CSE-571 Probabilistic Robotics

Probabilistic Sensor Models

Beam-based Scan-based Landmarks

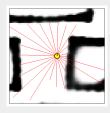
Sensors for Mobile Robots

- Contact sensors: Bumpers
- Internal sensors
 - Accelerometers (spring-mounted masses)
 - Gyroscopes (spinning mass, laser light)
 - Compasses, inclinometers (earth magnetic field, gravity)
- Proximity sensors
 - Sonar (time of flight)
 - Radar (phase and frequency)
 - Laser range-finders (triangulation, tof, phase)
 - Infrared (intensity)
- Visual sensors: Cameras, depth cameras
- Satellite-based sensors: GPS

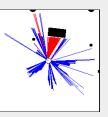
10/12/15

CSE-571 - Probabilistic Robotics

Proximity Sensors







- The central task is to determine P(z|x), i.e. the probability of a measurement z given that the robot is at position x.
- Question: Where do the probabilities come from?
- Approach: Let's try to explain a measurement.

10/12/15

CSE-571 - Probabilistic Robotics

Beam-based Sensor Model

Scan z consists of K measurements.

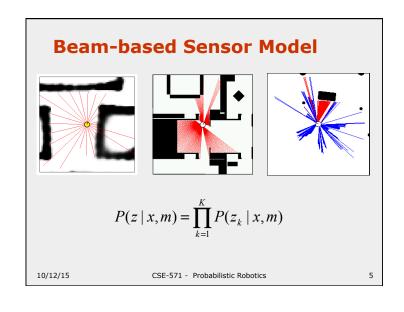
$$z = \{z_1, z_2, ..., z_K\}$$

• Individual measurements are independent given the robot position.

$$P(z \mid x, m) = \prod_{k=1}^{K} P(z_k \mid x, m)$$

10/12/15

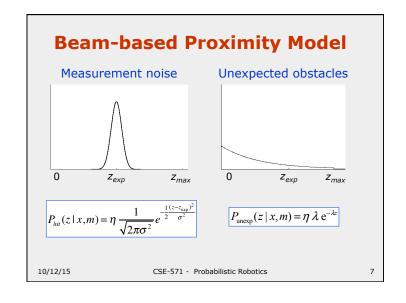
CSE-571 - Probabilistic Robotics

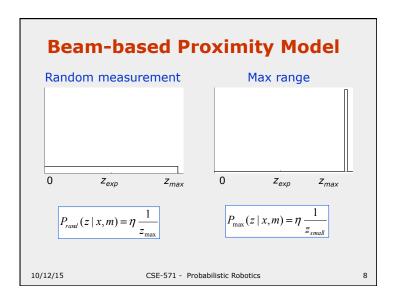


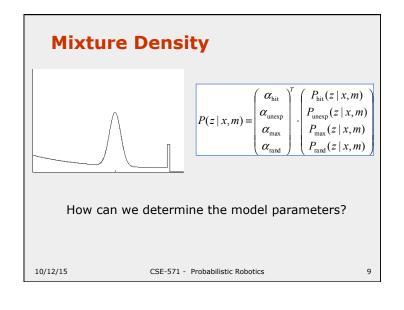
Proximity Measurement

- Measurement can be caused by ...
 - a known obstacle.
 - cross-talk.
 - an unexpected obstacle (people, furniture, ...).
 - missing all obstacles (total reflection, glass, ...).
- Noise is due to uncertainty ...
 - in measuring distance to known obstacle.
 - in position of known obstacles.
 - in position of additional obstacles.
 - whether obstacle is missed.

10/12/15 CSE-571 - Probabilistic Robotics







Approximation

- \bullet Maximize log likelihood of the data $P(z\,|\,z_{\rm exp})$
- Search parameter space.
- EM to find mixture parameters
 - Assign measurements to densities.
 - Estimate densities using assignments.

10

• Reassign measurements.

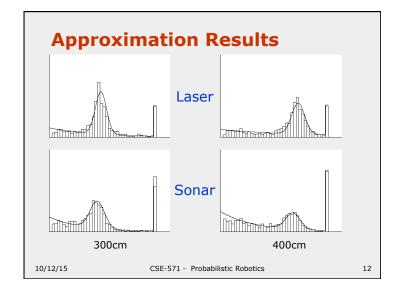
10/12/15 CSE-571 - Probabilistic Robotics

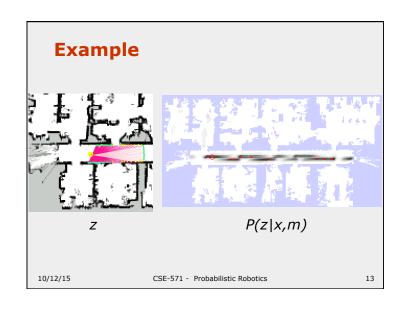
Raw Sensor Data

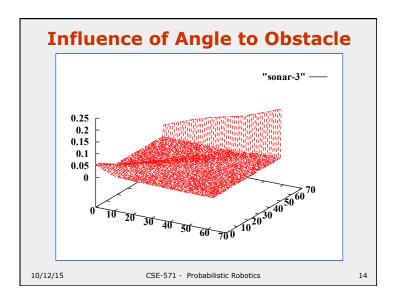
Measured distances for expected distance of 300 cm.

Sonar

Laser







Summary Beam-based Model

- Assumes independence between beams.
 - Justification?
 - Overconfident!
- Models physical causes for measurements.
 - Mixture of densities for these causes.
- Implementation
 - · Learn parameters based on real data.
 - Different models should be learned for different angles at which the sensor beam hits the obstacle.

15

- Determine expected distances by ray-tracing.
- · Expected distances can be pre-processed.

10/12/15 CSE-571 - Probabilistic Robotics

Scan-based Model

- Beam-based model is ...
 - not smooth for small obstacles and at edges.
 - not very efficient.
- Idea: Instead of following along the beam, just check the end point.

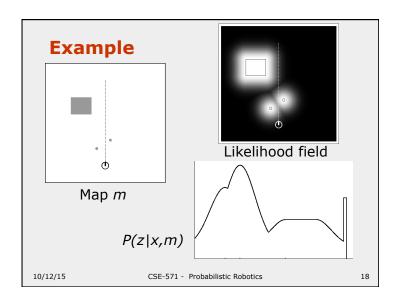
10/12/15 CSE-571 - Probabilistic Robotics

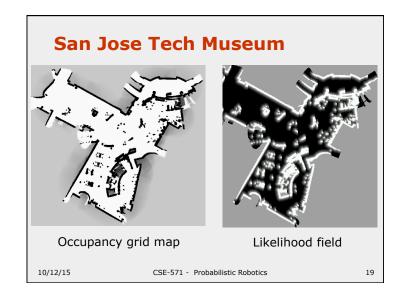
Scan-based Model

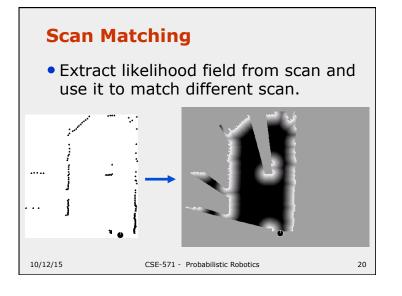
- Probability is a mixture of ...
 - a Gaussian distribution with mean at distance to closest obstacle,
 - a uniform distribution for random measurements, and
 - a small uniform distribution for max range measurements.
- Again, independence between different components is assumed.

10/12/15

CSE-571 - Probabilistic Robotics







Scan Matching

• Extract likelihood field from first scan and use it to match second scan.



~0.01 sec

21

10/12/15

CSE-571 - Probabilistic Robotics

Properties of Scan-based Model

- Highly efficient, uses 2D tables only.
- Smooth w.r.t. to small changes in robot position.
- Allows gradient descent, scan matching.
- Ignores physical properties of beams.
- Works for sonars?

10/12/15

CSE-571 - Probabilistic Robotics

Additional Models of Proximity Sensors

- Map matching (sonar,laser): generate small, local maps from sensor data and match local maps against global model.
- Scan matching (laser): map is represented by scan endpoints, match scan into this map using ICP, correlation.
- Features (sonar, laser, vision): Extract features such as doors, hallways from sensor data.

10/12/15

CSE-571 - Probabilistic Robotics

23

Landmarks

- Active beacons (e.g. radio, GPS)
- Passive (e.g. visual, retro-reflective)
- Standard approach is triangulation
- Sensor provides
 - distance, or
 - bearing, or
 - distance and bearing.

10/12/15

CSE-571 - Probabilistic Robotics

24





Probabilistic Model

1. Algorithm landmark_detection_model(z,x,m):

$$z = \langle i, d, \alpha \rangle, x = \langle x, y, \theta \rangle$$

- 2. $\hat{d} = \sqrt{(m_x(i) x)^2 + (m_y(i) y)^2}$
- 3. $\hat{\alpha} = \operatorname{atan2}(m_{v}(i) y, m_{x}(i) x) \theta$
- 4. $p_{\text{det}} = \text{prob}(\hat{d} d, \varepsilon_d) \cdot \text{prob}(\hat{\alpha} \alpha, \varepsilon_\alpha)$
- 5. Return $z_{\text{det}} p_{\text{det}} + z_{\text{fp}} P_{\text{uniform}}(z \mid x, m)$

10/12/15

CSE-571 - Probabilistic Robotics

26

28

Distributions for P(z|x)10/12/15 27 CSE-571 - Probabilistic Robotics

Summary of Sensor Models

- Explicitly modeling uncertainty in sensing is key to robustness.
- In many cases, good models can be found by the following
 - 1. Determine parametric model of noise free measurement.
 - 2. Analyze sources of noise.
 - 3. Add adequate noise to parameters (eventually mix in densities
 - 4. Learn (and verify) parameters by fitting model to data.
 - 5. Likelihood of measurement is given by "probabilistically comparing" the actual with the expected measurement.
- This holds for motion models as well.
- It is extremely important to be aware of the underlying assumptions!

10/12/15

CSE-571 - Probabilistic Robotics

