
$0.5$

## Precedence Graph

- Nodes $n$ are operations
- Attributes of each node
- type - kind of operation
- delay - latency
- If node n2 uses the result of node n1, there is an edge $e=(n 1, n 2)$ in the graph

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## Example Graph

- Code
a LOAD rl <-w
b ADD r1 <-r1,r1
c LOAD $\mathrm{r} 2<-\mathrm{x}$
d MULT $\mathrm{rl}<-\mathrm{r} 1, \mathrm{r} 2$
e LOAD $\quad r 2<-y$
f MULT $\mathrm{r} 1<-\mathrm{r} 1, \mathrm{r} 2$
$g$ LOAD $r 2<-z$
h MULT $\mathrm{r} 1<-\mathrm{r} 1, \mathrm{r} 2$
i STORE $\mathrm{w}<-\mathrm{rl}$


## Schedules (1)

- A correct schedule $S$ maps each node n into a non-negative integer representing its cycle number, and
- $S(n)>=0$ for all nodes $n$ (obvious)
- If ( $n 1, n 2$ ) is an edge, then
$\mathrm{S}(\mathrm{n} 1)+$ delay $(\mathrm{n} 1)<=\mathrm{S}(\mathrm{n} 2)$
- For each type $t$ there are no more operations of type $t$ in any cycle than the target machine can issue


## Constraints

- Main points
- All operands must be available
- Multiple operations can be ready at any given point
- Moving operations can lengthen register lifetimes
- Moving uses near definitions can shorten register lifetimes
- Operations can have multiple predecessors
- Collectively this makes scheduling NP-complete
- Local scheduling is the simpler case
- Straight-line code
- Consistent, predictable latencies


## Schedules

- The length of a schedule $S$, denoted $\mathrm{L}(\mathrm{S})$ is

$$
\mathrm{L}(\mathrm{~S})=\max _{n}(\mathrm{~S}(\underline{n})+\operatorname{delay}(n))
$$

- The goal is to find the shortest possible correct schedule
- Other possible goals: minimize use of registers, power, space, ...


## Algorithm Overview

- Build a precedence graph $P$
- Compute a priority function over the nodes in
$P$ (typical: longest latency-weighted path)
- Use list scheduling to construct a schedule, one cycle at a time
- Use queue of operations that are ready
- At each cycle
- Chose a ready operation and schedule it
- Update ready queue
- Rename registers to avoid false dependencies and conflicts

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## Variations

- Backward list scheduling
- Work from the root to the leaves
- Schedules instructions from end to beginning of the block
- In practice, try both and pick the result that minimizes costs
- Little extra expense since the precedence graph and other information can be reused
- Global scheduling and loop scheduling
- Extend basic idea in more aggressive compilers

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