

CodeContracts: Specification & Verification for the working programmer

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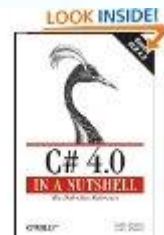
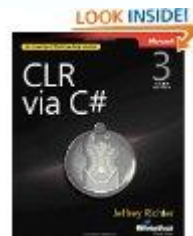
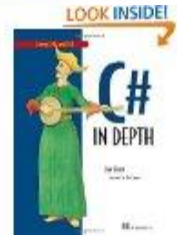
joint work with

M. Barnett and M. Fahndrich

Demo!!!

CodeContracts Impact

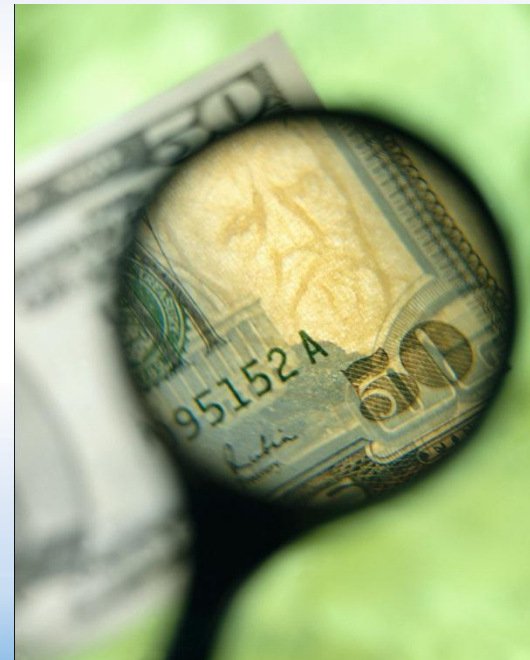
- API in .NET 4.0
- Externally available ~20 months
 - > 50,000 downloads, very active forum
 - 3 book chapters on CodeContracts
 - Many dozens of blog articles
 - Active forum
- Internal and external adoption
- Publications, talks, lectures
 - POPL, ECOOP, OOPSLA, VMCAI, APLAS, SAS, SAC, FoVeOOS, VSTTE ...



Program verification

- *"The program does not go wrong"*
 - What does it mean?
- It does not crash
 - Division by zero
 - Dereference of null (or 0 or nil)
 - No exception is thrown
 - ...
- It meets its specification
 - Specification???
 - What's that?

Verification 101



Specification

- Informally: “What the program should do”
 - “It should sort all the elements of the array”
- Computers do not like English
 - (or Italian for what it matters ;-)
- Which *formal* language?
 - How close to the computer?
 - How close to the human?
 - How close to the programmer?
 - How close to the verification tool?

A plethora of specification lang.

- Implementation
 - Temporal Logic?
 - Z (B) notation?
 - UML?
 - TLA+ ?
 - Abstract state machines (ASM)?
 - JML? Code Contracts?
 - SAL?
 - ...
 - Many many
 - ...

Potato



The program behavior is included in the behaviors admissible from the specification:

Program is correct 😊

Potato



A Venn diagram consisting of two overlapping ovals. The larger, light blue oval is labeled 'Specification'. The smaller, purple oval is labeled 'Program' and is positioned to overlap with the bottom-left portion of the 'Specification' oval.

Specification

Program

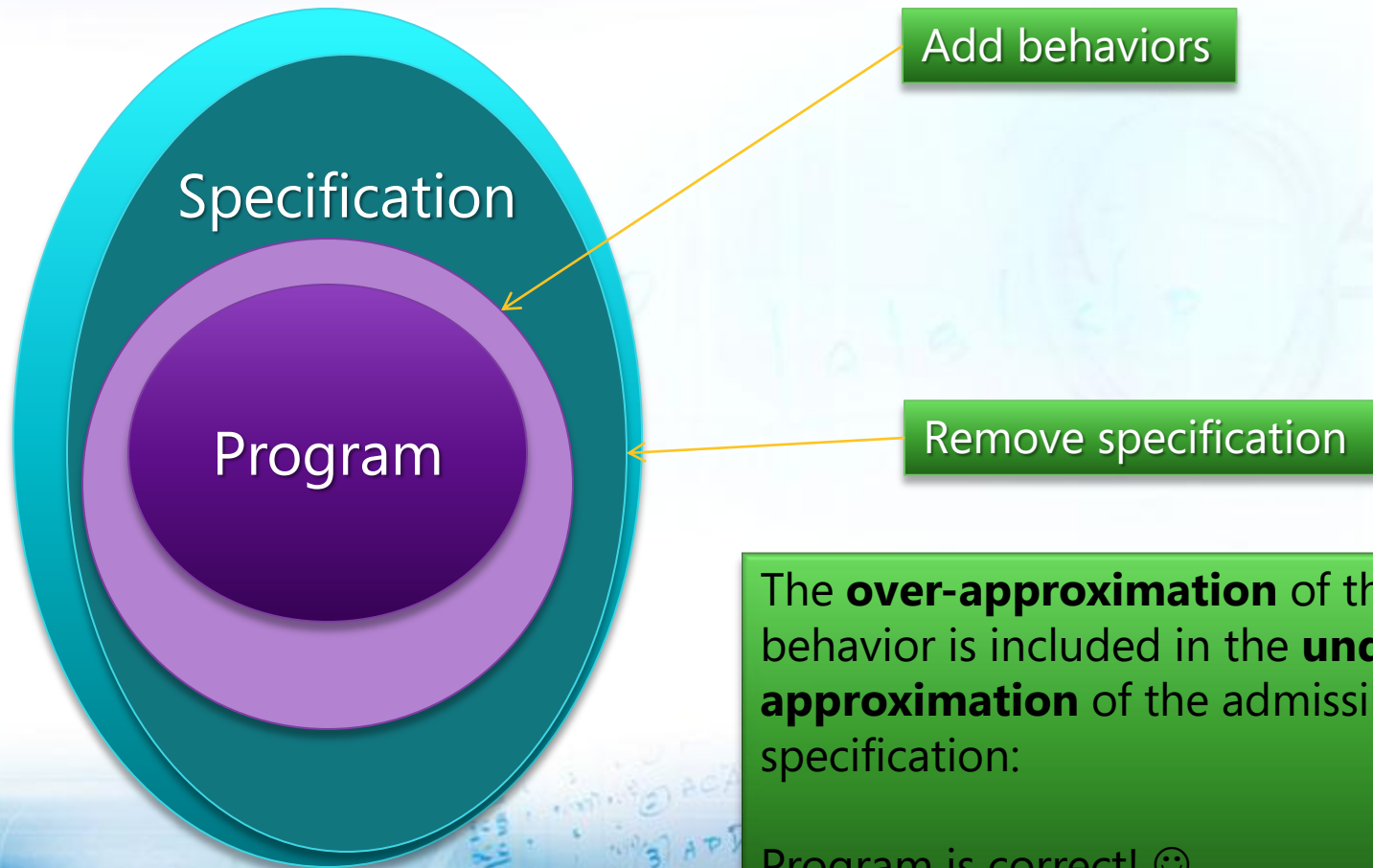
The program behavior is **not** included in the behaviors admissible from the specification:

Program is incorrect ☹️
(Some behavior may not meet the specification)

How do we check potatoes?

- The problem is undecidable
- Need to perform abstraction
- In the concrete:
 - Is the program correct? Yes/No
- In the abstract:
 - Is the program correct? Yes/No/I do not know
- Which abstraction?
 - Upper-approximate the program semantics
 - Under-approximate the specification semantics

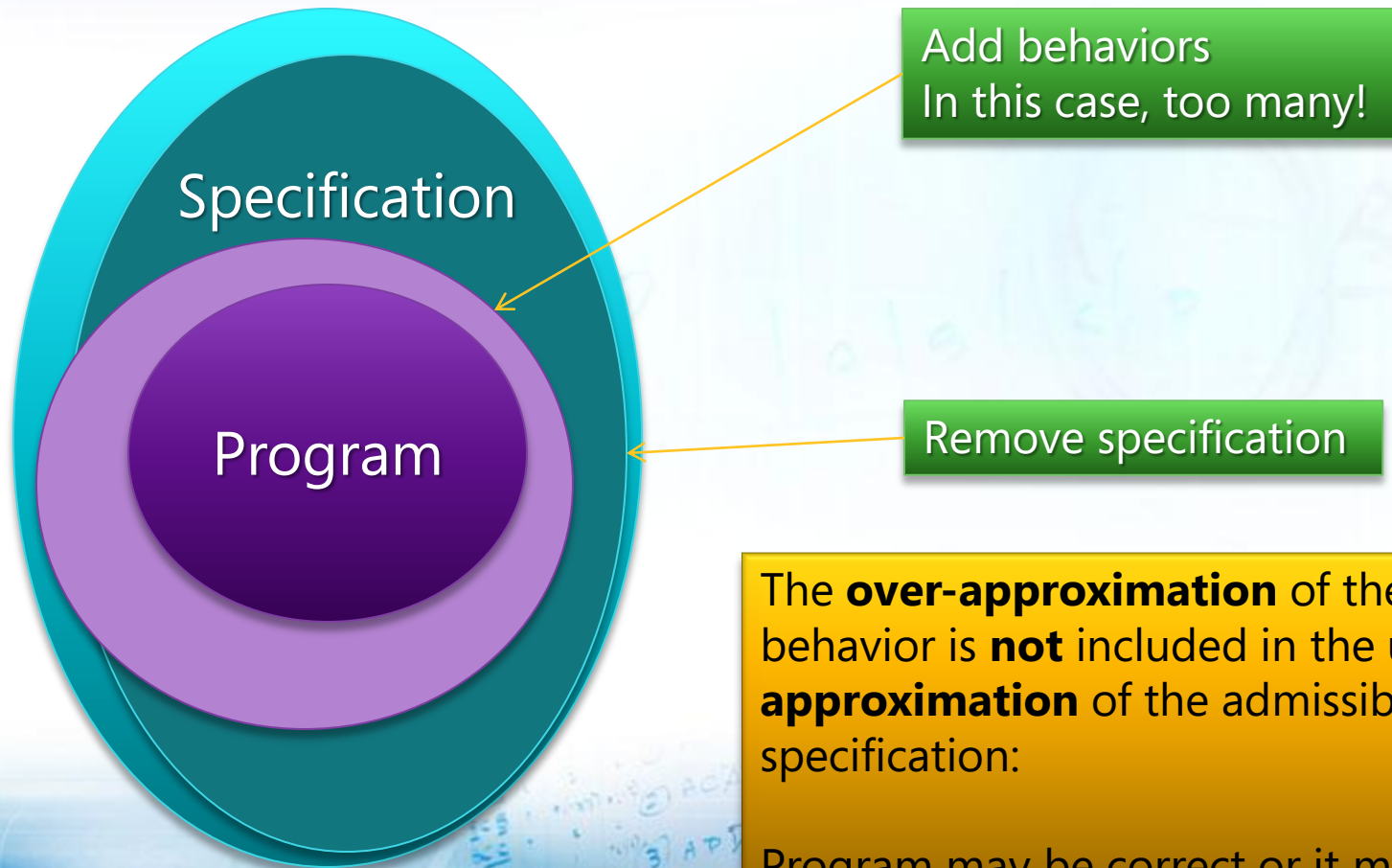
Potato (when lucky)



The **over-approximation** of the program behavior is included in the **under-approximation** of the admissible specification:

Program is correct! 😊

Potato (when unlucky)



The **over-approximation** of the program behavior is **not** included in the **under-approximation** of the admissible specification:

Program may be correct or it may not ☹

To sum up...

- Specification
 - How do we specify the intent?
 - We should not over-specify
- Verification
 - How do we check the program is doing the right thing?
 - Runtime (testing)
 - Static time (verification)

Specification with Contracts



Contracts: What for?

- Document design decisions

C#

```
public virtual int Next(  
    int minValue,  
    int maxValue  
)
```

Parameters

minValue

Type: [System.Int32](#)

The inclusive lower bound of the random number returned.

maxValue

Type: [System.Int32](#)

The exclusive upper bound of the random number returned. *maxValue* must be greater than or equal to *minValue*.

Return Value

Type: [System.Int32](#)

A 32-bit signed integer greater than or equal to *minValue* and less than *maxValue*; that is, the range of return values includes *minValue* but not *maxValue*. If *minValue* equals *maxValue*, *minValue* is returned.

Exceptions

| Exception | Condition |
|---|---|
| ArgumentOutOfRangeException | <i>minValue</i> is greater than <i>maxValue</i> . |

Remarks

Unlike the other overloads of the [Next](#) method, which return only non-negative values, this method can return a negative random integer.

Notes to Inheritors:

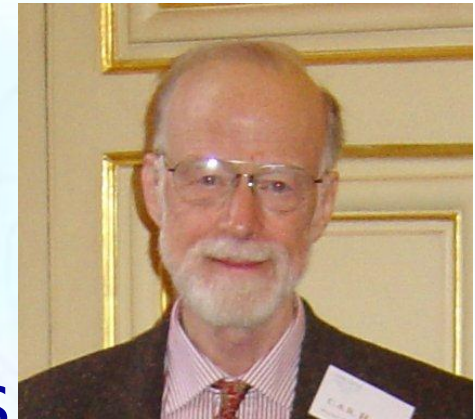
Starting with the .NET Framework version 2.0, if you derive a class from [Random](#) and override the [Sample](#) method, the distribution provided by the derived class implementation of the [Sample](#) method is not used in calls to the base class implementation of the [Random.Next\(Int32, Int32\)](#) method overload if the difference between the *minValue* and *maxValue* parameters is greater than [Int32.MaxValue](#). Instead, the uniform distribution returned by the base [Random](#) class is used. This behavior improves the overall performance of the [Random](#) class. To modify this behavior to call the [Sample](#) method in the derived class, you must also override the [Random.Next\(Int32, Int32\)](#) method overload.

Precondition

Postcondition

Contracts: What for?

- Amplify runtime checking (debugging)
 - More assertions in the code
 - More stable the code
 - Assertions can be disabled in release builds
- Enable modular static analysis
 - Improved precision
 - Analysis should not assume worst case
 - More scalability
 - A little bit as a type-checker (but more refined!)



But we already have assertions!

- All languages have an assert
 - `assert(exp)` macro in C/C++
 - `assert exp` keyword in Java
 - `Debug.Assert(exp)` static method in .NET
- Assert is not visible from the caller!

```
static public int GCD(int x, int y)
{
    Debug.Assert(x > 0);
    Debug.Assert(y > 0);
}
```


Exceptions

- Use exceptions for parameter validation:

```
static public int GCD(int x, int y)
{
    if (x < 0)
        throw new ArgumentException("Error");
    ... }

```

- At library surface
- To protect from unwanted values
- To early detect API misuses
- Again, not visible to callers

But we have Debug.Assert!

- Cannot (easily) specify a postcondition

```
static public int GCD(int x, int y)
{
    Debug.Assert(x > 0);
    Debug.Assert(y > 0);

    while (true)
        if (x < y) { y %= x; if (y == 0) return x; }
        else { x %= y; if (x == 0) return y; }
}
```

Debug.Assert(Result > 0) ?

Assert & OOP : ☹️

- Inheritance
 - Precondition: Should be weaker
 - Postcondition: Should be stronger
 - How do I enforce it?
- Object invariants
 - Valid in steady states
 - Ex: `this.x != null`
 - Should I add it at every method?
- Interfaces, abstract methods
 - Where I put my assert?

Contracts yesterday

- First class citizens in the language
- Provide syntax to express contracts
 - Examples: Eiffel, D, Spec# ...

```
decrement is
    -- Decrease counter by one.
    require
        item > 0
    do
        item := item - 1
    ensure
        item = old item - 1
    end
```

- Why not everyone was using it?
 - New language (start from scratch, or almost)
 - New compiler (do you trust it?)

Contracts yesterday

- Inside comments or as code annotation
 - Ex. JML, Eclipse for non-null ...

```
//@ public invariant balance >= 0 && balance <= MAX_BALANCE;

//@ assignable balance;
//@ ensures balance == 0;
public BankingExample() { balance = 0; }

//@ requires 0 < amount && amount + balance < MAX_BALANCE;
//@ assignable balance;
//@ ensures balance == \old(balance + amount);
public void credit(int amount) { balance += amount; }

//@ requires 0 < amount && amount <= balance;
//@ assignable balance;
//@ ensures balance == \old(balance) - amount;
public void debit(int amount) { balance -= amount; }
```

- Why not everyone is using it?
 - Persistence?
 - Need for serialization, parsing...
 - Separate type checking, name resolution...

Code contracts



Code Contracts
Specify code with code

ERROR LIST
0 Errors
1 contracts

Code Contracts
Invariant fa

```
public Chunk  
Contract.F  
Contract.F  
this.arrin
```


Code Contracts

- Idea: Use the IL as contract representation
- Use static methods to a contract library
 - Language agnostic: same for C#, VB, F# ...

```
Contract.Requires(source != null);  
Contract.Requires(!String.IsNullOrEmpty(suffix));
```

```
Contract.Ensures(Contract.Result<string>() != null);  
Contract.Ensures(!Contract.Result<string>().EndsWith(suffix));
```

```
Contract.Assert(trimmed IsNot Nothing)  
Contract.Assert(Not trimmed.EndsWith(".dll"))
```

What are they?

- Plain code for contracts
- Static methods to a contract library
 - Language agnostic: same for C#, VB, F# ...
 - Standard from .NET 4.0
- No need for a new compiler/language
 - Precondition: `Contract.Requires(...)`
 - Postcondition: `Contract.Ensures(...)`
 - Invariant: `Contract.Invariant(...)`

Preconditions

- `Contract.Requires(exp)`

```
int foo(String s, int y)
{
    Contract.Requires(s != null);
    Contract.Requires(y > 0);
    // ...
}
```

C# expressions



Preconditions

- Which is the underlying language specification?

Your programming language!!!

```
Public Function foo(ByVal s As String, ByVal y As Integer)
    As Integer
        Contract.Requires(s IsNot Nothing)
        Contract.Requires(y > 0)
        ' ...
    End Function
```

VB expressions

C++ expressions

```
Int32 __gc* foo(String __gc* s, Int32 __gc* y)
```

```
Contract::Requires(s != 0);
Contract::Requires(y > 0);
```


Postconditions

- `Contract.Ensures(exp)`

```
Class Field
{
    int x;

    int Set(int y)
    {
        Contract.Ensures(this.x == y);
        this.x = y;
    }
}
```

Result value?

- In C#/VB/... no name for the returned value
- Use a dummy method

```
public int Fact(int x)
{
    Contract.Ensures(Contract.Result<int>() >= 0);
    ...
}
```

Question

- Why `<int>` ?
- Why `<bool[]>` ?

```
public int Fact(int x)
{
    Contract.Ensures(Contract.Result<int>() >= 0);
}
```

```
} public bool[] ArrayFactory(int x)
{
    Contract.Ensures(Contract.Result<bool[]>() != null);
    return new bool[x];
}
```

T Contract.Result<T>()

Old value?

- No name for the old value

```
Class Account
{
  int balance;
```

T Contract.Old<T>(T value)

```
int Add(int k)
{
```

```
    Contract.Ensures(this.balance ==
        Contract.Old(this.balance) + k);
    this.balance += k;
```

```
    }
}
```

Quantifiers

- Limited form:
 - `Contract.ForAll(0, A.Length, i => A[i] > 0);`
 - `Contract.Exists(0, A.Length, i => A[i] > 0);`
- Exploit higher order functions

Class Invariant

```
Class Account
{
    int balance;

    [ContractInvariantMethod]
    protected void ObjectInvariant()
    {
        Contract.Invariant(balance >= 0);
    }
}
```

Interfaces

```
[ContractClass(typeof(WithdrawContracts))]  
interface IWithdraw  
{  
    long Balance { get; }  
    void Withdraw(long money);  
}
```

```
[ContractClassFor(typeof(IWithdraw))]  
public class WithdrawContracts : IWithdraw {  
    public long Balance { get {  
        Contract.Ensures(Contract.Result<long>() >= 0);  
        return -111; } }  
    public void Withdraw(long money) {  
        Contract.Requires(money < this.Balance);}}}
```

Other

- Abstract classes
 - Similar to interfaces
- Out/ref parameters
 - Use dummy method
- Legacy code: *"if !exp throw exception"*
 - Use Contract.EndContract()

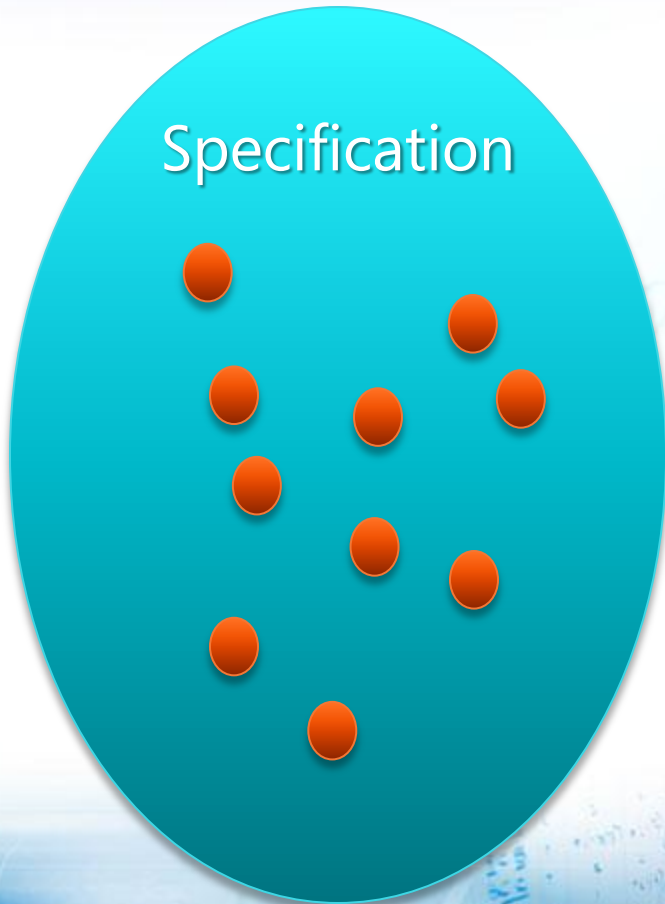
Advantages

- Produced by all the compilers
- Free:
 - Types
 - Intellisense
 - Name resolution...
- Cross language
- Precise semantics
- Uniform format understood by our tools

Runtime checking (aka Testing)

Potato & testing

Specification



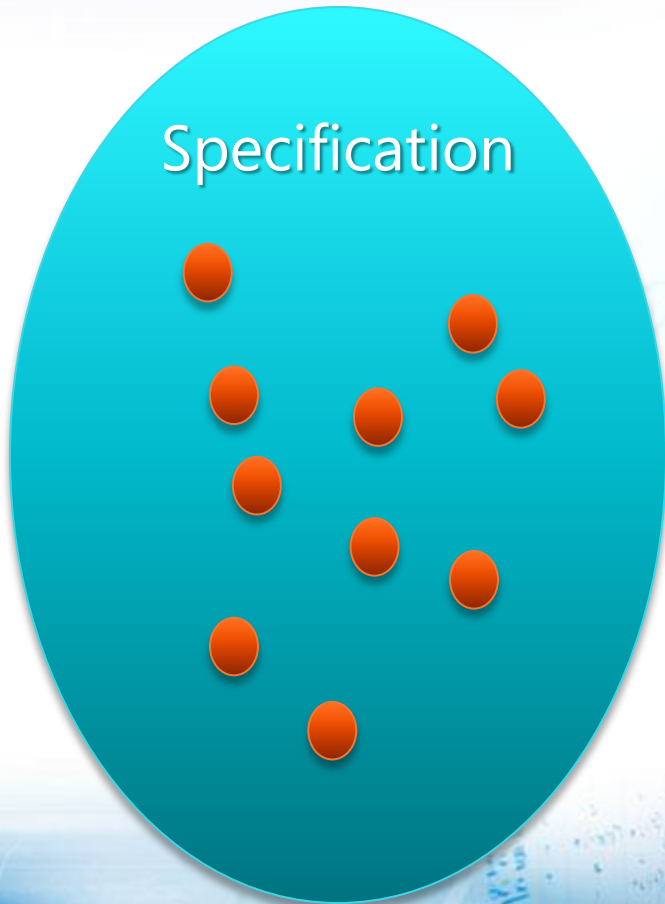
One execution is outside the specification

The program is incorrect!

| | A | B | C | D |
|---|---|----|----|-----|
| 1 | Y | 80 | 40 | 100 |

Potato & testing

Specification



A **sample** of the program behavior is included in the behaviors admissible from the specification

Is the program correct?

Testing

- Prove the existence of specification violations
 - i.e. the existence of bugs
 - If a test fails, then there is a bug
- Cannot verify the program
 - i.e. the existence of no bug!
 - Can try only finitely main inputs
 - 100% code coverage do not imply 100% data coverage
- Yet, very useful!!!

Runtime checking of contracts

- C# compiler does not know about contracts
- Achieved via binary rewriting
 - Handle old, result ...
 - Inherit contracts
 - Stick contracts to interface implementations

Binary rewriting

```
public virtual int Add(object value){  
    Contract.Requires( value != null );
```

```
    Contract.Ensures( Count == Contract.OldValue(Count) + 1 );  
    Contract.Ensures( Contract.Result<int>() == Contract.OldValue(Count) );
```

```
    if ( _size == _items.Length) EnsureCapacity(_size+1);  
    _items[_size] = value;  
    return _size++;  
}
```

csc/vbc/

/d:CONTRACTS_FULL

csc/vbc/

ccrewrite

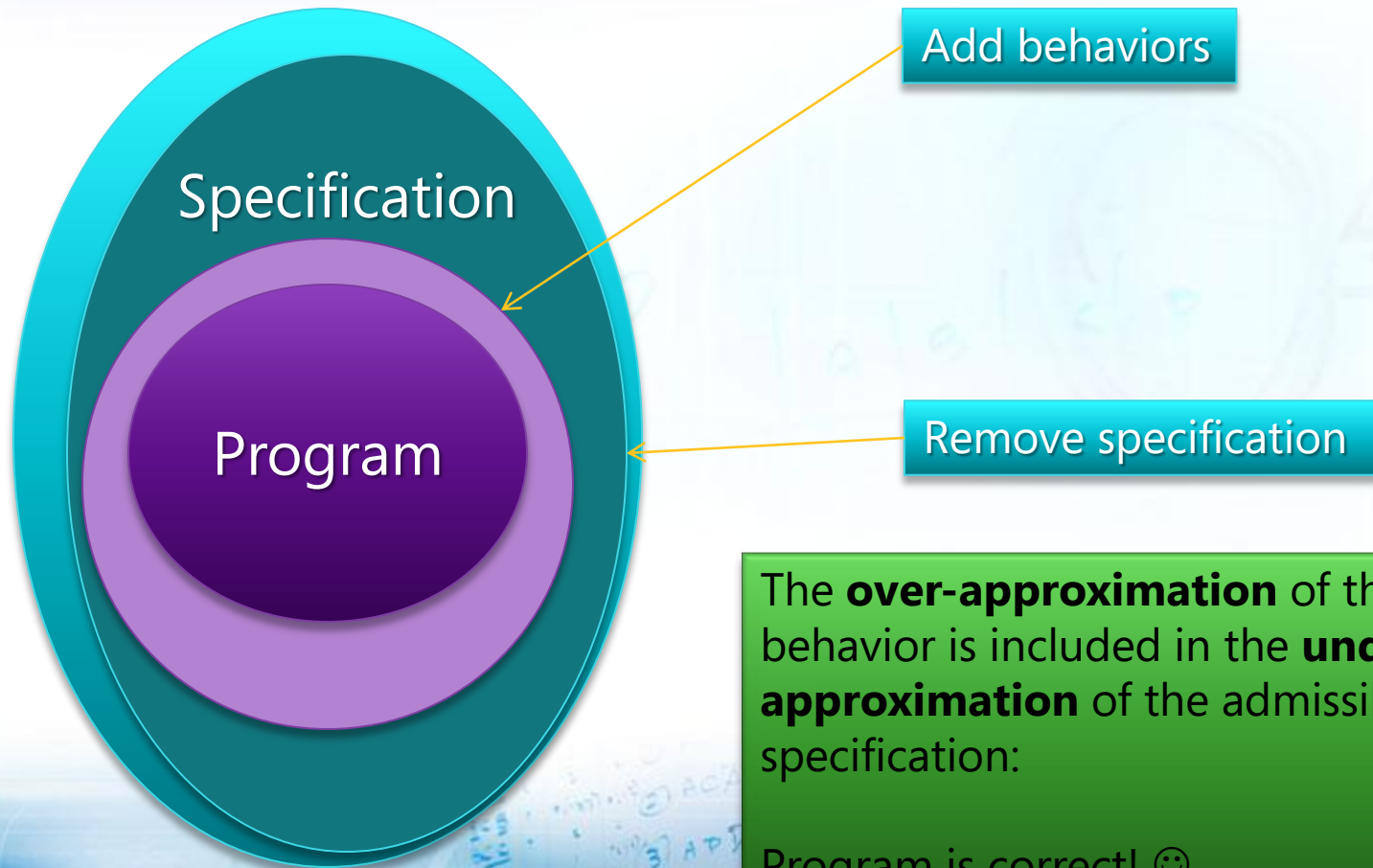
```
.method public hidebysig newslot virtual instance int32 Add(object 'value') cil managed  
{  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldarg.0  
    ldftd object[] TabDemo.BaseList:items  
    ldlen  
    conv.i4  
    ceq  
    ldc.i4.0  
    ceq  
    stloc.1  
    ldloc.1  
    brtrue.s IL_0029  
    ldarg.0  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldc.i4.1  
    add  
    call instance void TabDemo.BaseList:EnsureCapacity(int32)  
    ldarg.0  
    ldftd object[] TabDemo.BaseList:items  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldarg.1  
    stelem.ref  
    ldarg.0  
    dup  
    ldftd int32 TabDemo.BaseList:count  
    dup  
    stloc.2  
    ldc.i4.1  
    add  
    stfld int32 TabDemo.BaseList:count  
    ldloc.2  
    stloc.0  
    br.s IL_004b  
    ldloc.0  
    ret  
}
```

```
.method public hidebysig newslot virtual instance int32 Add(object 'value') cil managed  
{  
    ldarg.1  
    ldnull  
    ceq  
    ldc.i4.0  
    ceq  
    call void [Microsoft.Contracts]Microsoft.Contracts.Contract:Requires(bool)  
    ldarg.0  
    call instance int32 TabDemo.BaseList:get_Count()  
    ldarg.0  
    call instance int32 TabDemo.BaseList:get_Count()  
    call !10 [Microsoft.Contracts]Microsoft.Contracts.Contract:Old<int32>(!10)  
    ldarg.0  
    ldc.i4.1  
    add  
    ceq  
    call void [Microsoft.Contracts]Microsoft.Contracts.Contract:Ensures(bool)  
    call !10 [Microsoft.Contracts]Microsoft.Contracts.Contract:Result<int32>(!10)  
    ldarg.0  
    call instance int32 TabDemo.BaseList:get_Count()  
    call !10 [Microsoft.Contracts]Microsoft.Contracts.Contract:Old<int32>(!10)  
    ceq  
    call void [Microsoft.Contracts]Microsoft.Contracts.Contract:Ensures(bool)  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldarg.0  
    ldftd object[] TabDemo.BaseList:items  
    ldlen  
    conv.i4  
    ceq  
    ldc.i4.0  
    ceq  
    stloc.1  
    ldloc.1  
    brtrue.s IL_0069  
    ldarg.0  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldc.i4.1  
    add  
    call instance void TabDemo.BaseList:EnsureCapacity(int32)  
    ldarg.0  
    ldftd object[] TabDemo.BaseList:items  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldarg.1  
    stelem.ref  
    ldarg.0  
    dup  
    ldftd int32 TabDemo.BaseList:count  
    dup  
    stloc.2  
    ldc.i4.1  
    add  
    stfld int32 TabDemo.BaseList:count  
    ldloc.2  
    stloc.0  
    br.s IL_008b  
    ldloc.0  
    ret  
}  
// end of method BaseList:Add
```

```
.method public hidebysig newslot virtual instance int32 Add(object 'value') cil managed  
{  
    .locals init (int32 'Contract.Old(Count)',  
                int32 'Contract.Result<int>()')  
    ldarg.0  
    call instance int32 TabDemo.BaseList:get_Count()  
    stloc.3  
    ldarg.1  
    ldnull  
    ceq  
    ldc.i4.0  
    ceq  
    ldstr "value != null"  
    call void _RewriterMethods:RewriterRequiresPST06000009(bool, string)  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldarg.0  
    ldftd object[] TabDemo.BaseList:items  
    ldlen  
    conv.i4  
    ceq  
    ldc.i4.0  
    ceq  
    stloc.1  
    ldloc.1  
    brtrue IL_004d  
    nop  
    ldarg.0  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldc.i4.1  
    add  
    call instance void TabDemo.BaseList:EnsureCapacity(int32)  
    nop  
    ldarg.0  
    ldftd object[] TabDemo.BaseList:items  
    ldarg.0  
    ldftd int32 TabDemo.BaseList:count  
    ldarg.1  
    stelem.ref  
    ldarg.0  
    dup  
    ldftd int32 TabDemo.BaseList:count  
    dup  
    stloc.2  
    ldc.i4.1  
    add  
    stfld int32 TabDemo.BaseList:count  
    ldloc.2  
    stloc.0  
    br IL_0072  
    ldloc.0  
    stloc.s 'Contract.Result<int>()'   
    br IL_007a  
    ldarg.0  
    call instance int32 TabDemo.BaseList:get_Count()  
    ldloc.3  
    ldc.i4.1  
    add  
    ceq  
    ldstr "Count == Contract.Old(Count) + 1"  
    call void _RewriterMethods:RewriterEnsuresPST0600000B(bool, string)  
    ldloc.s 'Contract.Result<int>()'   
    ldloc.s V_4  
    ceq  
    ldstr "Contract.Result<int>() == Contract.Old(Count)"  
    call void _RewriterMethods:RewriterEnsuresPST0600000B(bool, string)  
    ldloc.s 'Contract.Result<int>()'   
    ret  
}
```


Static verification

Static verification with potatoes



Static verification

- Any static verification method is incomplete
 - Verification is not decidable

```
public static bool NotDecidable()  
{  
    if (SolvableDiophantineEquation)  
        return 1;  
    else  
        Contract.Assert(false);  
}
```

Not decidable
(Hilbert's 10th
problem)

Verification techniques

- Many, many out there...
- Model Checking
- Theorem proving
 - Automatic
 - SMT solvers, resolution based, ...
 - Semi-automatic
 - 2nd order
- All those instances of Abstract interpretation!

Abstract interpretation

Abstract Interpretation



- Theory of approximations
- Semantics are ordered according to the precision
- The more the precise the semantics
The more the properties captured
- A static analysis is a semantics
 - Precise enough to capture the properties of interest
 - Rough enough to be computable

Basic Concepts

- Concrete domain
 - A mathematical structure describing the most precise information on the program
 - Usually the program semantics
 - Traces, operational, denotational ...
- Abstract domain
 - A mathematical structure describing the property of interests
 - Ex.: range of a variable

Example: Rule of signs

- Abstract semantics is over signs

$$a[[k]]\rho = \text{sign}(k)$$

$$a[[x]]\rho = \rho(x)$$

$$a[[e1 + e2]]\rho = a[[e1]]\rho \pm a[[e2]]\rho$$

$$a[[e1 * e2]]\rho = a[[e1]]\rho * a[[e2]]\rho$$

| \pm | \perp | neg | zero | pos | T |
|---------|---------|---------|---------|---------|---------|
| \perp | \perp | \perp | \perp | \perp | \perp |
| neg | \perp | neg | neg | T | T |
| zero | \perp | neg | zero | pos | T |
| pos | \perp | T | pos | Pos | T |
| T | \perp | T | T | T | T |

Example: Rule of signs

- $(12345565 * 13456) + (-9873 * -1344678)$
- Sign of the result?
- Do the computation: 179 397 928 534
 - Then take the sign : pos
- Do the abstract computation:
 $(\text{pos} _ * \text{pos}) \pm (\text{neg} _ * \text{neg})$
 $= \text{pos} \pm \text{pos}$
 $= \text{pos}$

CodeContracts Static checker *aka Clousot*



Algorithm: High level

- For each assembly A, class C, method M
 1. Extract the proof obligations
 - What should I prove?
 2. Run the analyses
 - Discover facts on the program
 3. Use the facts to prove the proof obligations
 - If not, do something else...

Proof obligations

- Two kinds: Implicit and explicit
- Implicit
 - NonNull checking
 - Bounds checking
 - Arithmetic: Divisions by zero, overflows,
 - ...
- Explicit
 - Assertions
 - When calling a method, its precondition
 - When returning from a method, its postcondition

NonNull dereference

```
public bool IsCiao(string s)
{
    return s.Contains("ciao!");
}
```

- The string `s` should not be null
 - Otherwise, exception at run time
- Generate the proof obligation: `s != null`

Array bounds

```
public int[] RandomArray(int len)
{
    var random = new Random(len);
    var arr = new int[len];
    for (var i=0; i < len; i++)
    {
        arr[i] = random.Next();
    }
    return arr;
}
```

len >= 0



i >= 0



i < arr.Length



Overflows

```
public int Div(int x, int y)
{
    return x / y;
}
```

y != 0

```
public int Abs(int x)
{
    if (x < 0)
        return -x;
    return x;
}
```

x != MinValue

x != MinValue || y != -1

Explicit obligation: Assertions

```
public string Concat(string p, string q)
{
    Contract.Requires(p != null);
    Contract.Requires(q != null);

    var concat = p + q;

    Contract.Assert(concat != null);
    Contract.Assert(concat.Length > 0);

    return concat;
}
```

concat != null



concat.Length > 0



Preconditions

```
public string Concat(string p, string q)
{
    Contract.Requires(p != null);
    Contract.Requires(q != null);
    // ...
}

public string MyConcat()
{
    return Concat("Ciao", null);
}
```

Concat "believes"
(assumes)
those preconditions

"Ciao" != null

null != null

Postconditions

```
public double Abs(double x)
{
    Contract.Ensures(
        Contract.Result<double>() >= 0);

    if (x < 0)
        return -x;
    return x;
}

public double Sqrt(double z)
{
    return Math.Sqrt(Abs(z));
}
```

$-x \geq 0$

$x \geq 0$

Note: the program is wrong, why???

Sqrt "believes"
(assumes)
 $Abs(z) \geq 0$

Algorithm: High level

- For each assembly A, class C, method M
 1. Extract the proof obligations
 - What should I prove?
 2. Run the analyses
 - Discover facts on the program
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Inferred facts

- Heap structure
- Null/Not-Null
- Numerical values
 - Ranges, relations, floating points ...
- Enum values
- Array/Collection contents
- ...

Example

```
public string TrimSuffix(string s, string suffix)
{
    Contract.Requires(s != null);
    Contract.Requires(suffix != null);

    string res = s;

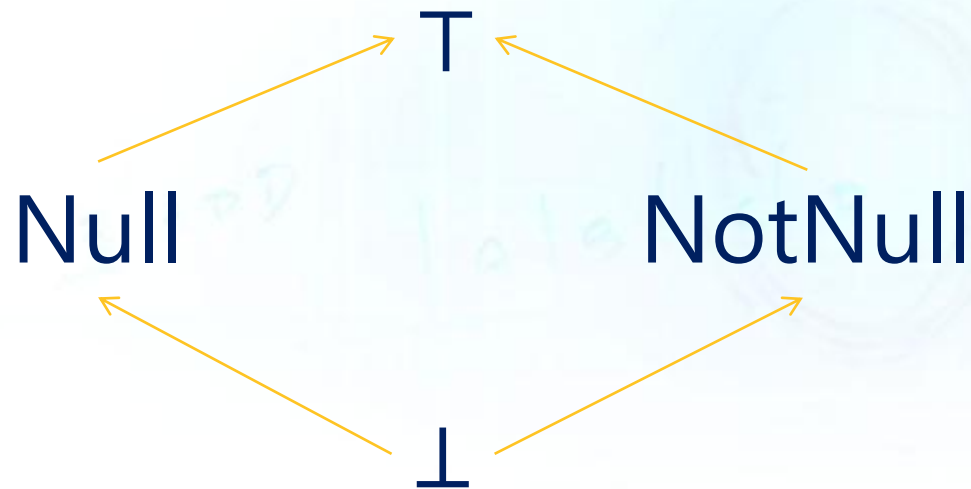
    while (res.EndsWith(suffix))
    {
        int len = res.Length - suffix.Length;
        res = res.Substring(0, len);
    }

    Contract.Assert(res != null);

    return res;
}
```

Nonnull analysis

- Associate to each variable an element of



With proof obligations explicit

```
public string TrimSuffixWPO(string s, string suffix)
{
    Contract.Requires(s != null);
    Contract.Requires(suffix != null);

    string res = s;

    Contract.Assert(res != null);
    while (res.EndsWith(suffix))
    {
        Contract.Assert(res != null);
        Contract.Assert(suffix != null);
        int len = res.Length - suffix.Length;
        Contract.Assert(res != null);
        res = res.Substring(0, len);
        Contract.Assume(res != null); // Postcondition of res
    }

    Contract.Assert(res != null);

    return res;
}
```

Checking

```
public string TrimSuffixWPO(string s, string suffix)
{
    Contract.Requires(s != null);
    Contract.Requires(suffix != null);

    string res = s;

    Contract.Assert(res != null);
    while (res.EndsWith(suffix))
    {
        Contract.Assert(res != null);
        Contract.Assert(suffix != null);
        int len = res.Length - suffix.Length;
        Contract.Assert(res != null);
        res = res.Substring(0, len);
        Contract.Assume(res != null); // Postcondition of res
    }

    Contract.Assert(res != null);

    return res;
}
```

s, suffix: NotNull, res : Null

s, suffix, res: NotNull

s, suffix, res: NotNull

s, suffix : NotNull, res: T

s, suffix, res: NotNull



What we did?

- We over-approximated the semantics
- We kept the concrete specification



Example: Numerical analysis

```
static public int GCD(int x, int y)
{
    Contract.Requires(x > 0);
    Contract.Requires(y > 0);

    Contract.Ensures(Contract.Result<int>() > 0);

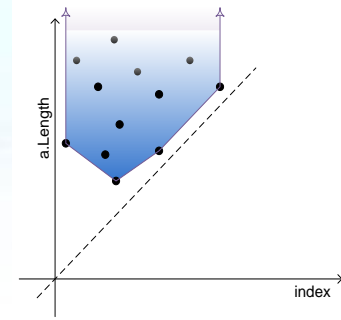
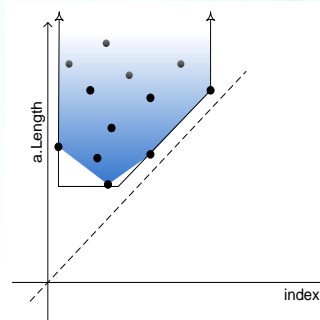
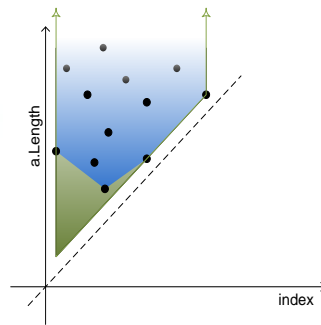
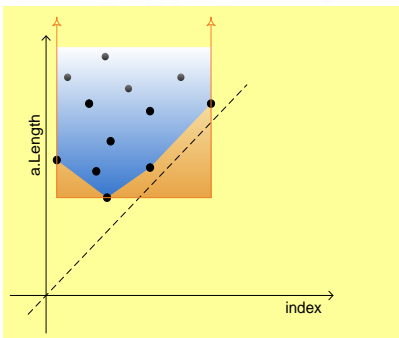
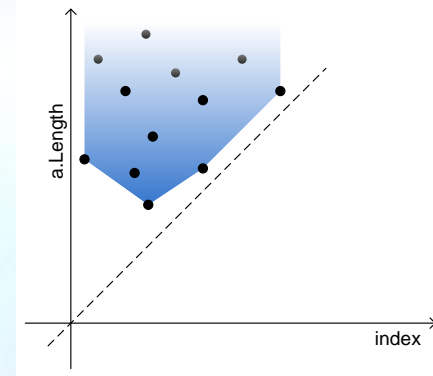
    while (true)
    {
        if (x < y)
        {
            y %= x;
            if (y == 0)
                return x;
        }
        else
        {
            x %= y;
            if (x == 0)
                return y;
        }
    }
}
```

We need numerical reasoning

We need to infer loop invariants

Numerical Analysis

- $0 \leq \text{index} < \text{array.Length}$?



Intervals

$O(n)$

$a \leq x \leq b$

No ☹️

Pentagons

$O(n)$

$a \leq x \leq b \ \& \ x < y$

Yes 😊

Octagons

$O(n^3)$

$\pm x \pm y \leq a$

Yes 😊

Polyhedra

$O(2^n)$

$\sum a_i x_i \leq b$

Yes 😊

Intervals

- Approximate each variable with a range
[a, b] where $a, b \in \mathbb{Z} \cup \{+\infty, -\infty\}$
- More complex in reality because of
 - Overflows
 - Different Int types (16, 32, 64 bits, signed/unsigned)
- Idea: Replace a value, a set of values with an interval

Example

```
static public int GCD(int x, int y)
{
    Contract.Requires(x > 0);
    Contract.Requires(y > 0);

    Contract.Ensures(Contract.Result<int>() > 0);

    while (true)
    {
        if (x < y)
        {
            y %= x;
            if (y == 0)
                return x;
        }
        else
        {
            x %= y;
            if (x == 0)
                return y;
        }
    }
}
```

x : [1, +∞] y : [1, +∞]

x : [1, +∞] y : [1, +∞]

x : [1, +∞], y : [2, +∞]

x : [1, +∞], y : [0, +∞]

x : [1, +∞], y : [1, +∞]

x : [1, +∞], y : [1, +∞]

x : [0, +∞], y : [1, +∞]

x : [1, +∞], y : [1, +∞]

Loop invariant!



Bounds checking example

```
public void AllToZero(int[] a)
{
    for (int i = 0; i < a.Length; i++)
    {
        Contract.Assert(i >= 0);
        Contract.Assert(i < a.Length);

        a[i] = 0;
    }
}
```

a.Length : [0, +∞] i : [0, +∞]



Not Ok!

What are we missing?

- Intervals keep only numerical information
- No symbolic information
 - Ex. $i < a.Length$
- No relations
- Intervals are an example of a non-relational domain
 - Non-null is non-relational too

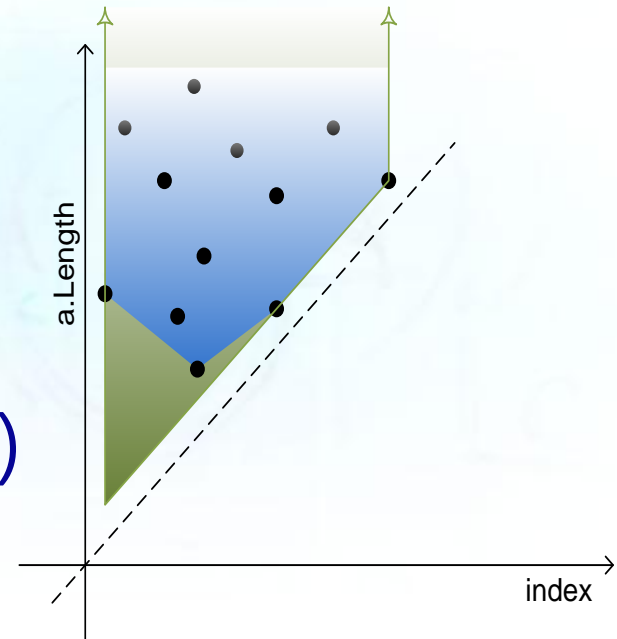
Pentagons



- Capture properties in the form of

$$x \in [a, b] \wedge x < y$$

- x, y variables
- a, b constants
- Elements are pairs of maps
($\text{Var} \rightarrow \text{Intv}$) \times ($\text{Var} \rightarrow \wp(\text{Var})$)
- Information is propagated
 - "reduction"



Subpolyhedra



- Needed for more complex examples
- $\sum a_i x_i \leq k \Leftrightarrow \sum a_i x_i = \beta \wedge \beta \leq k$
 - Introduce a slack variable β
- Reduced product of
 - **Intervals**
 - Scalable, fast...
 - **Linear Equalities**
 - Precise join, fast ...
- Challenge: Have a precise Join

Inferring array contents...

```
public void Init(int N)
{
    Contract.Requires(N > 0);

    int[] a = new int[N];
    int i = 0;

    while (i < N)
    {
        a[i] = 222;
        i = i + 1;
    }

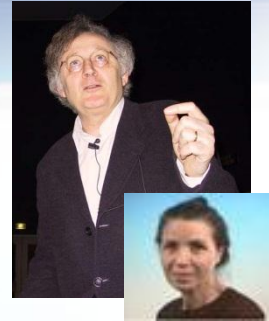
    Contract.Assert( $\forall k \in [0, N). a[k] == 222$ );
}
```

Challenge 1:
Effective handling of disjunction

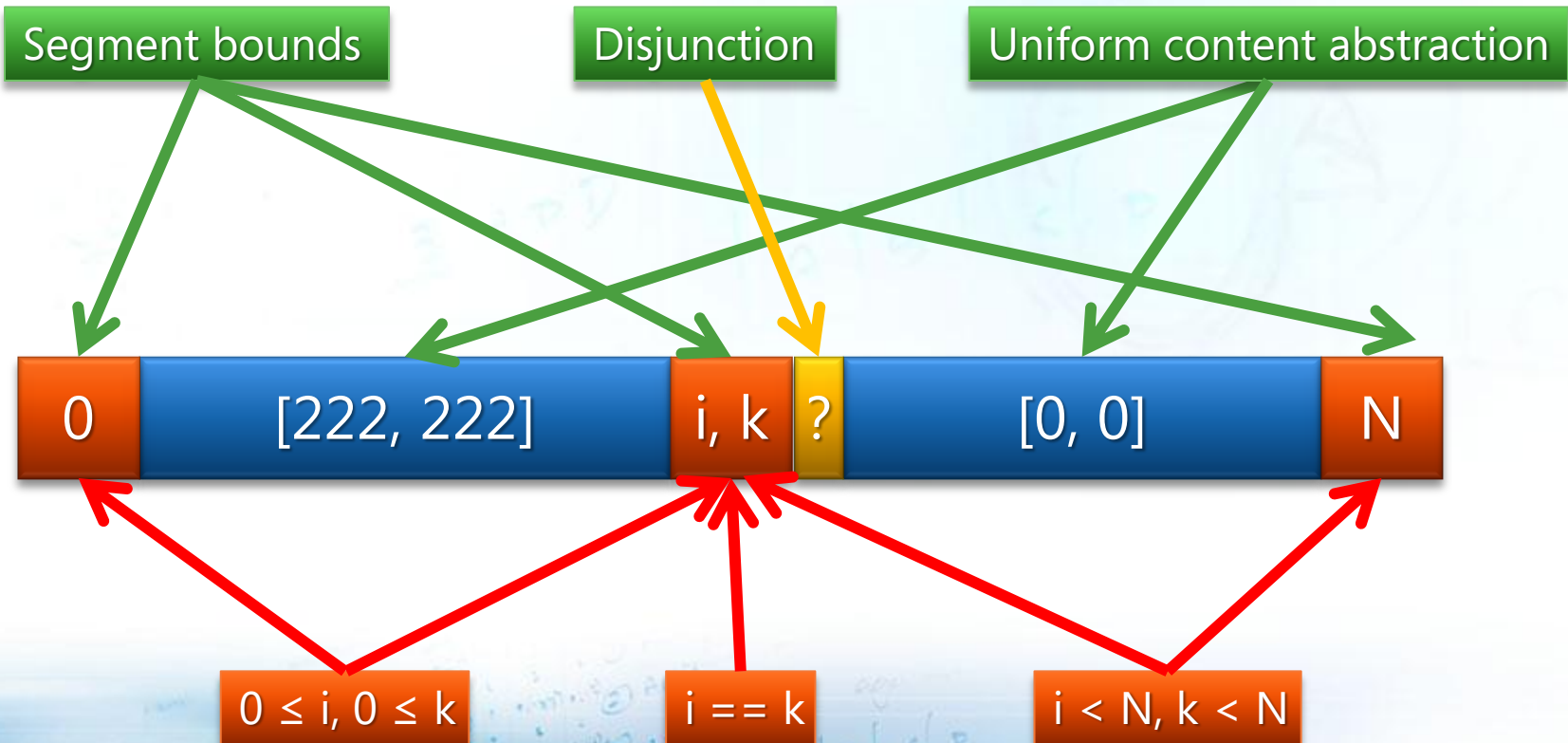
If $i == 0$ then
a not initialized
else if $i > 0$
 $a[0] == \dots a[i] == 222$
else
impossible

Challenge 2:
No overapproximation (can be unsound)
(no hole, *all* the elements are initialized)

Our idea



- Precise and very very fast!
- Basis: Array segments



Example

```
Contract.Requires(N > 0);  
int[] a = new int[N];
```

```
int i = 0;
```



```
assume i ≥ N
```

```
assume i < N
```



```
a[i] = 222;
```

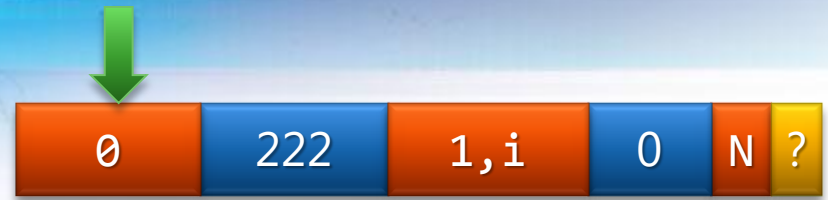
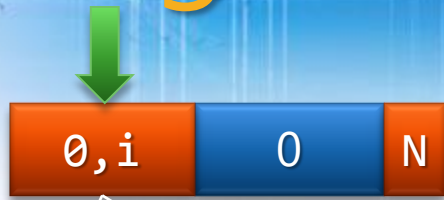


```
j = i+1;
```



```
i -> _  
j -> i  
N -> N
```

Segment unification



Join

Can be empty segments!
(Disjunction)



Example

```
Contract.Requires(N > 0);  
int[] a = new int[N];
```

```
int i = 0;
```



```
assume i ≥ N
```

Remove doubts

```
(i == N && N > 0) && i < N
```



We visited all the elements in [0, N)



```
a[i] = 222;
```

```
j = i+1;
```

And so on up to a fixpoint ...

```
i -> _  
j -> i  
N -> N
```

Algorithm: High level

- For each assembly A, class C, method M
 1. Extract the proof obligations
 - What should I prove?
 2. Run the analyses
 - Discover facts on the program
 3. Use the facts to prove the proof obligations
 - If not, do something else...

Proving things

- We inferred many facts on the program
- We use those to prove assertions
- Algorithm:
 - For each assertion a at program point p
 - For each set of facts F
 - Check if $F(p)$ implies a :
 - True: It is always ok
 - False: It is always not ok
 - Bottom: The assertion is never reached
 - Top: We do not know

Why do we get Top?

- The analysis is not precise enough
 - Abstract domain not precise
 - Widening loses too many constraints
 - Algorithmic properties
 - Implementation bug
 - Incompleteness
- Some contract is missing
 - Precondition or Postcondition
 - Object-invariant
- The assertion is sometimes wrong

Incremental analysis in Clousot

- First analyze with “cheap” domains
 - If check != Top
Done!
 - If check == Top
Try a more precise domain
- On the average great performance gains
 - Persist analysis options in different runs



Disjunctions

- (So far) Join approximates disjunction
 - Compact representation
- Sometimes not enough:

```
public int Simple(bool b)
{
    int z;
    if (b)
        z = 12;
    else
        z = -12;
    return 1 / z;
}
```

```
public string Simple2(bool b)
{
    Contract.Ensures(
        Contract.Result<string>() == null
        || Contract.Result<string>().Length > 0);

    if (b)
        return null;
    else
        return "Ciao!";
}
```

The solution in Clousot

- Backward analysis
- The failing assertion is pushed back to the program



```
public int Simple(bool b)
{
    int z;
    if (b)
        z = 12;
    else
        z = -12;

    return 1 / z;
}
```

$z : [12, 12]$

$z \neq 0$

$z : [-12, -12]$

$z \neq 0$

$z : [-\infty, +\infty]$

$z \neq 0$

More complex example

```
public string Simple2(bool b)
{
    Contract.Ensures(
        Contract.Result<string>() == null
        || Contract.Result<string>().Length > 0);

    if (b)
        return null;
    else
        return "Ciao!";
}
```


Example with loop

```
public void NonNull()  
{  
    string foo = null;  
  
    for (int i = 0; i < 5; i++)  
    {  
        foo += "foo";  
    }  
  
    Contract.Assert(foo != null);  
}
```

foo: Null

~~foo: null~~

foo: T

foo: NotNull

foo != null

foo: T

foo != null

Contract Inference



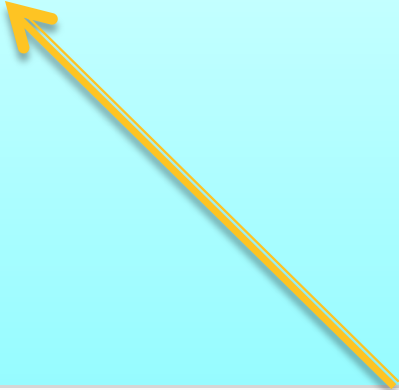
Ideal world



- Programmers write all the contracts
 - Even loop invariants?
- Reality
 - Should infer “evident” contracts

Precondition inference

```
public int ZeroValues(int[] a)
{
    int count = 0;
    for (int i = 0; i < a.Length; i++)
    {
        if (a[i] == 0)
            count++;
    }

    return count;
}
```



-  1 CodeContracts: Suggested precondition: Contract.Requires(a != null);
-  2 CodeContracts: Possible use of a null array 'a'

The problem

- An inferred precondition should
 - Remove bad runs
 - Keep all the good runs
- Several algorithms in Clousot
 - Precision/cost tradeoff

Static Checking

| | | |
|---|---|--|
| <input checked="" type="checkbox"/> Perform Static Contract Checking | <input checked="" type="checkbox"/> Check in Background | <input checked="" type="checkbox"/> Show squiggles |
| <input checked="" type="checkbox"/> Implicit Non-Null Obligations | <input type="checkbox"/> Implicit Arithmetic Obligations | <input type="checkbox"/> Cache Results |
| <input checked="" type="checkbox"/> Implicit Array Bounds Obligations | <input type="checkbox"/> Redundant Assumptions | <input type="checkbox"/> Show Assumptions |
| <input type="checkbox"/> Implicit Enum Writes Obligations | <input type="checkbox"/> Implicit Pointer Usage Obligations | |
| <input checked="" type="checkbox"/> Infer Requires | <input checked="" type="checkbox"/> Suggest Requires | <input checked="" type="checkbox"/> Disjunctive Requires |
| <input type="checkbox"/> Infer Ensures | <input checked="" type="checkbox"/> Suggest Ensures | |
| <input type="checkbox"/> Infer Invariants for readonly | <input type="checkbox"/> Suggest Invariants for readonly | |

low hi

Baseline Warning Level:

The solution

- Propagate a failing assertion the entry
- If it respects the visibility rules,
 - then it is a precondition
- Otherwise
 - Try to suggest as object invariant
 - E.g. assertion on private fields on public method
 - Try to suggest as an assumption
 - The programmer is making some implicit assumption

Postcondition inference: theory

- Have a method m
- For each program point
 - Abstract state a
 - Approximate the concrete states at that point
- Take the abstract state at the exit point of the method

```
public int HalfSum(int x, int y)
{
    Contract.Requires(x >= 0);
    Contract.Requires(y >= 0);

    return x + (y - x) / 2;
}
```

CodeContracts: Suggested postcondition: `Contract.Ensures(Contract.Result<System.Int32>() >= 0);`

In practice

- Filter locals
- Take into account inheritance rules
- Remove redundant information
 - Ex. $x \geq 0, y == 0, x + y \geq 0$
- Avoid suggesting existing precondition
- ...

Message prioritization



So we have a Top...

- We should report it to the programmer
- It can be:
 - a real bug?
 - a false positive?
- In general impossible to tell
 - Undecidability of the analysis
- Should sort all the messages
 - The one most likely to be bugs at the top

1. Warning partitioning

- Partition warnings in classes
 - Contract violation
 - Non-null
 - Arrays
 - Overflows
 - ...
- Assign a *fixed* reward R to each class
 - $R \in [C \rightarrow \mathbb{N}]$
- The highest the reward the more important

2. Scale rewards with outcome

- False = $1.0 * R(c)$
 - Important
 - Always wrong...
- Bottom = $0.75 * R(c)$
 - Unreached, we wanted it?
- Top = $0.50 * R(c)$
 - So many ...
- True = $0 * R(c)$
 - Don't care

3. Scale rewards with info

- Proof obligation p contains
 - Variables from parameters
 - Variables result of a method call
 - ...
 - ...
- The scale the reward

```
public foo(int z)
{
  // ...
  Contract.Assert(z + x > 0);

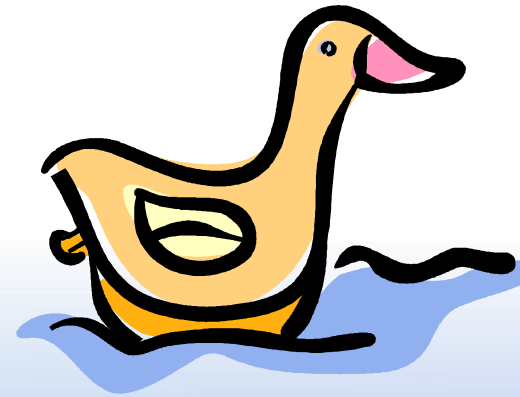
  var f = Add();
  Contract.Assert(f != null);
  // ...
}
```

Caching

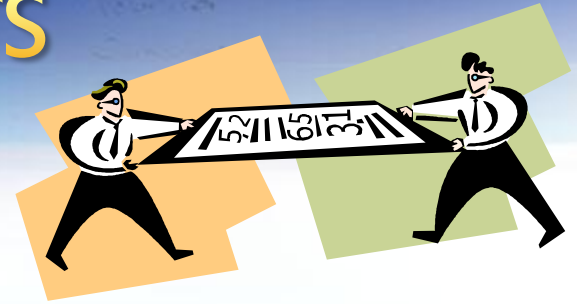
Caching?

- At design time, few changes between two builds
- Avoid re-analysis by caching
- Algorithm
 - Construct the CFG for the method
 - Includes contracts explicit/inferred
 - Hash the CFG
 - If in the DB, just report the same output
 - Otherwise, re-analyze the method
 - Save it in the cache

Floating points...



Computers & numbers



- Computers crunch numbers
- But computer numbers are not mathematical ones!
- Plethora of Int*
 - Int8, Int16, Int32, Int64, BigInt
 - UInt8, UInt16, UInt32, UInt64
- And even more fun:
Floating points

$Y > 0 \Rightarrow X + Y > X?$

True: Epsilon > 0



```
Contract.Assert(Double.Epsilon != Double.Epsilon * Double.Epsilon);
```

```
Contract.Assert(1.0d == 1.0d + Double.Epsilon);
```



```
Contract.Assert(1000000000d == 1000000000d + Double.Epsilon);
```



True!

$$(x + k) - (x - k) == 2k?$$

```
double x, y, z, r;  
  
x = 1.000000019e+38d;  
y = x + 1.0e21d;  
z = x - 1.0e21d;  
r = y - z;  
  
Contract.Assert(r == 2.0e21d);
```



Assert is false!

X == X?

Assert is true!

```
Contract.Assert(0.0 == 0.0);
```

```
Contract.Assert(Double.NegativeInfinity == Double.NegativeInfinity);
```

```
Contract.Assert(Double.NaN == Double.NaN);
```

Assert is false!!!!!!

1/0 is NaN

Sqrt(-1) is NaN

$$K \neq 0 \Rightarrow (x + k) - (x - k) \neq 0$$

```
double x, y, z, r;  
  
x = 1.000000019e+38d;  
y = x + 1.0e21d;  
z = x - 1.0e21d;  
r = y - z;  
  
Contract.Assert(r == 0.0d);
```



Assert is true!

X == X?

```
public class Point
{
    public double X, Y;

    Point(double x, double y)
    {
        this.X = x;
        this.Y = y;
    }
}

public CreatePoint(double x)
{
    var p = new Point(x, x);

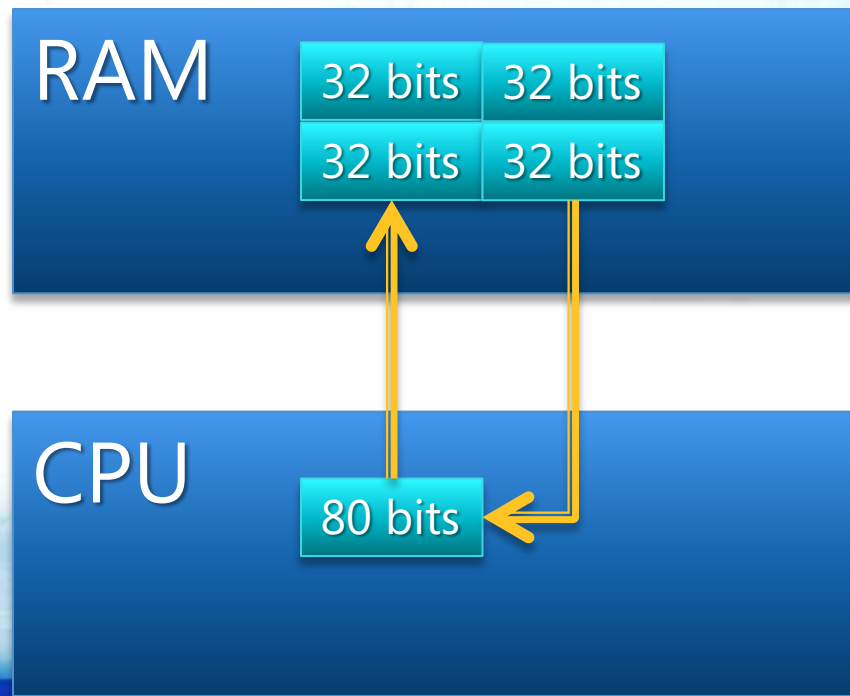
    Contract.Assert(x == p.X);
}
```

Assert is false!!!!!!



Why?

- A double is a synonym for Float64
- A Float64 is represented
 - in RAM with 64 bits
 - in the CPU with 80 bits!!!



Conclusions...

CodeContracts

- Specify code with code
 - No change to the build environment
 - Part of .NET v4
- Documentation generation
- Runtime checking
- Static checking
 - Based on abstract interpretation
 - Predicatable, tunable, scalable, automatic!!!!
- Try it today!!!!