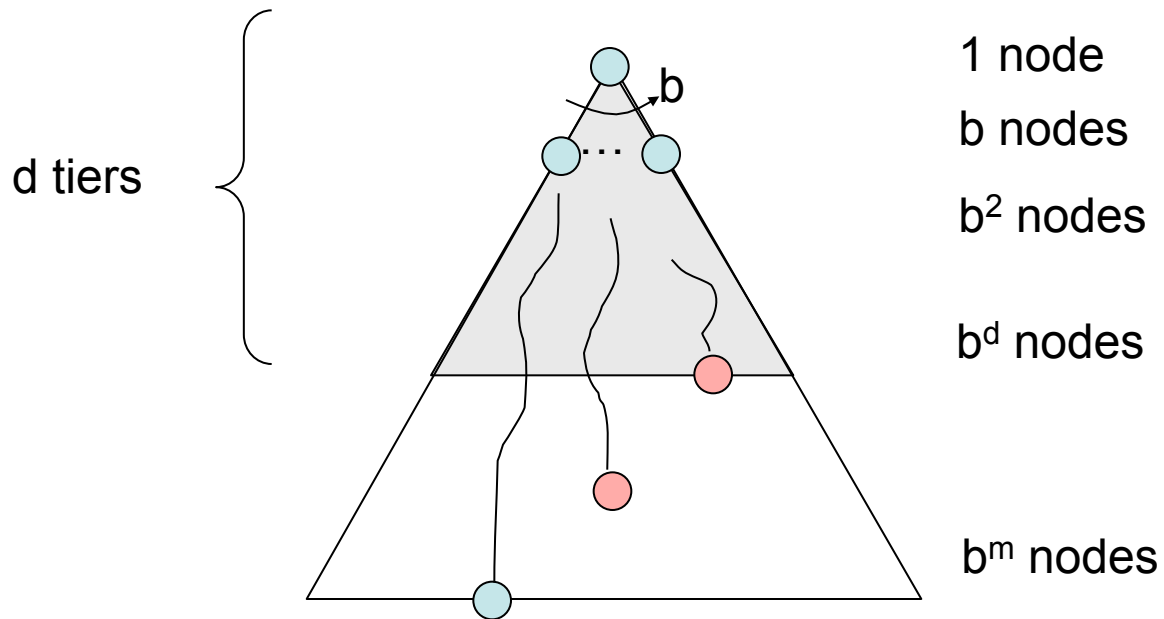


Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y if finite	N	$O(b^m)$	$O(bm)$

* Or graph search – next lecture.

BFS

Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y	N	$O(b^m)$	$O(bm)$
BFS		Y	Y*	$O(b^d)$	$O(b^d)$



Memory a Limitation?

- **Suppose:**

- 4 GHz CPU
 - 6 GB main memory
 - 100 instructions / expansion
 - 5 bytes / node
-
- 400,000 expansions / sec
 - Memory filled in 300 sec ... 5 min

Comparisons

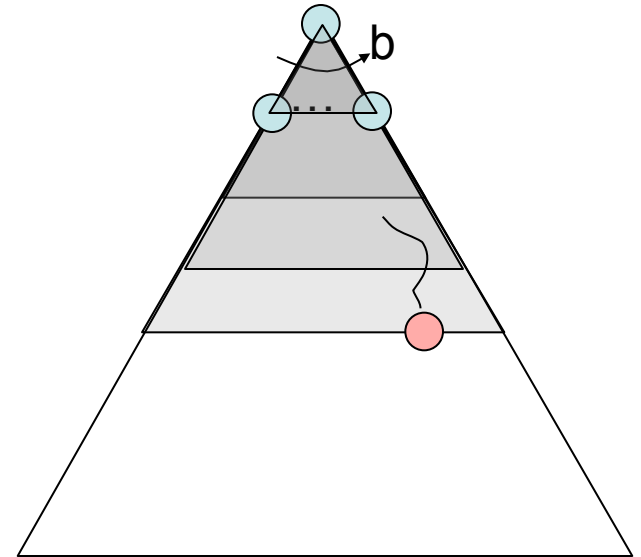
- When will BFS outperform DFS?
- When will DFS outperform BFS?

Iterative Deepening

Iterative deepening uses DFS as a subroutine:

1. Do a DFS which only searches for paths of length 1 or less.
2. If “1” failed, do a DFS which only searches paths of length 2 or less.
3. If “2” failed, do a DFS which only searches paths of length 3 or less.

....and so on.



Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y	N	$O(b^m)$	$O(bm)$
BFS		Y	Y*	$O(b^d)$	$O(b^d)$
ID		Y	Y*	$O(b^d)$	$O(bd)$

Speed

Assuming 10M nodes/sec & sufficient memory

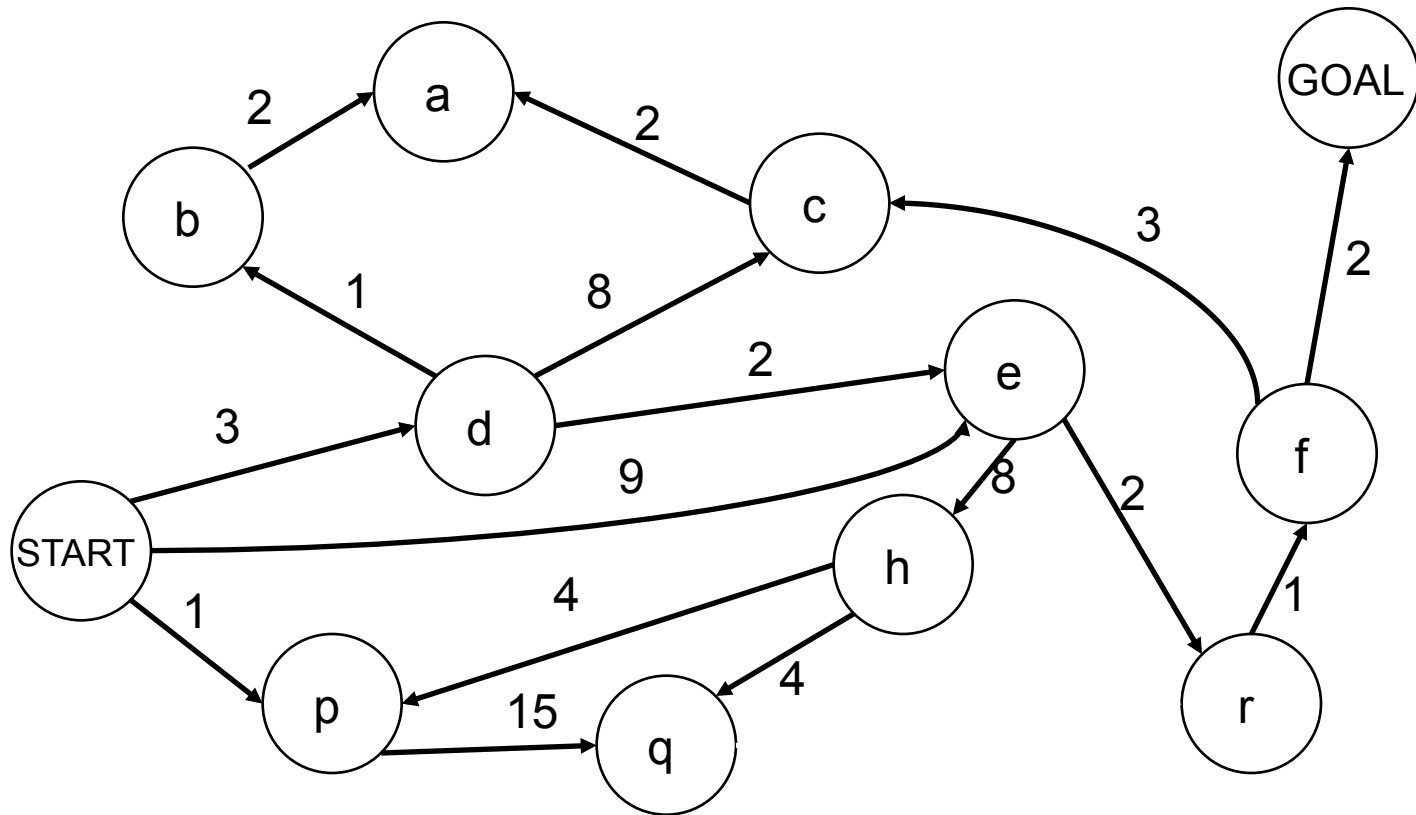
	BFS			Iter. Deep.	
	Nodes	Time		Nodes	Time
8 Puzzle	10^5	.01 sec		10^5	.01 sec
2x2x2 Rubik's	10^6	.2 sec		10^6	.2 sec
15 Puzzle	10^{13}	6 days	1Mx	10^{17}	20k yrs
3x3x3 Rubik's	10^{19}	68k yrs	8x	10^{20}	574k yrs
24 Puzzle	10^{25}	12B yrs		10^{37}	10^{23} yrs

Why the difference?

Rubik has higher branch factor
15 puzzle has greater depth

of duplicates

Costs on Actions

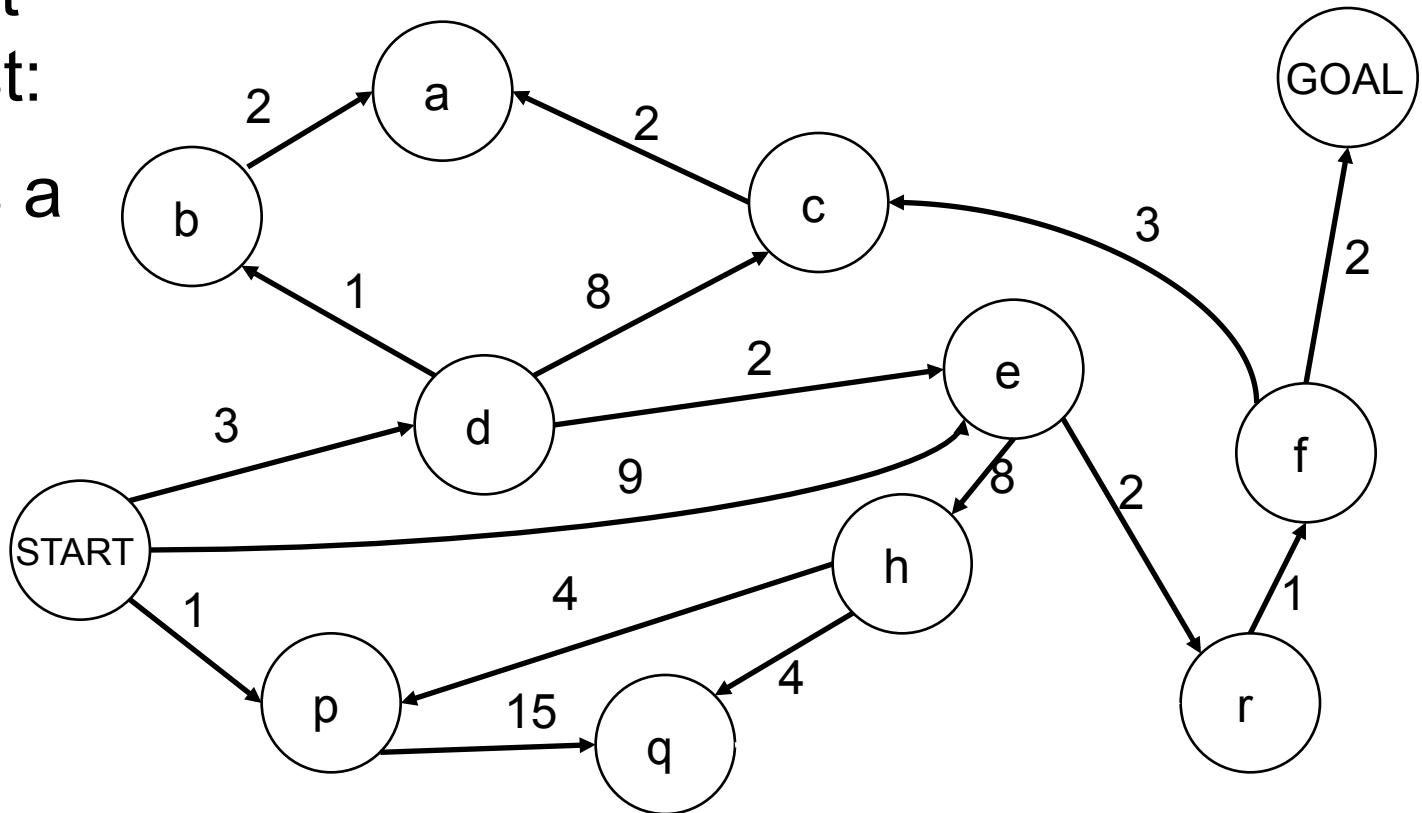


Notice that BFS finds the shortest path in terms of number of transitions. It does not find the least-cost path.

Uniform Cost Search

Expand
cheapest
node first:

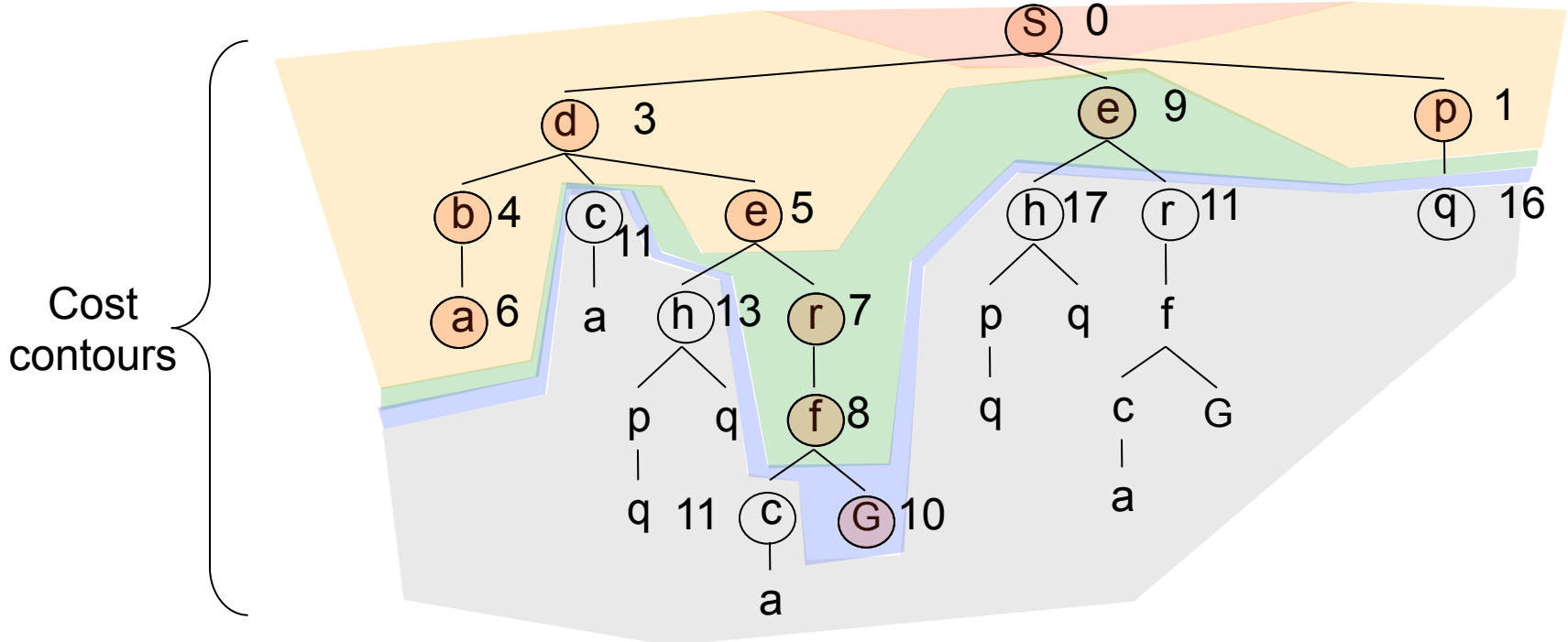
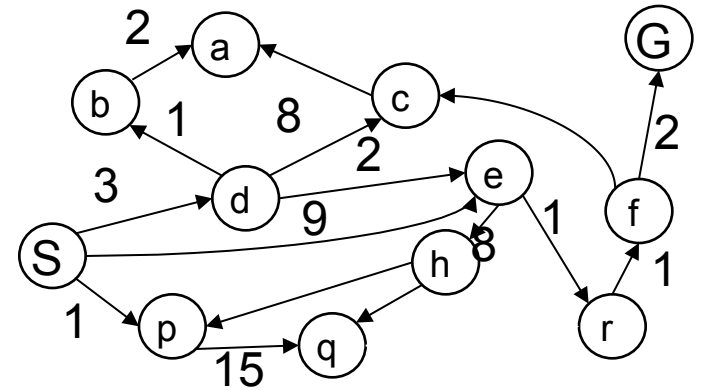
Fringe is a
priority
queue



Uniform Cost Search

Expansion order:

(S,p,d,b,e,a,r,f,e,G)





Priority Queue Refresher

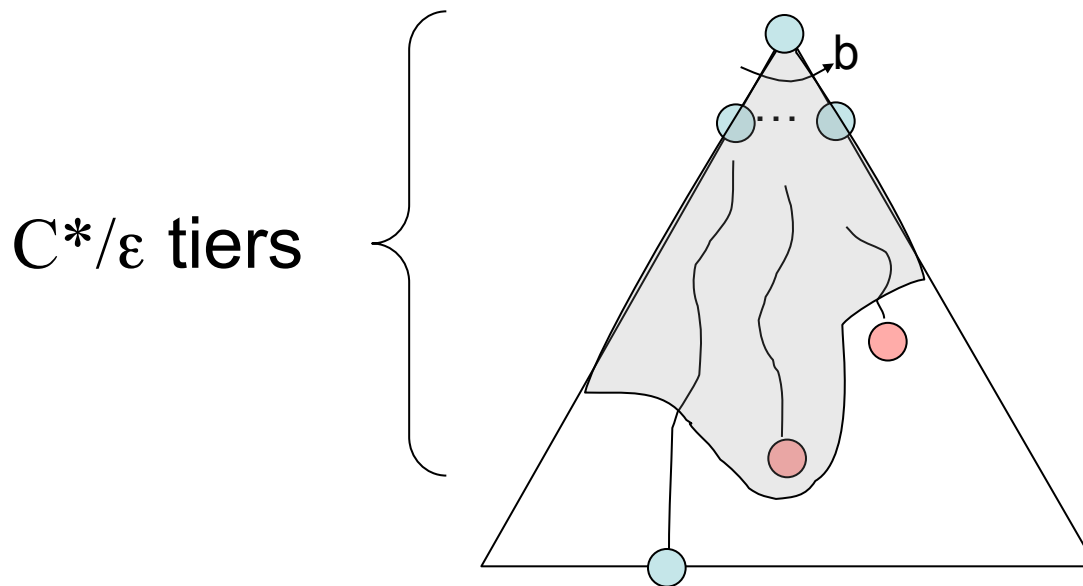
- A priority queue is a data structure in which you can insert and retrieve (key, value) pairs with the following operations:

<code>pq.push(key, value)</code>	inserts (key, value) into the queue.
<code>pq.pop()</code>	returns the key with the lowest value, and removes it from the queue.

- You can decrease a key's priority by pushing it again
- Unlike a regular queue, insertions aren't constant time, usually $O(\log n)$
- We'll need priority queues for cost-sensitive search methods

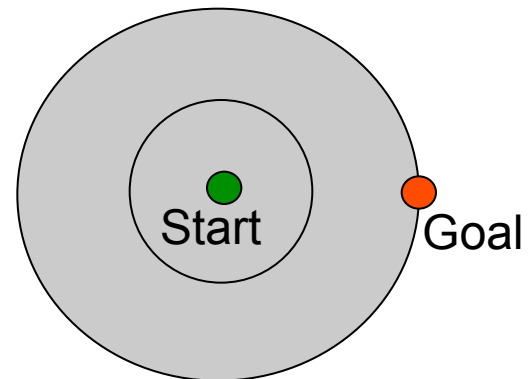
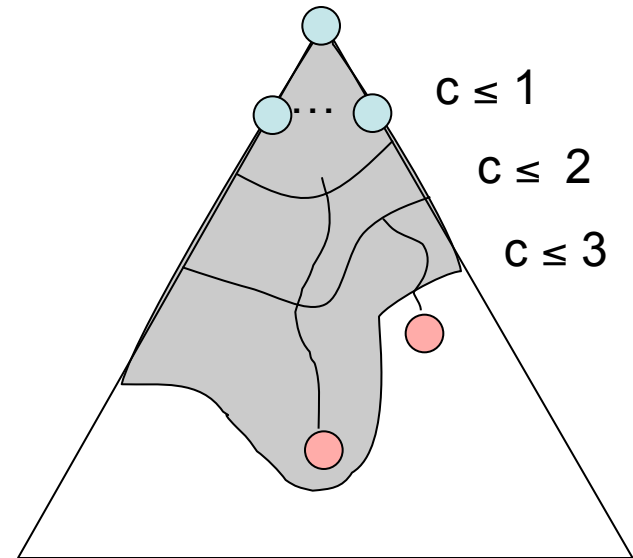
Uniform Cost Search

Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y	N	$O(b^m)$	$O(bm)$
BFS		Y	Y*	$O(b^d)$	$O(b^d)$
UCS		Y*	Y	$O(b^{C^*/\epsilon})$	$O(b^{C^*/\epsilon})$



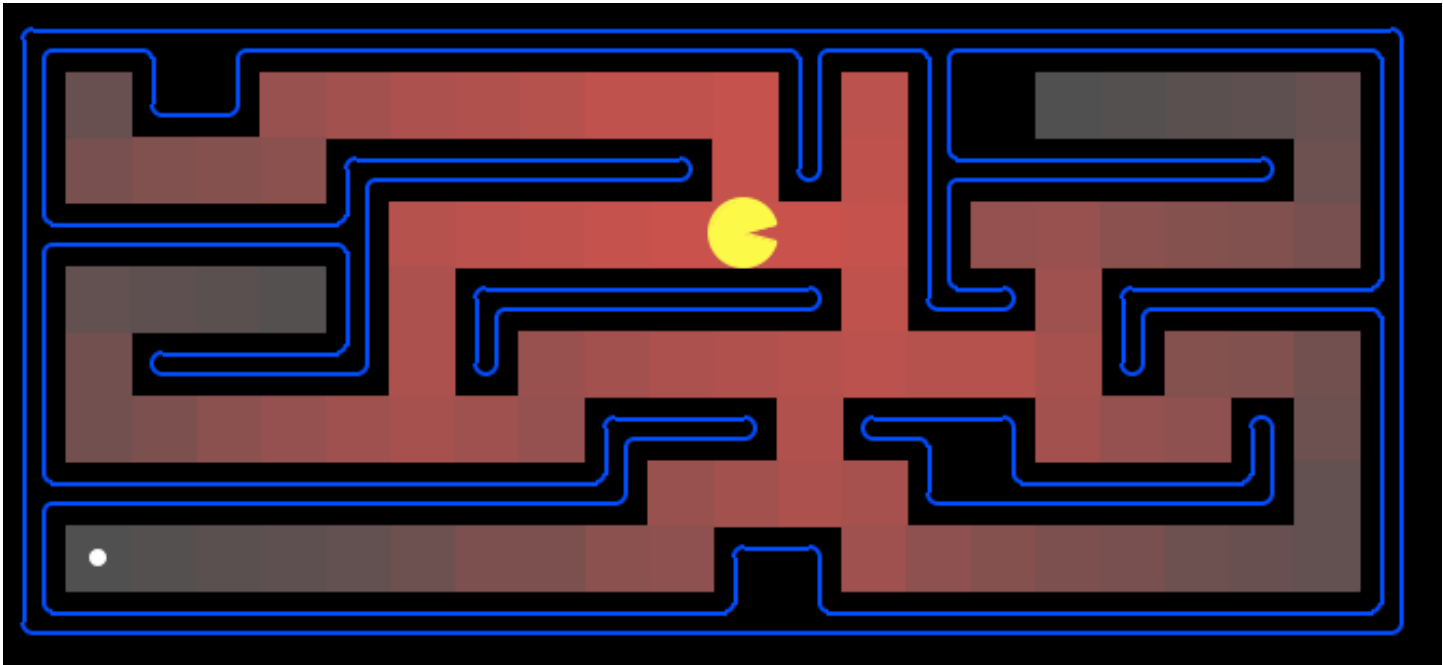
Uniform Cost Issues

- Remember: explores increasing cost contours
- The good: UCS is complete and optimal!
- The bad:
 - Explores options in every “direction”
 - No information about goal location



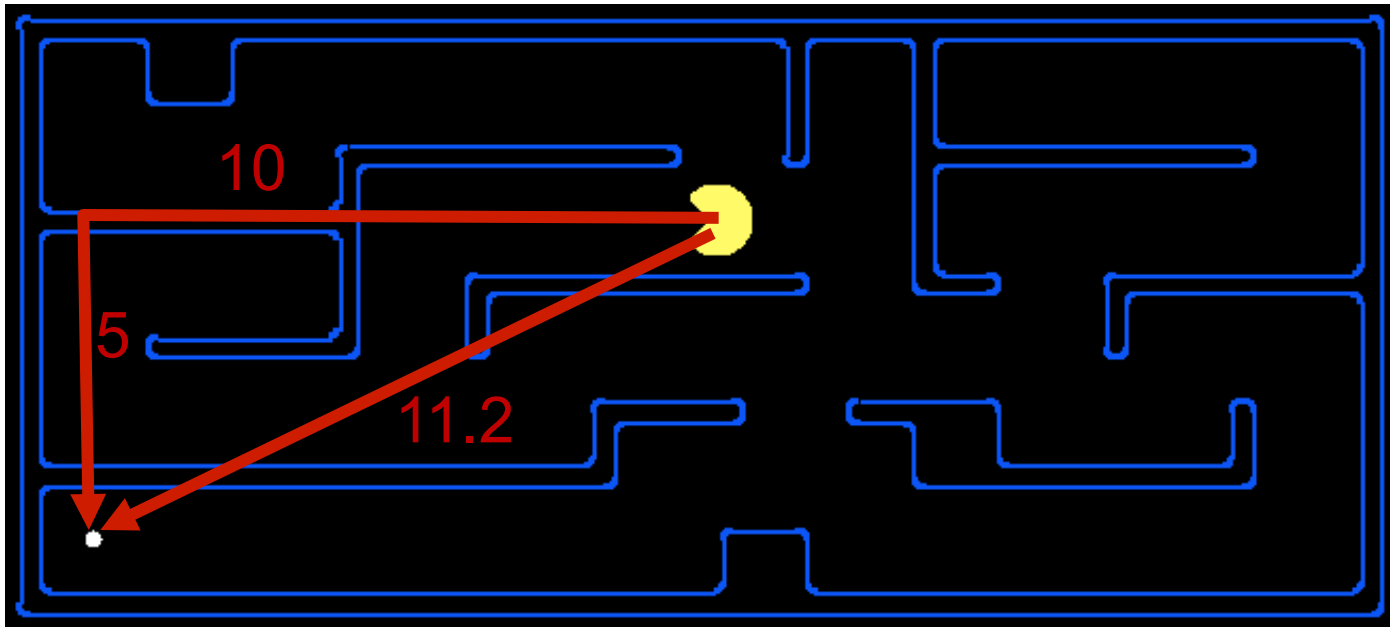
Uniform Cost: Pac-Man

- Cost of 1 for each action
- Explores all of the states, but one



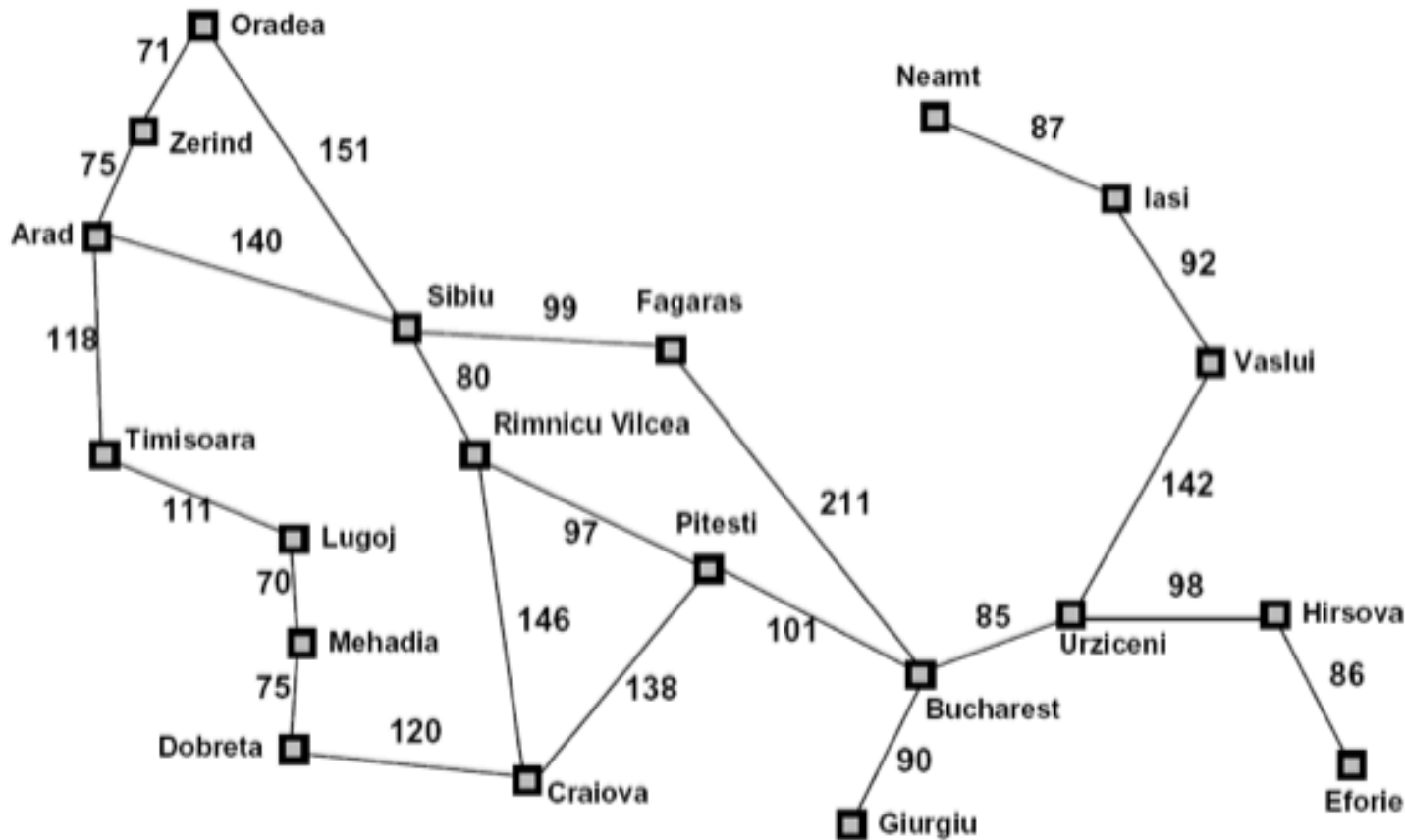
Search Heuristics

- Any estimate of how close a state is to a goal
- Designed for a particular search problem



- Examples: Manhattan distance, Euclidean distance

Heuristics

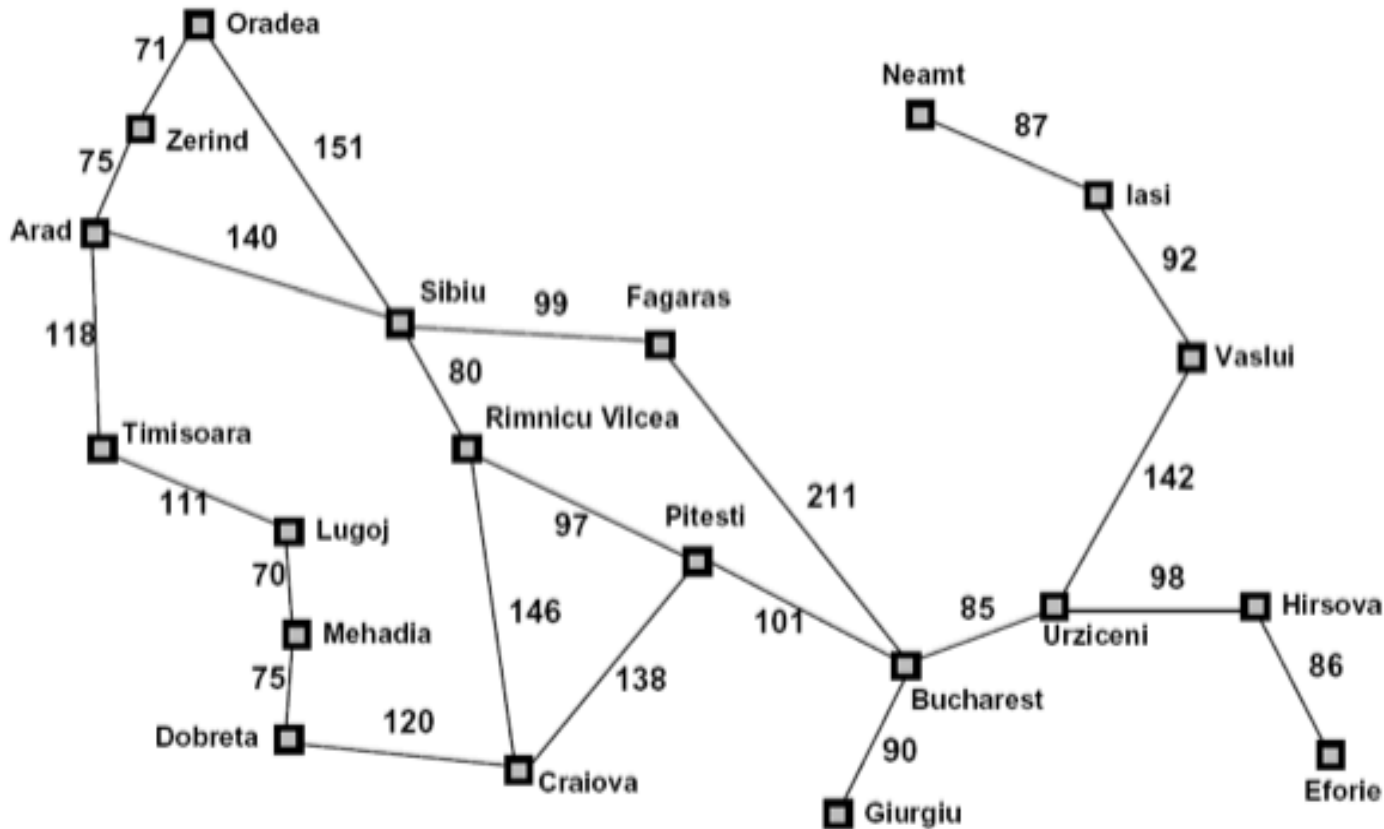


Straight-line distance to Bucharest

Arad	366
Bucharest	0
Craiova	160
Dobreta	242
Eforie	161
Fagaras	178
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244
Mehadia	241
Neamt	234
Oradea	380
Pitesti	98
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

Best First / Greedy Search

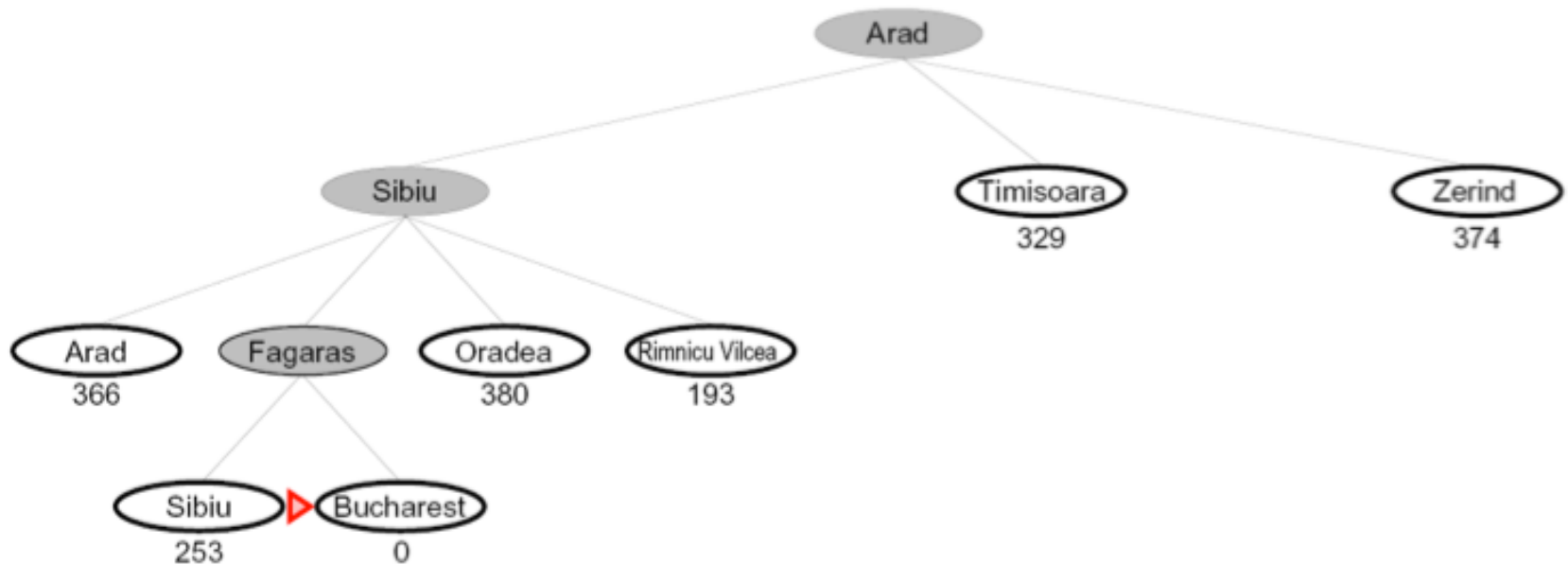
Expand closest node first: Fringe is a priority queue



Straight-line distance to Bucharest	
Arad	366
Bucharest	0
Craiova	160
Dobreta	242
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Best First / Greedy Search

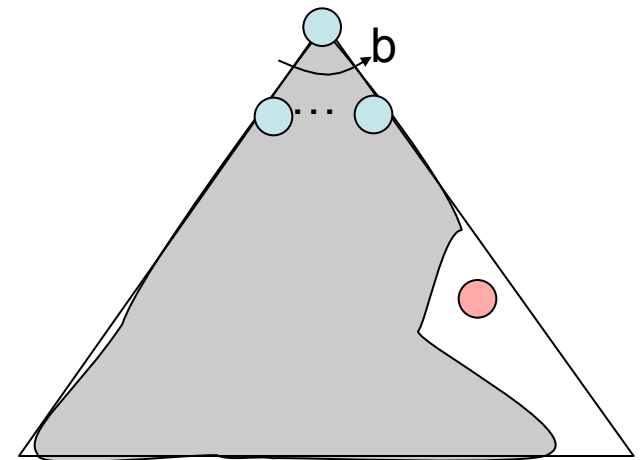
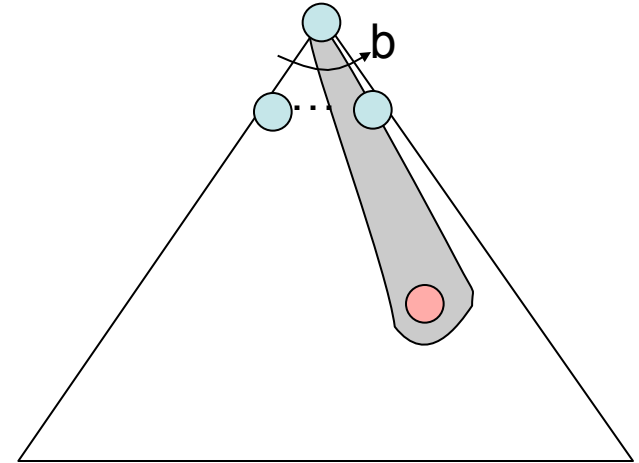
- Expand the node that seems closest...



- What can go wrong?

Best First / Greedy Search

- A common case:
 - Best-first takes you straight to the (wrong) goal
- Worst-case: like a badly-guided DFS in the worst case
 - Can explore everything
 - Can get stuck in loops if no cycle checking
- Like DFS in completeness (finite states w/ cycle checking)



To Do:

- Look at the course website:
 - <http://www.cs.washington.edu/cse473/12sp>
- Do the readings (Ch 3)
- Do PS0 if new to Python
- Start PS1, when it is posted