# **Shading**

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# Basic 3D graphics

With affine matrices, we can now transform virtual 3D objects in their local coordinate systems into a global (world) coordinate system:

$$z_1$$
 $z_2$ 
 $z_2$ 

To synthesize an image of the scene, we also need to add light sources and a viewer/camera:

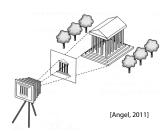


Required:

• Shirley, Chapter 10

## Pinhole camera

To create an image of a virtual scene, we need to define a camera, and we need to model lighting and shading. For the camera, we use a **pinhole camera**.



The image is rendered onto an **image plane** (usually in front of the camera).

Viewing rays emanate from the **center of projection** (COP) at the center of the pinhole.

The image of an object point  ${\bf P}$  is at the intersection of the viewing ray through  ${\bf P}$  and the image plane.

# **Shading**

Next, we'll need a model to describe how light interacts with surfaces.

Such a model is called a shading model.

Other names:

- Lighting model
- Light reflection model
- Local illumination model
- Reflectance model
- BRDF

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## An abundance of photons

Given the camera and shading model, properly determining the right color at each pixel is *extremely hard*.

Look around the room. Each light source has different characteristics. Trillions of photons are pouring out every second.

These photons can:

- interact with molecules and particles in the air ("participating media")
- strike a surface and
  - be absorbed
  - · be reflected (scattered)
  - · cause fluorescence or phosphorescence.
- interact in a wavelength-dependent manner
- generally bounce around and around

# N p lmage

#### Given:

Setup...

- a point **P** on a surface visible through pixel p
- The normal N at P
- The lighting direction, L, and (color) intensity, I<sub>L</sub>, at P
- The viewing direction, V, at P
- The shading coefficients at P

Compute the color, I, of pixel p.

Assume that the direction vectors are normalized:

$$\|\mathbf{N}\| = \|\mathbf{L}\| = \|\mathbf{V}\| = 1$$

## Our problem

We're going to build up to a *approximations* of reality called the **Phong and Blinn-Phong illumination models**.

They have the following characteristics:

- not physically correct
- gives a "first-order" approximation to physical light reflection
- very fast
- widely used

In addition, we will assume **local illumination**, i.e., light goes: light source -> surface -> viewer.

No interreflections, no shadows.

## "Iteration zero"

The simplest thing you can do is...

Assign each polygon a single color:

$$I = k_{P}$$

where

- I is the resulting intensity
- $k_e$  is the **emissivity** or intrinsic shade associated with the object

This has some special-purpose uses, but not really good for drawing a scene.

[Note:  $k_{\rho}$  is omitted in Shirley.]

## "Iteration one"

Let's make the color at least dependent on the overall quantity of light available in the scene:

$$I = k_e + k_a I_{La}$$

- $k_a$  is the ambient reflection coefficient.
  - · really the reflectance of ambient light
  - "ambient" light is assumed to be equal in all directions
- I<sub>ta</sub> is the ambient light intensity.

Physically, what is "ambient" light?

[Note: Shirley uses  $c_a$  instead of  $I_{la}$ .]

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# Wavelength dependence

Really,  $k_{e}$ ,  $k_{a}$ , and  $I_{La}$  are functions over all wavelengths  $\lambda$ .

Ideally, we would do the calculation on these functions. For the ambient shading equation, we would start with:

$$I(\lambda) = k_a(\lambda)I_{La}(\lambda)$$

then we would find good RGB values to represent the spectrum  $I(\lambda)$ .

Traditionally, though,  $k_a$  and  $l_{La}$  are represented as RGB triples, and the computation is performed on each color channel separately:

$$I^R = k_a^R \ I_{La}^R$$

$$I^{G} = k_{a}^{G} I_{La}^{G}$$

$$I^B = k_a^B I_{la}^B$$

#### **Diffuse reflection**

Let's examine the ambient shading model:

- objects have different colors
- we can control the overall light intensity
  - · what happens when we turn off the lights?
  - · what happens as the light intensity increases?
  - · what happens if we change the color of the lights?

So far, objects are uniformly lit.

- not the way things really appear
- in reality, light sources are localized in position or direction

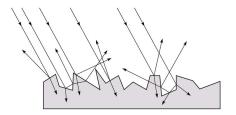
**Diffuse**, or **Lambertian** reflection will allow reflected intensity to vary with the direction of the light.

## **Diffuse reflectors**

Diffuse reflection occurs from dull, matte surfaces, like latex paint, or chalk.

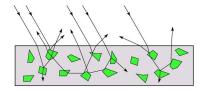
These **diffuse** or **Lambertian** reflectors reradiate light equally in all directions.

Picture a rough surface with lots of tiny microfacets.



## **Diffuse reflectors**

...or picture a surface with little pigment particles embedded beneath the surface (neglect reflection at the surface for the moment):



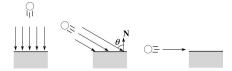
The microfacets and pigments distribute light rays in all directions.

Embedded pigments are responsible for the coloration of diffusely reflected light in plastics and paints.

Note: the figures above are intuitive, but not strictly (physically) correct.

# Diffuse reflectors, cont.

The reflected intensity from a diffuse surface does not depend on the direction of the viewer. The incoming light, though, does depend on the direction of the light source:



#### "Iteration two"

The incoming energy is proportional to \_\_\_\_\_, giving the diffuse reflection equations:

$$I = K_e + K_a I_{La} + K_d I_L B \underline{\hspace{1cm}}$$

$$= k_e + k_a I_{La} + k_d I_L B( )$$

#### where:

- $k_d$  is the diffuse reflection coefficient
- I, is the (color) intensity of the light source
- **N** is the normal to the surface (unit vector)
- L is the direction to the light source (unit vector)
- B prevents contribution of light from below the surface:

$$B = \begin{cases} 1 & \text{if } \mathbf{N} \cdot \mathbf{L} > \mathbf{0} \\ 0 & \text{if } \mathbf{N} \cdot \mathbf{L} \le \mathbf{0} \end{cases}$$

[Note: Shirley uses  $c_r$  and  $c_l$  instead of  $k_d$  and L.]

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# **Specular reflection**

**Specular reflection** accounts for the highlight that you see on some objects.

It is particularly important for *smooth*, *shiny* surfaces, such as:

- metal
- polished stone
- plastics
- apples
- skin

#### Properties:

- Specular reflection depends on the viewing direction V.
- For non-metals, the color is determined solely by the color of the light.
- For metals, the color may be altered (e.g., brass)

## Specular reflection "derivation"



For a perfect mirror reflector, light is reflected about  ${\it N}$ , so

$$I = \begin{cases} I_{L} & \text{if } \mathbf{V} = \mathbf{R} \\ 0 & \text{otherwise} \end{cases}$$

For a near-perfect reflector, you might expect the highlight to fall off quickly with increasing angle  $\phi$ .

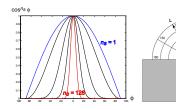
Also known as:

- "rough specular" reflection
- "directional diffuse" reflection
- "glossy" reflection

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# Phong specular reflection



One way to get this effect is to take  $(\mathbf{R-V})$ , raised to a power  $n_s$ .

As n<sub>s</sub> gets larger,

- the dropoff becomes {more,less} gradual
- gives a {larger,smaller} highlight
- simulates a {more,less} mirror-like surface

Phong specular reflection is proportional to:

$$I_{\text{specular}} \sim B(\mathbf{R} \cdot \mathbf{V})_{+}^{n_{\text{S}}}$$

where  $(x)_{+} \equiv \max(0, x)$ .

## **Blinn-Phong specular reflection**

A common alternative for specular reflection is the **Blinn-Phong model** (sometimes called the **modified Phong model**.)

We compute the vector halfway between  ${\bf L}$  and  ${\bf V}$  as:





Analogous to Phong specular reflection, we can compute the specular contribution in terms of (**N-H**), raised to a power  $n_c$ :

$$I_{\text{specular}} \sim B(\mathbf{N} \cdot \mathbf{H})_{+}^{n_{\text{S}}}$$

where, again,  $(x)_{\perp} \equiv \max(0, x)$ .

## "Iteration three"

The next update to the Blinn-Phong shading model is then:

$$I = k_e + k_a I_{La} + k_d I_L B(\mathbf{N} \cdot \mathbf{L}) + k_s I_L B(\mathbf{N} \cdot \mathbf{H})^{n_s}$$

$$= k_e + k_a I_{La} + I_L B \left[ k_{\sigma} (\mathbf{N} \cdot \mathbf{L}) + k_s (\mathbf{N} \cdot \mathbf{H})^{n_s} \right]$$

where:

- $k_s$  is the specular reflection coefficient
- n<sub>s</sub> is the specular exponent or shininess
- H is the unit halfway vector between L and V, where V is the viewing direction.

[Note: Shirley uses **e**, **r**, **h**, and p instead of **V**, **R**, **H**, and  $n_s$ .]

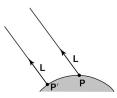
## **Directional lights**

The simplest form of lights supported by renderers are ambient, directional, and point. Spotlights are also supported often as a special form of point light.

We've seen ambient light sources, which are not really geometric.

**Directional light** sources have a single direction and intensity associated with them.





Using affine notation, what is the homogeneous coordinate for a directional light?

# **Point lights**

The direction of a **point light** sources is determined by the vector from the light position to the surface point.



Physics tells us the intensity must drop off inversely with the square of the distance:

$$f_{\text{atten}} = \frac{1}{r^2}$$

Sometimes, this distance-squared dropoff is considered too "harsh." A common alternative is:

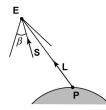
$$f_{\text{atten}} = \frac{1}{a + br + cr^2}$$

with user-supplied constants for a, b, and c.

Using affine notation, what is the homogeneous coordinate for a point light?

## **Spotlights**

We can also apply a *directional attenuation* of a point light source, giving a **spotlight** effect.



A common choice for the spotlight intensity is:

$$f_{\text{spot}} = \begin{cases} \frac{\left(\mathbf{L} \cdot \mathbf{S}\right)^e}{a + br + cr^2} & \text{if } \mathbf{L} \cdot \mathbf{S} \leq \cos \beta \\ 0 & \text{otherwise} \end{cases}$$

where

- L is the direction to the point light.
- **S** is the center direction of the spotlight.
- $\beta$  is the cutoff angle for the spotlight
- e is the angular falloff coefficient

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#### "Iteration four"

Since light is additive, we can handle multiple lights by taking the sum over every light.

Our equation is now:

$$I = K_e + K_a I_{La} +$$

$$\sum_{j} \frac{\left(\mathbf{L}_{j} \cdot \mathbf{S}_{j}\right)_{\beta_{j}}^{e_{j}}}{a_{j} + b_{j} r_{j} + c_{j} r_{j}^{2}} I_{L,j} B_{j} \left[ k_{d} \left(\mathbf{N} \cdot \mathbf{L}_{j}\right) + k_{s} \left(\mathbf{N} \cdot \mathbf{H}_{j}\right)^{n_{s}} \right]$$

This is the Phong illumination model.

Which quantities are spatial vectors?

Which are RGB triples?

Which are scalars?

#### **Choosing the parameters**

Experiment with different parameter settings. To get you started, here are a few suggestions:

- Try *n*<sub>s</sub> in the range [0,100]
- Try  $k_a + k_d + k_s < 1$
- Use a small  $k_a$  (~0.1)

	n <sub>s</sub>	k <sub>d</sub>	k <sub>s</sub>
Metal	large	Small, color of metal	Large, color of metal
Plastic	medium	Medium, color of plastic	Medium, white
Planet	0	varying	0

#### **BRDF**

The diffuse+specular parts of the Blinn-Phong illumination model are a mapping from light to viewing directions:

$$I = I_L B \left[ k_d(\mathbf{N} \cdot \mathbf{L}) + k_s \mathbf{N} \cdot \left( \frac{\mathbf{L} + \mathbf{V}}{\|\mathbf{L} + \mathbf{V}\|} \right)^{n_s} \right]$$
$$= I_L f_c(\mathbf{L}, \mathbf{V})$$

The mapping function  $f_r$  is often written in terms of incoming (light) directions  $\omega_{\rm in}$  and outgoing (viewing) directions  $\omega_{\rm out}$ :

$$f_r(\omega_{in}, \omega_{out})$$
 or  $f_r(\omega_{in} \to \omega_{out})$ 

This function is called the **Bi-directional Reflectance Distribution Function (BRDF)**.

Here's a plot with  $\omega_{in}$  held constant:



BRDF's can be quite sophisticated...

## More sophisticated BRDF's

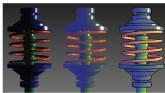


[Cook and Torrance, 1982]





Anisotropic BRDFs [Westin, Arvo, Torrance 1992]



Artistics BRDFs [Gooch]

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# **Gouraud vs. Phong interpolation**

Now we know how to compute the color at a point on a surface using the Blinn-Phong lighting model.

Does graphics hardware do this calculation at every point? Not by default...

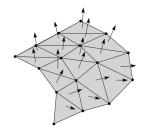
Smooth surfaces are often approximated by polygonal facets, because:

- Graphics hardware generally wants polygons (esp. triangles).
- Sometimes it easier to write ray-surface intersection algorithms for polygonal models.

How do we compute the shading for such a surface?

# **Faceted shading**

Assume each face has a constant normal:



For a distant viewer and a distant light source and constant material properties over the surface, how will the color of each triangle vary?

Result: faceted, not smooth, appearance.

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# Faceted shading (cont'd)



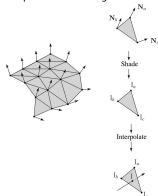


# Gouraud interpolation

To get a smoother result that is easily performed in hardware, we can do **Gouraud interpolation**.

Here's how it works:

- 1. Compute normals at the vertices.
- 2. Shade only the vertices.
- 3. Interpolate the resulting vertex colors.



[Williams and Siegel 1990]

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## Facted shading vs. Gouraud interpolation





[Williams and Siegel 1990]

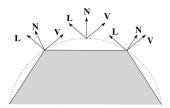
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# **Gouraud interpolation artifacts**

Gouraud interpolation has significant limitations.

1. If the polygonal approximation is too coarse, we can miss specular highlights.



2. We will encounter **Mach banding** (derivative discontinuity enhanced by human eye).

This is what graphics hardware does by default.

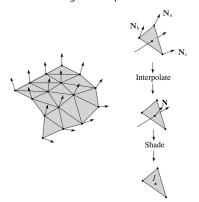
A substantial improvement is to do...

# **Phong interpolation**

To get an even smoother result with fewer artifacts, we can perform **Phong** *interpolation*.

Here's how it works:

- 1. Compute normals at the vertices.
- 2. Interpolate normals and normalize.
- 3. Shade using the interpolated normals.



## **Gouraud vs. Phong interpolation**





[Williams and Siegel 1990]

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