

# CSE P 501 – Compilers

---

SSA  
Hal Perkins  
Autumn 2009



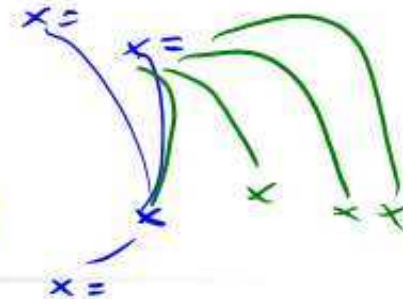
# Agenda

---

- Overview of SSA IR
  - Constructing SSA graphs
  - SSA-based optimizations
  - Converting back from SSA form
  
- Source: Appel ch. 19, also an extended discussion in Cooper-Torczon sec. 9.3



## Def-Use (DU) Chains



- Common dataflow analysis problem: Find all sites where a variable is used, or find the definition site of a variable used in an expression
- Traditional solution: def-use chains – additional data structure on the dataflow graph
  - Link each statement defining a variable to all statements that use it
  - Link each use of a variable to its definition



## DU-Chain Drawbacks

for (k = ...) {  
    a[k] = 0  
}

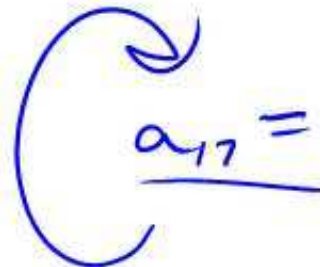
3  
for (k = ...) {  
    b[k] = -  
}

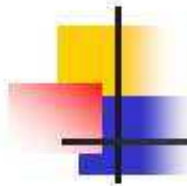
- Expensive: if a typical variable has  $N$  uses and  $M$  definitions, the total cost is  $O(N * M)$ 
  - Would be nice if cost were proportional to the size of the program
- Unrelated uses of the same variable are mixed together
  - Complicates analysis



# SSA: Static Single Assignment

- IR where each variable has only one definition in the program text
  - This is a single *static* definition, but it may be in a loop that is executed dynamically many times





## SSA in Basic Blocks

We've seen this before when looking at value numbering

- Original

a := x + y

b := a - 1

a := y + b

b := x \* 4

a := a + b

- SSA

a<sub>1</sub> := x + y

b<sub>1</sub> := a<sub>1</sub> - 1

a<sub>2</sub> := y + b<sub>1</sub>

b<sub>2</sub> := x \* 4

a<sub>3</sub> := a<sub>2</sub> + b<sub>2</sub>





## Merge Points

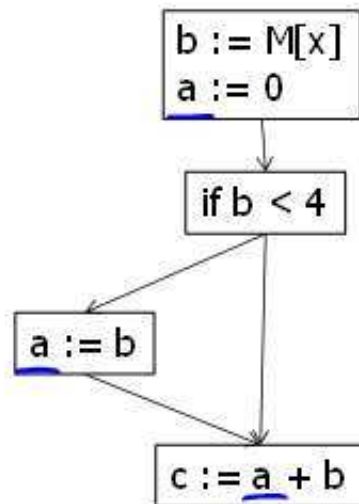


- The issue is how to handle merge points
- Solution: introduce a  $\Phi$ -function  
 $a_3 := \Phi(a_1, a_2)$
- Meaning:  $a_3$  is assigned either  $a_1$  or  $a_2$  depending on which control path is used to reach the  $\Phi$ -function

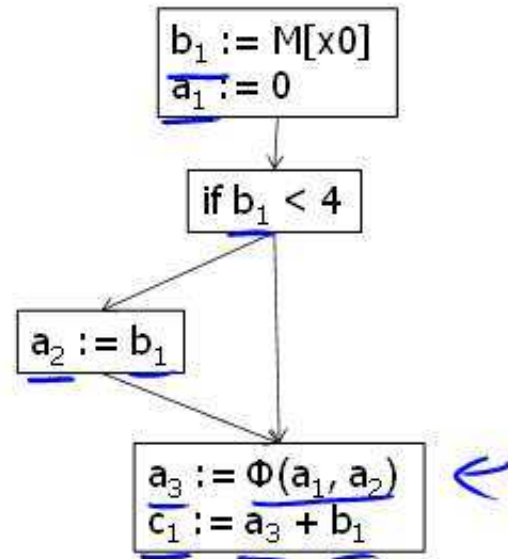


# Example

Original



SSA







## How Does $\Phi$ “Know” What to Pick?

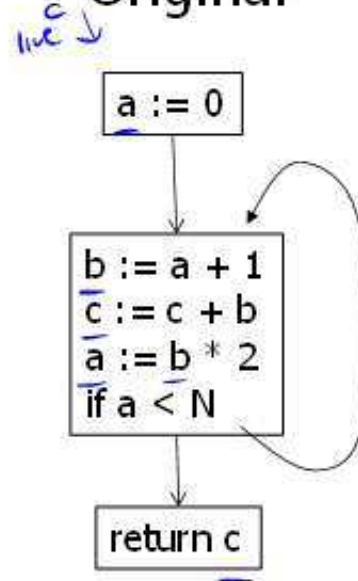
---

- It doesn't
  - When we translate the program to executable form, we can add code to copy either value to a common location on each incoming edge
  - For analysis, all we may need to know is the connection of uses to definitions – no need to “execute” anything

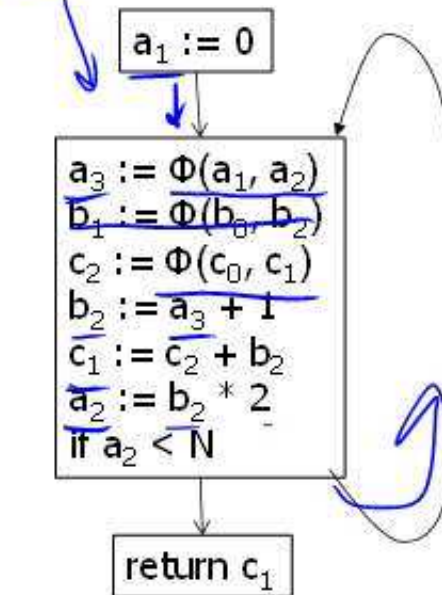


# Example With Loop

Original



*c<sub>0</sub>* SSA



Notes:

- $a_0, b_0, c_0$  are initial values of  $a, b, c$  on block entry
- $b_1$  is dead – can delete later
- $c$  is live on entry – either input parameter or uninitialized



# Converting To SSA Form

---

- Basic idea
  - First, add  $\Phi$ -functions
  - Then, rename all definitions and uses of variables by adding subscripts

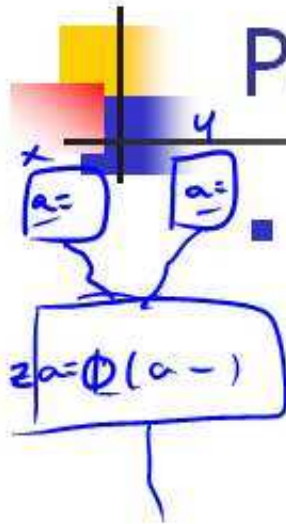


## Inserting $\Phi$ -Functions

---

- Could simply add  $\Phi$ -functions for every variable at every join point(!)
- But
  - Wastes *way* too much space and time
  - Not needed

## Path-convergence criterion



- Insert a  $\Phi$ -function for variable a at point z when
  - There are blocks x and y, both containing definitions of a, and  $x \neq y$
  - There are nonempty paths from x to z and from y to z
  - These paths have no common nodes other than z
  - z is not in both paths prior to the end (it may appear in one of them)



## Details

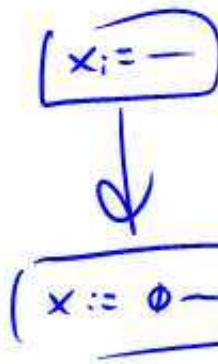


- The start node of the flow graph is considered to define every variable (even if to “undefined”)
- Each  $\Phi$ -function itself defines a variable, so we need to keep adding  $\Phi$ -functions until things converge





## Dominators and SSA



- One property of SSA is that definitions dominate uses; more specifically:
  - If  $x := \Phi(\dots, x_i, \dots)$  in block  $n$ , then the definition of  $x$  dominates the  $i$ th predecessor of  $n$
  - If  $x$  is used in a non- $\Phi$  statement in block  $n$ , then the definition of  $x$  dominates block  $n$



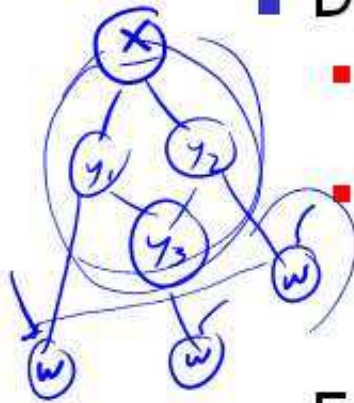


## Dominance Frontier (1)

---

- To get a practical algorithm for placing  $\Phi$ -functions, we need to avoid looking at all combinations of nodes leading from  $x$  to  $y$
- Instead, use the dominator tree in the flow graph

## Dominance Frontier (2)



- Definitions

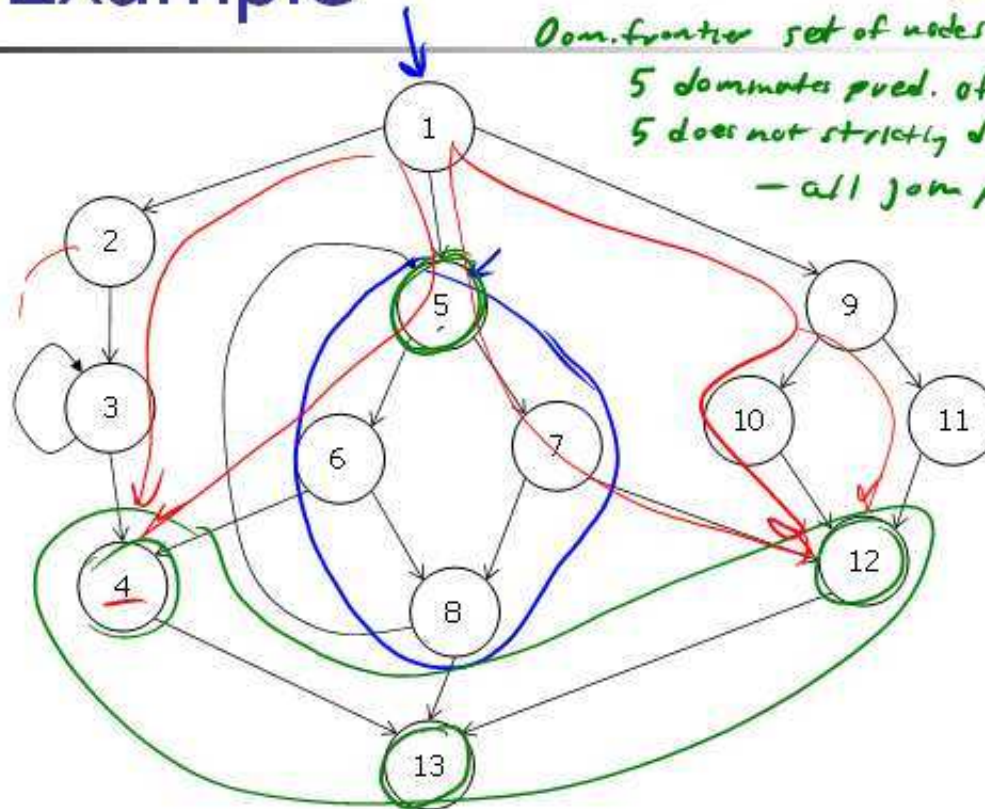
- $x$  *strictly dominates*  $y$  if  $x$  dominates  $y$  and  $x \neq y$
- The *dominance frontier* of a node  $x$  is the set of all nodes  $w$  such that  $x$  dominates a predecessor of  $w$ , but  $x$  does not strictly dominate  $w$

- Essentially, the dominance frontier is the border between dominated and undominated nodes



# Example

Dom. frontier of 5  
5 dominates 6, 7, 8, 5  
5 strictly dominates 6, 7, 8  
Dom. frontier set of nodes  $x$  st.  
5 dominates pred. of  $x$  but  
5 does not strictly dom.  $x$   
- all join points





## Dominance Frontier Criterion



- If a node  $x$  contains the definition of variable  $a$ , then every node in the dominance frontier of  $x$  needs a  $\Phi$ -function for  $a$ 
  - Since the  $\Phi$ -function itself is a definition, this needs to be iterated until it reaches a fixed-point
- Theorem: this algorithm places exactly the same set of  $\Phi$ -functions as the path criterion given previously



## Placing $\Phi$ -Functions: Details

- The basic steps are:
  1. Compute the dominance frontiers for each node in the flowgraph
  2. Insert just enough  $\Phi$ -functions to satisfy the criterion. Use a worklist algorithm to avoid reexamining nodes unnecessarily
  3. Walk the dominator tree and rename the different definitions of variable  $a$  to be  $a_1, a_2, a_3, \dots$





# Efficient Dominator Tree Computation

---

- Goal: SSA makes optimizing compilers faster since we can find definitions/uses without expensive bit-vector algorithms
- So, need to be able to compute SSA form quickly
- Computation of SSA from dominator trees are efficient, but...



## Lengauer-Tarjan Algorithm

- Iterative set-based algorithm for finding dominator trees is slow in worst case
- Lengauer-Tarjan is near linear time
  - Uses depth-first spanning tree from start node of control flow graph
  - See books for details





## SSA Optimizations

---

- Given the SSA form, what can we do with it?
- First, what do we know? (i.e., what information is kept in the SSA graph?)



## SSA Data Structures

- Statement: links to containing block, next and previous statements, variables defined, variables used.
  - Statement kinds are: ordinary,  $\Phi$ -function, fetch, store, branch
- Variable: link to definition (statement) and use sites
- Block: List of contained statements, ordered list of predecessors, successor(s)



## Dead-Code Elimination

$v_{17} = x_{35}$

- A variable is live iff its list of uses is not empty(!)

- Algorithm to delete dead code:

while there is some variable  $v$  with no uses

[ if the statement that defines  $v$  has no other side effects, then delete it

- Need to remove this statement from the list of uses for its operand variables – which may cause those variables to become dead



## Simple Constant Propagation

- If  $c$  is a constant in  $v := c$ , any use of  $v$  can be replaced by  $c$ 
  - Then update every use of  $v$  to use constant  $c$
- If the  $c_i$ 's in  $v := \Phi(c_1, c_2, \dots, c_n)$  are all the same constant  $c$ , we can replace this with  $v := c$
- Can also incorporate copy propagation, constant folding, and others in the same worklist algorithm



## Simple Constant Propagation

```
[ W := list of all statements in SSA program
  while W is not empty
    [ remove some statement S from W
      if S is  $v := \Phi(c, c, \dots, c)$ , replace S with  $v := c$ 
      if S is  $v := c$ 
        delete S from the program
        for each statement T that uses v
          substitute c for v in T
          add T to W
```



## Converting Back from SSA

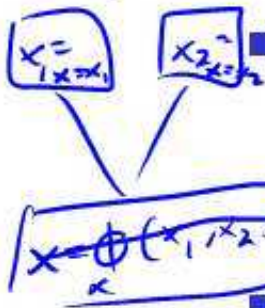
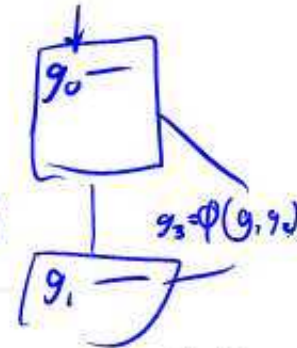
---

- Unfortunately, real machines do not include a  $\Phi$  instruction
- So after analysis, optimization, and transformation, need to convert back to a “ $\Phi$ -less” form for execution





# Translating $\Phi$ -functions



■ The meaning of  $x := \Phi(x_1, x_2, \dots, x_n)$  is "set  $x := x_1$  if arriving on edge 1, set  $x := x_2$  if arriving on edge 2, etc."

- So, for each  $i$ , insert  $x := x_i$  at the end of predecessor block  $i$
- Rely on copy propagation and coalescing in register allocation to eliminate redundant moves





## SSA Wrapup

---

- More details in recent compiler books (but not the new dragon book!)
- Allows efficient implementation of many optimizations
- Used in many new compiler (e.g. llvm) & retrofitted into many older ones (gcc)
- Not a silver bullet – some optimizations still need non-SSA forms