Problem 1 (10 points):
Page 112, Exercise 12.

Problem 2 (10 points):
Page 189, Exercise 3.

Problem 3 (10 points):
Page 191, Exercise 6

## Problem 4 (10 points):

Page 195, Exercise 14.

## Problem 5 (10 points):

Let $G=(V, E)$ be a directed graph, where each edge $e=(u, v)$ has a value $r_{e}$ with $0 \leq r_{e} \leq 1$ that represents the reliability of a communication channel from $u$ to $v$. We interpret $r_{e}$ as the probability that the channel from $u$ to $v$ will not fail, and we assume that these probabilities are independent. Give an efficient algorithm to find the most reliable path from vertex $s$ to vertex $t$.

## Problem 6 (10 points):

Let $G=(V, E)$ be a directed graph with integer edge weights in the range $0, \ldots, 10$. Modify Dijkstra's algorithm to compute the shortest paths from a given source vertex $s$ in $O(n+m)$ time where $n=|V|$ and $m=|E|$.

