# CSE524 Parallel Computation 

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## Announcements

- Recall that you need to turn in a brief (paragraph) description ON PAPER of your progress on the project this week
- Account information given out after break


## Comment on Projects

- As the civil rights song puts it, "Keep your eyes on the prize."
n I want to understand conceptually how you used parallelism to solve your problem
n I want to understand how your P1 works
n I want to know how you analyzed P1's |lism using the CTA model and other classroom material to understand its parallel performance
n I want to know what you did in response to create P2 and how P2 works
Once that's done, anything else is gravy ... I like gravy


## ZPL

- ZPL, a research parallel language w/ 3 goals
n Performance $==$ as good as platform-specific custom code
n Portability $==$ runs well on all platforms
n Convenience ==clean, easy-to-understand programs; no parallel grunge
- Developed at UW by 6 really smart grad students: Brad Chamberlain, Sung-Eun Choi, Steve Deitz, E Chris Lewis, Calvin Lin, Derrick Weathersby


## ZPL Is Important To Us

- ZPL is our representative high-level parallel language ... few competitors because achieving those goals is tough
- To realize a solution ...
$n$ ZPL is designed and built on the CTA
$n$ ZPL is the first high-level language to achieve "performance portability"
n ZPL presents programmers with a visually-cued performance model: WYSIWYG
n ZPL is insensitive to shared or message passing architectures, making it universal

ZPL is "designed from first principles"

## Today's Plan

- Example programs with discussion of principles
- Key language features
- Review of pgmming w/ performance model
- WYSIWYG performance model
n Reflect on Life


## Conway's Game of Life

- Life: organisms w/2,3 neighbors live, birth occurs w/ 3 neighbors; death otherwise; world is a torus

- Organism in next generation if position is alive in this generation and has 2 neighbors, or in this generation it has 3 neighbors
- Or: (thisGen \&\& neighbors==2) || (neighbors==3)

See Life As An Array Computation $\qquad$

## Compute Over Whole Arrays

- Count neighbors by adding organisms (bits)


TW@^nw is the array of Northwest neighbors

## Express Array Computation in ZPL



## Life $\ln$ ZPL

```
program Life;
Conway's Life
config const n : integer = 10; The world is n }\timesn\mathrm{ ; default to 10
region R = [1..n, 1..n]; Index set of computation
direction nW = [-1, -1]; no = [-1, 0]; ne = [-1, 1];
    w}=[0,-1]; e=[0, 1]
    SW=[1,-1]; so= [1, 0]; se= = [1, 1];
var TW: [R] boolean;
    NN : [R] sbyte;
procedure Life();
begin -- Initialize the world
[R] repeat
NN := TW@^nW + TW@^no + TW@^n ne Add 8 nearest neighbor bits (type
            +TW@^W + TW@^e coercion like C); carat(^) means
            + TW@^SW + TW@^so + TW@^se; toroidal neighbor reference
            TW := (TW & NN = 2) | (NN = 3); Update world with next generation
    until !(|<< TW);
        Continue till all die out
end;

\section*{Life \(\ln\) ZPL -- The Detail}
program Life;
config const n : integer \(=10\);
region \(R=[1 \ldots n, 1 \ldots n]\);
direction nw \(=[-1,-1] ;\) no \(=[-1,0] ;\) ne \(=[-1,1]\);
\(w=[0,-1] ; \quad e=[0,1] ;\)
\(S W=[1,-1] ; \operatorname{so}=[1,0] ; \operatorname{se}=[1,1] ;\)
var TW: [R] boolean;
NN : [R] sbyte;
procedure Life();
begin -- Initialize the world
[R] repeat
NN : = TW@^nW + TW@^nO + TW@^ne
+ TW@^W + TW@^e
+ TW@^SW + TW@^SO + TW@^SE;
Topics
"Typical" Form
Regions
Directions
Config Vars
Reduce
TW \(:=(\) TW \& NN \(=2) \mid(\mathrm{NN}=3) ;\)
until ! \((\mid \ll\) TW);

\section*{Regions, A Key ZPL Idea}
- Regions are index sets ... not arrays
- Any number of dimensions, any bounds
\[
\text { region } V=[1 . . n] \text {; }
\]
region \(R=[1 . . m, 1 . . m] ; B\) BigR \(=[0 . . m+1,0 . . m+1] ;\)
region Left \(=[1 . . \mathrm{m}, 1]\);
region Odds = [1..n by 2];
- Short names are preferred--regions are used everywhere--and capitalization is a coding convention
- Naming regions is recommended, but literals are OK

\section*{Using Regions to Declare Arrays}
- Regions are used to declare arrays ... it's like adding data to the indices
- Capitals are used by convention to separate arrays from scalars
- Named or literal regions are OK
\(\operatorname{var} A, B, C:[R]\) double;
var Seq: [V] boolean;
var Huge : \(\left[0.2^{\wedge} n,-5 . .5\right]\) float;
- Regions are used once; no array has more than one region component
- Regions are a source of parallelism...

\section*{Regions Control Computation}
- Statements containing arrays need a region to specify which items participate
\([1 . . n, 1 . n] A:=B+C ;\)
\([R] A:=B+C ; \quad\)-- Same as above
- Regions are scoped
\begin{tabular}{cl}
\(0[R]\) begin & All array computations in compound \\
\(\ldots\) & statements are performed over indices \\
{\([\) Left \(]\)} & in \([R]\), except statement prefixed by \\
end; & {\([\) Left \(]\)}
\end{tabular}
- Operations over region elements performed in parallel

\section*{Parallelism In Statement Evaluation}
- Let A, B be arrays over [1..n, 1..n], and C be an array over [2..n-1,2..n-1] as in
var \(A, B:[1 . . n, 1 . . n]\) float; \(C:[2 . . n-1,2 . . n-1]\) float;
- Then
\([2 . . n-1,2 . . n-1] A:=C ;\)

[2..n-1,2..n-1] \(C:=A+B ;\)

[2..n-1,2] \(A:=B ;\)


\section*{@ Uses Regions \& Directions}

The @ operator combines regions with directions to allow references to neighbors
- Two forms, standard(@) and wrapping(@^)
n Syntax: A@east A@^east
- Semantics: the direction is added to elements of region giving new region, whose elements are referenced; think of a region translation
[1..n, 1..n] A :=A@^east; -- shift array left with wrap around

- @-modified variables caan appear on l or r of :=

\section*{Parallelism In Statement Evaluation}
- Let
var \(A, B:[1 . . n, 1 . . n]\) float; \(C:[2 . . n-1,2 . n-1]\) float; direction east \(=[0,1] ;\) ne \(=[-1,1]\);
- Then
\([2 . \mathrm{n}-1,2 . . \mathrm{n}-1] \mathrm{A}:=\mathrm{C} @^{\wedge}\) east;

\([2 . . n-1,2 . . n-1] A:=C @ \wedge n e+B @^{\wedge} n e ;\)


\section*{Reductions, Global Combining Operations}
- Reduction ( \(\ll\) ) "reduces" the size of an array by combining its elements
- Associative (and commutative) operations are \(+\ll,{ }^{*} \ll, \& \ll, \mid \ll\), max \(\ll\), min \(\ll\)
[1..n, 1..n] biggest := \(\max \ll A\);
[R] all_false :=1<< TW;
- All elements participate; order of evaluation is unspecified ... caution floating point users
- ZPL also has partial reductions, scans, partial scans, and user defined reductions and scans

\section*{Operations On Regions}
- The importance of regions motivates region operators
- Prepositions: at, of, in, with, by ... take region and direction and produce a new region
- at translates the region's index set in the direction
- of defines a new region adjacent to the given region along direction edge and of direction extent

var X, Y : [R] byte;
\(\mathrm{n}=[-1,0]\)
ne \(=[-1,1]\);


\section*{Applying Ideas: Jacobi Iteration}

- Model heat defusing through a plate
- Represent as array of floating point numbers
- Use a 4-point stencil to model defusing
- Main steps when thinking globally

\section*{Initialize}

Compute new averages
Find the largest error
Update array
until convergence
High-level Language should match high-level thinking

\section*{"High Level" Logic Of J-Iteration}
```

program Jacobi;
config var n : integer = 512;
eps : float = 0.00001;
R}=[1···n,1···n]
BigR = [0···.n+1,0···.n+1];
direction N}=\mathbf{N}=[-1,0]; S=[1,0]
E = [ 0, 1]; W = [ 0, -1];
var Temp: [R] float;
A : [BigR] float;
err: float;
procedure Jacobi();
[R] begin
[BigR] A := 0.0;
[S of R] A := 1.0;
Initialize Compute new averages Find the largest error Update array until convergence
repeat
Temp := (A@N + A@E + A@S + A@W)/4.0;
err := max<< abs(Temp - A);
A := Temp;
until err < eps

```
                end;

\section*{Reduce}
- ZPL has 'full' reduce: \(+\ll\), * \(\ll\), max \(\ll, \ldots\)
- ZPL also has 'partial' reduce
n Applies reduce across rows, down columns,...
n Requires two regions:
- One region on statement, as usual
- One region between operator and operand
\([1 . . n, 1] B:=+\ll[1 . . n, 1 . . n] A ; \quad-\) add across rows
\([1,1 . n] C:=\min \ll[1 . n, 1 . . n] A ;-\) min down columns
n In these examples, result stored in 1 st row/col
Collapsed dimensions indicate reduce dimension(s)

\section*{Flood -- Inverse of Partial Reduce}
- Reduce "reduces" 1 or more dimensions
- Opposite is flood -- fill 1 or more dimensions
\([1 . . n, 1 . . n] B:=\gg[1 . . n, 1] A\);

\([1 . n, 1 . n] B:=\gg[1 . n, n] A ;\)

- The replication uses multicast, often an efficient operation

\section*{Closer Look At Scaling Each Row}
[1..m,1] MaxC \(:=\max \ll[1 . . m, 1 . . n] A ;\) Max of each row
[1..m, 1..n] \(A:=A / \gg[1 . . \mathrm{m}, 1]\) MaxC; Scale each row
- Flooding distributes values (efficiently) so that the computation is element-wise ... lowers communication
\begin{tabular}{ccccccccc}
2 & 4 & 4 & 2 & 4 & 4 & 4 & 4 & 4 \\
0 & 2 & 3 & 6 & 6 & 6 & 6 & 3 & 6 \\
3 & 3 & 3 & 3 & 3 & 3 & 3 & 3 & 3 \\
8 & 2 & 4 & 0 & 8 & 8 & 8 & 8 & 8 \\
& \(A\) & & \(M a x C\) & \(\gg[1 . . m, 1]\) MaxC
\end{tabular}

\section*{Flood Regions and Arrays}

Flood dimensions recognize that specifying a particular column over specifies the situation Need a generic column -- or a column that does not have a specific position ... use "*) as value region FlCol \(=[1 . . \mathrm{m}, ~ *] ; \quad--\) Flood regions FlRow \(=[*, 1 \ldots\) n \(] ;\)
var MaxC : [FICol] double; --An m length col
Row : [FlRow] double; --An \(n\) length row
[1...m,*] MaxC \(:=\max \ll[1 . . m, 1 \ldots n] A ;--B e t t e r\) in every position

\section*{Flood arrays (continued)}

Since flood arrays have some unspecified dimensions, they can be "promoted" in those dimensions, i.e logically replicated
- Scaling a value by max of row w/o flooding:
\[
\begin{array}{rrr}
{[1 \ldots m, *]} & \operatorname{Max} C & :=\max \ll[1 \ldots \mathrm{~m}, 1 \ldots \mathrm{n}] \\
{[1 \ldots \mathrm{~A} ;}
\end{array}
\]

The promotion of flooded arrays is only logical

\section*{Flood \(v\). Singleton Difference}
- Lower dimensional arrays can specify a singleton or a flood ... it affects allocation
 Region [1..n,1..n] allocated to 4 processors

Regions [1...n,1] and [n,1..n] allocated to 4 processors


\section*{SUMMA Algorithm}

For each col-row in the common dimension, flood the item and combine it...
```

$\operatorname{var} A:[1 \ldots m, 1 \ldots n]$ double;
$B:[1 \ldots n, 1 \ldots p]$ double;
C: $[1 . . \mathrm{m}, 1 \ldots \mathrm{p}]$ double;
Col:[ 1..m,*] double;
Row: $[*, 1 \ldots p]$ double;
[1..m,1..p] $C:=0.0 ;$
for $k:=1$ to $n /$ do
[1..m,*] Col $:=\gg[, k] A ;--F l o o d k t h$ col of $A$
$[*, 1 \ldots p]$ Row $:=\gg[k] B ;,--F l o o d$ kth row of $B$
[1..m,1..p] C +=Col*Row; -- Combine elements
end;

```

\section*{SUMMA, The First Step}
\begin{tabular}{|c|c|c|c|}
\hline c11 c12 c13 & a11 & al2 al3 al4 & b11 b12 b13 \\
\hline c21 c22 c23 & a21 & a22 a23 a24 & b 21 b 22 b 23 \\
\hline c31 c32 c33 & a31 & a32 a33 a34 & b31 b32 b33 \\
\hline c41 c42 c43 & a 41 & a42 a43 a44 & b41 b42 b43 \\
\hline
\end{tabular}

Col Row C all a11 all b11 b12 b13 allb11 a11b12 allb13 a21 a21 a21 \(\times\) b11 b12 b13 \(=\) a 21 b11 a21b12 a \(a 1 \mathrm{~b} 13\) a31 a31 a31 b11 b12 b13 a31b11 a31b12 a31b13 a41 a41 a41 b11 b12 b13 a41b11 a41b12 a41b13

> SUMMA is the easiest MM algorithm to program in ZPL

\section*{SUMMA Algorithm (continued)}

For each col-row in the common dimension, flood the item and combine it...
\[
\begin{aligned}
& \text { [1..m, 1..p] } C:=0.0 ; \quad \text {-- Initialize } C \\
& \text { for } k:=1 \text { to } n \text { do } \\
& \text { [1...m,*] Col }:=\gg[, k] A ;--F l o o d k t h \text { col of } A \\
& \text { [*,1..p] Row : }=\gg[k,] B ;-- \text { Flood } k t h \text { row of } B \\
& \text { [1..m,1..p] C }+=\text { Col*Row; -- Combine elements } \\
& \text { end; } \\
& \text {--- or, more simply }- \text {-- } \\
& \text { for } k:=1 \text { to } n \text { do } \\
& {[1 . . m, 1 \ldots p] \quad C+=(\gg[, k] A) *(\gg[k,] B) \text {; }} \\
& \text { end; }
\end{aligned}
\]

\section*{Still Another MM Algorithm}

If flooding is so good for columns/rows, why not use it for whole planes?
region \(\mathrm{IK}=[1 \ldots \mathrm{n}, *, 1 \ldots \mathrm{n}]\); JK \(=[*, 1 \ldots n, 1 \ldots n]\); IJ \(=[1 \ldots \mathrm{n}, 1 \ldots \mathrm{n}, \star]\); IJK \(=[1 \ldots n, 1 \ldots n, 1 \ldots n]\);
[IJ] A2 := >>A\#[Index1, Index2];
[JK] B2 := >>B\#[Index2, Index3];
[IK] \(\quad \mathrm{C}:=+\ll[\mathrm{IJK}](\mathrm{A} 2 * \mathrm{~B} 2)\);


\section*{Partial Scan}
- Partial scans are possible too, but unlike reduction they do not reduce dimensionality, so the compiler cannot tell which dimension to reduce ... so specify

\(+\|[2] \begin{array}{rrrrrrrr}1 & 1 & 1 & 1 & 1 & 2 & 3 & 4 \\ 1 & 1 & 1 & 1 & 1 & 2 & 3 & 4 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4\end{array}\)

\section*{Recalling Reduce, Scan \& Flood}
- The operators for reduce, scan and flood are suggestive ...
- Reduce << produces a result of smaller size

- Scan || produces a result of the same size

- Flood \(\gg\) produces a result of greater size


\section*{Index1...}
- ZPL comes with "constant arrays" of any size
- Indeximeans indices of the \(i^{\text {th }}\) dimension
[1...n,1...n]begin
\[
\begin{aligned}
& \mathrm{Z}:=\text { Index } 1 ;- \text { fill with first index } \\
& \mathrm{P}:=\text { Index } 2 ;- \text { fill with second index } \\
& \mathrm{L}:=\mathrm{Z}=\mathrm{P} ; \quad-- \text { define identity array } \\
& \text { end; }
\end{aligned}
\]

Indexi arrays: compiler created using no space
\begin{tabular}{llllllllllll}
1 & 1 & 1 & 1 & 1 & 2 & 3 & 4 & 1 & 0 & 0 & 0 \\
2 & 2 & 2 & 2 & 1 & 2 & 3 & 4 & 0 & 1 & 0 & 0 \\
3 & 3 & 3 & 3 & 1 & 2 & 3 & 4 & 0 & 0 & 1 & 0 \\
4 & 4 & 4 & 4 & 1 & 2 & 3 & 4 & 0 & 0 & 0 & 1
\end{tabular}

Indext Index2 \(L\)

\section*{Remap}

The remap operator (\#) implements general data motion, including rank change
- Two cases:

Gather, \(\mathrm{A}:=\mathrm{BH}[\mathrm{C} 1, \mathrm{C} 2]\);
Scatter, A\#[C1,C2]:=B;
- For rrank array, provide rrank \(r\) arrays giving indices to be referenced
- Transpose: AT[i,j] = A[j,i]
[R]AT := A\#[Index2,Index1]; -- Standard ldiom for transpose

\section*{Remap (Gather)}

The index array in the ith position gives the indices for the ith dimension
[R] AT := A\#[Index2,Index1]; -- Idiom for transpose
Gather: For a position, where does value come from
\(\mathrm{a} c \mathrm{e} b \mathrm{~d} f \Leftrightarrow \mathrm{a} \mathrm{b} \mathrm{c} d \mathrm{~d} \mathrm{f}\) \# \(\left[\begin{array}{llllll}1 & 3 & 5 & 2 & 4 & 6\end{array}\right]\)


\section*{Remap (Scatter)}
- Scatter Remap has potential problem in that values can map to the same place ... order is unspecified
... use \(+=\), etc. if not unique
[R] AT\#[Index2, Index1]:=A; - - ddiom for transpose Scatter: For a value, where does it go?
a dbecf\#[1 35246\(] \Leftrightarrow \mathrm{a}\) b c def

b. \(f{ }^{j} n_{\#}\)
c \(\mathrm{gko}^{\circ}\)
dh1p
AT Index2


\section*{Break}

\section*{CTA and ZPL}
- ZPL was built on the CTA
n Semantics of operation customized to CTA
n Compiler targets CTA machines
n Performance model reflects the costs of CTA
- The benefit of building on the CTA:
n Programming constraints are realistic, scalable
n Programs are portable with performance
n Programmers can reliably estimate performance and observe it (or better) on every platform

Building on CTA is a main contribution of ZPL

\section*{Knowing Performance of Programs}
- Recall that in the sequential case, writing in a performance-sensitive language (C), the RAM model describes how the program will run
- Writing in ZPL, the CTA model describes how the program will run
n Programmer needs to know the CTA
n Language constructs' performance must be described in CTA terms
n Information must "compose"
- In CSE524 we've always explained performance this way

\section*{Assumes Many Pts Per Processor}

ZPL allocates regions (and therefore arrays) to processors so many contiguous elements are assigned to each to exploit locality
- Array Allocation Rules
n Union the regions together to compute the bounding region
n Get processor number and arrangement from the command line
n Allocate the bounding region to the processors

\section*{Union The Regions Together}

Create the "footprint" of the regions by aligning


Technical point: Only interacting regions are "unioned," e.g. if region \(R\) is used to declare an array which is manipulated in the scope of region \(S, R\) and \(S\) are said to interact

The bounding region is allocated to processors

\section*{Get Processor Num + Arrangement}

The number and arrangement of processors is given by the programmer on the command line [or programmed; more later]
- For the purpose of [understanding] allocation, processors are viewed as being arranged in grids ... this is simply an abstraction:
The CTA does not favor any arrangement, so use a generic one
\[
\begin{aligned}
& \begin{array}{|l|l|l|l|}
\hline \mathbf{P}_{\mathbf{0}} & \mathbf{P}_{1} & \mathbf{P}_{\mathbf{2}} & \mathbf{P}_{3} \\
\hline \mathbf{P}_{\mathbf{4}} & \mathbf{P}_{5} & \mathbf{P}_{6} & \mathbf{P}_{7} \\
\hline
\end{array}
\end{aligned}
\]

\section*{Allocate Bounding Region to Grid}

The bounding region is allocated to processor grid in the "most balanced" way possible
- Regions inherit their position from their position in the bounding region
- Array elements inherit their positions from their index's position in the region, and hence their


\section*{More Typical Allocations}


- 3D...

\section*{Fundamental Fact of ZPL}

Such allocations are mostly standard, but one fact makes ZPL performance clear:

ZPL has the property that for any arrays A, B of the same rank and having an element [i, ..., k], that element of each will be stored on the same processor


Corollary: Element-wise operations do not require any communication: [R] ... A+B ...

\section*{Performance Model (WYSIWYG)}

To state how ZPL performs operations, each operator's work and communication needs are given ... producing a performance model
\(n\) Performance is given in terms of the CTA
n Performance is relative, e.g. \(x\) is more expensive in communication than \(y\)
- Rules...

A + B -- Element-wise array operations
- No communication
- Per processor work is comparable to C
- Work fully parallelizable, i.e. time = work/P

\section*{Rules Of Operation (continued)}

B+A@^east -- @ references including @^
Arrays allocated with "fluff" for every direction used

- Nearest neighbor point-to-point communication of edge elements, i.e. small communication, little congestion
- Edge communication benefits from surface-to-volume advantage: an \(n\) increase in elements, adds \(\sqrt{ } n\) comm load

0 Local data motion, possibly

\section*{\(\ll \| \gg\)}
\(+\ll\) A -- Reduce
- Accumulate local elements
- O(log P) tree accumulation, or better
- Broadcast, which is worst case \(O(\log P)\), but usu. less

- Accumulate local elements
- Ladner/Fischer O(log P) tree parallel prefix logic
- Update of local elements
>>[1..n,k]A -- Flood
- Multicast array segments, \(O(\log P)\) w.c.
- Represent data "non-redundantly"


\section*{Rules of Operation (continued)}

A\# [I1, I2] -- Remap, both gather and scatter
- (Potential) all-to-all processors communication to distribute routing information implied by I1, I2
- (Potential) all-to-all processors communication to route the elements of \(A\)
- Heavily optimized, esp. to save first all-to-all
- Full information online in Chapter 8 of ZPL Programmer's Guide or in dissertations
- "What you see is what you get" performance model ... large performance features visible

\section*{ZPL is only parallel language with performance model}

\section*{Applying WYSIWYG In Real Life...}
program Life;
config var \(n\) : integer \(=512\);
region \(\quad \mathrm{R}=[1 \ldots \mathrm{n}, 1 \ldots \mathrm{n}]\);
\(B i g R=[0 \ldots n+1,0 \ldots n+1] ;\)
direction \(N=[-1,0] ; N E=[-1,1] ;\)
\(\mathbf{E}=[0,1] ; \operatorname{SE}=[1,1] ;\) \(\mathbf{S}=[1,0] ; S W=[1,-1] ;\)
\(W=[0,-1] ; N W=[-1,-1] ;\)
var NN: [R] ubyte; TW : [BigR] boolean;
procedure Life();
[R] begin
TW \(:=(\) Index \(1 *\) Index 2\() \div 2 ;-\) Make data
repeat
NN : = (TW@N + TW@NE + TW@E + TW@SE
+ TW@S + TW@SW + TW@W + TW@NW); \(T W:=(N N=2 \& T W) \mid\) NN \(=3\); until ! |<<TW;
end;
Code for performance costs implied by WYSIWYG

\section*{Analyzing Life By Color}
- Blue: Effectively no time ... each processor does set-up and scalar computation locally
- Pink: Element-wise computation perfectly parallel ... Indexiconstants are generated

How is TW allocated on 4 procs? Three basic choices...


Delay is \(c \lambda\)

\section*{Analyzing By Color (continued)}

Purple: Element-wise computation with @ operations ... expect \(\lambda\) delay for @ (all at once if synch'ed) and then full parallel speed-up for local operations
- Red: Reduce uses Ladner/Fischer parallel prefix, with local combining and \(\log (P)\) tree to communicate ... potentially the most complex operation in Life

Knowing the relative costs of the program allows us to optimize it for some purpose ... count generations

\section*{How Many Generations?}
- Compute count of generations before life dies out
```

program Life; Add a counter to previous program
config var n : intc, n, 1, n];
direction NW = [-1,-1];N= N=[-1, 0]; NE = [-1, 1];
W=[0,-1]; E=[ 0, 1];
SW=[1,-1];}\textrm{S}=[1,0];\textrm{SE}=[1,[1,1]
var NN:[R] ubyte; TW:[R] boolean; count:integer = 0;
procedure Life();
[R] begin read(TW); -- Input
repeat
count += 1;
NN := (TW@^N + TW@^NE + TW@^E + TW@^\E
+ TW@^S + TW@^SW + TW@^W + TW@^NW);
TW := (NN=2 \& TW) | NN=3;
until ! |<<TW;
writeln(count, " generations");
end;

```

\section*{How Many Generations?}

Testing on each generation my be excessive -- analyze
program Life;
config var \(n:\) integer \(=512\);
region \(\quad R=[1, \ldots, 1, \ldots n]\);
direction \(\mathrm{NW}=[-1,-1] ; \mathbb{N}=[-1,0] ; \mathrm{NE}=[-1,1]\);
\(\mathrm{W}=[0,-1] ; \quad \mathrm{E}=[0,1] ;\)
SW \(=[1,-1] ; \mathrm{S}=[1,0] ; \mathrm{SE}=[1,1] ;\)
var \(\mathbb{N N}:[R]\) ubyte; \(T W:[R]\) boolean; count:integer \(=0\);
procedure Life();
[R] begin read(TW); -- Input repeat
count \(+=1\);
NN : \(=\left(T W @^{\wedge} \mathrm{N}+\mathrm{TW} @^{\wedge} \mathrm{NE}+\mathrm{TW} @^{\wedge} \mathrm{E}+\mathrm{TW}{ }^{\wedge}\right.\) ^SE + TW@^S + TW@^SW + TW@^W + TW@^NW);
TW \(:=(\mathrm{NN}=2\) \& TW\() \mid\) NN=3; until ! <<<TW; writeln(count, " generations"); end;

\section*{Optimize To Reduce End Tests}
```

config var n : integer = 512; epoch : integer = 50;
var NN:[R] ubyte; IW,TWo:[R] boolean; count:integer = 0;
procedure Live(integer:gens);
begin var i : integer;
for i := 1 to gens do
NN := (TW@^N + TW@^NE + TW@^E + TW@^SE
+ TW@^S + TW@^SW + TW@^W + TW@^NW);
TW := (NN=2 \& TW) | NN=3;
end;
end;
procedure Life();
[R] begin read(TW);
while |<<TW do
TWO:=TW; Live(epoch); count += epoch;
end;
Recover State count -= epoch; TW := TWO; -- Roll back
repeat

```


\section*{Optimizations Can Help}
- WYSIWYG is the worst case ... optimizations are possible...
- Sequential Optimizations e.g. stencil opts


Sum of orange items performed once

7 additions are used for each element, but fewer adds are sufficient
- Parallel Optimizations e.g. communication motion -prefetching to overlap communication with computation

\section*{Guarantees}

ZPL uses a different approach to performance than other parallel languages
- Historically, performance came from compiler optimizations that might/might not fire ...
- WYSIWYG guarantees (it's a contract) that ZPL programs will work a certain way ...
n It may be better...WYSIWYG is a worst case that often doesn't materialize
n Aggressive optimizations help a lot If there are any surprises, they'll be pleasant

\section*{Summarizing WYSIWYG Model}
- Data and processing allocations are given
- All constructs of the language are explained in terms of the allocations and the CTA
- Result: relative, worst-case statement of how the computation runs anywhere ... rely on it
- Optimizations can improve on the times, but if they don't fire, nothing is lost

The best use of the WYSIWYG model is to make comparative programming decisions

\section*{Bottom Line for ZPL In 524}
- The reason we're learning ZPL is because it illustrates how a parallel programming language can give access to the CTA machine model, allowing programmers to write intelligent parallel programs
- You want your programming language to have that property, too!
- If it doesn't, dump it and use a library that lets you apply the CTA model yourself

\section*{Homework}
- No Textbook Reading For Next Week
- Project
n Bring paper statement of progress to class```

