CSE P 501 – Compilers

Instruction Scheduling
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Agenda

- Instruction scheduling issues – latencies
- List scheduling

Credits: Adapted from slides by Keith Cooper, Rice University

Issues

- Many operations have non-zero latencies
- Modern machines can issue several operations per cycle
- Loads & Stores may or may not block
  ∴ may be slots after load/store for other useful work
- Branch costs vary
- Branches on modern processors typically have delay slots
- GOAL: Scheduler should reorder instructions to hide latencies and take advantage of delay slots

Some Idealized Latencies

Operation	Cycles
LOAD	3
STORE	3
ADD	1
MULT	2
SHIFT	1
BRANCH	0 TO 8

Example: w = w*2*x*y*z;

- Simple schedule

```
1  LOAD    r1 <- w
4  ADD     r1 <- r1,r1
5  LOAD    r2 <- x
8  MULT    r1 <- r1,r2
9  LOAD    r2 <- y
12 MULT    r1 <- r1,r2
13 LOAD    r2 <- z
16 MULT    r1 <- r1,r2
18 STORE w <- r1
21 r1 free
     2 registers, 20 cycles
```

- Loads early

```
1  LOAD    r1 <- w
2  LOAD    r2 <- x
3  LOAD    r3 <- y
4  ADD     r1 <- r1,r1
5  MULT    r1 <- r1,r2
6  LOAD    r2 <- z
7  MULT    r1 <- r1,r3
9  MULT    r1 <- r1,r2
11 STORE   w <- r1
14 r1 is free
     3 registers, 13 cycles
```


Instruction Scheduling

- Problem
  - Given a code fragment for some machine and latencies for each operation, reorder to minimize execution time
- Constraints
  - Produce correct code
  - Minimize wasted cycles
  - Avoid spilling registers
  - Do this efficiently

Precedence Graph

- Nodes *n* are operations
- Attributes of each node
  - type – kind of operation
  - delay – latency
- If node n2 uses the result of node n1, there is an edge e = (n1,n2) in the graph

Example Graph

- Code

```
a  LOAD    r1 <- w
b  ADD     r1 <- r1,r1
c  LOAD    r2 <- x
d  MULT    r1 <- r1,r2
e  LOAD    r2 <- y
f  MULT    r1 <- r1,r2
g  LOAD    r2 <- z
h  MULT    r1 <- r1,r2
i  STORE   w <- r1
```


Schedules (1)

- A correct schedule *S* maps each node n into a non-negative integer representing its cycle number, and
  - *S* (*n*) >= 0 for all nodes *n* (obvious)
  - If (n1,n2) is an edge, then S(n1)+delay(n1) <= S(n2)
  - For each type *t* there are no more operations of type *t* in any cycle than the target machine can issue

Schedules (2)

- The *length* of a schedule S, denoted L(S) is

  $$L(S) = \max_n (S(n) + \text{delay}(n))$$

- The goal is to find the shortest possible correct schedule
  - Other possible goals: minimize use of registers, power, space, ...

Constraints

- Main points
  - All operands must be available
  - Multiple operations can be ready at any given point
  - Moving operations can lengthen register lifetimes
  - Moving uses near definitions can shorten register lifetimes
  - Operations can have multiple predecessors
- Collectively this makes scheduling NP-complete
- Local scheduling is the simpler case
  - Straight-line code
  - Consistent, predictable latencies

Algorithm Overview

- Build a precedence graph *P*
- Compute a *priority function* over the nodes in *P* (typical: longest latency-weighted path)
- Use list scheduling to construct a schedule, one cycle at a time
  - Use queue of operations that are ready
  - At each cycle
    - Chose a ready operation and schedule it
    - Update ready queue
- Rename registers to avoid false dependencies and conflicts

List Scheduling Algorithm

```
Cycle = 1;  Ready = leaves of P;  Active = empty;
while (Ready and/or Active are not empty)
    if (Ready is not empty)
        remove an op from Ready;
        S(op) = Cycle;
        Active = Active + op;
    Cycle++;
    for each op in Active
        if (S(op) + delay(op) <= Cycle)
            remove op from Active;
            for each successor s of op in P
                if (s is ready – i.e., all operands available)
                    add s to Ready
```


Example

- Code

```
a  LOAD    r1 <- w
b  ADD     r1 <- r1,r1
c  LOAD    r2 <- x
d  MULT    r1 <- r1,r2
e  LOAD    r2 <- y
f  MULT    r1 <- r1,r2
g  LOAD    r2 <- z
h  MULT    r1 <- r1,r2
i  STORE   w <- r1
```


Variations

- Backward list scheduling
  - Work from the root to the leaves
  - Schedules instructions from end to beginning of the block
- In practice, try both and pick the result that minimizes costs
  - Little extra expense since the precedence graph and other information can be reused
- Global scheduling and loop scheduling
  - Extend basic idea in more aggressive compilers