

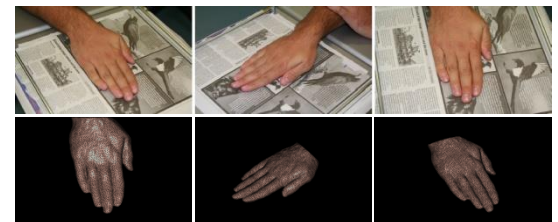
# Reconstruction

EE/CSE 576

Linda Shapiro

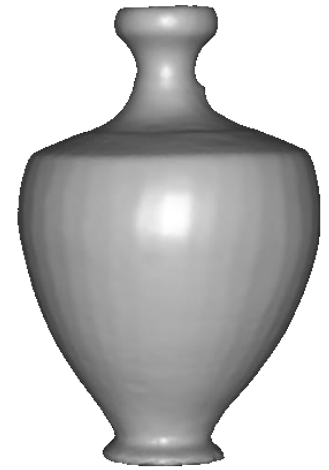
# 3D model

- “Digital copy” of real object
- Allows us to
  - Inspect details of object
  - Measure properties
  - Reproduce in different material
- Many applications
  - Cultural heritage preservation
  - Computer games and movies
  - City modelling
  - E-commerce



# Applications: cultural heritage

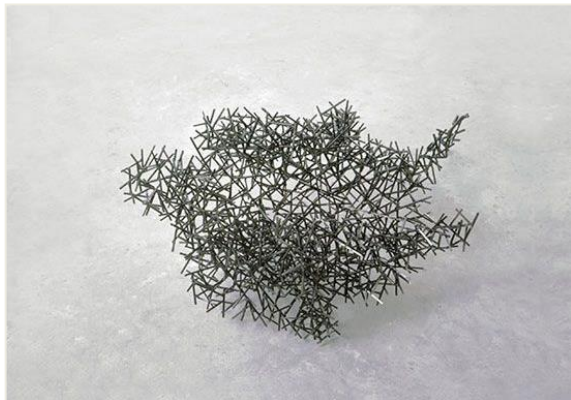
SCULPTEUR European project



# Applications: art



Block Works Precipitate III 2004  
*Mild steel blocks 80 x 46 x 66 cm*



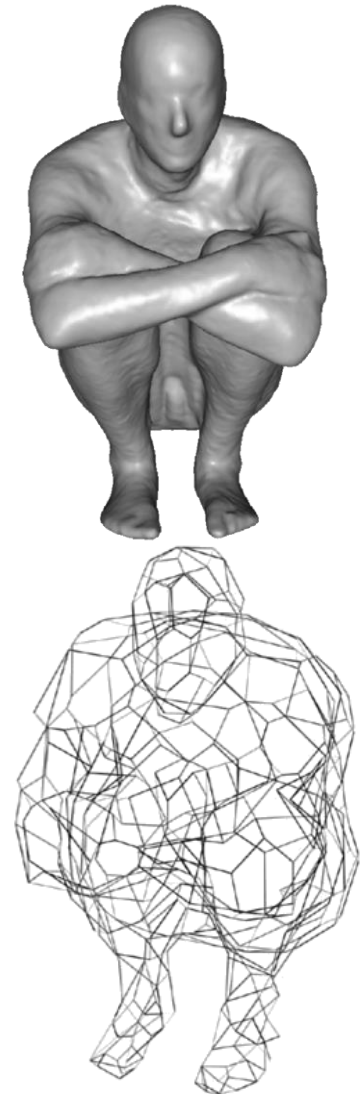
Domain Series Domain VIII Crouching  
1999 *Mild steel bar 81 x 59 x 63 cm*



# Applications: structure engineering



BODY / SPACE / FRAME, Antony Gormley, Lelystad, Holland



# Applications: 3D indexation

The image displays a 3D indexing application interface. On the left, a large 3D model of a female torso sculpture is highlighted. To its right, a grid of smaller 3D models is shown, with four specific models labeled with IDs and similarity scores:

0 : deesse0 0.000000	1 : deesse5 0.092800
5 : deesse2 0.211000	6 : ARCHI3203 0.236800

Below the grid, several blue question marks are placed over the 3D models, indicating a search or classification process. On the right side, an inset image shows a real-world scene of a museum or gallery with various artifacts on display. The interface also features a top row of small 3D models and a bottom row of small 3D models, likely representing different views or categories of objects.

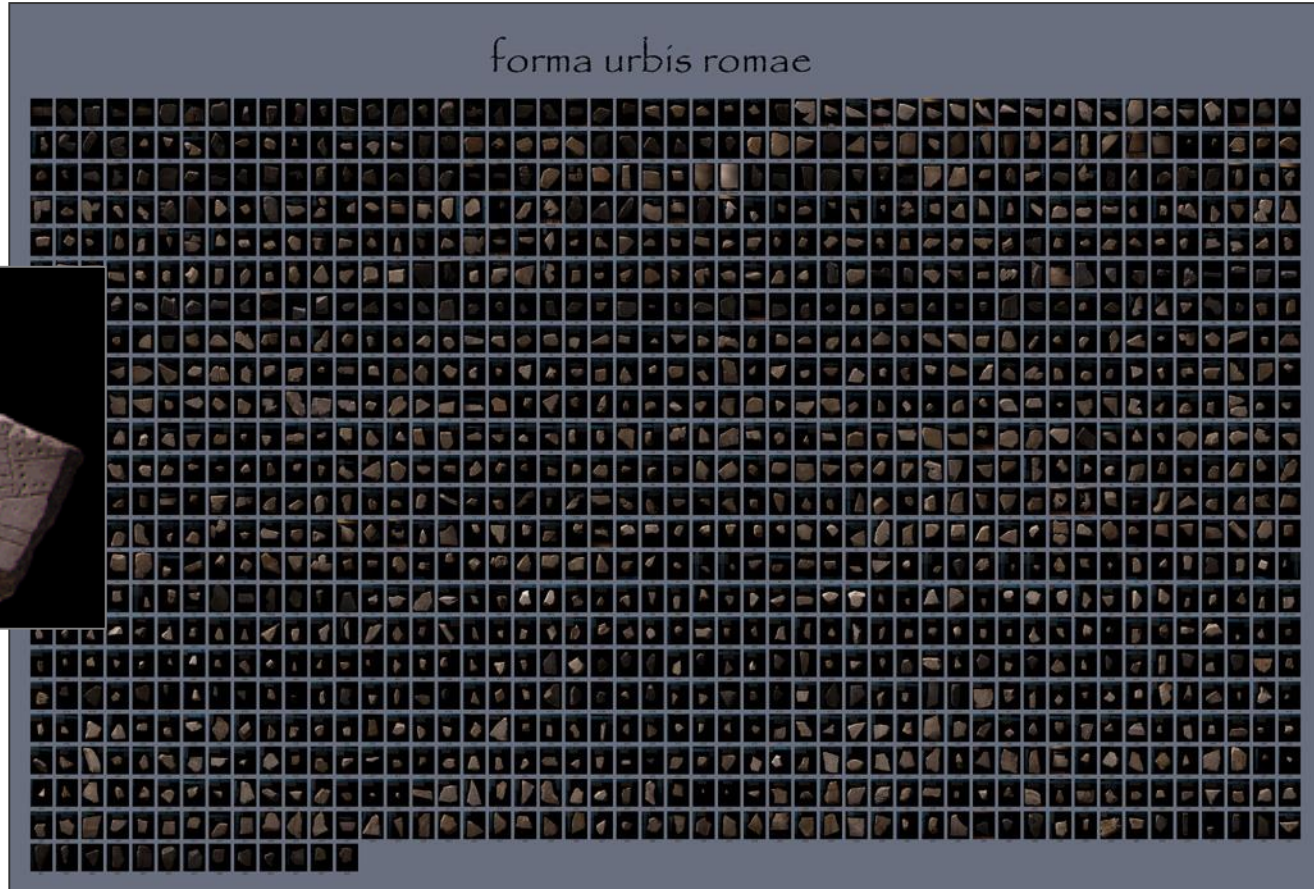
# Applications: archaeology

- “forma urbis romae” project

**Fragments of the City: Stanford's Digital Forma Urbis Romae Project**

David Koller, Jennifer Trimble, Tina Najbjerg, Natasha Gelfand, Marc Levoy

*Proc. Third Williams Symposium  
on Classical Architecture,  
Journal of Roman Archaeology  
supplement, 2006.*



1186 fragments

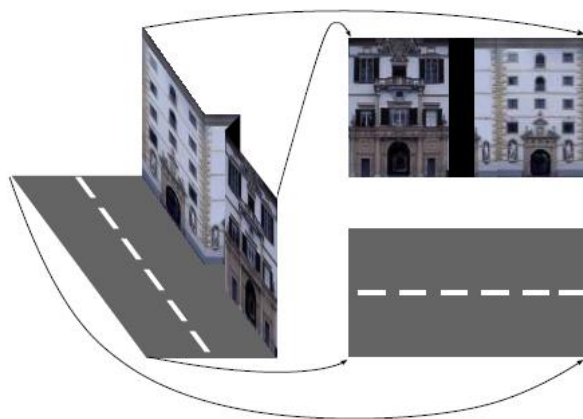
# Applications: large scale modelling



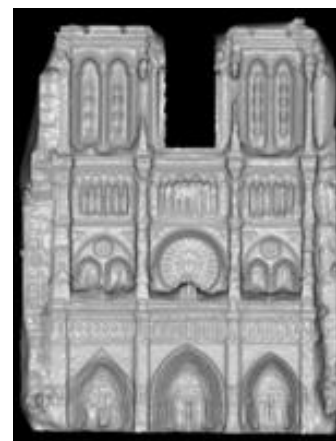
[Furukawa10]



[Pollefeys08]



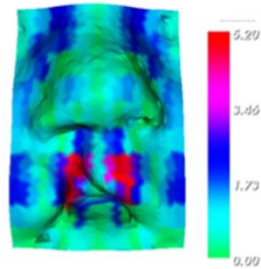
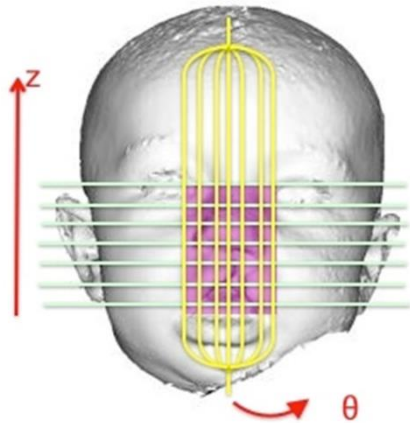
[Cornelis08]



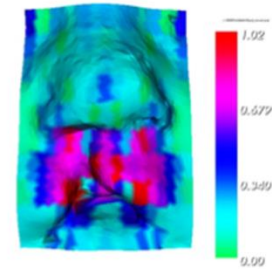
[Goesele07]



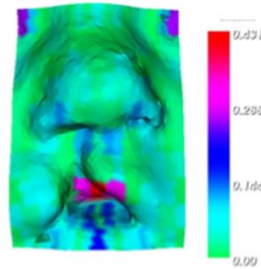
# Applications: Medicine



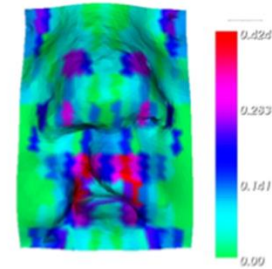
(a) Radius difference



(b) Angle difference



(c) Curvature difference

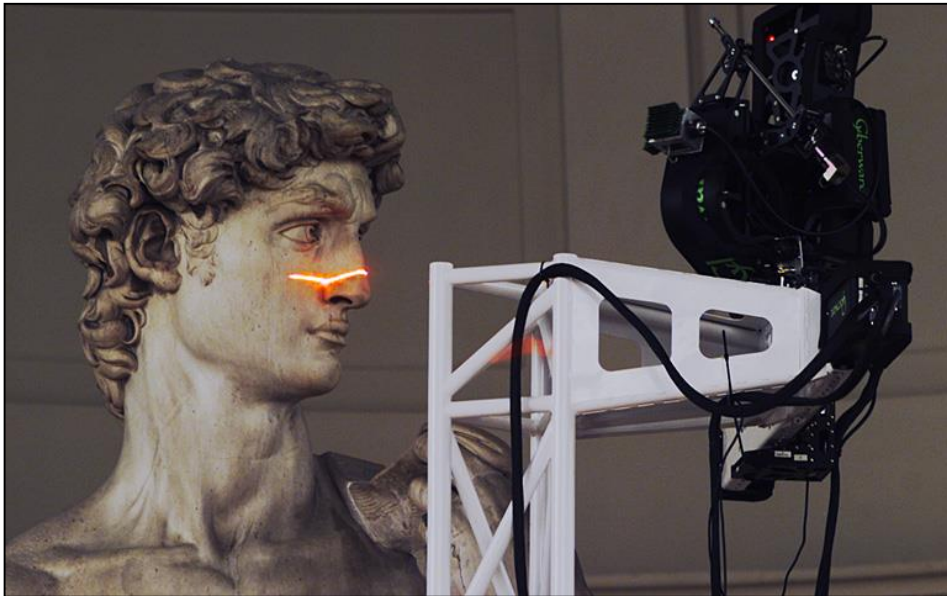


(d) Edge difference

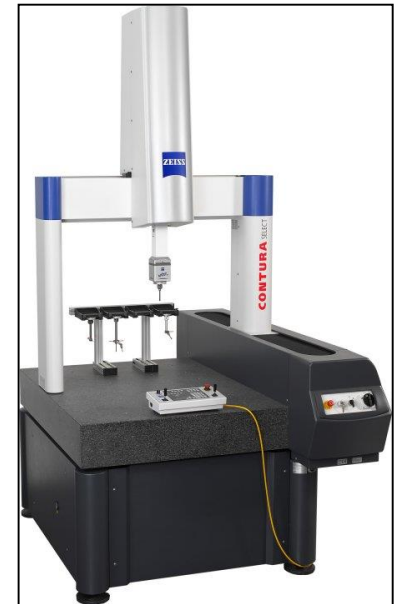
expert's order	1	2	3	4	5	6	7	8	9	10
images										
learning	1	3	2	4	5	6	8	9	7	10
a-lmk	1	2	3	5	6	4	8	7	9	10
mirror	1	2	4	8	5	6	9	3	7	10
m-lmk	1	2	3	4	5	6	9	7	10	8
plane	1	2	3	5	4	6	7	9	10	8

# Scanning technologies

- Laser scanner, coordinate measuring machine
  - Very accurate
  - Very Expensive
  - Complicated to use

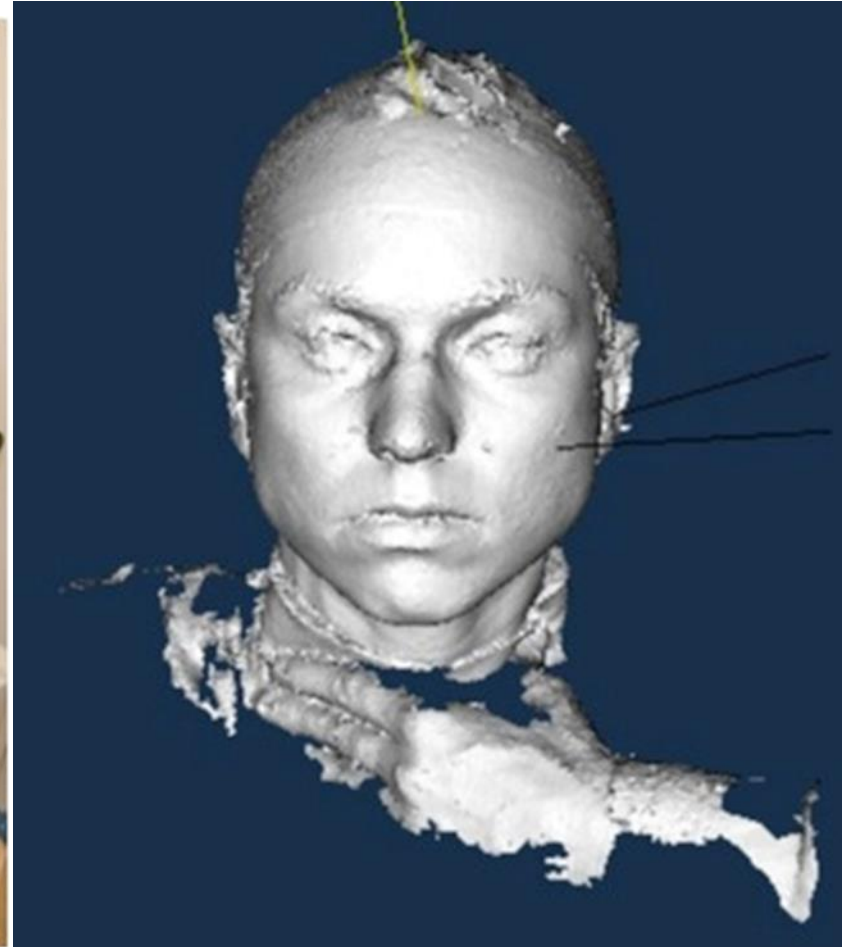


Minolta

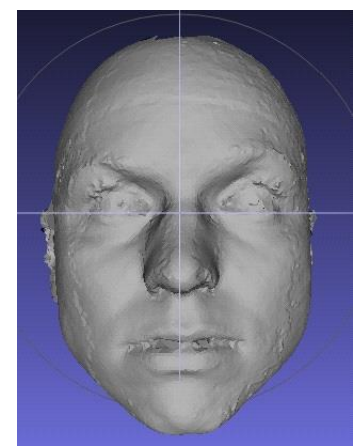
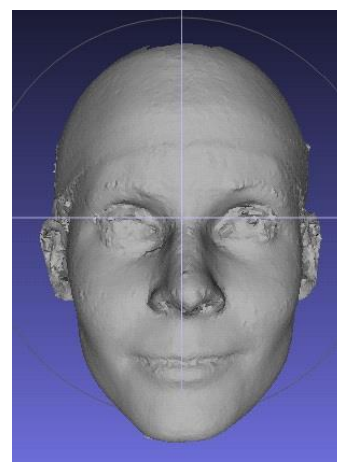
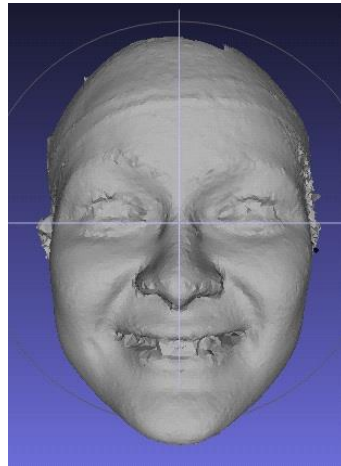
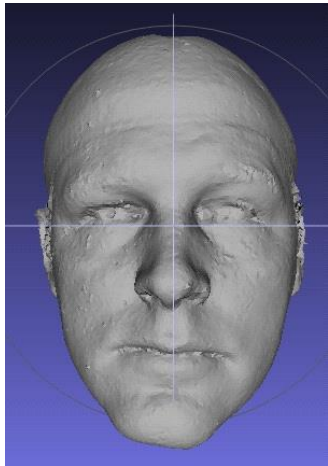
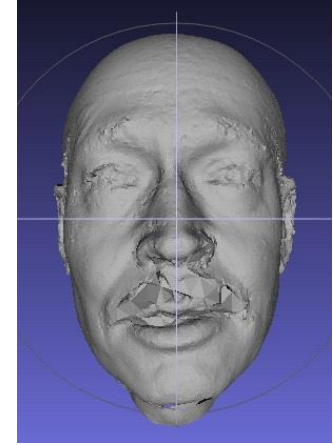
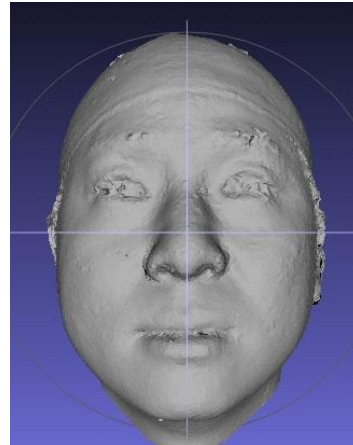
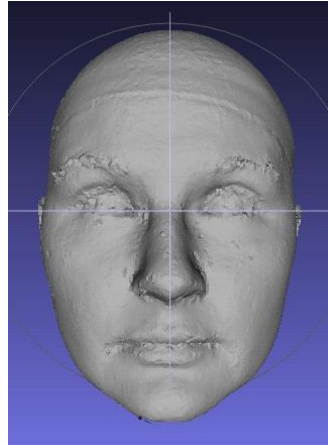
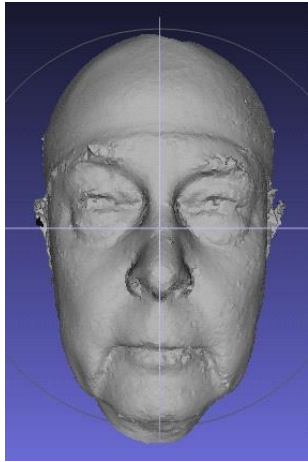


Contura CMM

# Medical Scanning System

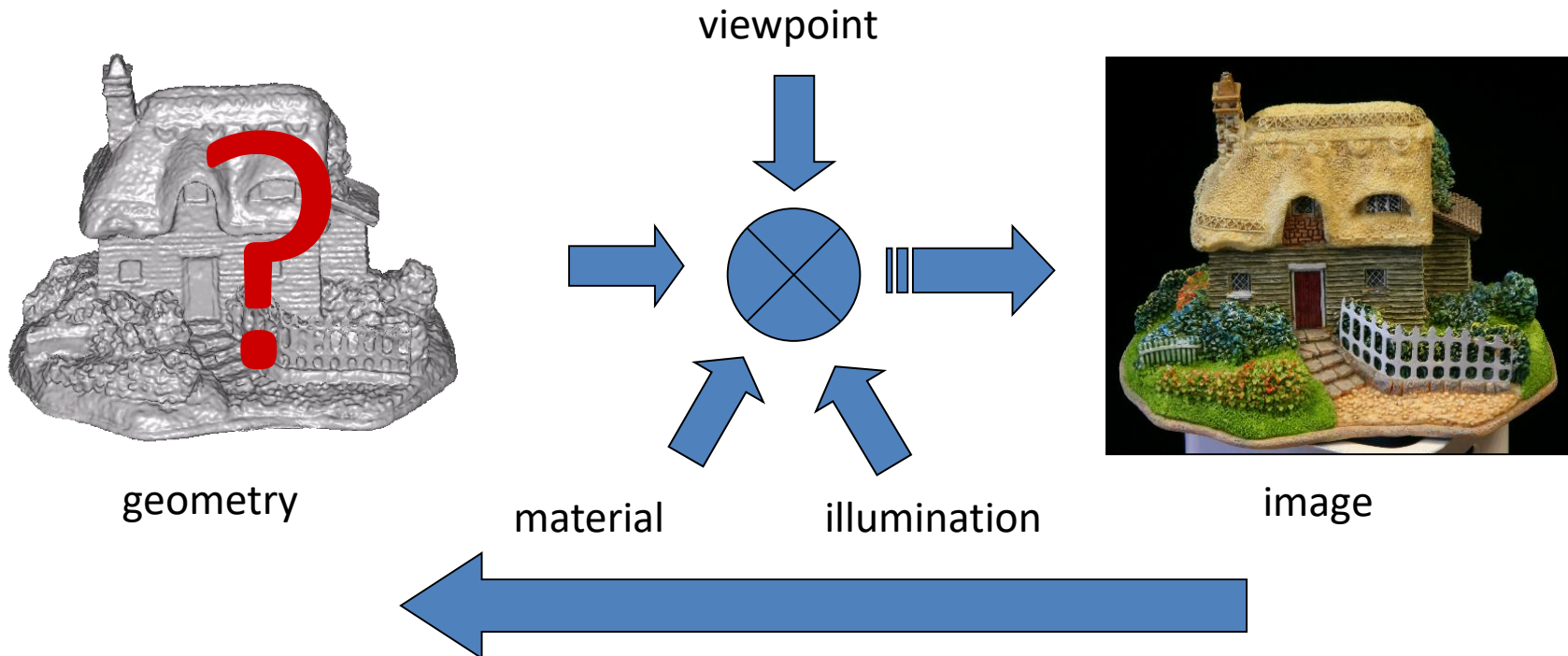


# The “Us” Data Set (subset)



# 3d shape from photographs

*“Estimate a 3d shape that would generate the input photographs given the same material, viewpoints and illumination”*



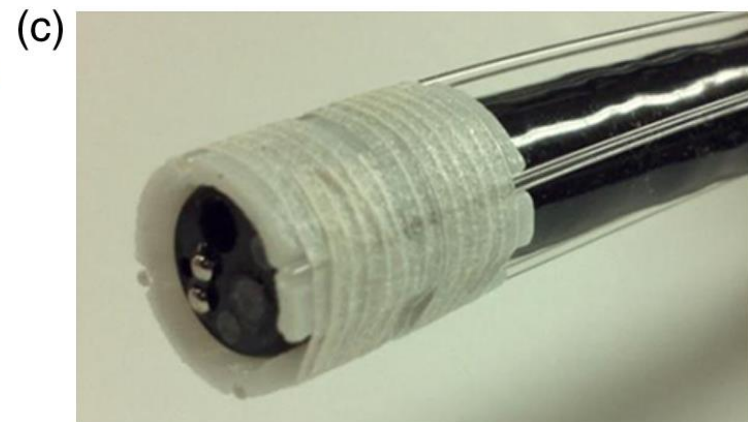
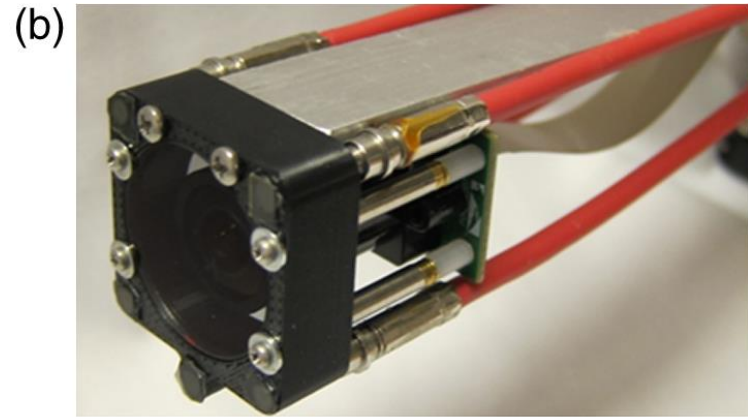
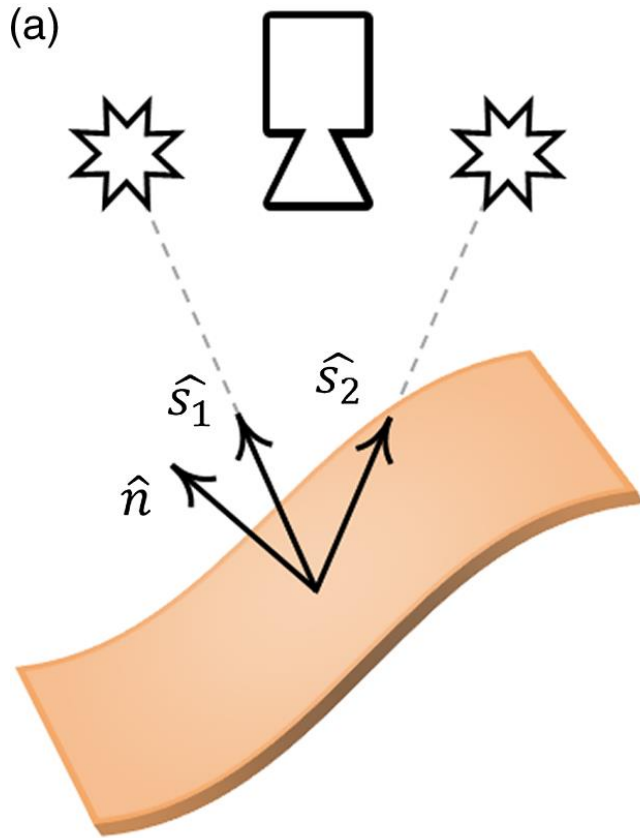
# Photometric Stereo

- Estimate the surface normals of a given scene given multiple 2D images taken from the *same* viewpoint, but under *different lighting* conditions.
- **Basic photometric stereo** required a Lambertian reflectance model:

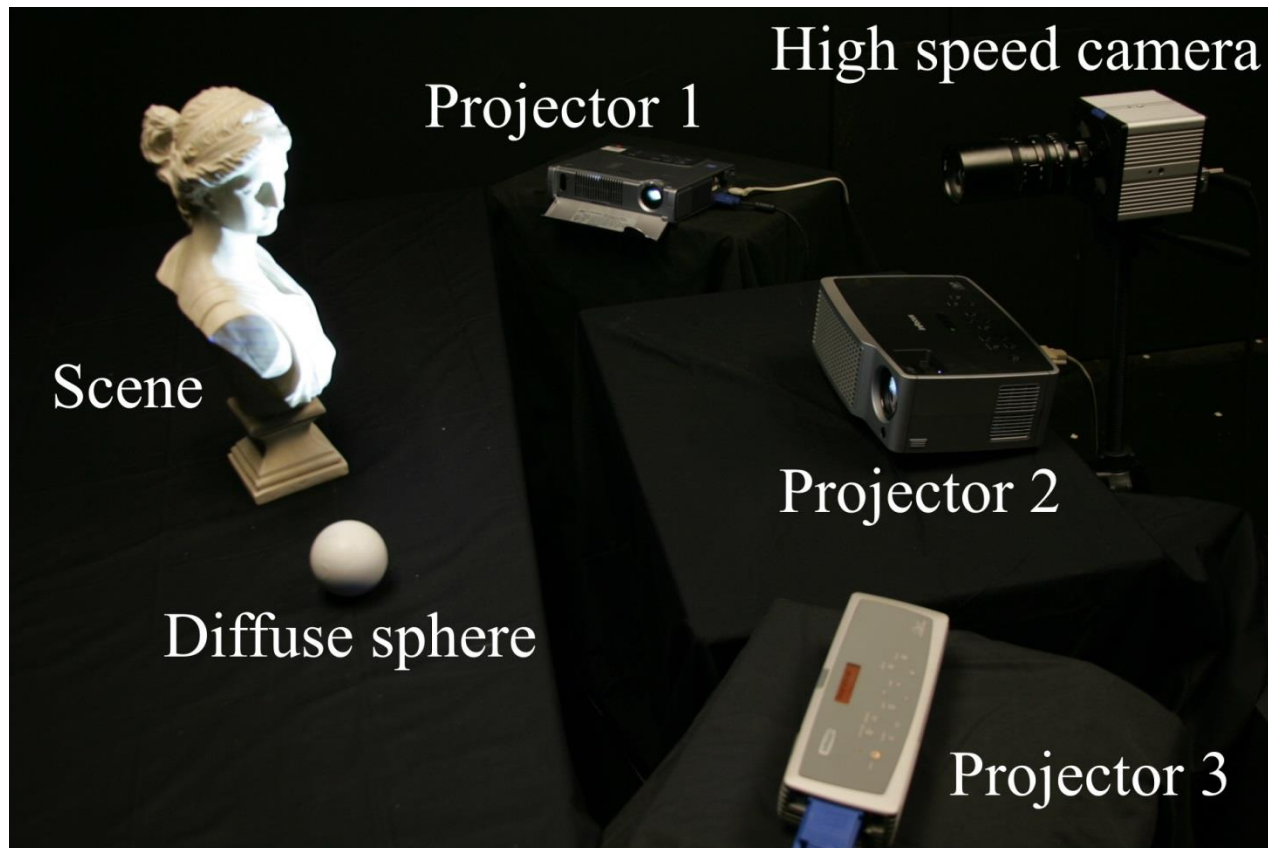
$$I = \rho \mathbf{n} \cdot \mathbf{v}$$

where  $I$  is pixel **intensity**,  $\mathbf{n}$  is the **normal**,  $\mathbf{v}$  is the **lighting direction**, and  $\rho$  is diffuse albedo constant, which is a reflection coefficient.

# Basic Photometric Stereo



# Basic Photometric Stereo





# Basic Photometric Stereo

- $K$  light sources
- Lead to  $K$  images  $R_1(p,q), \dots, R_K(p,q)$  each from just one of the light sources being on
- For any  $(p,q)$ , we get  $K$  intensities  $I_1, \dots, I_K$
- Leads to a set of linear equations of the form

$$I_k = \rho \mathbf{n} \cdot \mathbf{v}_k$$

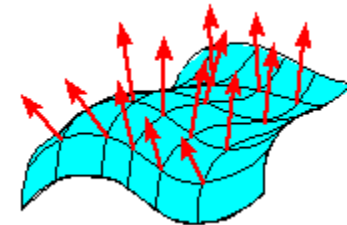
- Solving leads to a surface normal map.

# Photometric Stereo

Inputs



3D normals



# 3d shape from photographs

Photograph based 3d reconstruction is:

- ✓ practical
- ✓ fast
- ✓ non-intrusive
- ✓ low cost
- ✓ Easily deployable outdoors
- ✗ “low” accuracy
- ✗ Results depend on material properties

# Reconstruction

---

- Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape



# Reconstruction

---

- **Generic problem formulation:** given several images of the same object or scene, compute a representation of its 3D shape
- **“Images of the same object or scene”**
  - Arbitrary number of images (from two to thousands)
  - Arbitrary camera positions (camera network or video sequence)
  - Calibration may be initially unknown
- **“Representation of 3D shape”**
  - Depth maps
  - Meshes
  - Point clouds
  - Patch clouds
  - Volumetric models
  - Layered models

# Multiple-baseline stereo

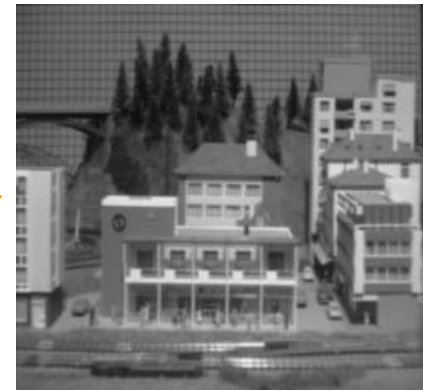
---



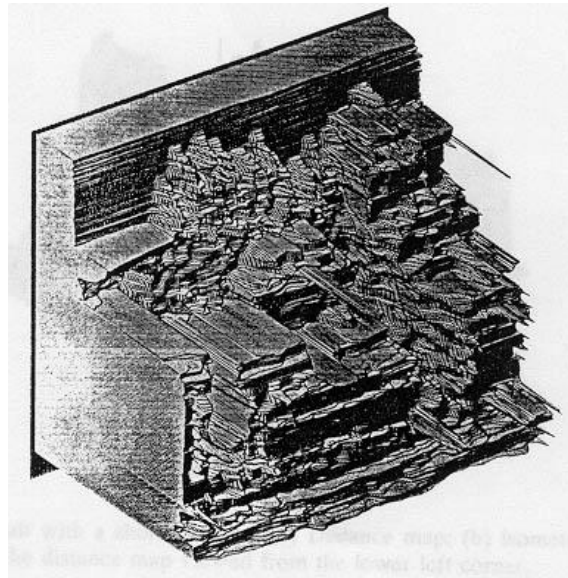
I1



I2



I10



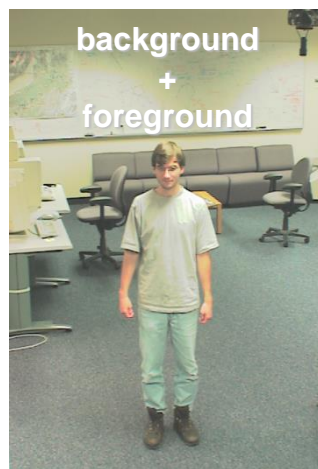
M. Okutomi and T. Kanade, ["A Multiple-Baseline Stereo System,"](#) IEEE Trans. on Pattern Analysis and Machine Intelligence, 15(4):353-363 (1993).

# Reconstruction from silhouettes

---

Can be computed robustly

Can be computed efficiently



-



=

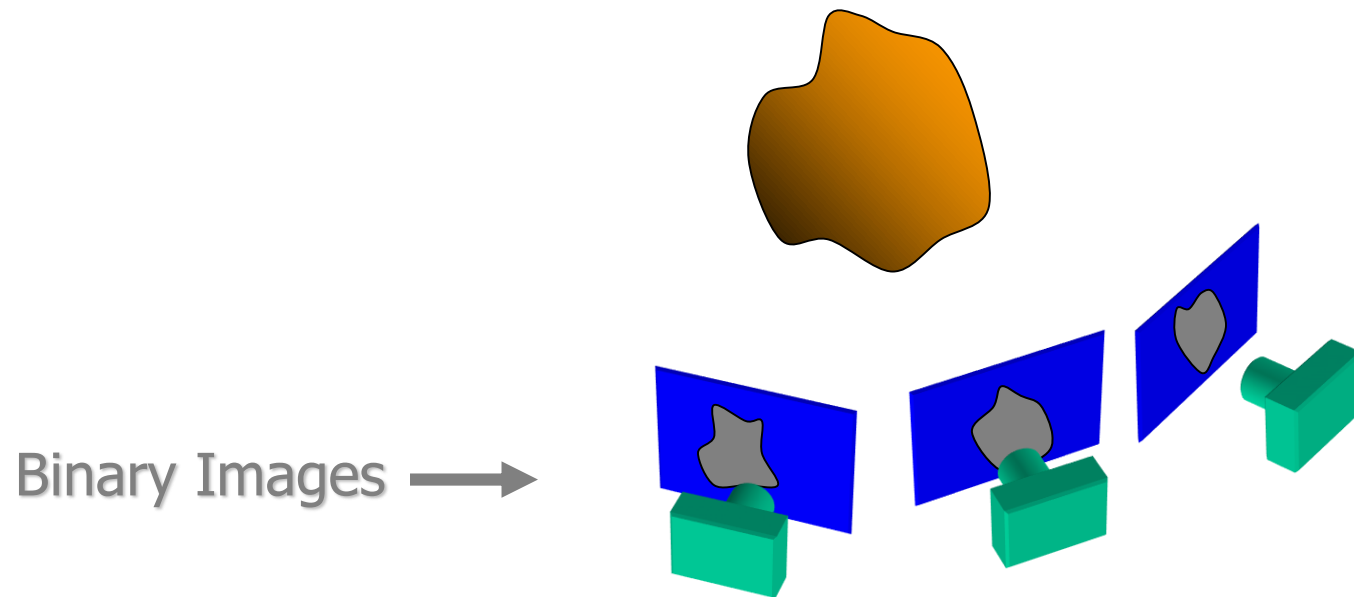
foreground



# Reconstruction from Silhouettes

---

- The case of binary images: a voxel is **photo-consistent** if it lies inside the object's silhouette in **all** views

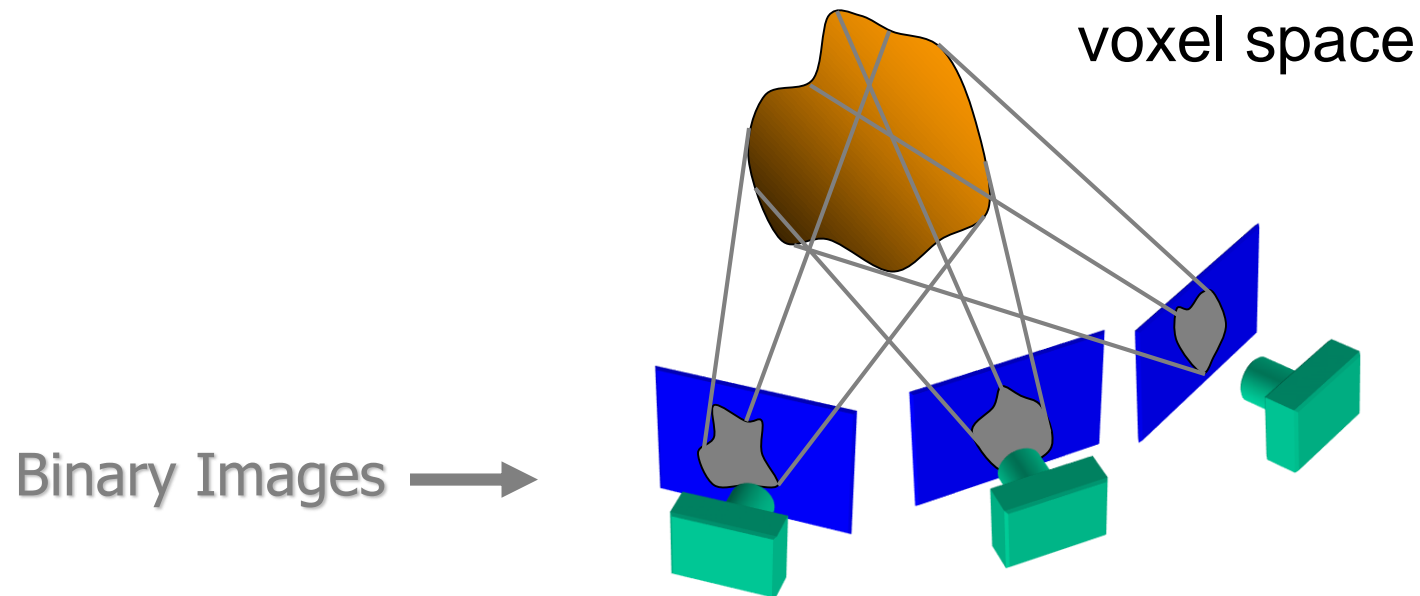




# Reconstruction from Silhouettes

---

- The case of binary images: a voxel is **photo-consistent** if it lies inside the object's silhouette in **all views**



Finding the silhouette-consistent shape (*visual hull*):

- *Backproject* each silhouette
- Intersect backprojected volumes

# Calibrated Image Acquisition

---



*Calibrated Turntable*



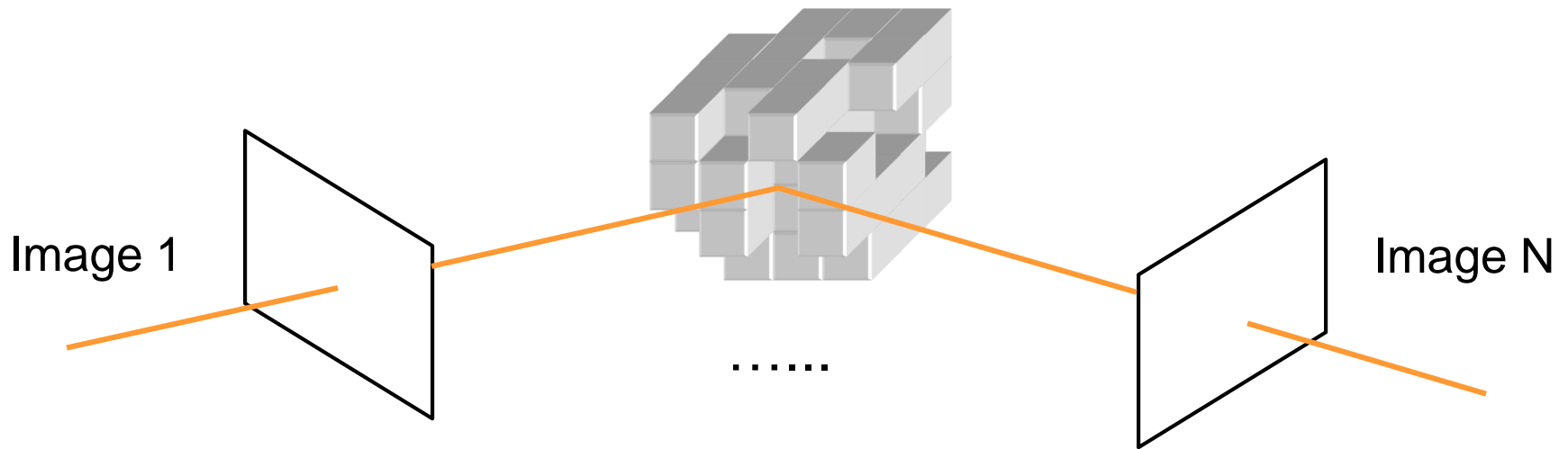
**Selected Dinosaur Images**



**Selected Flower Images**

# Space Carving in General

---

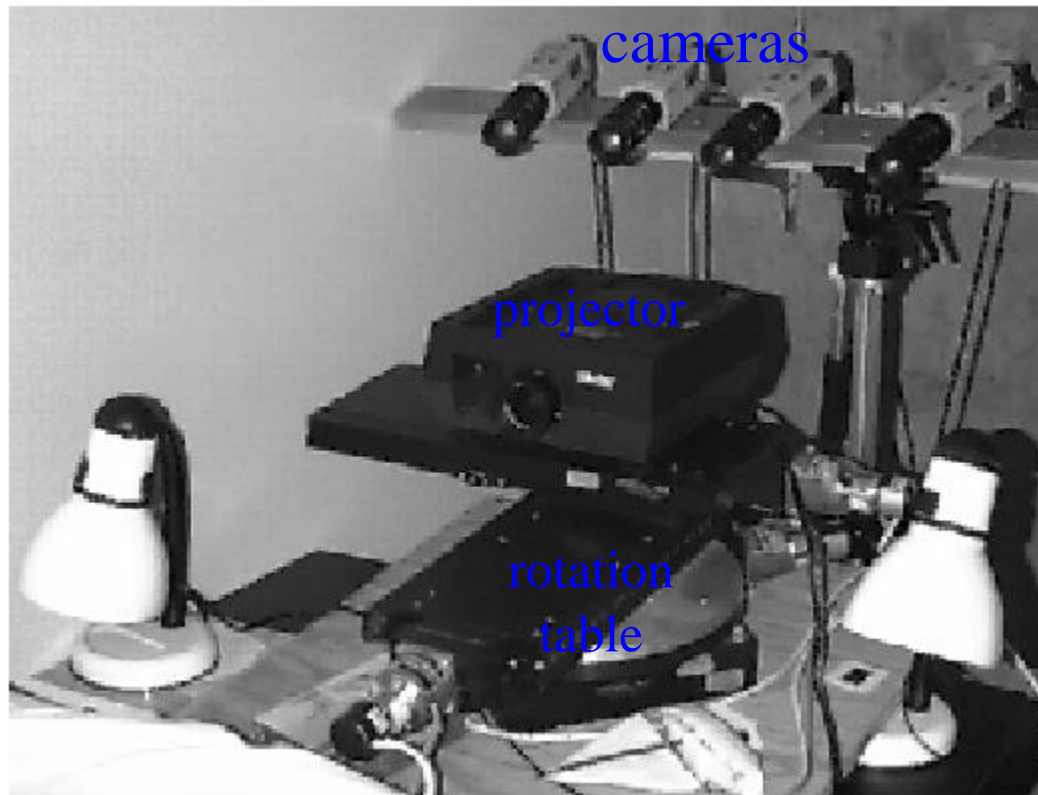


## Space Carving Algorithm

- Initialize to a volume  $V$  containing the true scene
- Choose a voxel on the outside of the volume
- Project to visible input images
- Carve if not photo-consistent (inside object's silhouette)
- Repeat until convergence

# Our 4-camera light-striping stereo system

(now deceased)



3D  
object

# Calibration Object

---

The idea is to snap images at different depths and get a lot of **2D-3D point correspondences**.



# Surface Modeling and Display from Range and Color Data



Kari	Pulli	UW
Michael	Cohen	MSR
Tom	Duchamp	UW
Hugues	Hoppe	MSR
John	McDonald	UW
Linda	Shapiro	UW
Werner	Stuetzle	UW

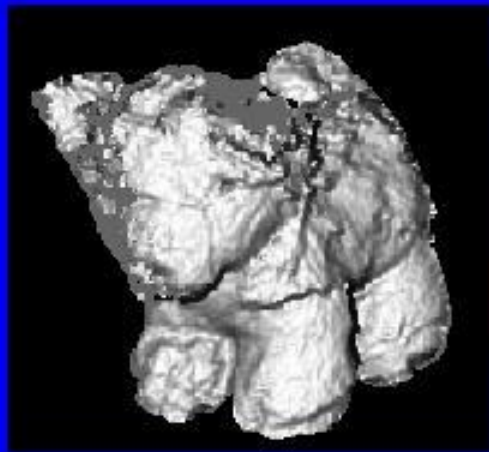
UW = University of Washington  
Seattle, WA USA  
MSR = Microsoft Research  
Redmond, WA USA

# Introduction

---

## Goal

- develop robust algorithms for constructing 3D models from range & color data
- use those models to produce realistic renderings of the scanned objects



# Surface Reconstruction

---

## Step 1: Data acquisition

Obtain range data that covers the object. Filter, remove background.

## Step 2: Registration

Register the range maps into a common coordinate system.

## Step 3: Integration

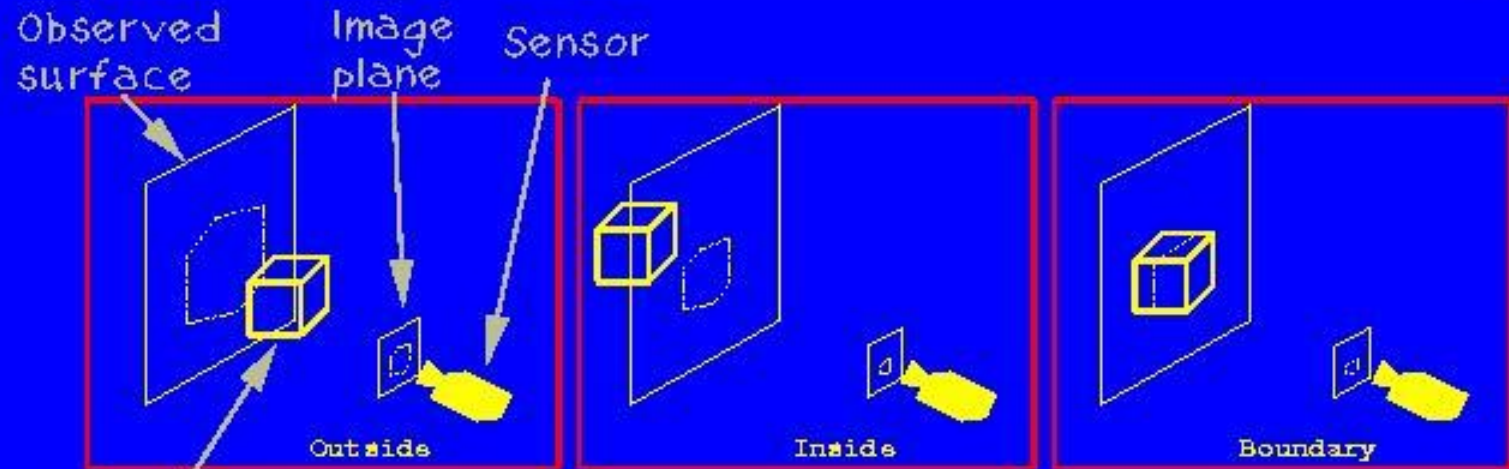
Integrate the registered range data into a single surface representation.

## Step 4: Optimization

Fit the surface more accurately to the data, simplify the representation.



# Carve space in cubes



Volume under consideration

## Label cubes

- Project cube to image plane (hexagon)
- Test against data in the hexagon

# 3D space is made up of many cubes.

---

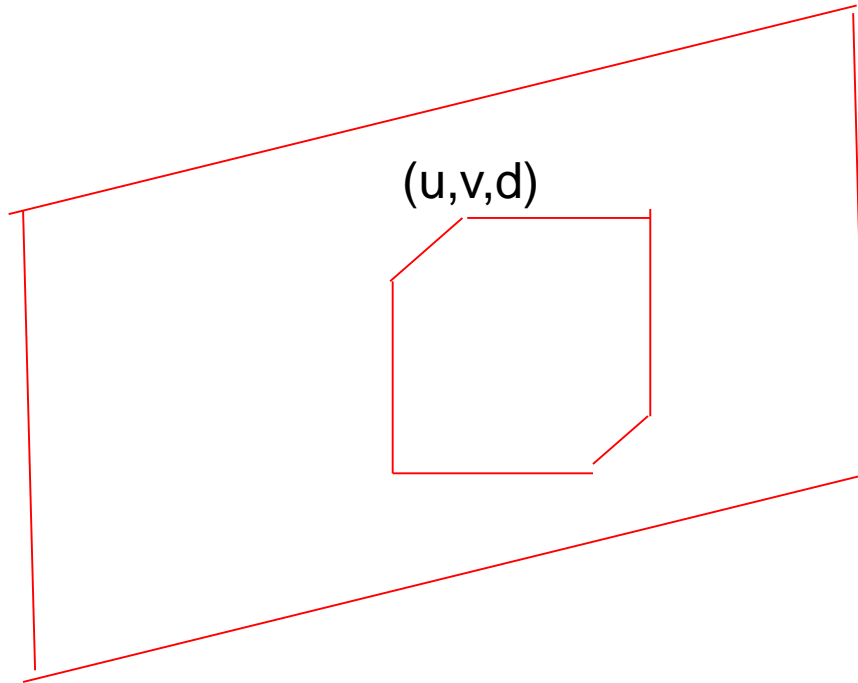
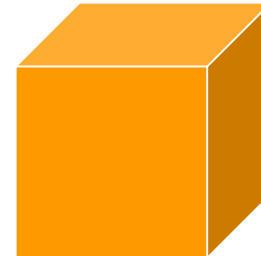


image plane  
depth map

$(x,y,z)$



OUTSIDE

one of many cubes  
in virtual 3D cube space

# Several views

---

Processing order:  
FOR EACH cube  
FOR EACH view

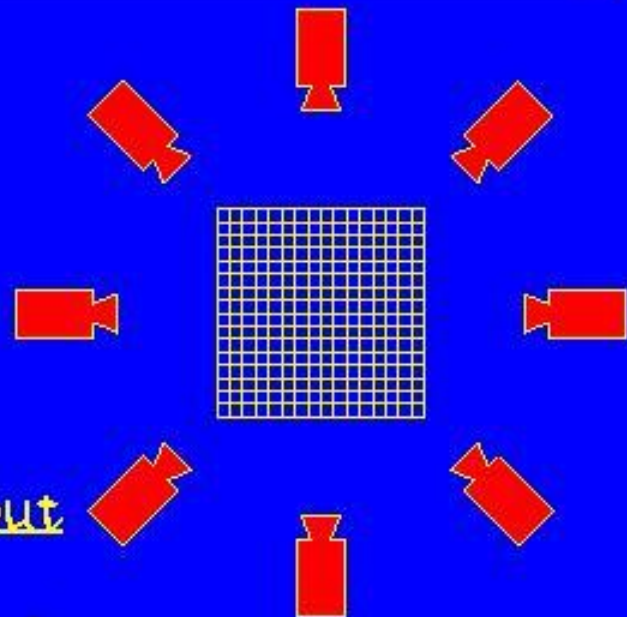
Rules:

any view thinks cube's out  
=> it's out

every view thinks cube's in  
=> it's in

else

=> it's at boundary



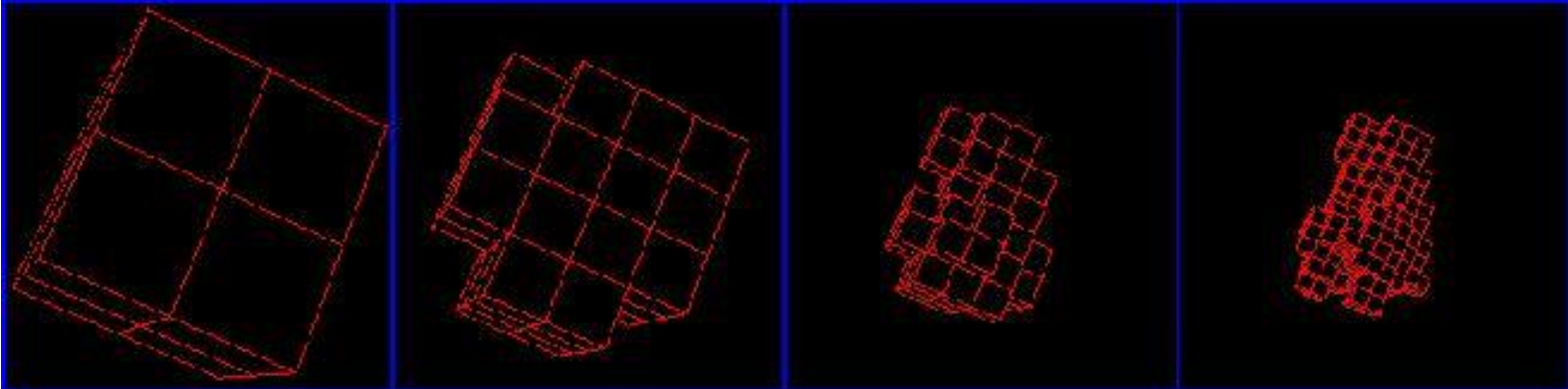
# Hierarchical space carving

---

- Big cubes => fast, poor results
- Small cubes => slow, more accurate results
- Combination = octrees

RULES:

- cube's out => done
- cube's in => done
- else => recurse



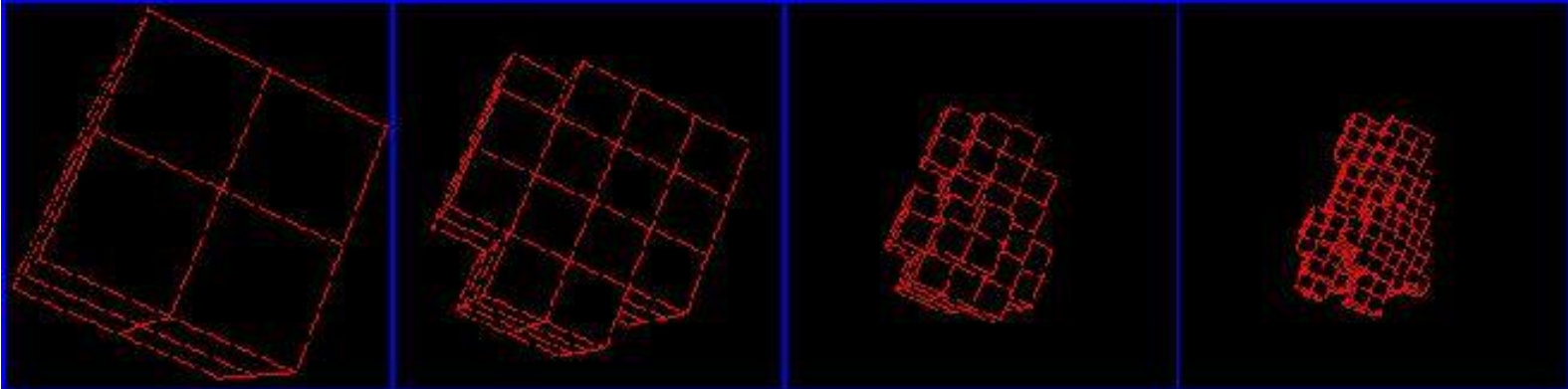
# Hierarchical space carving

---

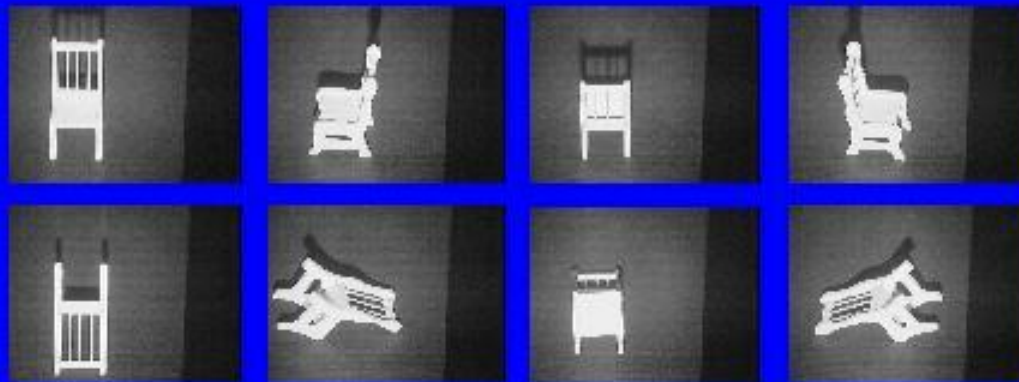
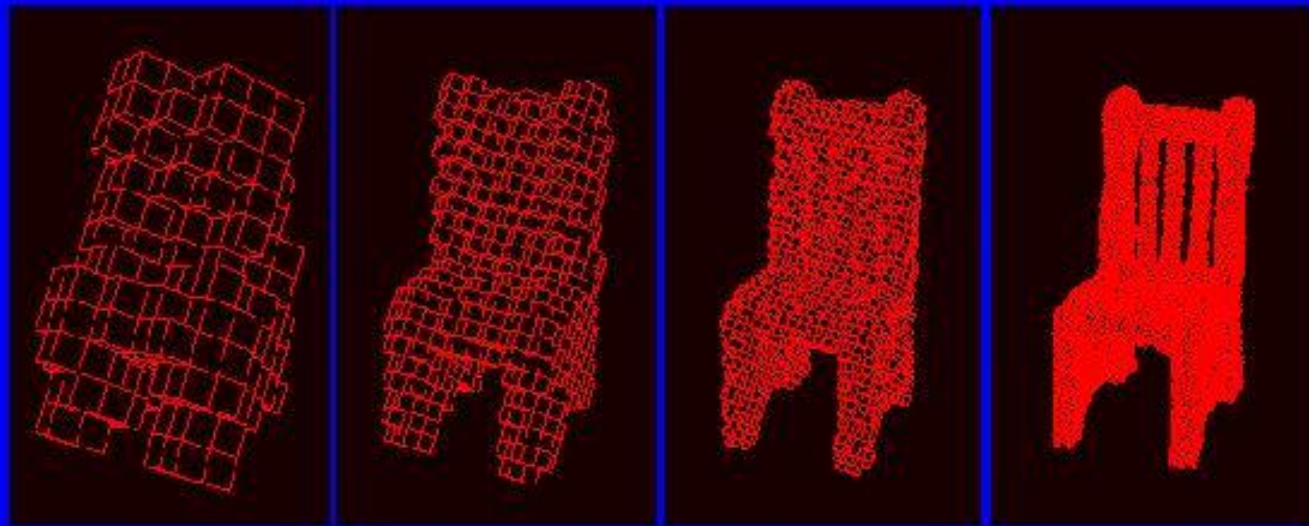
- Big cubes => fast, poor results
- Small cubes => slow, more accurate results
- Combination = octrees

RULES:

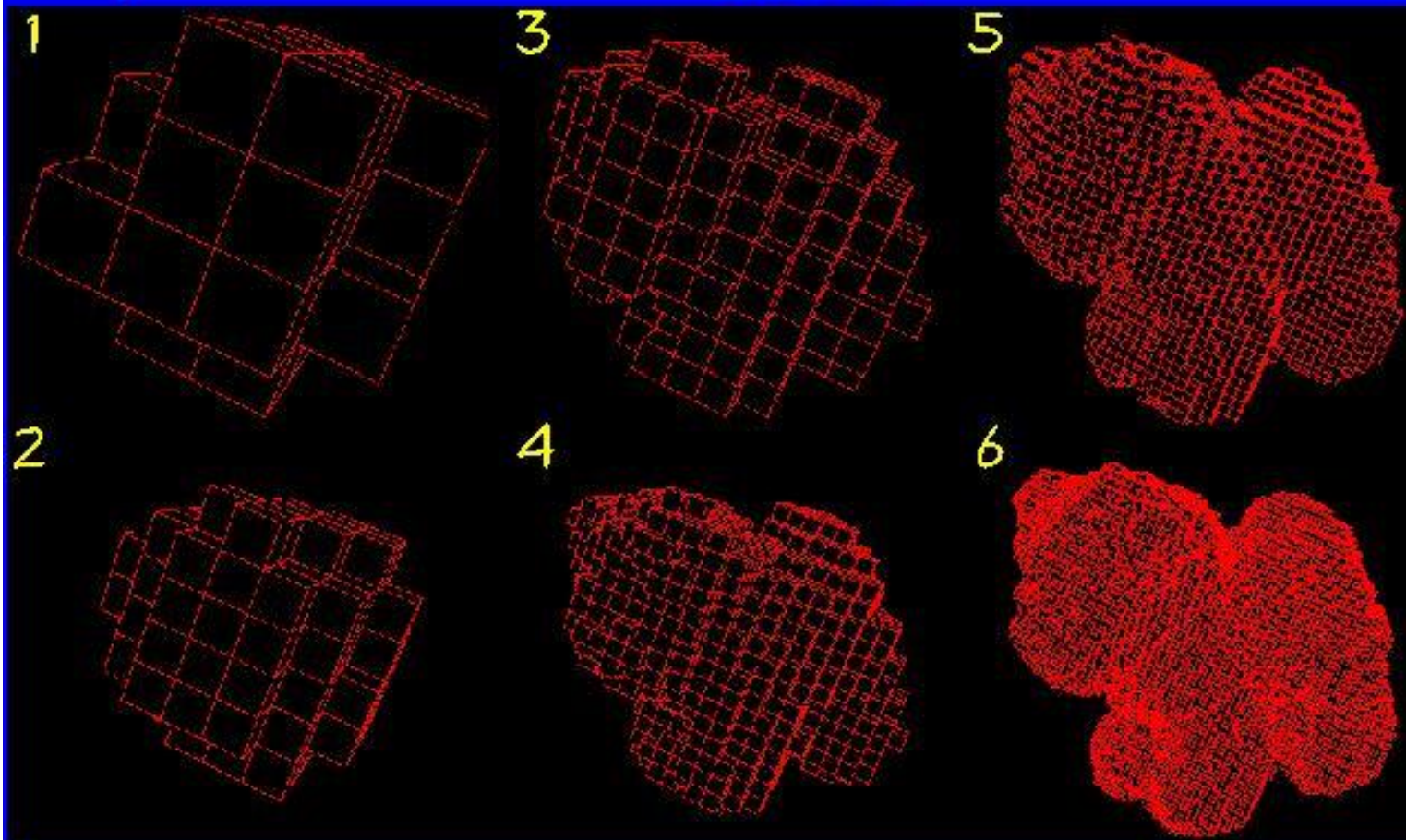
- cube's out => done
- cube's in => done
- else => recurse



# The rest of the chair

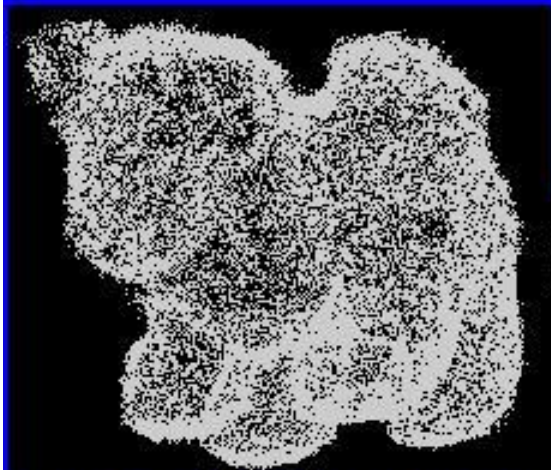


# Same for a husky pup

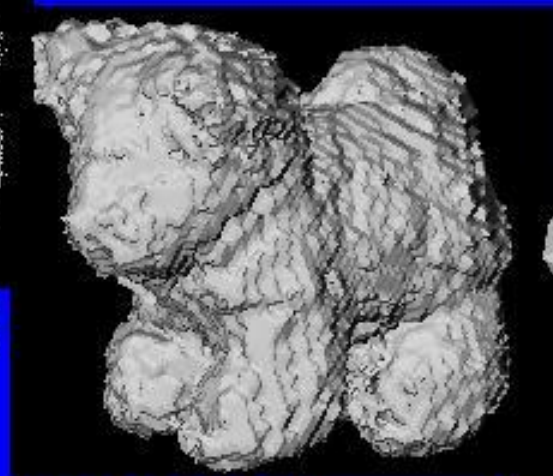


# Optimizing the dog mesh

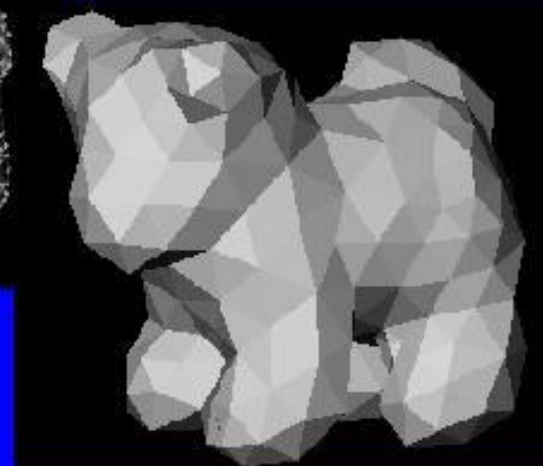
---



Registered points



Initial mesh



Optimized mesh

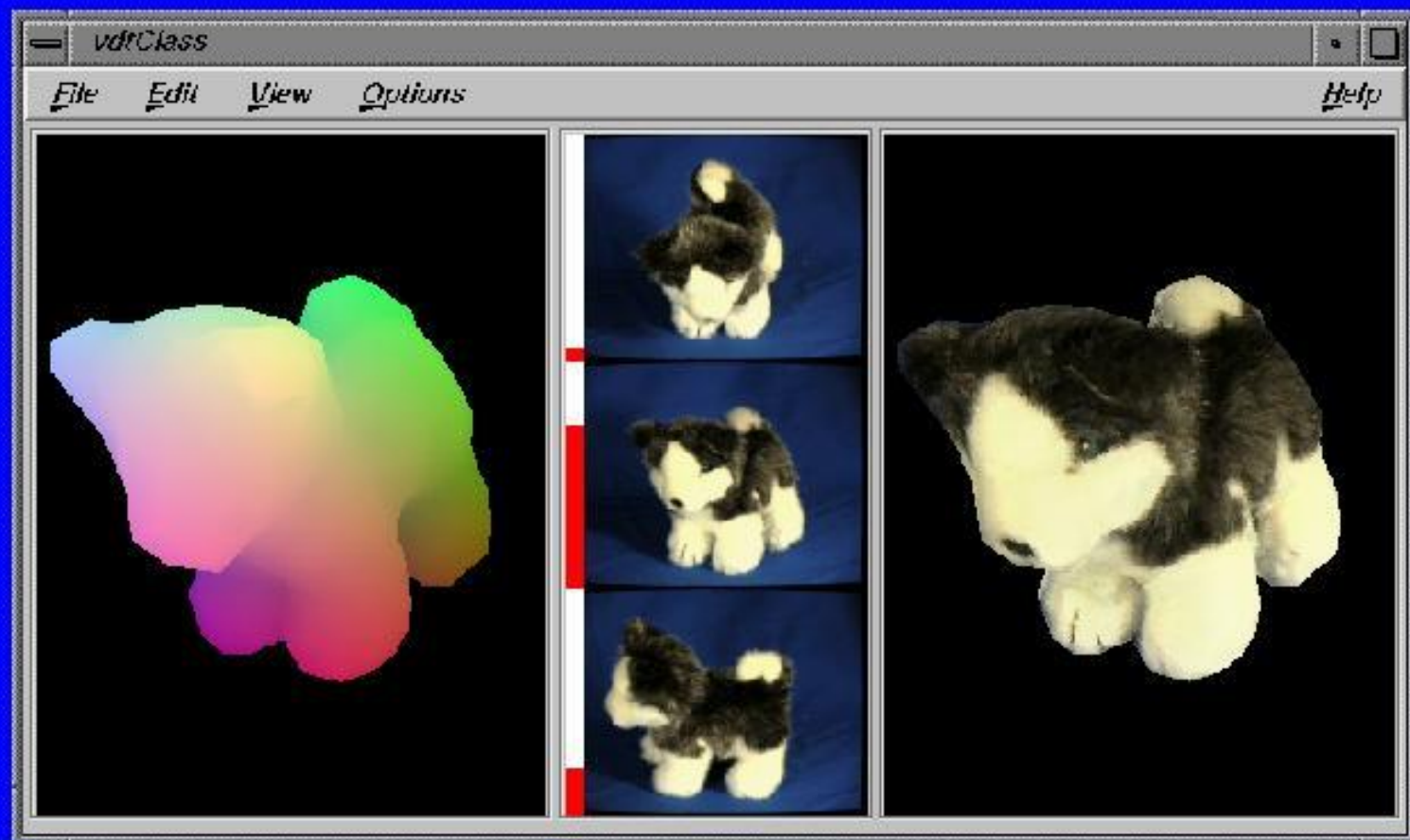


# View dependent texturing



# Our viewer

---



# More: Space Carving Results: African Violet

---



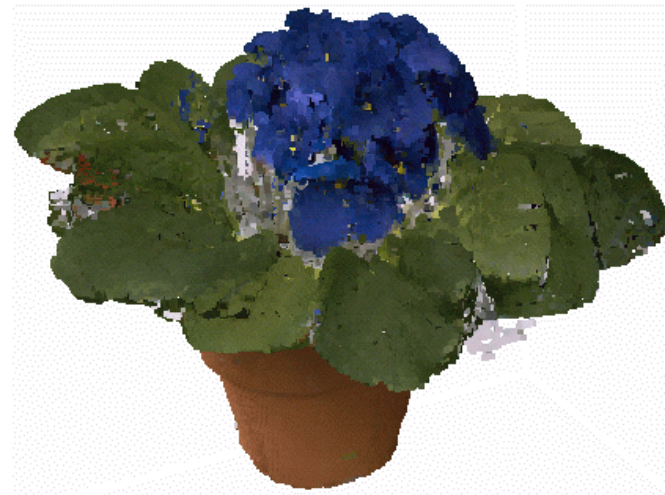
**Input Image (1 of 45)**



**Reconstruction**



**Reconstruction**



**Reconstruction**

# More: Space Carving Results: Hand

---



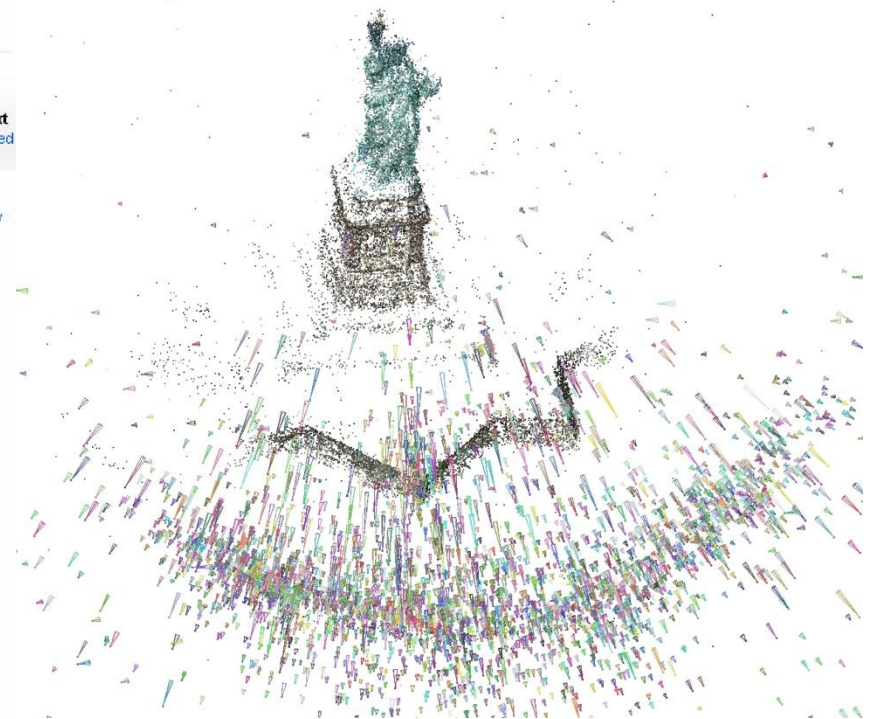
**Input Image  
(1 of 100)**

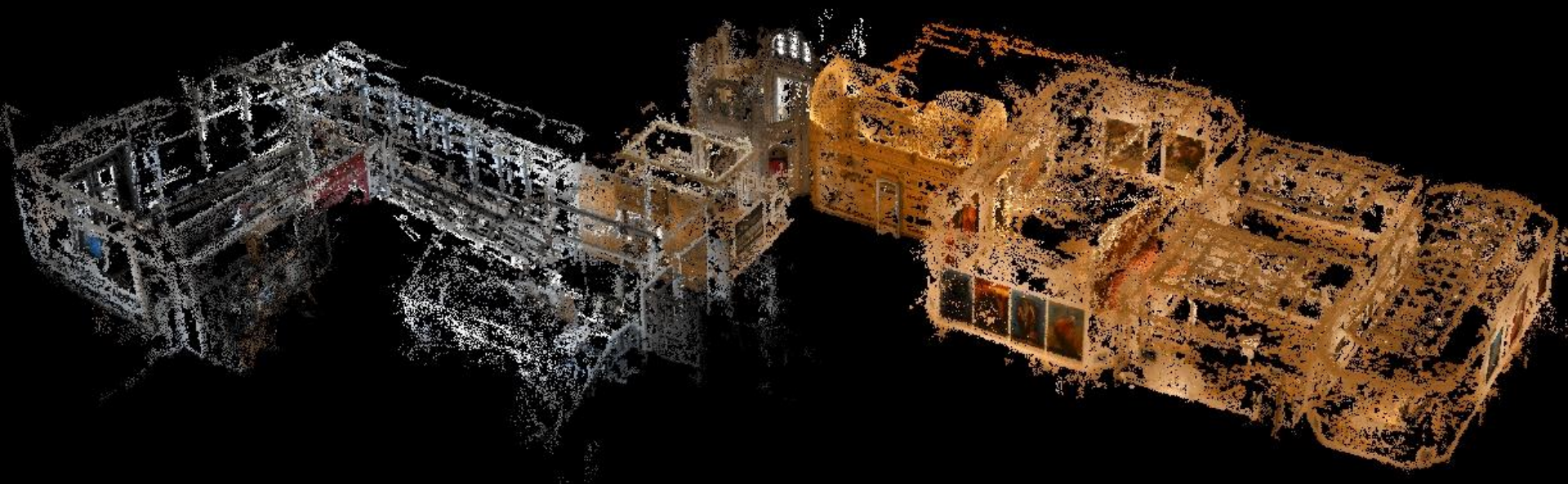


**Views of Reconstruction**

# Stereo from community photo collections

- Up to now, we've always assumed that camera calibration is known
- For photos taken from the Internet, we need *structure from motion* techniques to reconstruct both camera positions and 3D points. (SEE POSTED VIDEO)





# Head Reconstruction from Uncalibrated Internet Photos

Input: Internet photos in different poses and expressions



Output: 3D model of the head



work of  
Shu Liang

---

# Recognizing Deformable Shapes

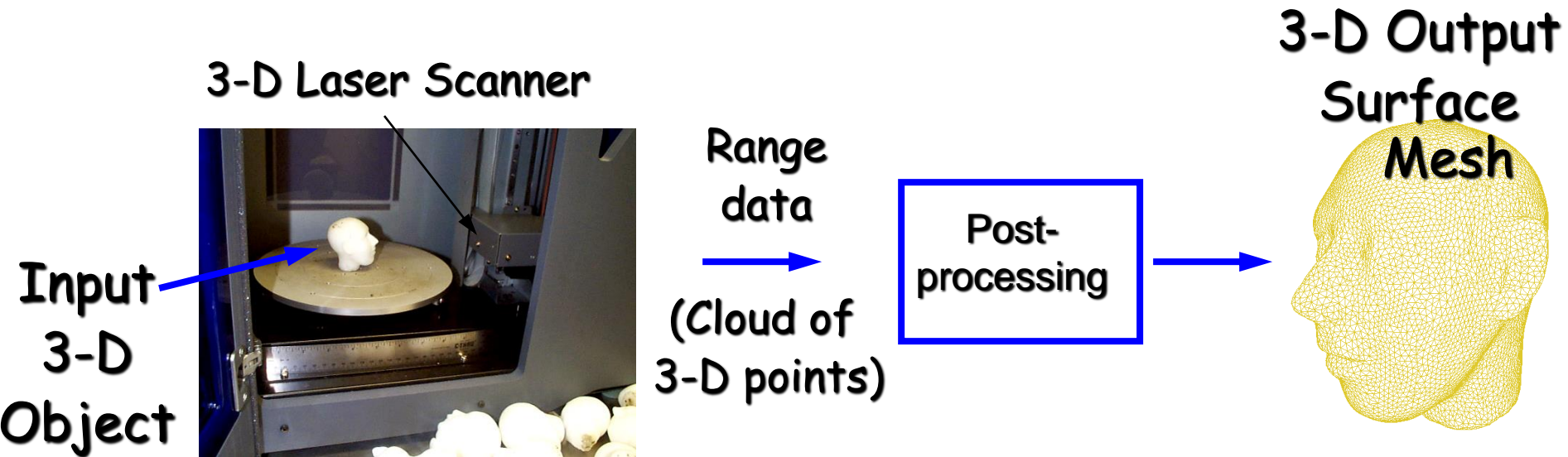
Salvador Ruiz Correa  
(CSE/EE576 Computer Vision I)



# Goal

---

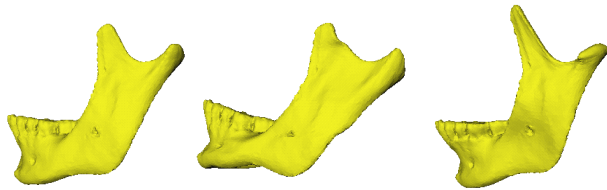
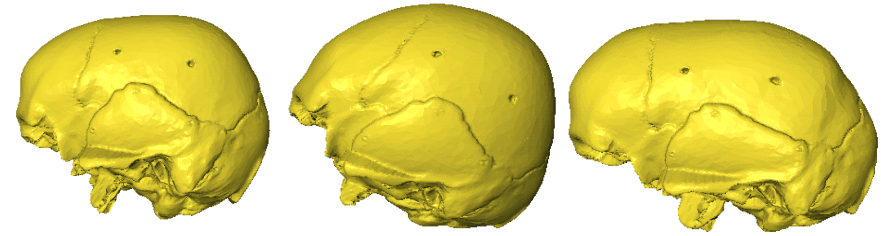
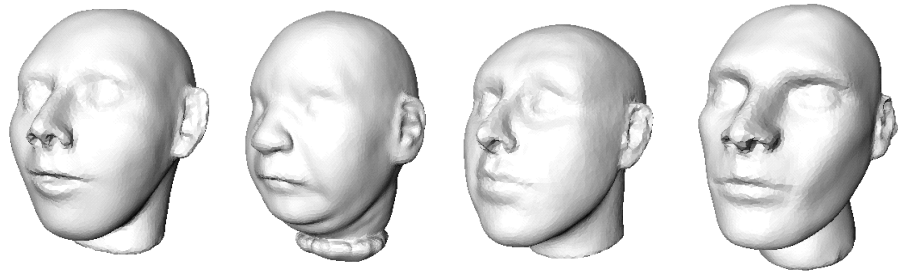
We are interested in developing algorithms for recognizing and classifying deformable object shapes from range data.



- This is a difficult problem that is relevant in several application fields.

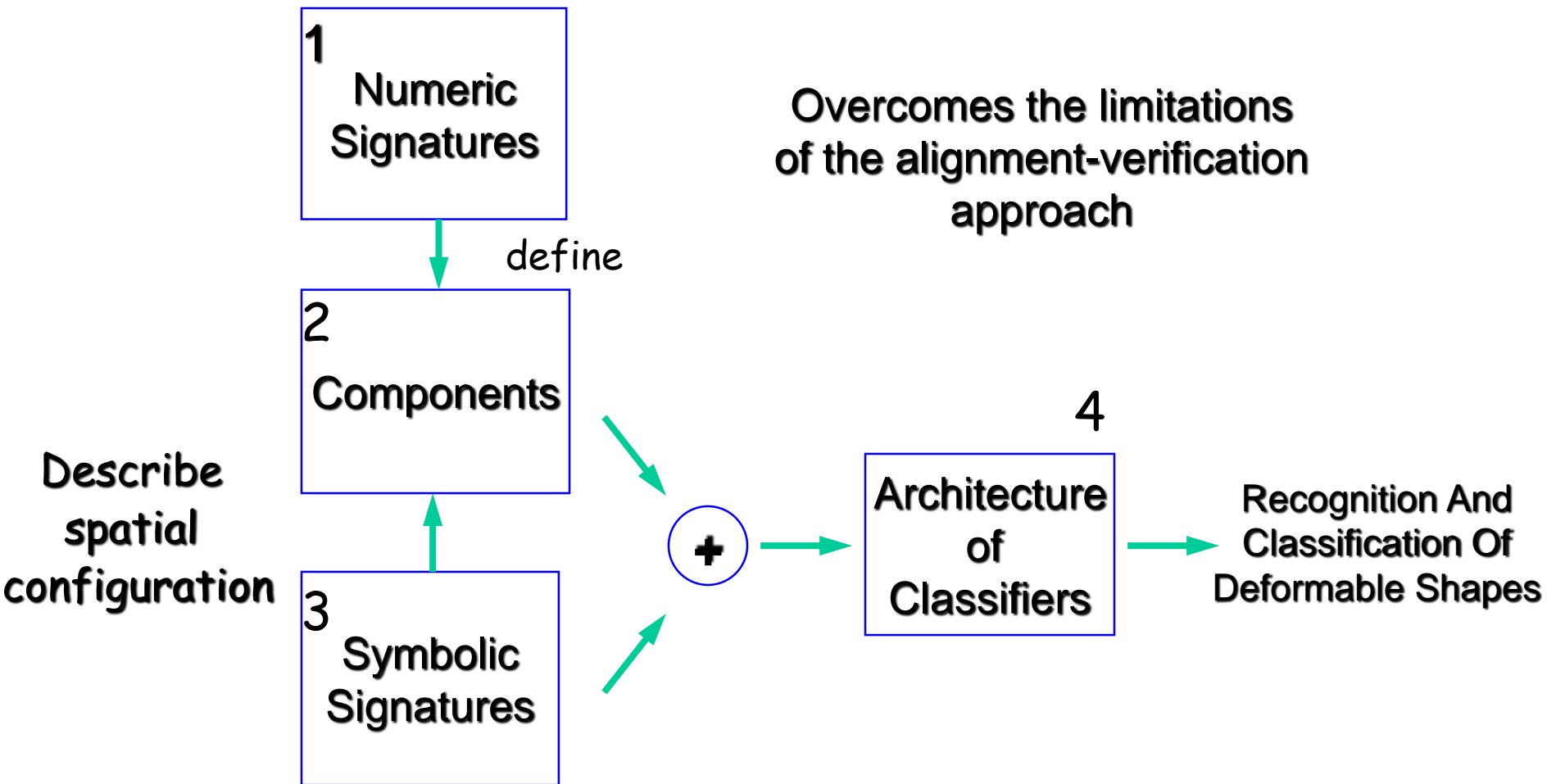
# What Kind Of Deformations?

---



# Component-Based Methodology

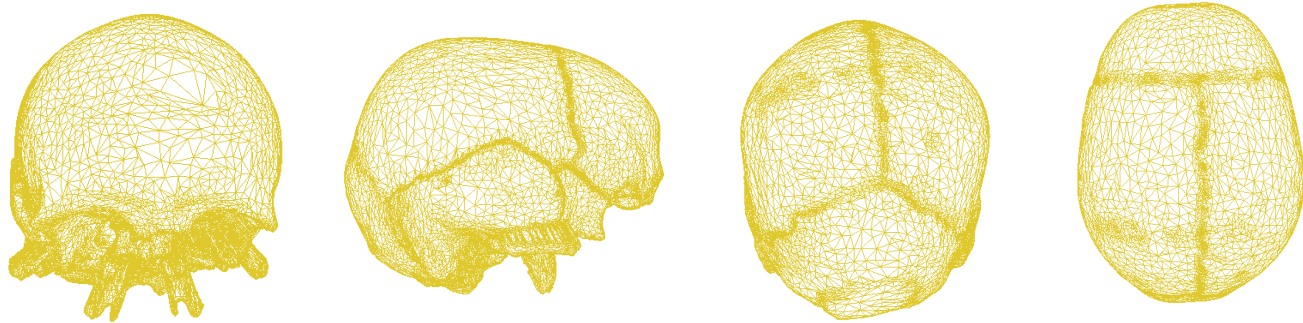
---



# Assumptions

---

All shapes are represented as oriented surface meshes of fixed resolution.

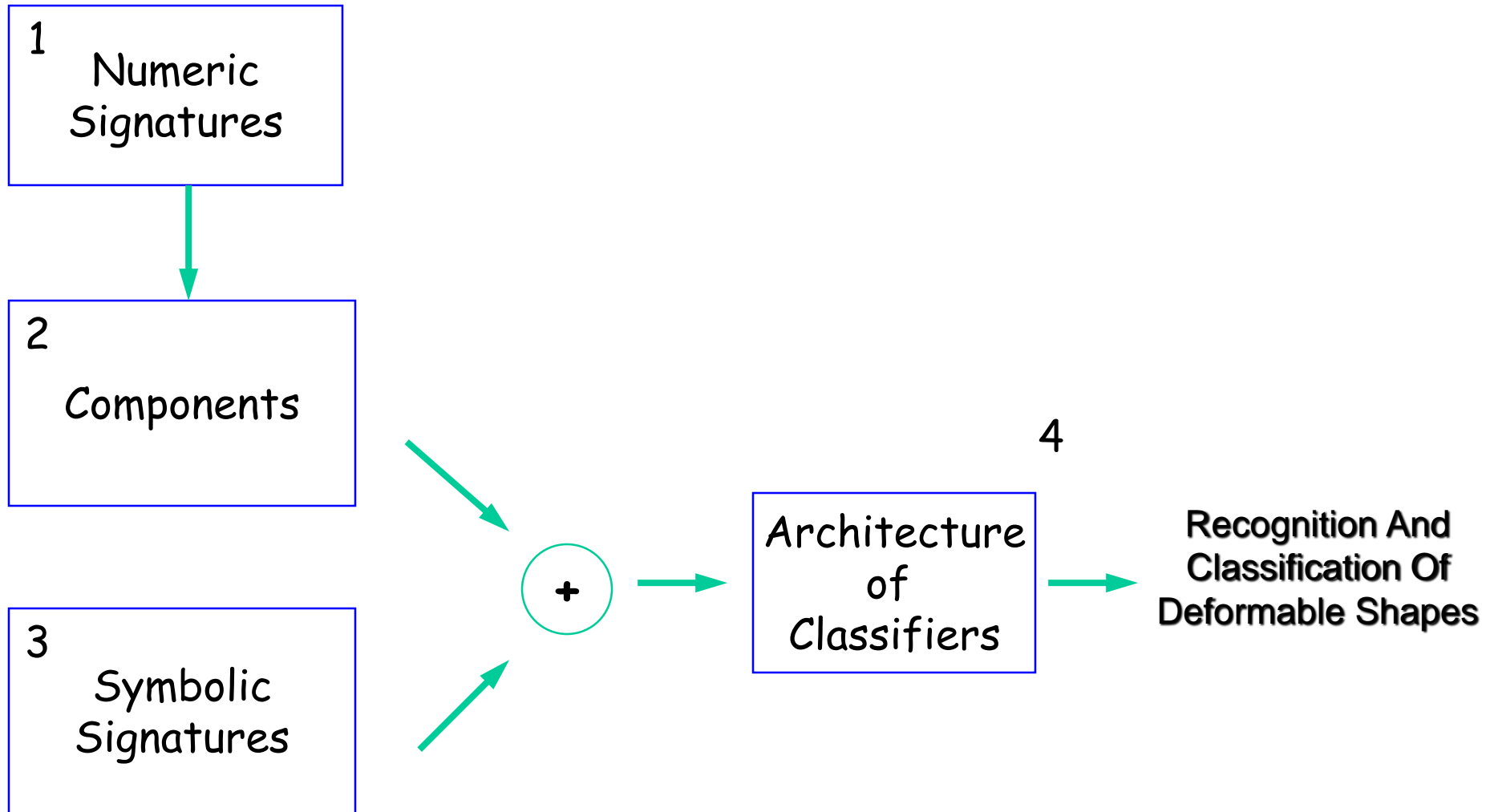


The **vertices** of the meshes in the **training set** are in full correspondence.

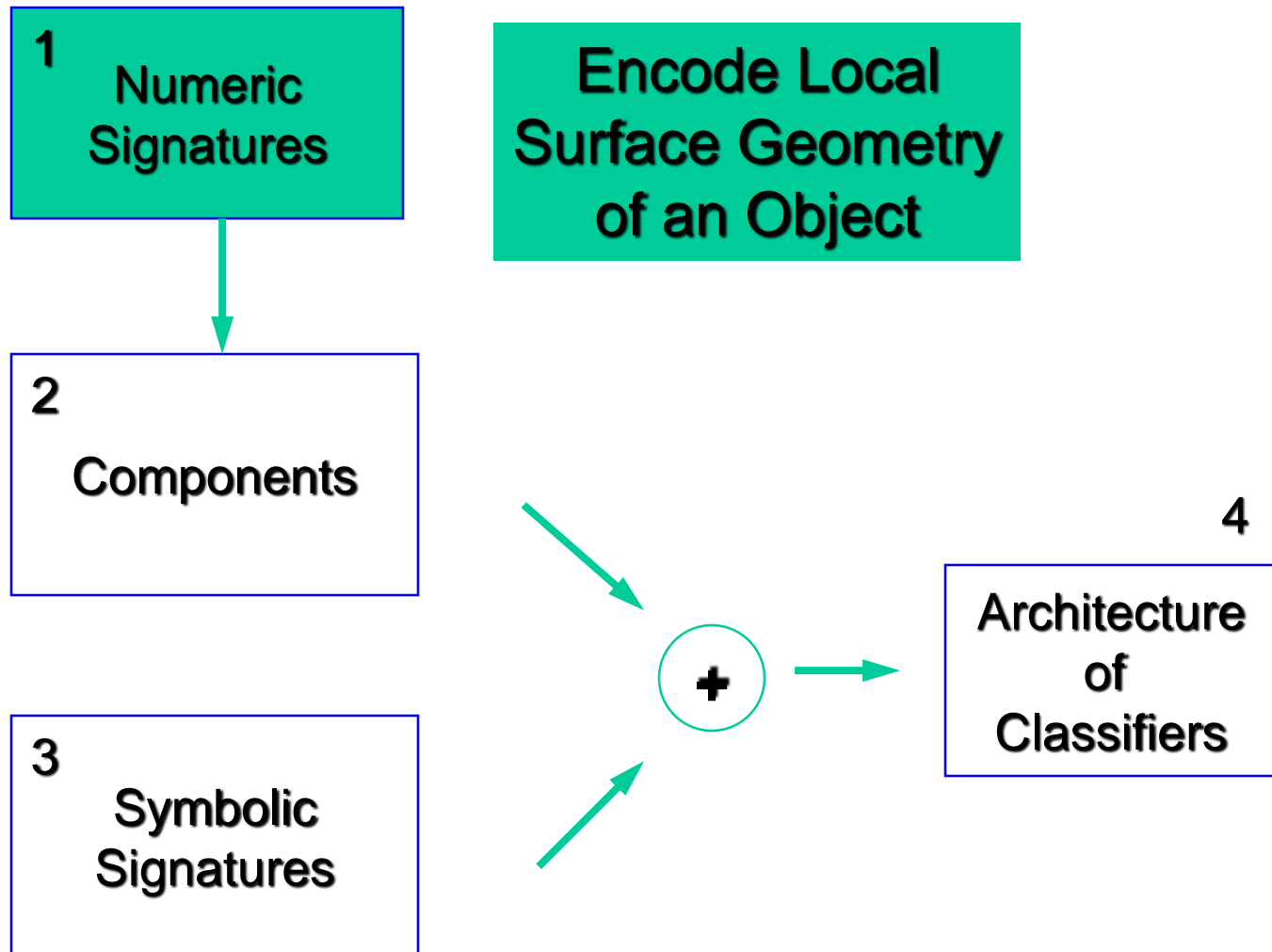
Finding full correspondences : hard problem yes ... but it is approachable ( use **morphable models technique**: Blantz and Vetter, SIGGRAPH 99; C. R. Shelton, IJCV, 2000; Allen et al., SIGGRAPH 2003).

# Four Key Elements To Our Approach

---



# Numeric Signatures

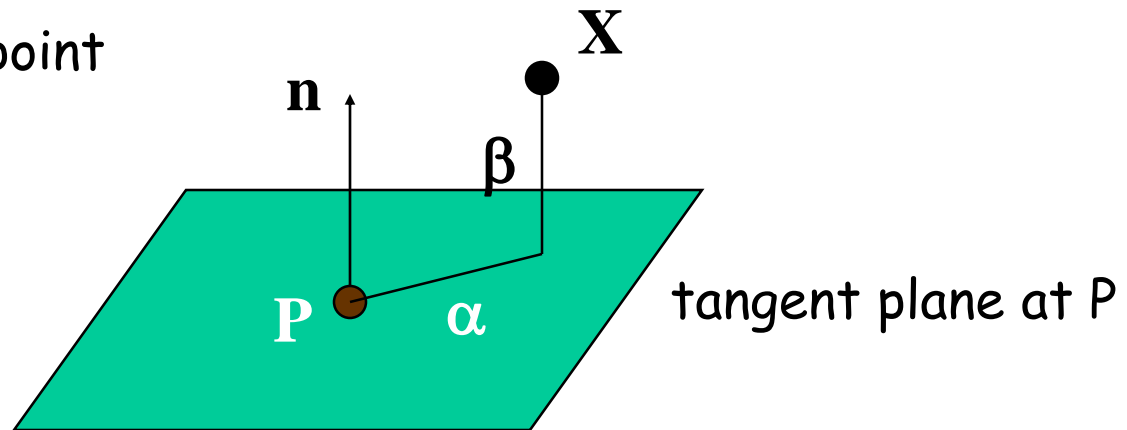


# The Spin Image Signature

---

$P$  is the selected vertex.

$X$  is a contributing point of the mesh.



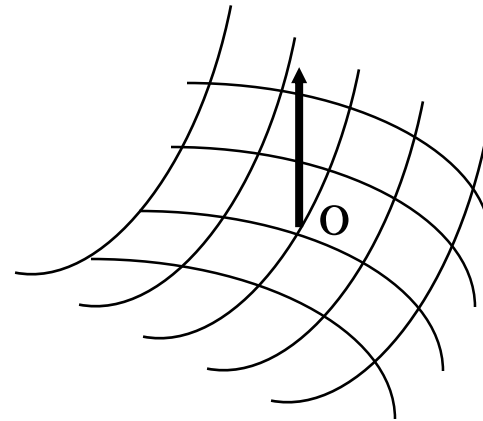
$\alpha$  is the perpendicular distance from  $X$  to  $P$ 's surface normal.

$\beta$  is the signed perpendicular distance from  $X$  to  $P$ 's tangent plane.

# Spin Image Construction

---

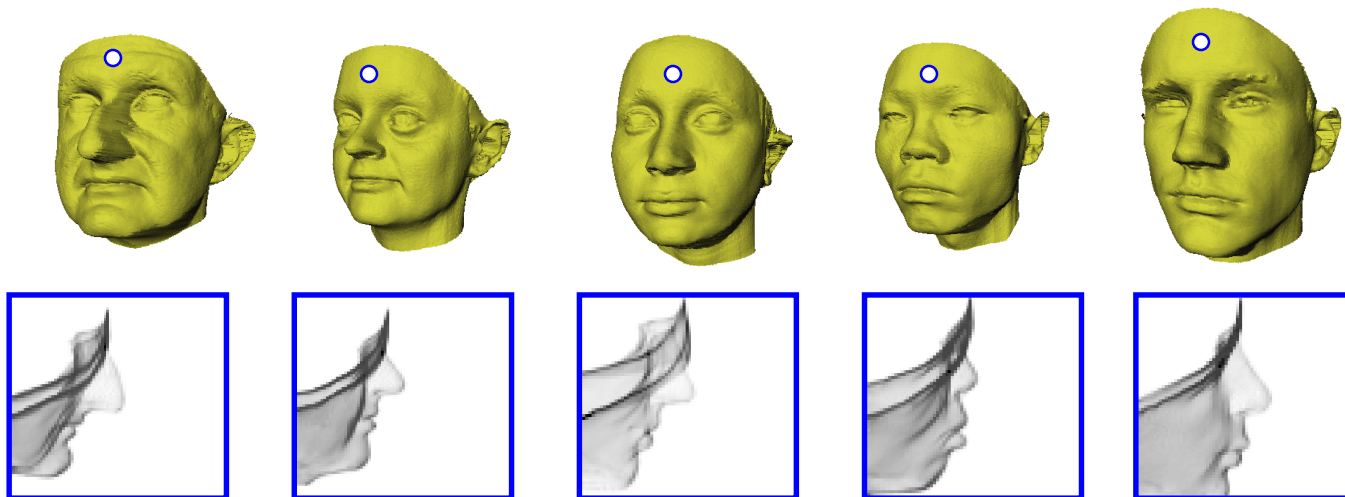
- A spin image is constructed
  - about a specified oriented point  $o$  of the object surface
  - with respect to a set of contributing points  $C$ , which is controlled by maximum distance and angle from  $o$ .
- It is stored as an array of accumulators  $S(\alpha, \beta)$  computed via:
- For each point  $c$  in  $C(o)$ 
  1. compute  $\alpha$  and  $\beta$  for  $c$ .
  2. increment  $S(\alpha, \beta)$





# Numeric Signatures: Spin Images

---



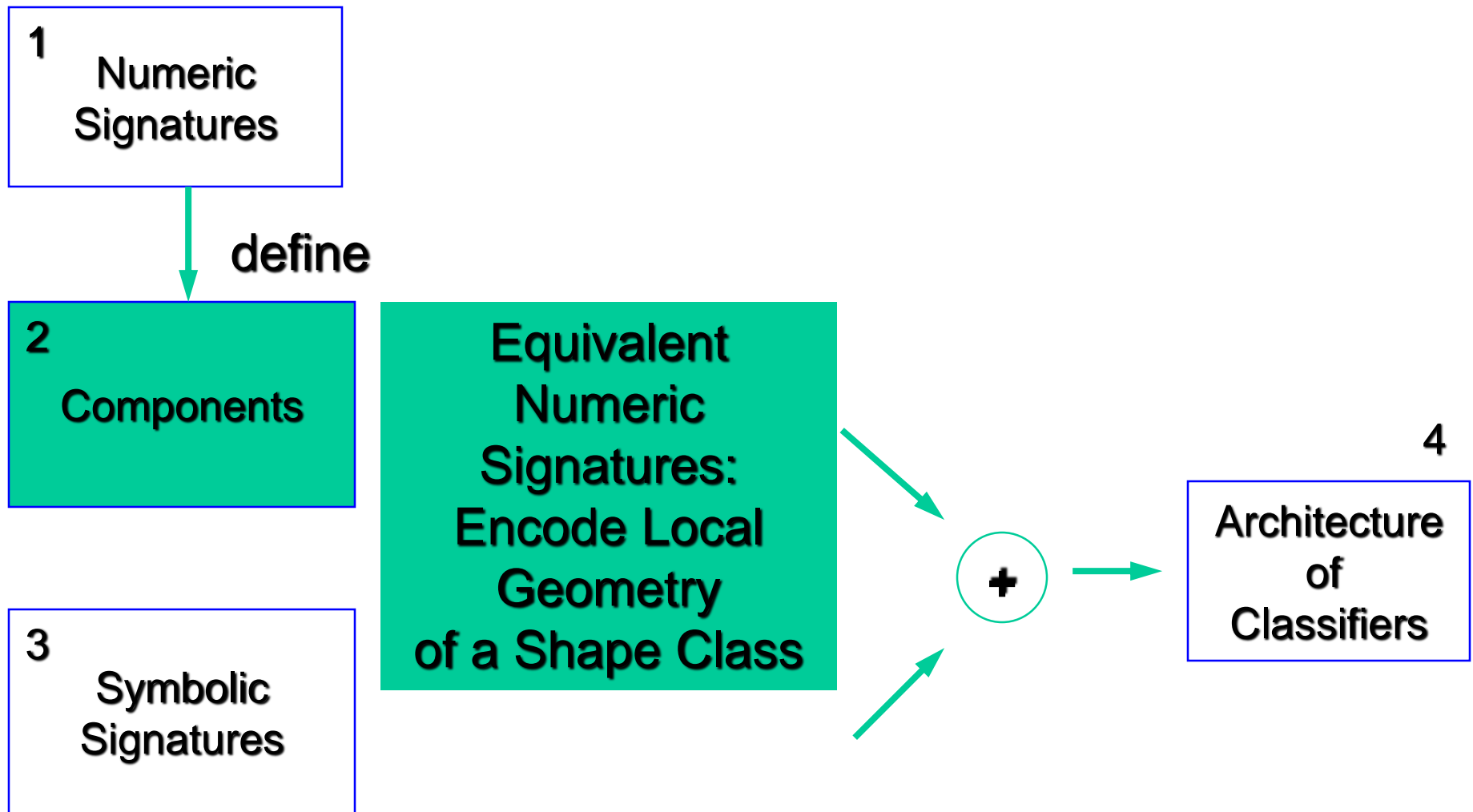
Rich set of surface shape descriptors.

Their spatial scale can be modified to include local and non-local surface features.

Representation is robust to scene clutter and occlusions.

# Components

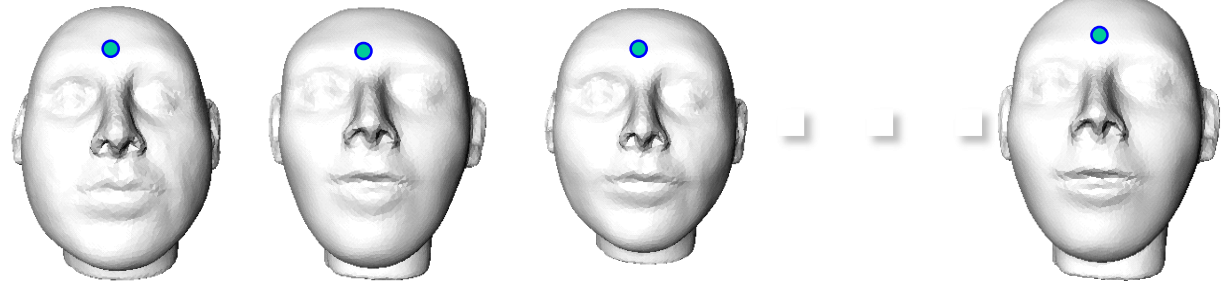
---



# How To Extract Shape Class Components?

Training Set

Select  
Seed  
Points



Compute  
Numeric  
Signatures



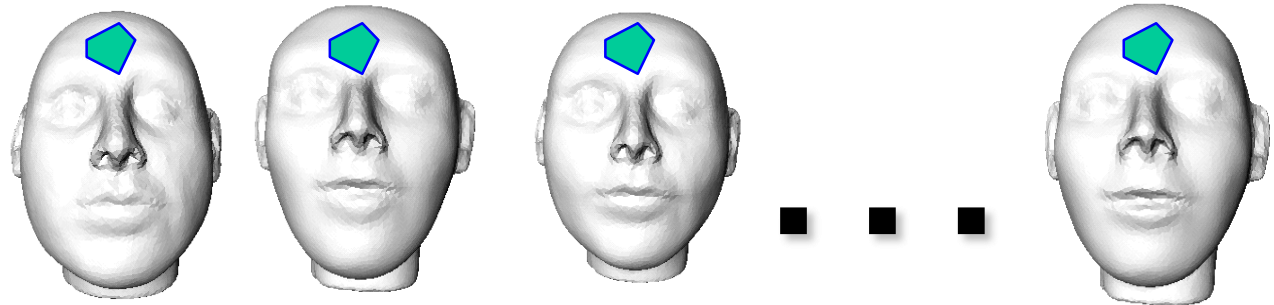
Region  
Growing  
Algorithm



Component  
Detector



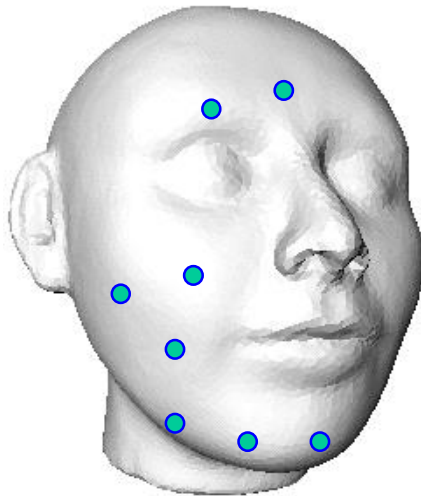
Grown components  
around seeds



# Component Extraction Example

---

Selected 8 seed points by hand

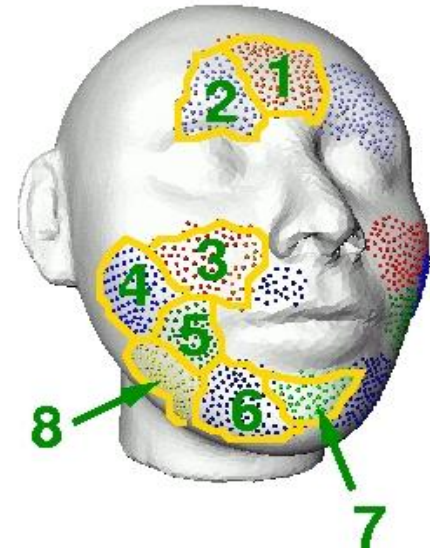


Grow one region at the time  
(get one detector  
per component)

Region  
Growing



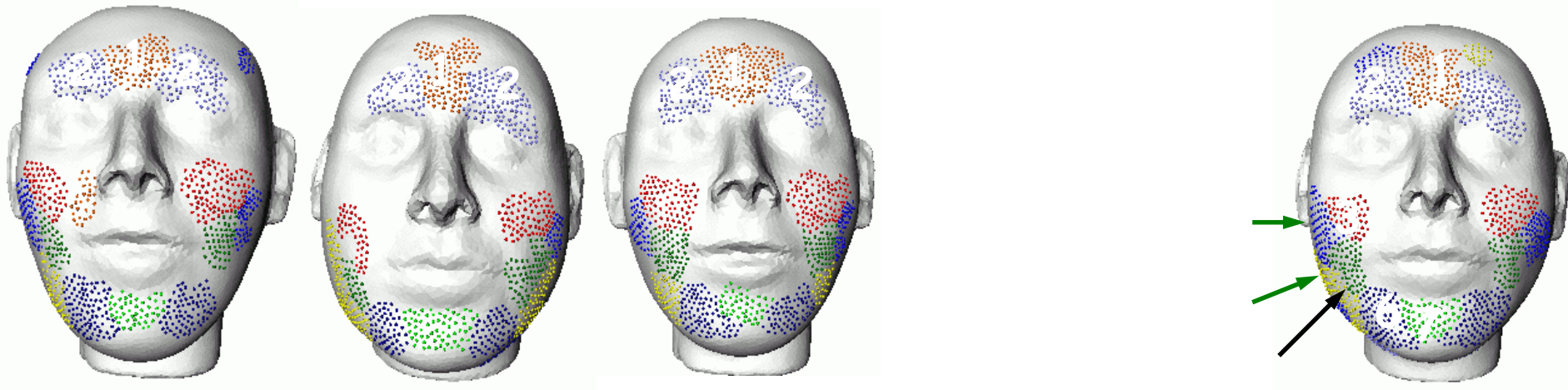
Labeled  
Surface Mesh



Detected  
components on a  
training sample

# How To Combine Component Information?

---



# Symbolic Signatures

---

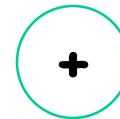
1  
Numeric  
Signatures



2  
Components

3  
Symbolic  
Signatures

Encode  
Geometrical  
Relationships  
Among  
Components

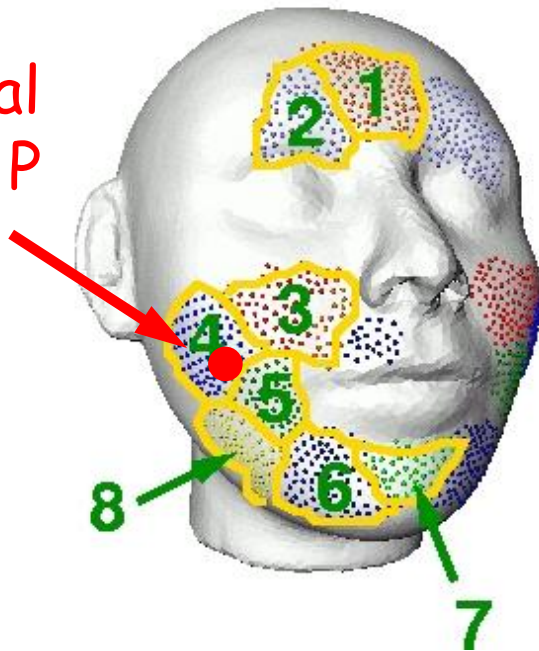


4  
Architecture  
of  
Classifiers

# Symbolic Signature

Labeled  
Surface Mesh

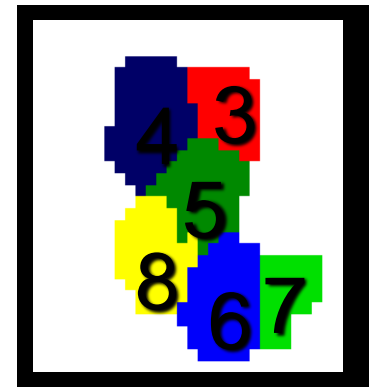
Critical  
Point P



Encode  
Geometric  
Configuration



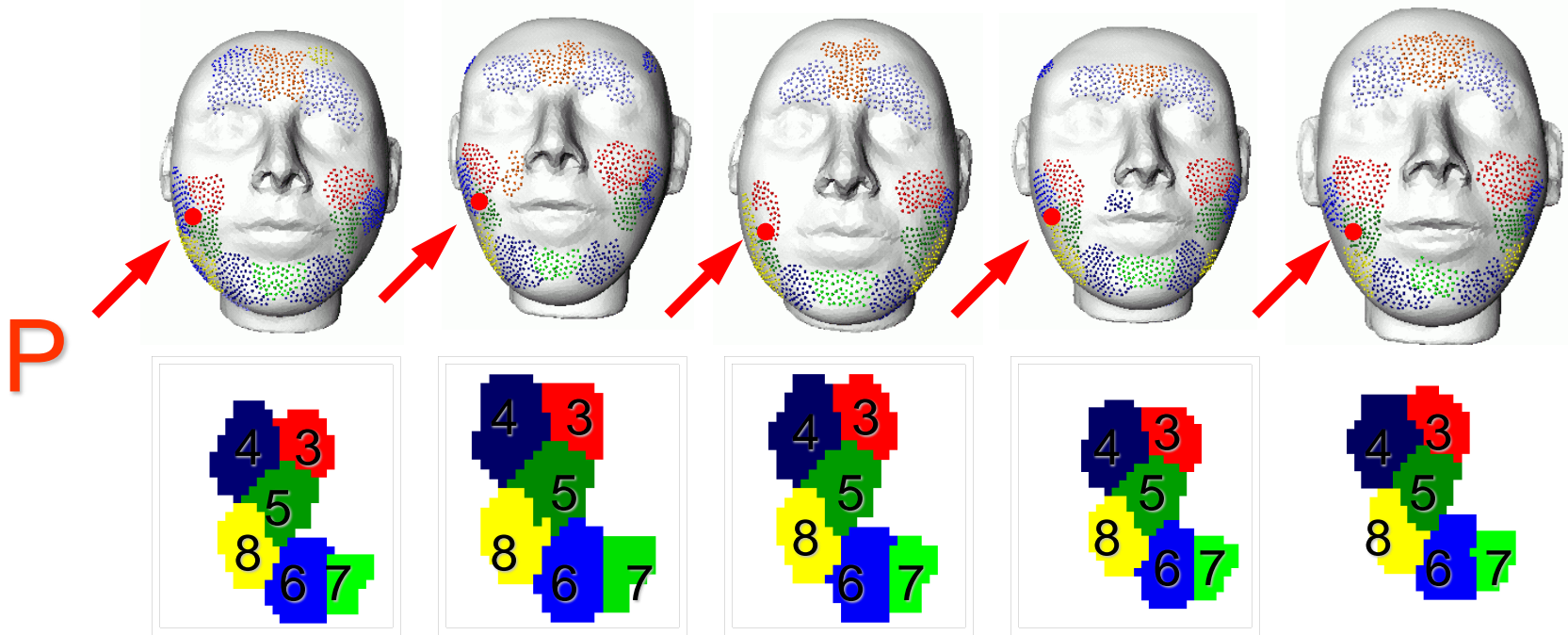
Symbolic  
Signature at P



Matrix storing  
component  
labels

# Symbolic Signatures Are Robust To Deformations

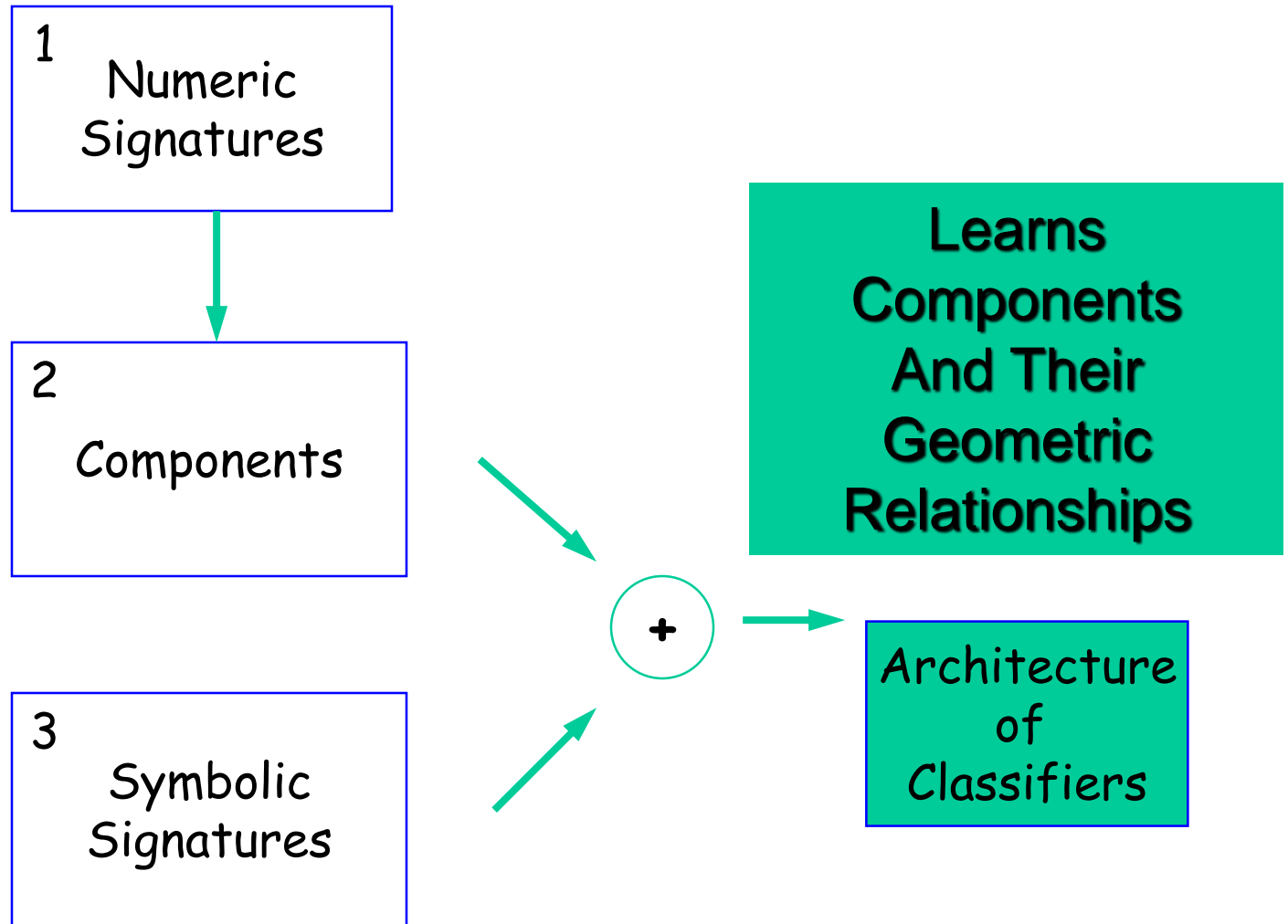
---



*Relative position of components is stable across deformations:  
experimental evidence*

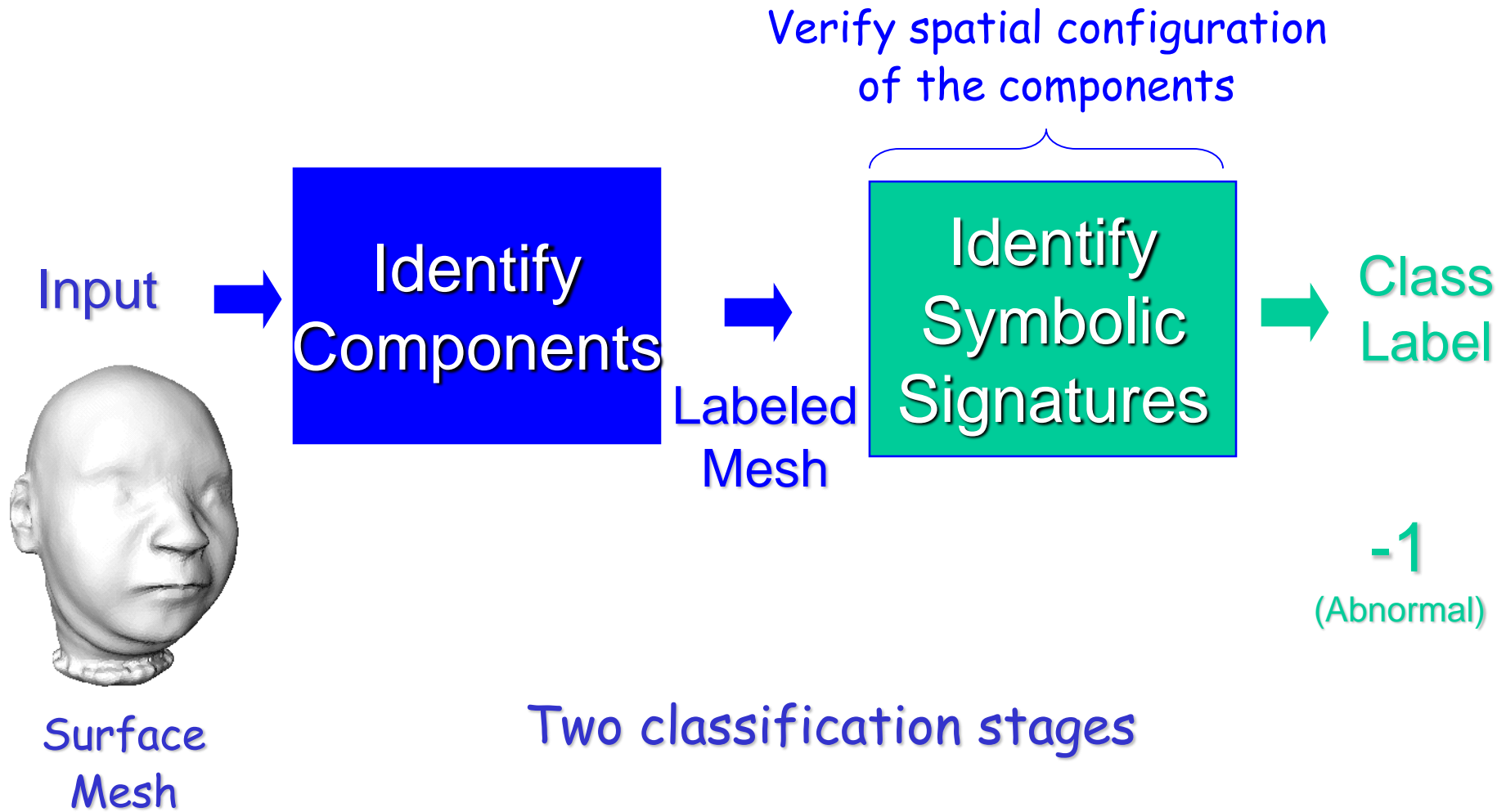


# Architecture of Classifiers



# Proposed Architecture

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# Architecture Implementation

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ALL our classifiers are (off-the-shelf)  $\nu$ -Support Vector Machines ( $\nu$ -SVMs) (Schölkopf et al., 2000 and 2001).

Component (and symbolic signature) detectors are **one-class classifiers**.

Component label assignment: performed with a **multi-way classifier** that uses **pairwise classification scheme**.

**Gaussian kernel**.

# Experimental Validation

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Recognition Tasks: 4 (T1 - T4)  
Classification Tasks: 3 (T5 - T7)  
No. Experiments: 5470

Rotary Table



Recognition

Setup

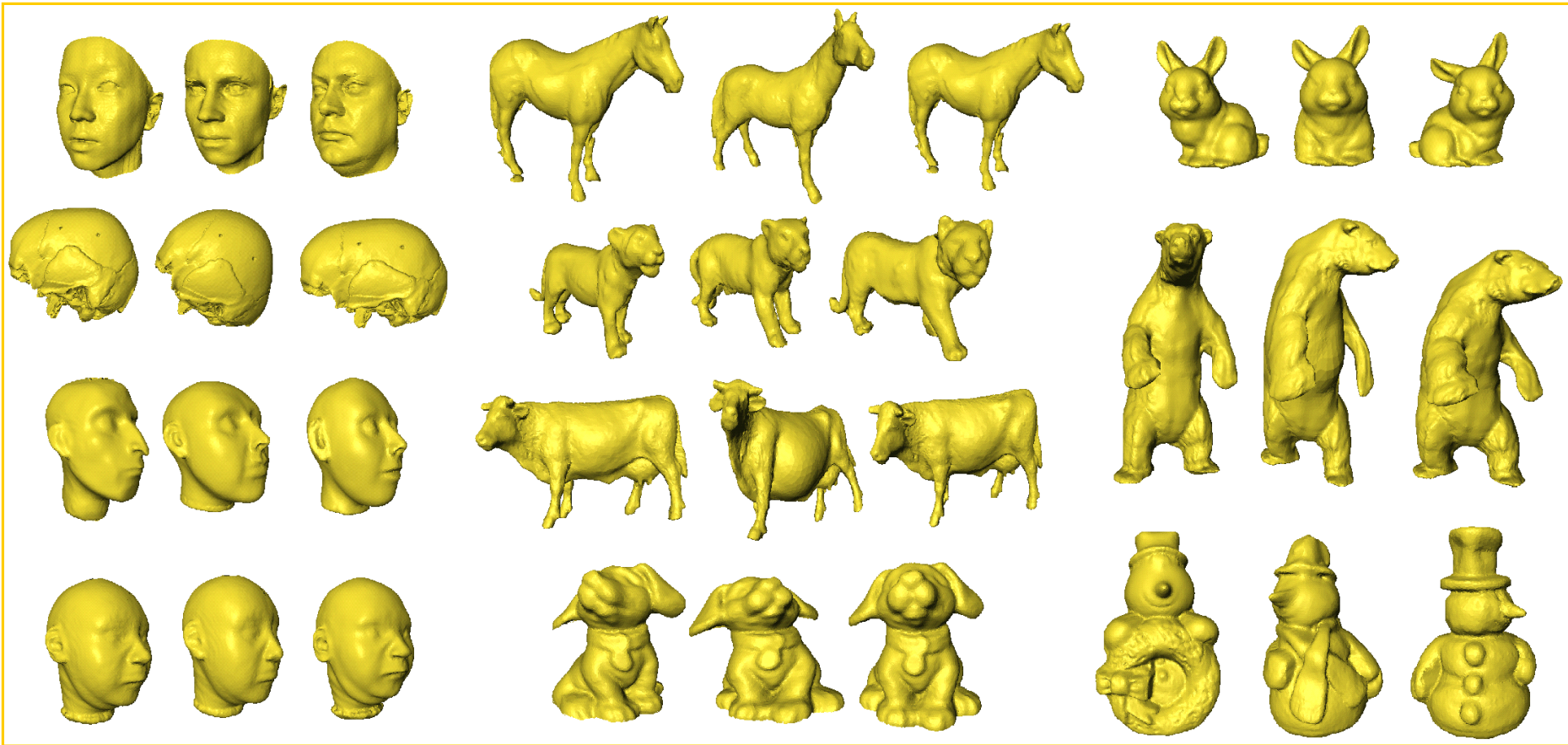


Laser

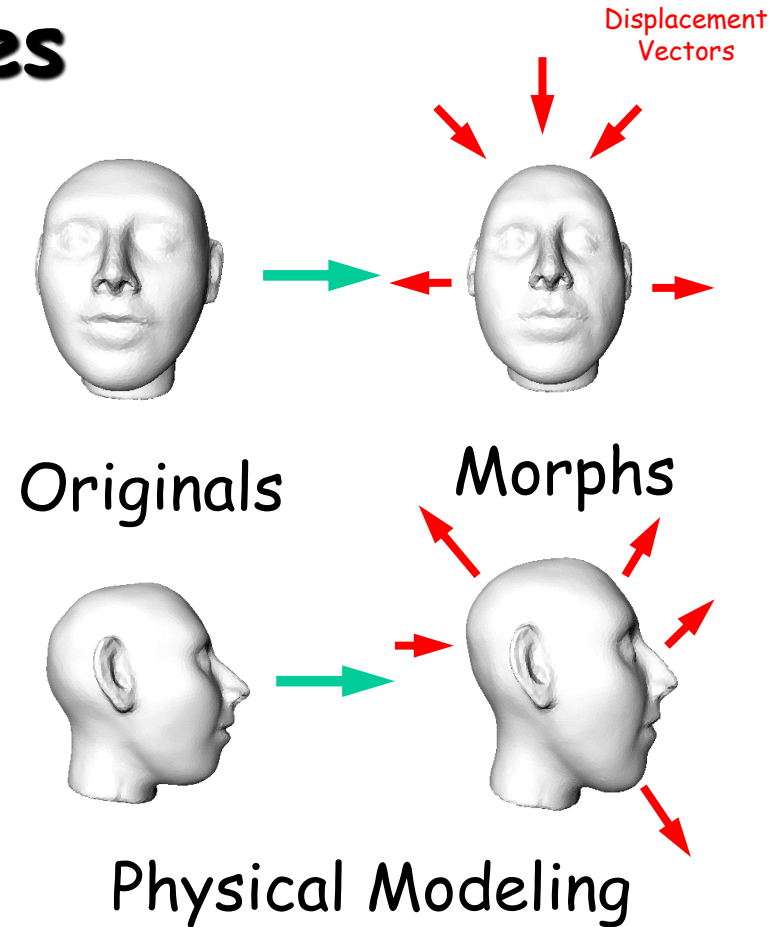
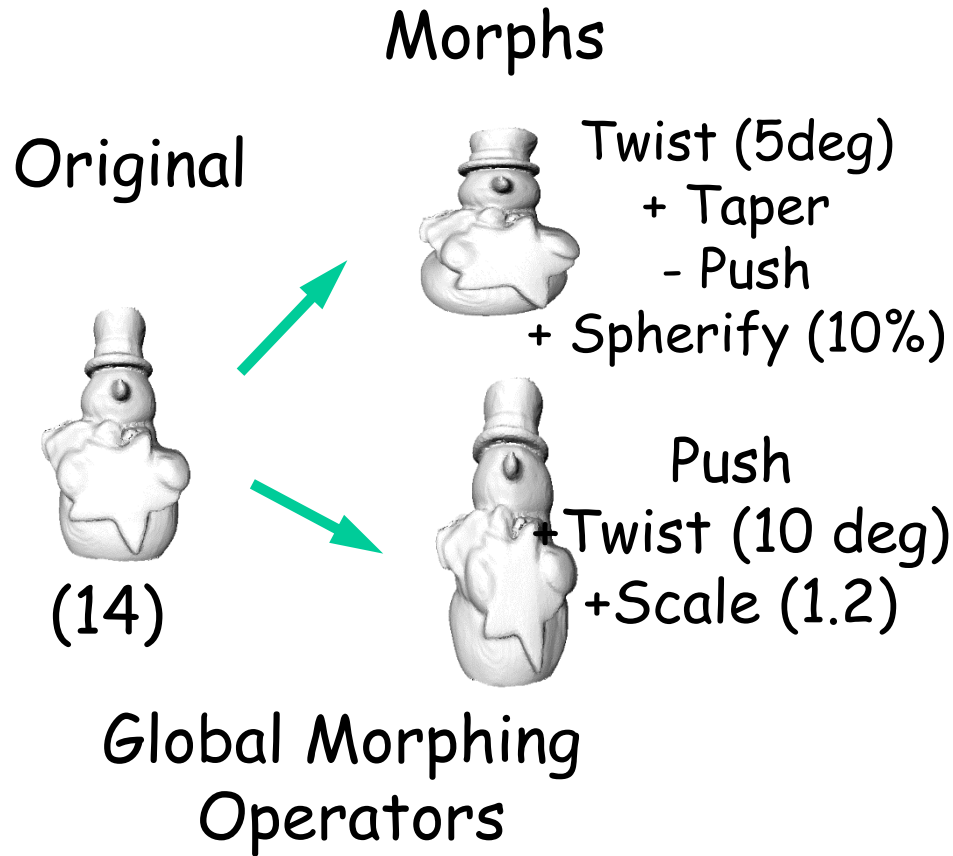
Classification

# Shape Classes

---



# Enlarging Training Sets Using Virtual Samples



# Task 1: Recognizing Single Objects (1)

---

No. Shape classes: 9.

Training set size: 400 meshes.

Testing set size: 200 meshes.

No. Experiments: 1960.

No. Component detectors: 3.

No. Symbolic signature detectors: 1.

Numeric signature size: 40x40.

Symbolic signature size: 20x20.

No clutter and occlusion.

# Task 1: Recognizing Single Objects (2)

---

Snowman: 93%.

Rabbit: 92%.

Dog: 89%.

Cat: 85.5%.

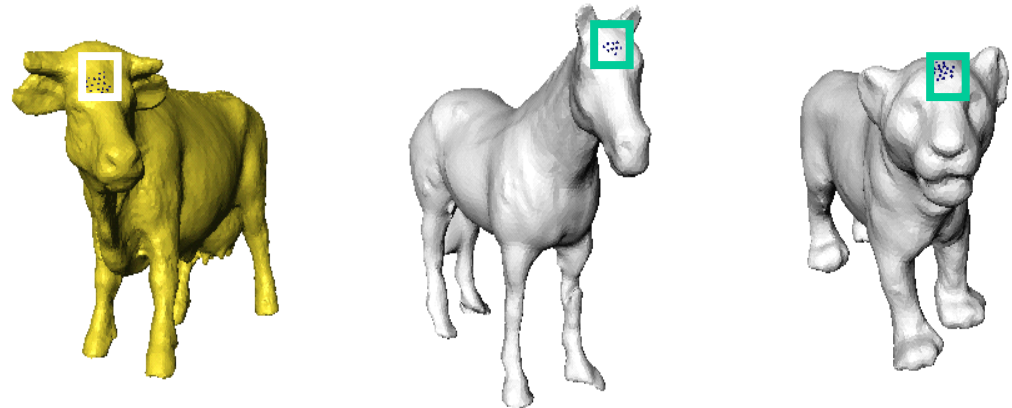
Cow: 92%.

Bear: 94%.

Horse: 92.7%.

Human head: 97.7%.

Human face: 76%.



**Recognition rates (true positives)**

(No clutter, no occlusion, complete models)



## Tasks 2-3: Recognition In Complex Scenes (1)

---

No. Shape classes: 3.

Training set size: 400 meshes.

Testing set size: 200 meshes.

No. Experiments: 1200.

No. Component detectors: 3.

No. Symbolic signature detectors: 1.

Numeric signature size: 40x40.

Symbolic signature size: 20x20.

T2 - low clutter and occlusion.

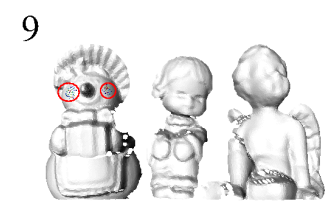
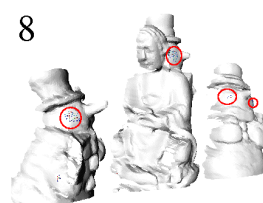
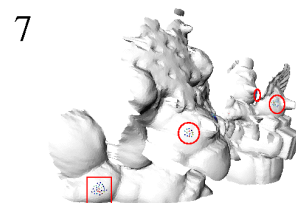
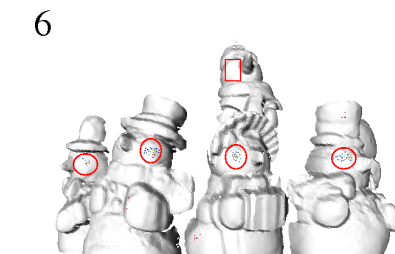
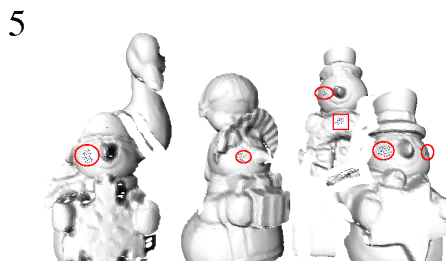
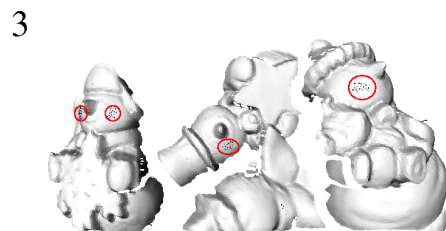
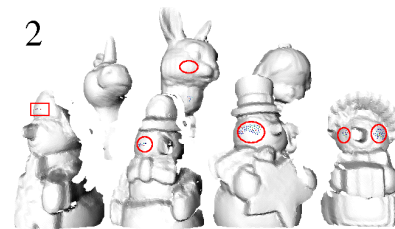
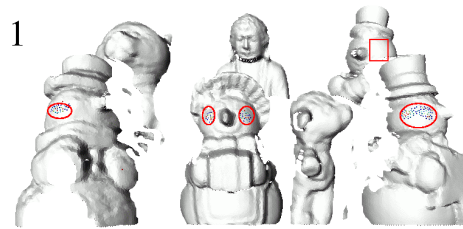
# Task 2-3: Recognition in Complex Scenes (2)

Shape Class	True Positives	False Positives	True Positives	False Positives
Snowmen	91%	31%	87.5%	28%
Rabbit	90.2%	27.6%	84.3%	24%
Dog	89.6%	34.6%	88.12%	22.1%

Task 2

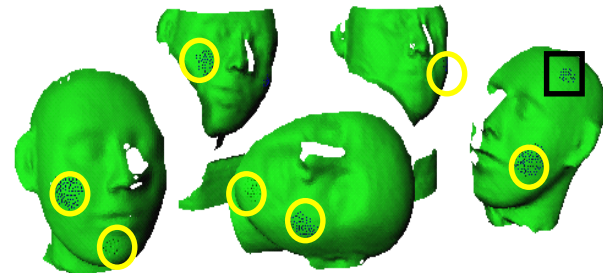
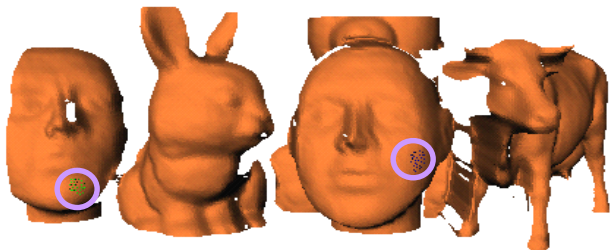
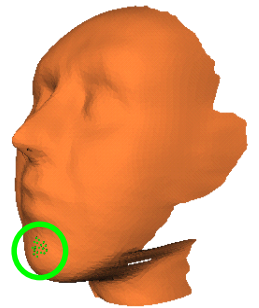
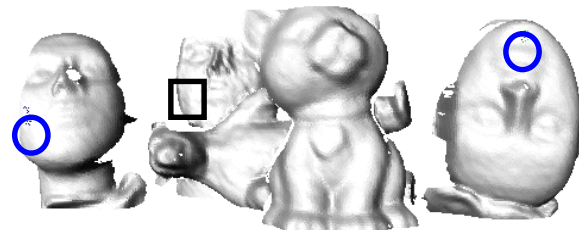
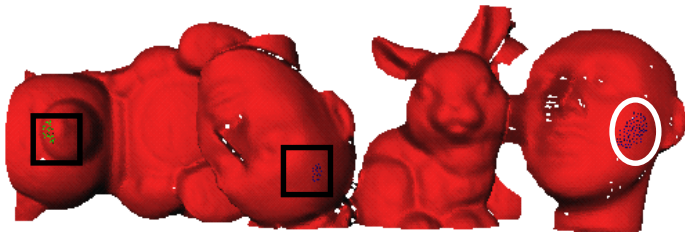
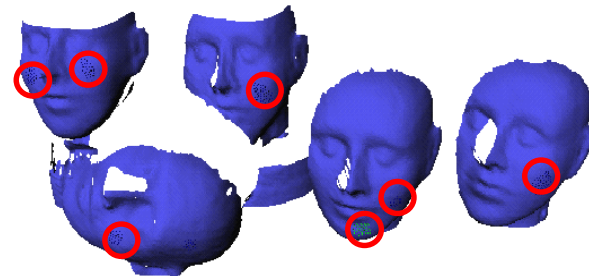
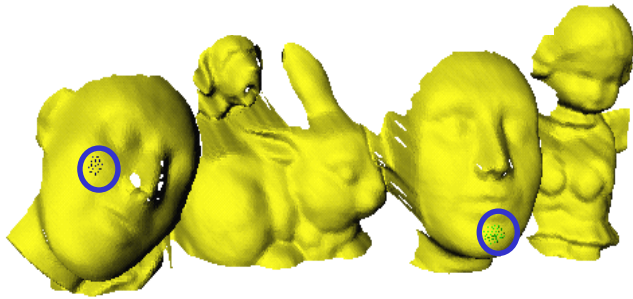
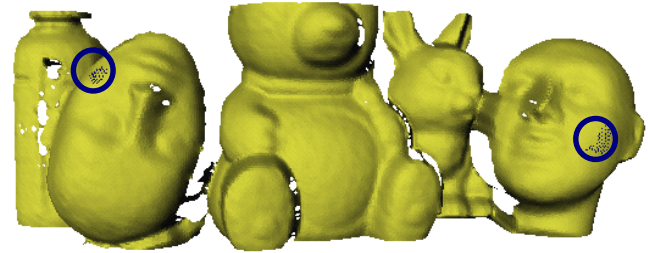
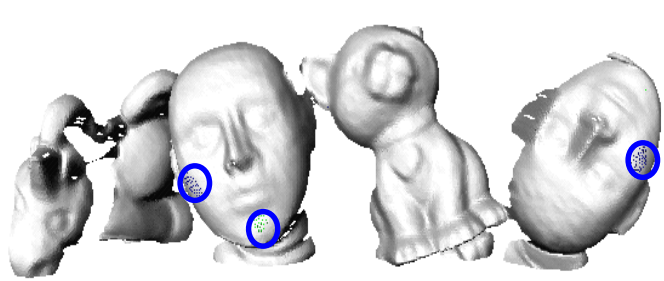
Task 3

# Task 2-3: Recognition in Complex Scenes (3)



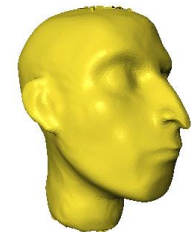
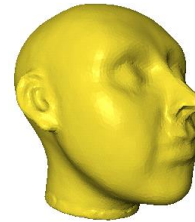
# Task 4: Recognizing Human Heads (3)

---



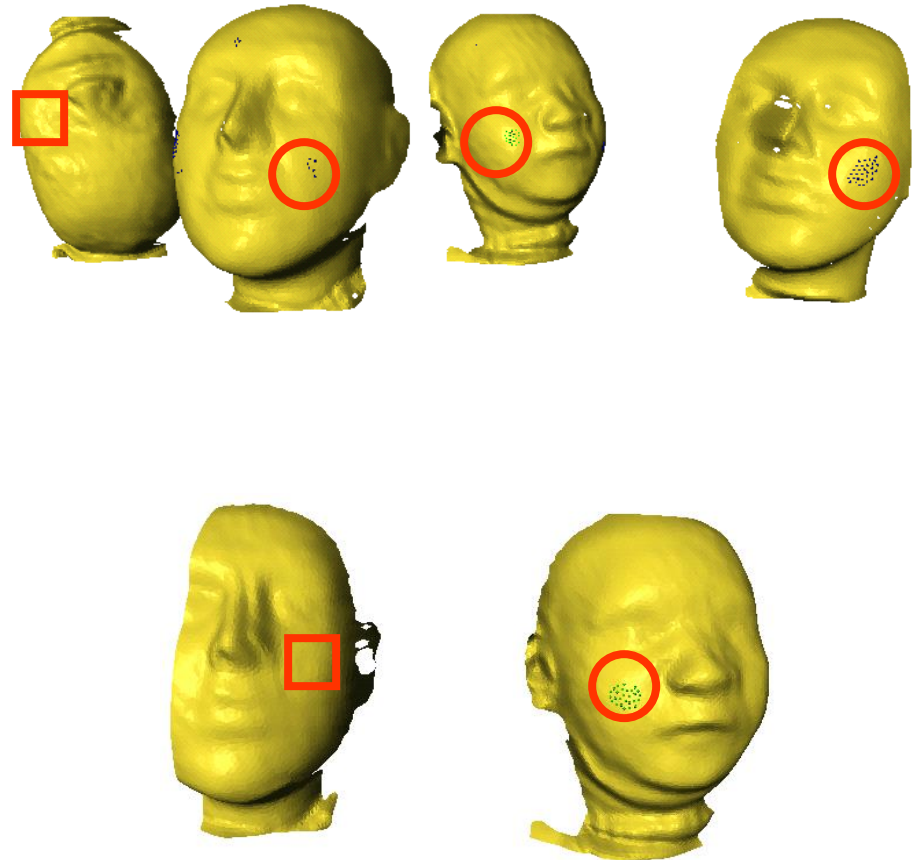
# Task 5: Classifying Normal vs. Abnormal Human Heads (1)

Shape Classes	Classification Accuracy %
Normal vs. Abnormal 1	98
Normal vs. Abnormal 2	100
Abnormal 1 vs. 3	98
Abnormal 1 vs. 4	97
Abnormal 1 vs. 5	92



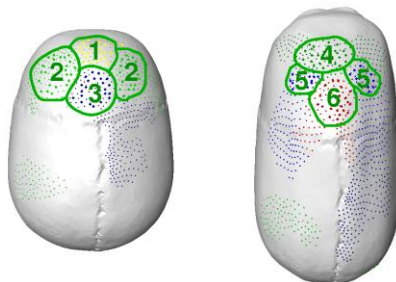
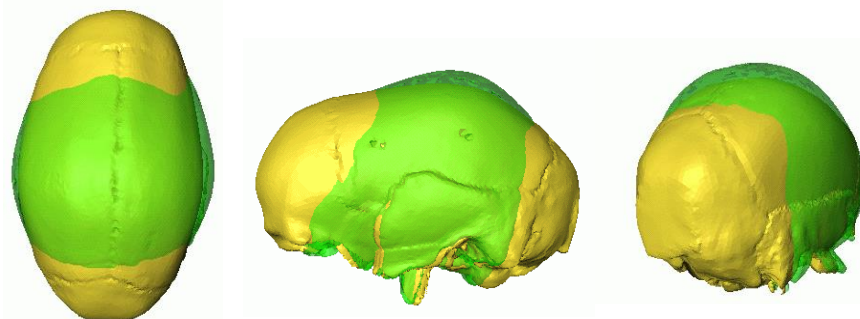
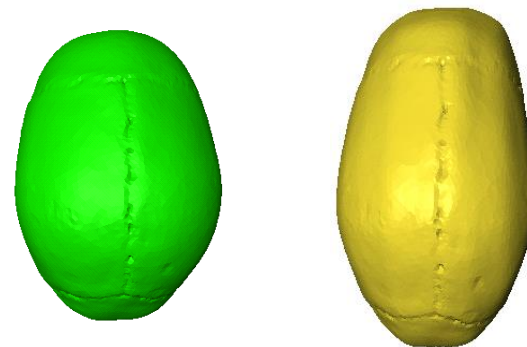
# Task 6: Classifying Normal vs. Abnormal Human Heads In Complex Scenes(1)

Shape Classes	Classification Accuracy %
Normal vs. Abnormal 1	88



# Task 7: Classifying Normal vs. Abnormal Neurocranium (2)

Shape Classes	Classification Accuracy %
Normal vs. Abnormal	89



# Main Contributions (1)

A novel **symbolic signature representation** of deformable shapes that is robust to intra-class variability and missing information, as opposed to a **numeric representation** which is often tied to a specific shape.

A novel **kernel function** for quantifying symbolic signature similarities.



# Main Contributions (2)

A **region growing** algorithm for learning shape class components.

A novel **architecture of classifiers** for abstracting the geometry of a shape class.

A validation of our methodology in a set of **large scale** recognition and classification experiments aimed at applications in scene analysis and medical diagnosis.