

# Introduction to Database Systems

## CSE 544

Lecture #2

January 16, 2007

# Review Questions: NULLS

From Lecture 1:

- What is 3-valued logic ? Why do we need it ?
- What is a left outer join ?
- Why do we sometimes need left outer joins in aggregate queries ?

# Review Question:

## Expressive Power of SQL

From HW1:

- Acted together table:  $A(id1, id2)$ 
  - This is a graph
- Pairs of actors connected by a path of length 2
  - How many joins ?
- Pairs of actors connected by a path of length 5
  - How many joins ?
- Pairs of actors connected by a path of any length
  - How many joins ?

# Review Question: ACID

From the reading assignment  
SQL for Web Nerds:

- What does ACID mean ?

# Discussion of Project/Phase 1

- Task 1: Schema design
- Task 2: Import sample data
- Task 3: Modify starter code

# Task 1: Schema Design

Official requirement

- Read the project description
- Design a “good” database schema

# Task 1: Schema Design

What you should do:

- Read description AND look inside the starter code `App_code/Provided/...`
- Read the classes, determine the fields...

# Task 1: Schema Design

- Optional: draw an E/R diagram
- Create a file:

```
CREATE TABLE Customer ( ... )  
CREATE TABLE Invoice ( ... )  
...
```

- Create a second file:

```
DROP TABLE Customer  
DROP TABLE Invoice  
...
```

(why ?)



# Task 1: Schema Design

Things to worry about:

- Keys/foreign keys: note table order matters!
- Make sure you represent all the data
- Null-able or not (don't worry too muchh)

Things not to worry about:

- fname or FirstName or PersonFirstName ?
- varchar(20) or char(200) or varchar(120) ?

# Task 2: Import Sample Data

- Create a file:

```
INSERT INTO Customer ( ... )  
VALUES ('John', ....)  
INSERT INTO Customer ( ... )  
VALUES ('Sue', ....)  
...
```

- You may need to run this:

```
DROP TABLE Customer  
DROP TABLE Invoice  
...
```

(why ?)

# Task 3: Modify Starter Code

The starter code:

- C#
- ASP.NET (you do not need to understand it)

It provides a Website for accessing your online store  
BUT it misses the fragments of code that get the  
data from the database

See

[http://iisqlsrv.cs.washington.edu/CSEP544/  
Phase1\\_Example/](http://iisqlsrv.cs.washington.edu/CSEP544/Phase1_Example/)

# C# - Crash Course

- Hello World
- Properties (getters/setters)
- Enums
- Partial classes
- Dataset: DataTable, DataRow
- Connecting to a database

<http://www.ecma-international.org/activities/Languages/Introduction%20to%20Csharp.pdf>

# C# - Highlights

- C# = C++.Syntax + Java.Semantics
- It is a “safe” language (like Java)
- Can be embedded in Webpages
- Can access a database
  - Complex, but you should see the predecessors !

# Hello World

```
using System;

class Hello {
    static void Main() {
        Console.WriteLine("Hello world");
    }
}
```

# Properties: Getters and Setters

```
public class Point {  
    private int x;  
    private string c;  
  
    public int position {  
        get { return x; }  
        set { x = value; c = "red"; }  
    }  
  
    public string color {  
        get { return c; }  
        set { c = value; x++; }  
    }  
}
```

```
Point uvw = new Point();  
  
uvw.position = 55;  
uvw.color = "green";  
uvw.position =  
    uvw.position * 2;  
if (uvw.color == "green")  
    ...
```

# Indexers

```
public class Stuff {  
    private int x[];  
  
    public int this[int i] {  
        get { x[2*i+1]=0; return x[2*i]; }  
        set { x[2*i] = value; x[2*i+1]=1; }  
    }  
}
```

```
Stuff uvw = new Stuff();
```

```
uvw[12] = 55;
```

```
uvw[99] = uvw[12]*7 + 2;
```



# Enum

```
enum Color: byte {  
    Red = 1,  
    Green = 2,  
    Blue = 4,  
    Black = 0,  
    White = Red | Green | Blue,  
}
```

# Partial Classes

- Some fields defined in file 1
- Other fields defined in file 2
  
- Why ?  
Nguyen creates file 1, you create file 2

# Dataset

This is an important class that allows you to interact with a database

Dataset = a “mini” database in main memory

- DataTable
- DataRow

# DataSet

```
DataSet myLocalDB = new DataSet();  
  
.....  
..... /* create inside a table called “books” */  
..... /* (this is shown on a following slide) */  
  
/* now use “books” */  
DataTable x = myLocalDB.Tables[“books”]  
  
foreach (DataRow y in x.Rows) {  
    if (y[“title”] == “Harry Potter”) y[“price”]++;  
}
```

# Connecting to a Database

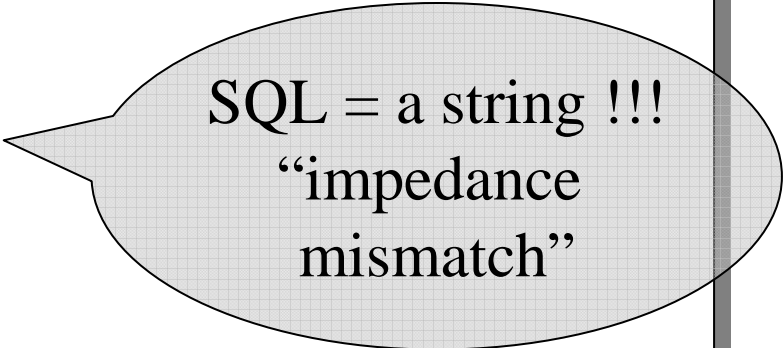
- Create or edit web.config file
  - Specify iisqlsrv, user, password
  - Give a 'name'
- Create a SqlConnection
  - refer to 'name'
- Create a SqlDataAdapter
  - embed SQL query string
- Execute the Fill( ) method to run query and store answers in a datarow

# Connecting to a Database

```
/* create inside a table called "books" */
```

```
SqlConnection c = new SqlConnection( . . . "name" . . . );
```

```
string q = "select title, price year  
from products  
where price < 100";
```



SQL = a string !!!  
"impedance  
mismatch"

```
SqlDataAdapter a = new SqlDataAdapter(q, c);
```

```
DataSet myLocalDB = new DataSet();
```

```
a.Fill(myLocalDB, "books");
```

# Task 3: Modify Starter Code

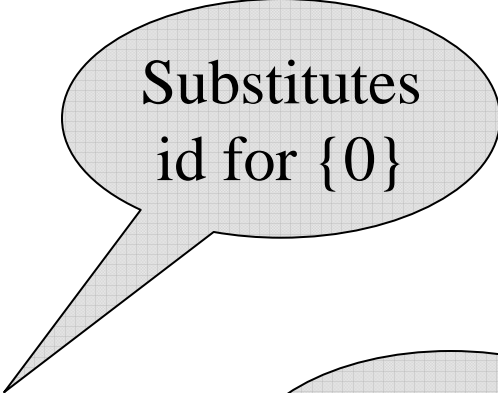
- What you have to do:
- App\_Code/Phase1/Billing and Shipping/...

```
Public partial class Customer {  
    /* add your own fields, like: */  
    private int id,  
  
    Procedure List<invoice> GetInvoices() {  
        /* your GetInvoices code goes here */  
    }  
}
```

# Task 3: Modify Starter Code

```
/* your GetInvoices code goes here */
```

```
string s = String.Format(  
    @“SELECT ...  
    FROM ....  
    WHERE x.customerId = {0} ...”, id);
```



Substitutes  
id for {0}



Defined in  
Provided

```
StoreContext store = StoreContext.current;  
DataSet ds = new DataSet( );  
DataTable invoices = store.GetDataTable(s, ds, “invoices”);  
/* continued on next slide.... */
```



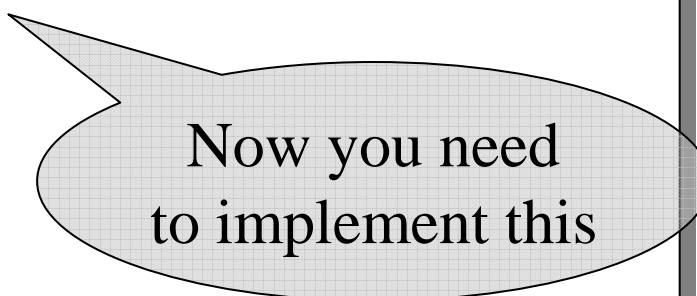
## Task 3: Modify Starter Code

```
/* ... continued from previous slide */
```

```
List<Invoice> invoiceList new List<Invoice> ( );
```

```
foreach(datarow r in invoices.Rows) {  
    invoiceList.Add(new Invoice( r ));  
}
```

```
return invoiceList;  
}
```



Now you need  
to implement this

# Task 3: Modify Starter Code

```
public partial class Invoice {  
    public Invoice(DataRow invoiceData) {  
        /* here goes your code, something like that: */  
        init(invoiceData); /* may need it in several places */  
    }  
    ....  
    private void init(DataRow invoiceData) {  
        invoiceId = (int) invoiceData["invoiceId"];  
        orderDate = (DateTime) invoiceData["date"];  
        ....  
    }  
}
```

In Provided

In you SQL

# Time Estimate

- Task 1: about 9 tables or so, 2 hours or more
- Task 2: try 2 tuples per table, 1 hour
- Task 3: finding out what to do, errors, 7-8 hours

# E/R Diagrams

- E/R diagrams: Chapter 2
- Functional Dependencies and Normal Forms: Chapter 19

# Database Design

1. Requirements Analysis: e.g. Phase 1 of the project
2. Conceptual Database Design: E/R diagrams
3. Logical Database Design: from E/R to relations
4. Schema Refinement: Normal Forms
5. Physical Database Design: indexes, etc
6. Application and security: not covered in this course

# Conceptual Design = Entity / Relationship Diagrams

Objects → entities  
Classes → entity sets



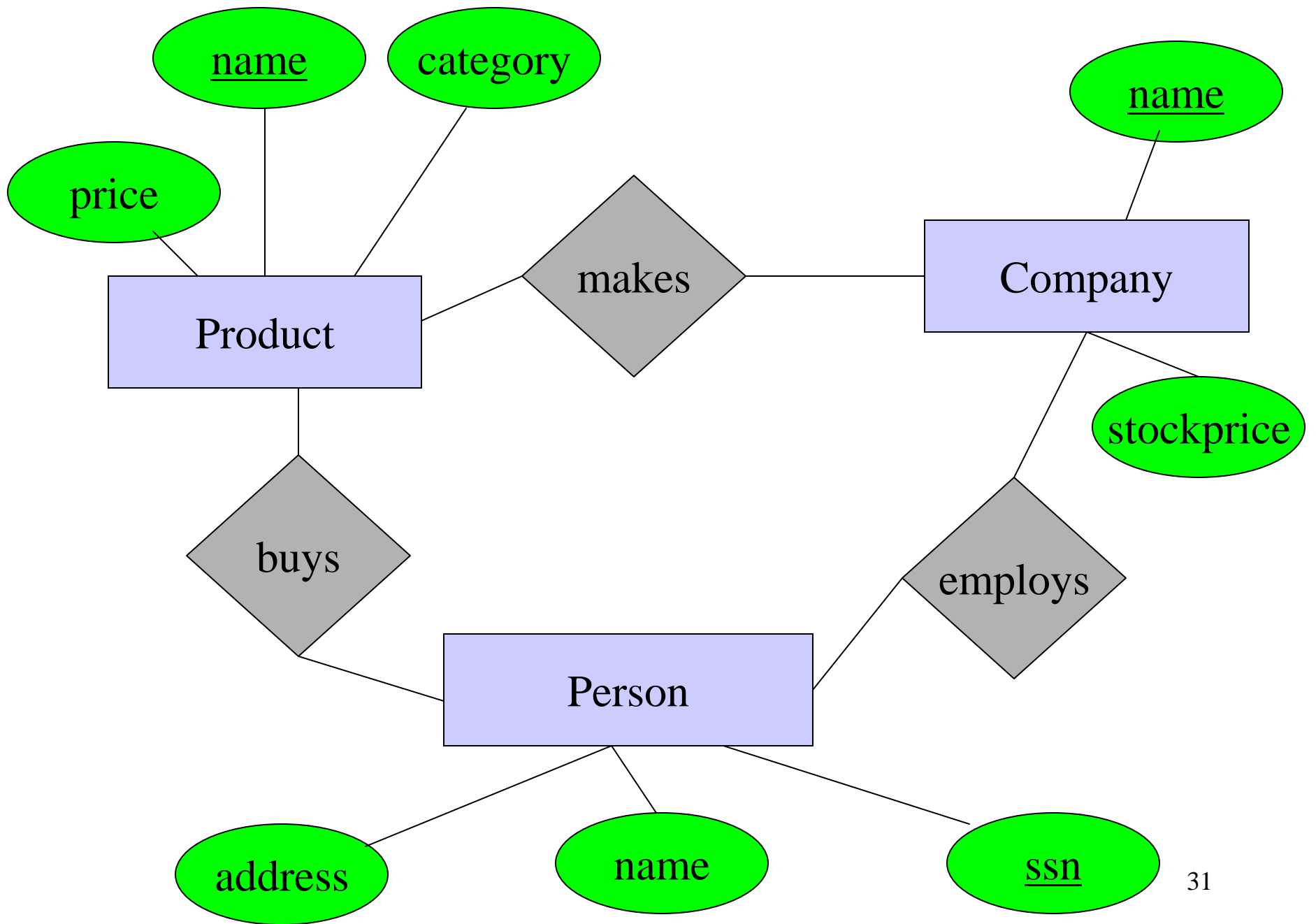
Attributes are like in ODL.



Relationships: like in ODL except

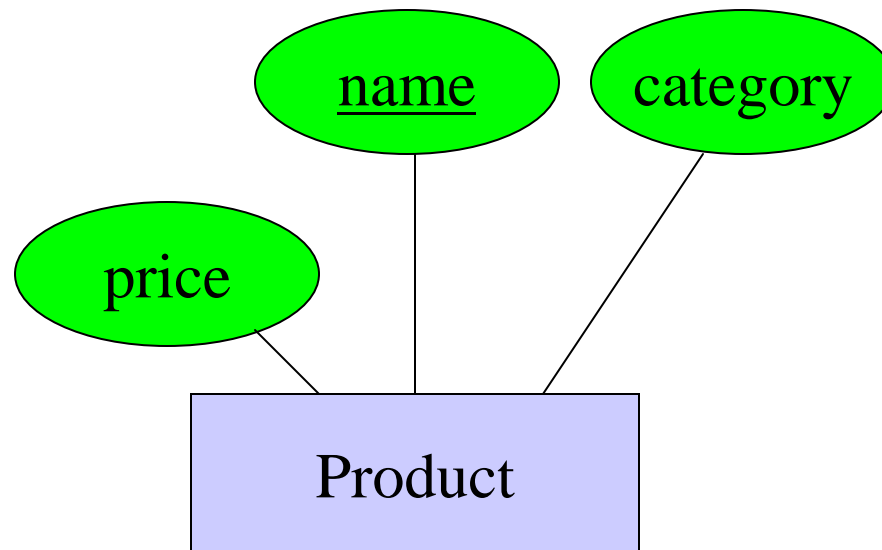


- first class citizens (not associated with classes)
- not necessarily binary



# Keys in E/R Diagrams

- Every entity set must have a key

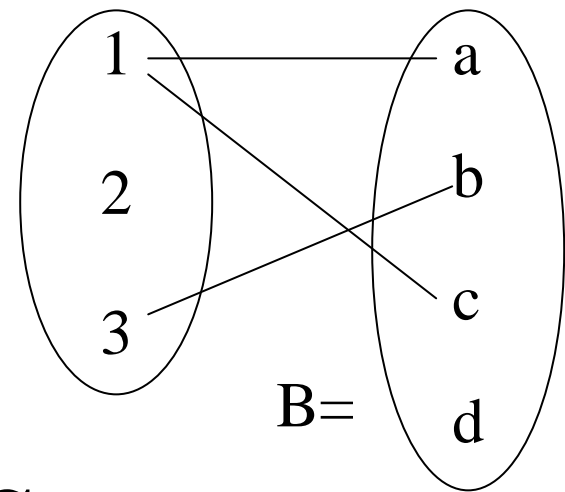




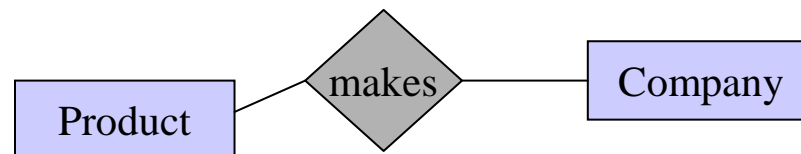
# What is a Relation ?

- A mathematical definition:
  - if  $A, B$  are sets, then a relation  $R$  is a subset of  $A \times B$

- $A = \{1, 2, 3\}$ ,  $B = \{a, b, c, d\}$ ,  
 $A \times B = \{(1, a), (1, b), \dots, (3, d)\}$   
 $R = \{(1, a), (1, c), (3, b)\}$

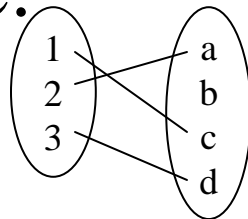


- **makes** is a subset of **Product**  $\times$  **Company**:

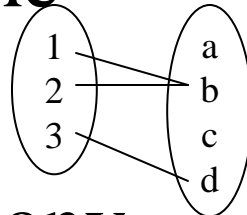


# Multiplicity of E/R Relations

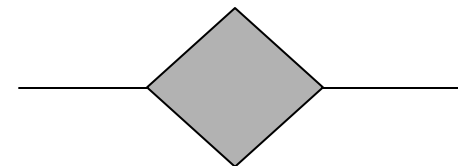
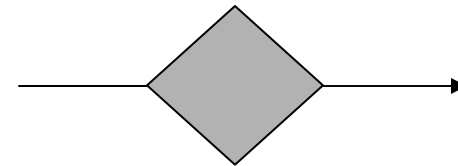
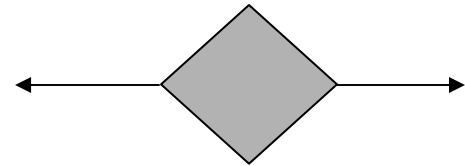
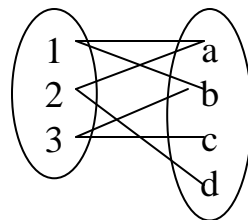
- one-one:



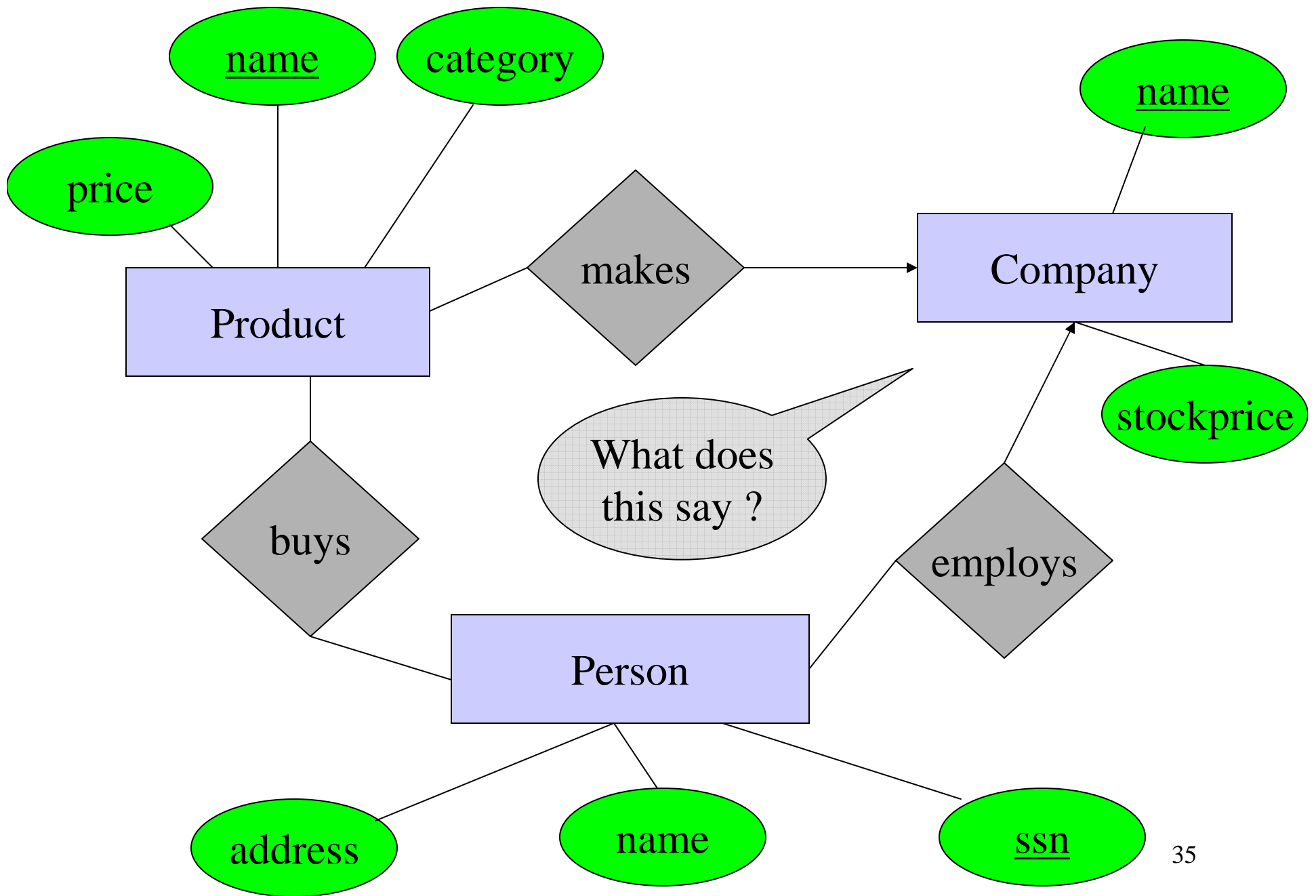
- many-one



- many-many

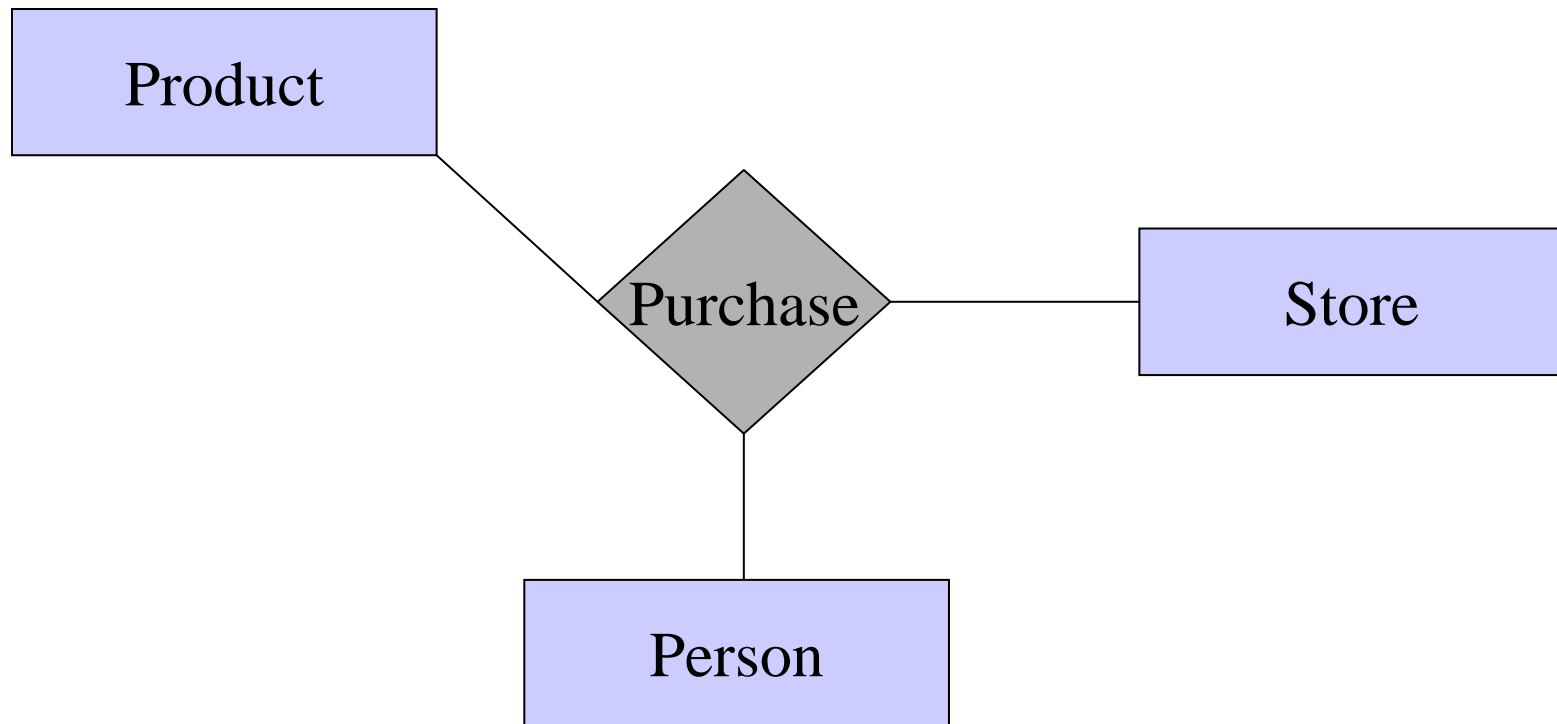


Note: book places arrow differently



# Multi-way Relationships

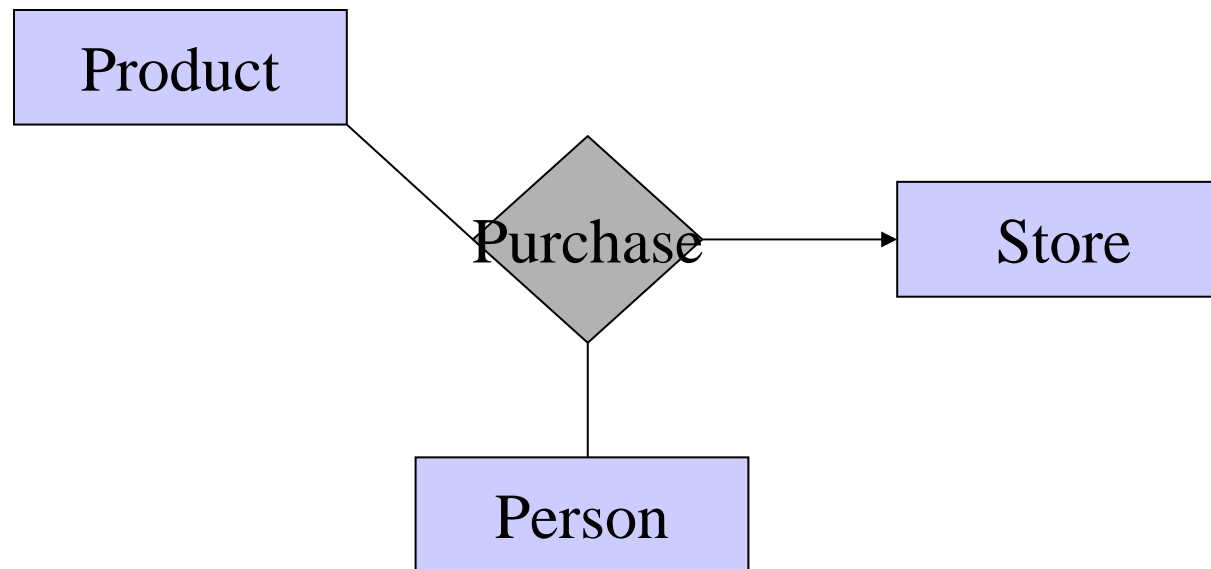
How do we model a purchase relationship between buyers, products and stores?



Can still model as a mathematical set (how ?)

# Arrows in Multiway Relationships

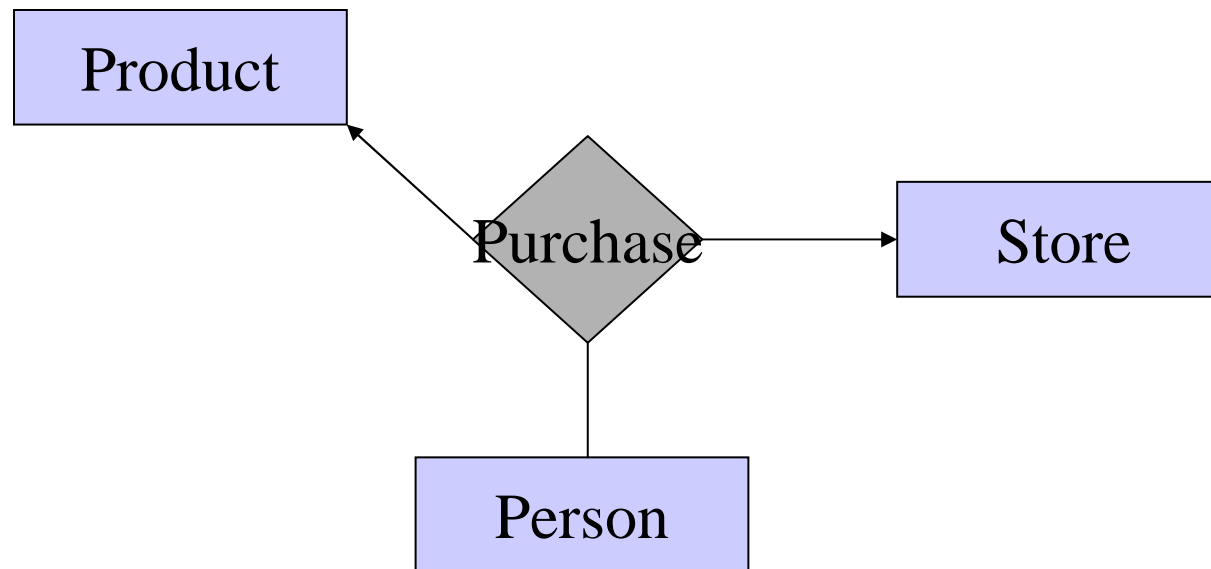
**Q:** what does the arrow mean ?



**A:** a given person buys a given product from at most one store

# Arrows in Multiway Relationships

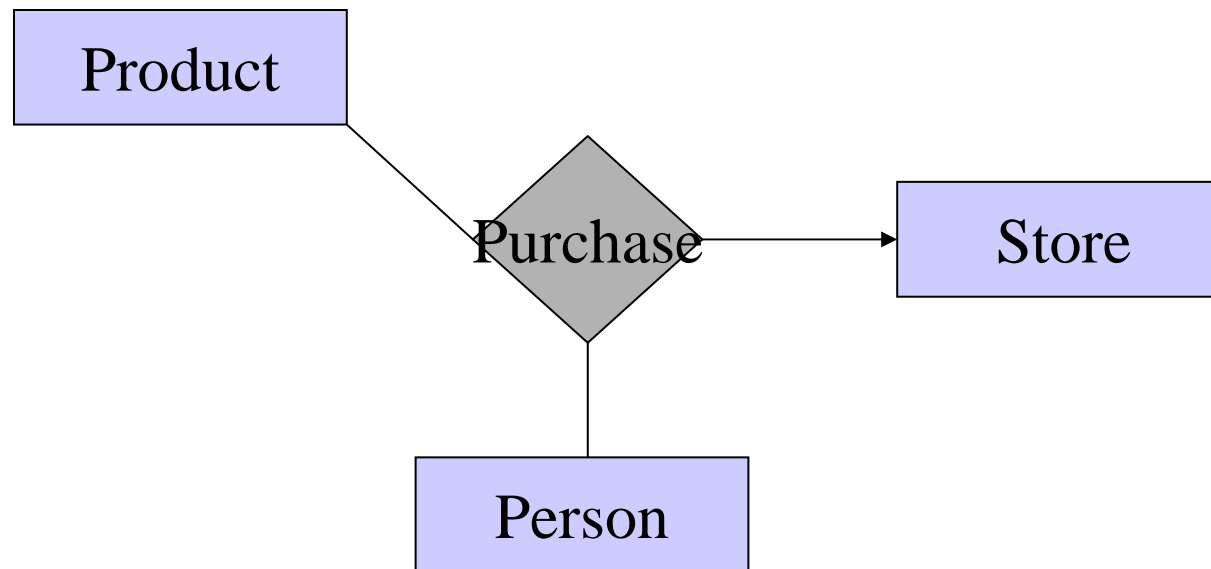
**Q:** what does the arrow mean ?



**A:** a given person buys a given product from at most one store  
AND every store sells to every person at most one product

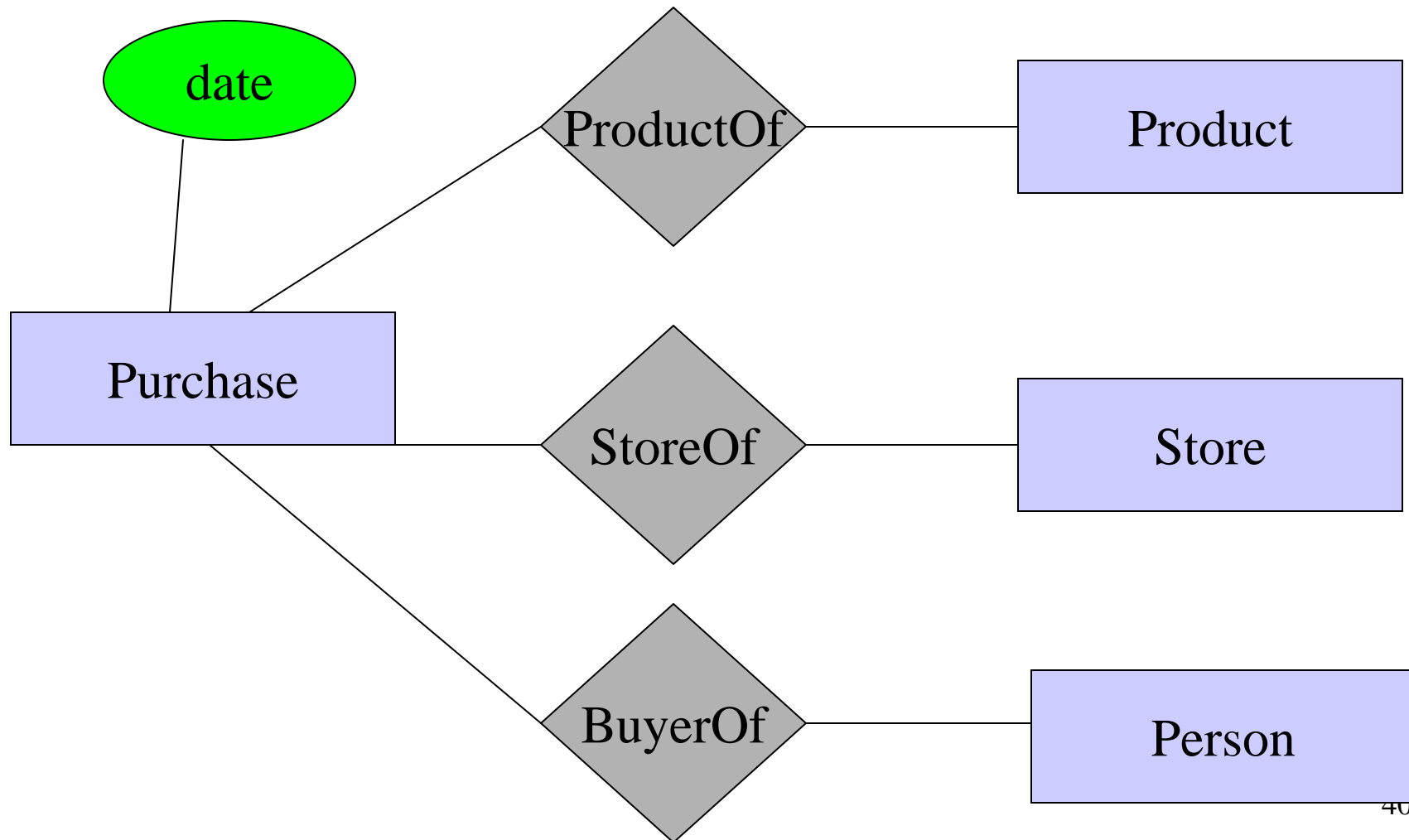
# Arrows in Multiway Relationships

**Q:** How do we say that every person shops at at most one store ?



**A:** cannot. This is the best approximation.  
(Why only approximation ?)

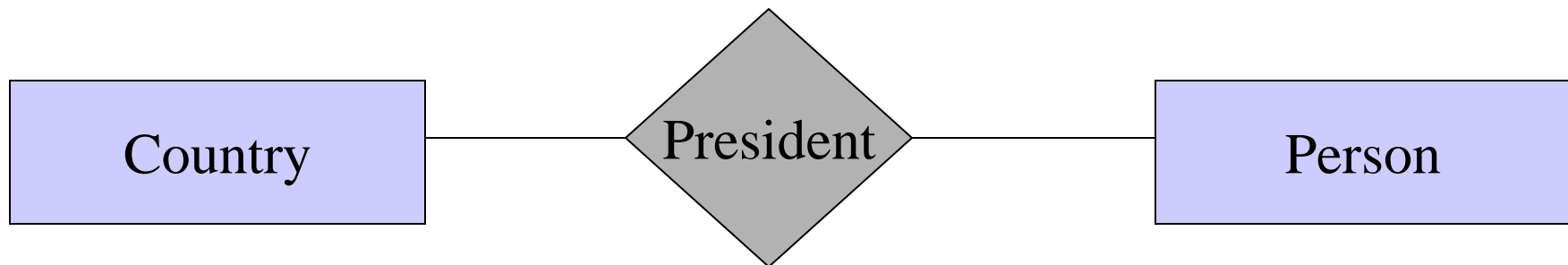
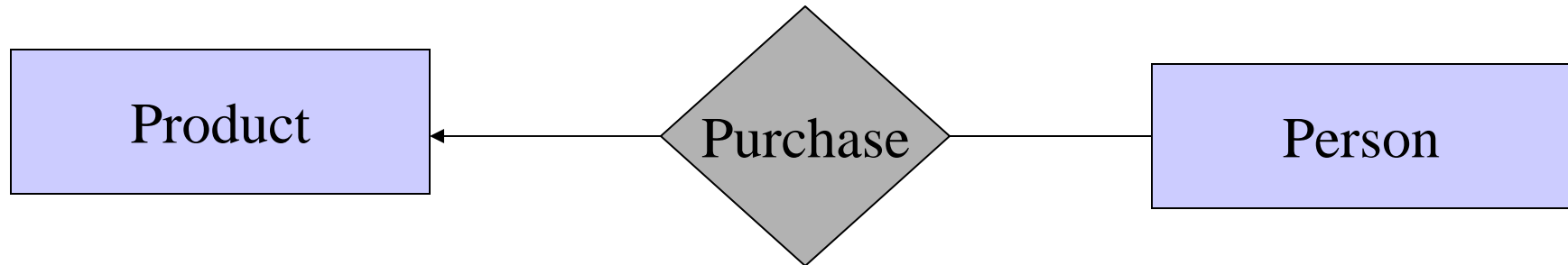
# Converting Multi-way Relationships to Binary





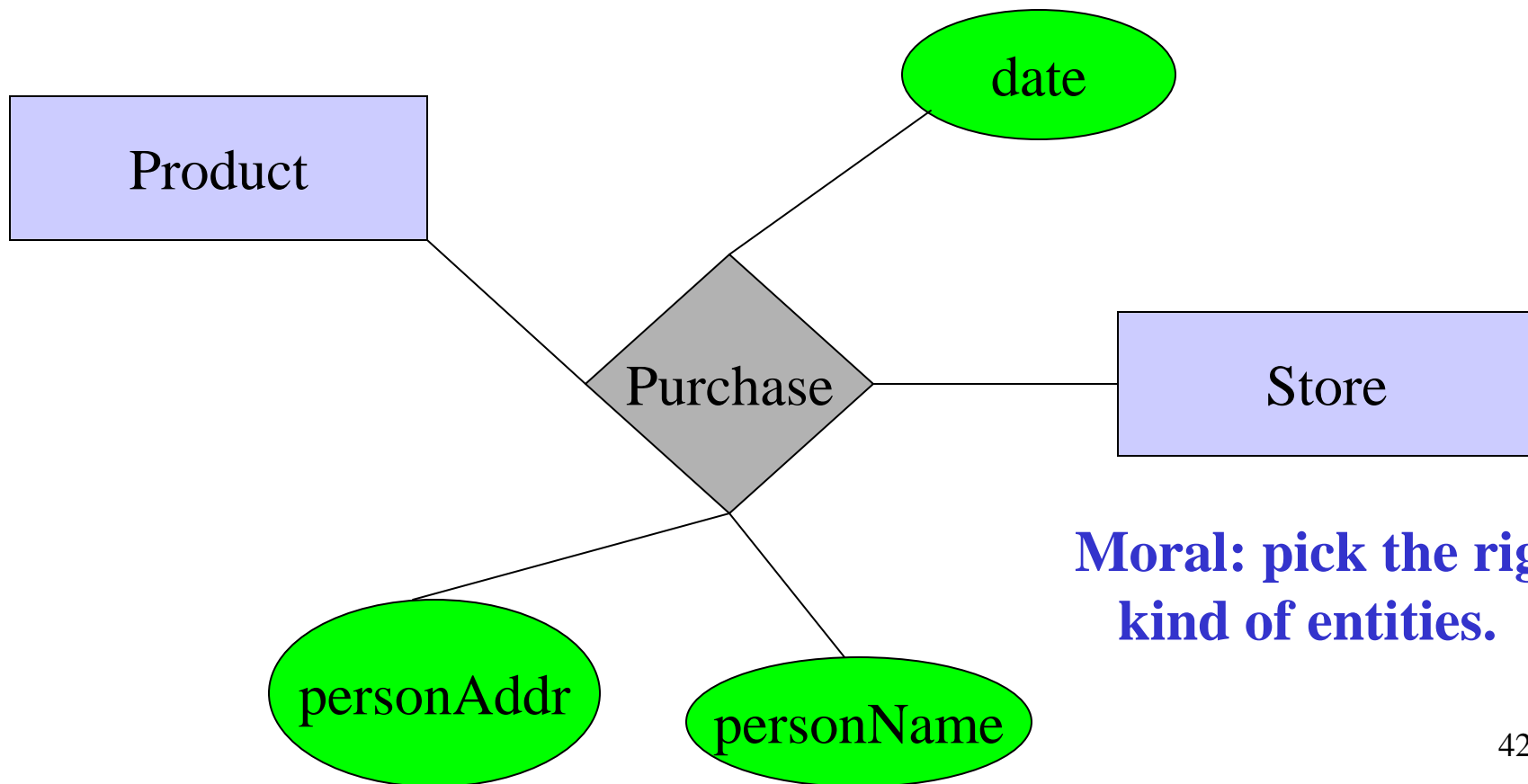
# 3. Design Principles

**What's wrong?**



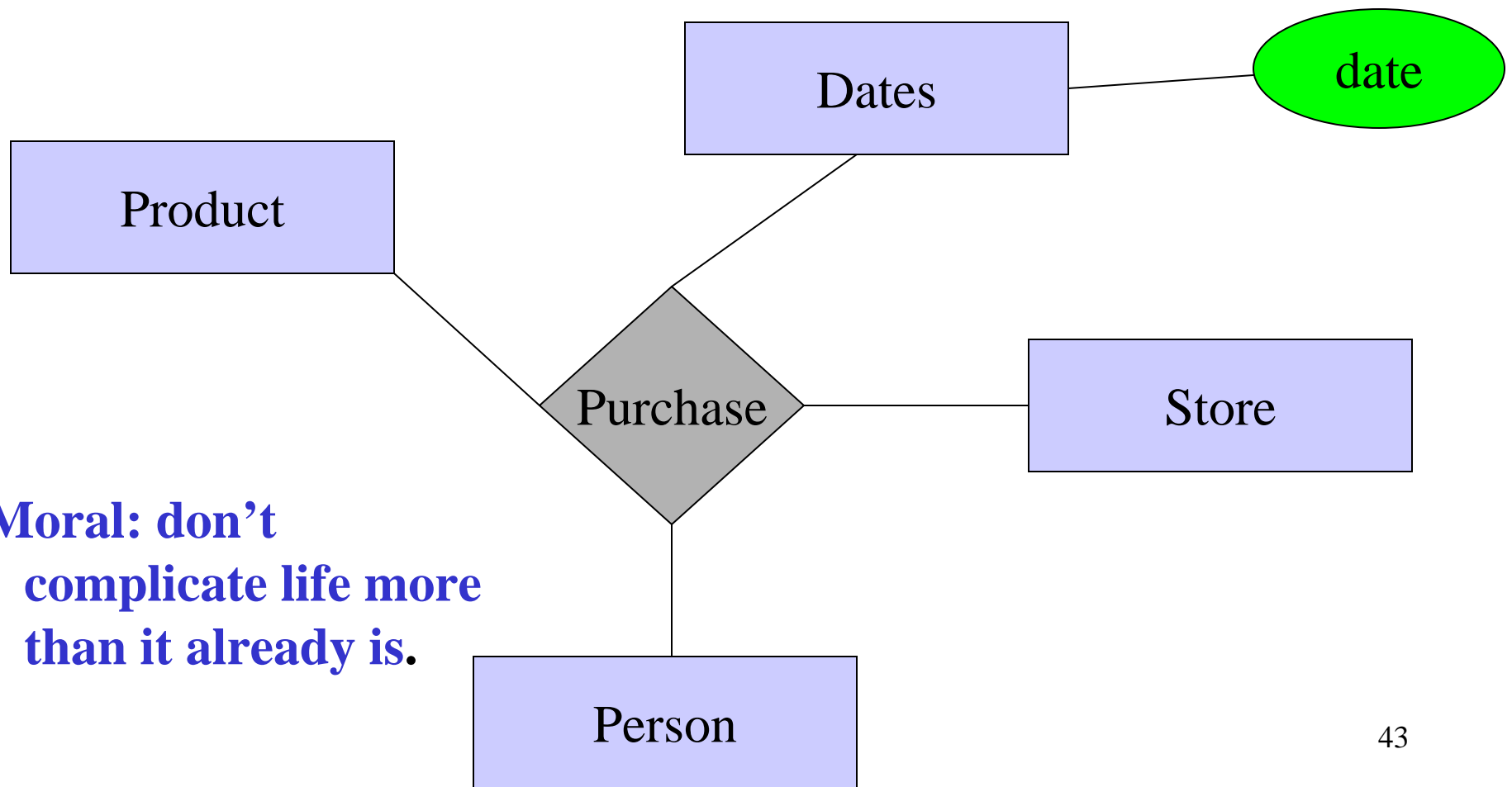
**Moral: be faithful!**

# Design Principles: What's Wrong?



**Moral: pick the right  
kind of entities.**

# Design Principles: What's Wrong?

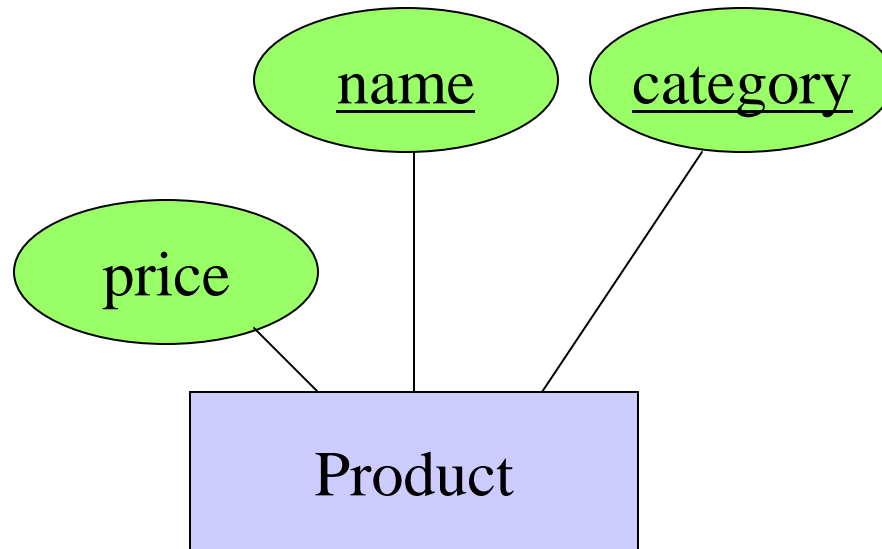


**Moral: don't  
complicate life more  
than it already is.**

# Logical Database Design = E/R $\rightarrow$ Relations

- Entity set  $\rightarrow$  relation
- Relationship  $\rightarrow$  relation

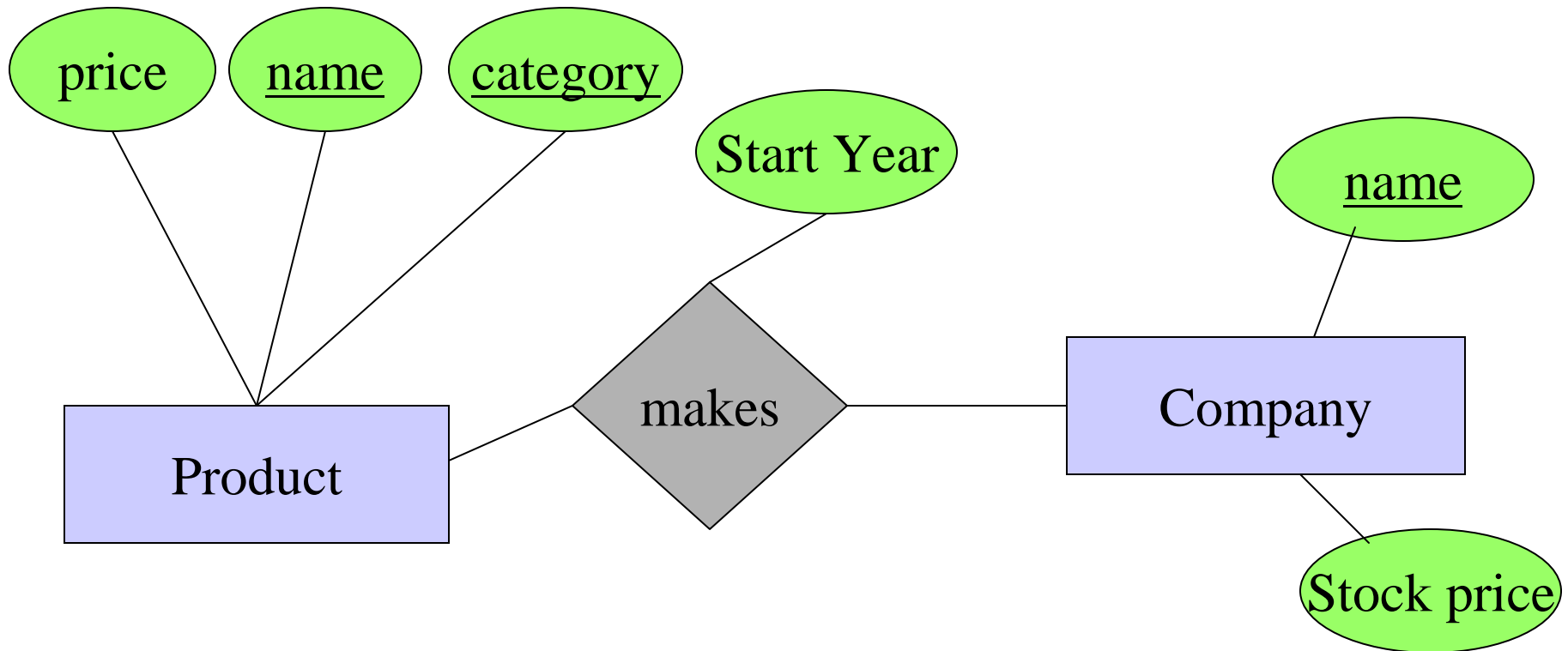
# Entity Set to Relation



**Product**(name, category, price)

name	category	price
gizmo	gadgets	\$19.99

# Relationships to Relations

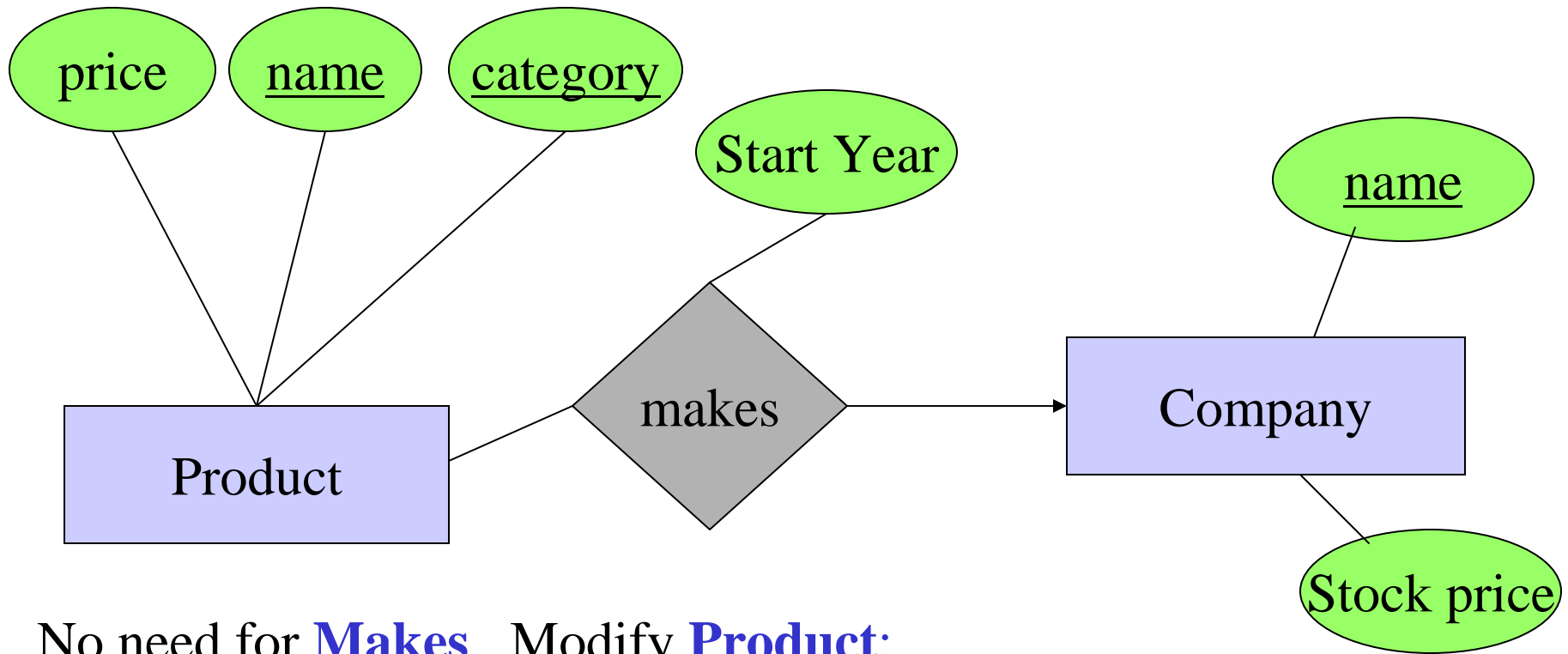


Makes(product-name, product-category, company-name, year)

Product-name	Product-Category	Company-name	Starting-year
gizmo	gadgets	gizmoWorks	1963

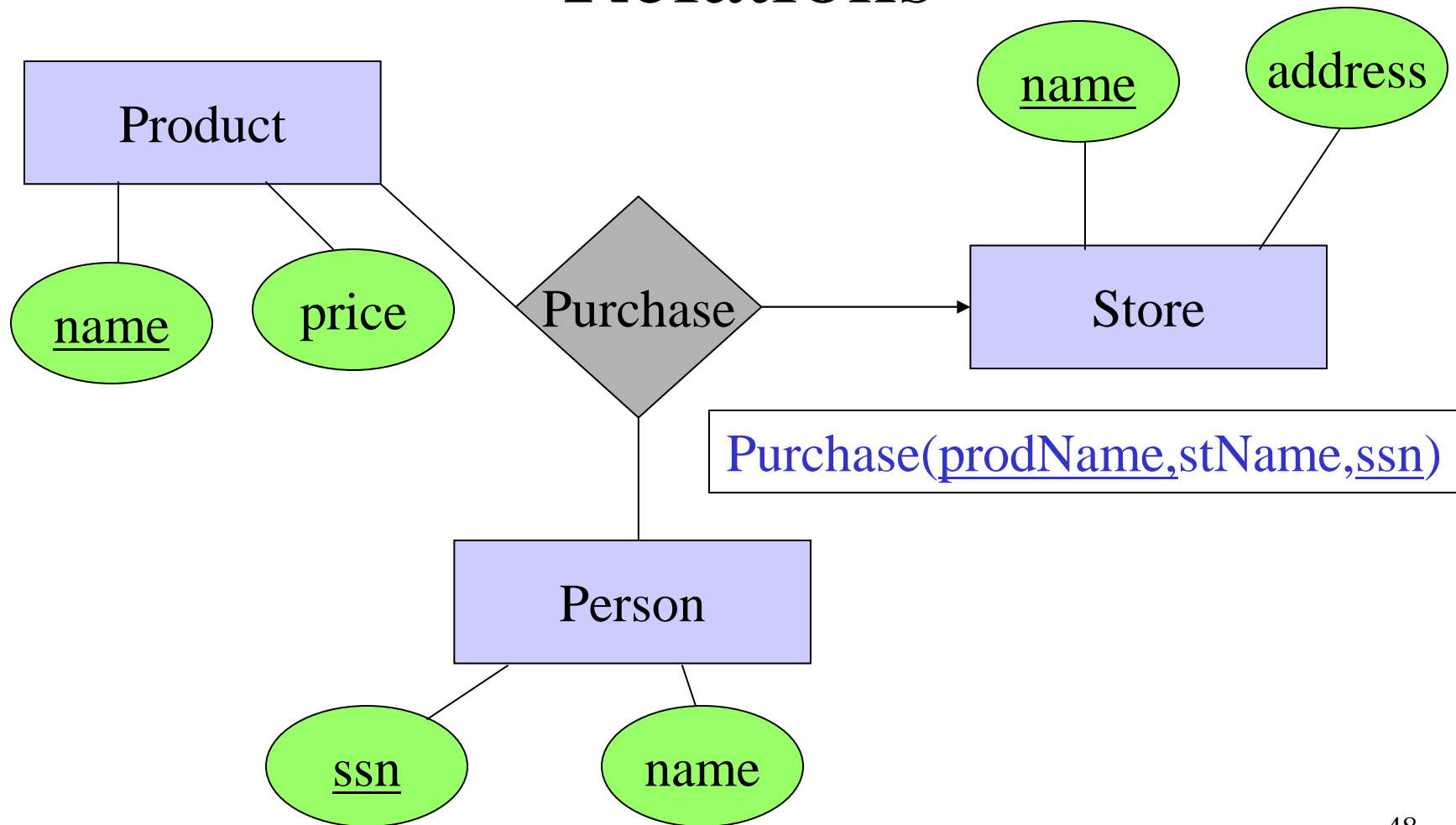
(watch out for attribute name conflicts)

# Relationships to Relations



<u>name</u>	<u>category</u>	<u>price</u>	<u>StartYear</u>	<u>companyName</u>
gizmo	gadgets	19.99	1963	gizmoWorks

# Multi-way Relationships to Relations

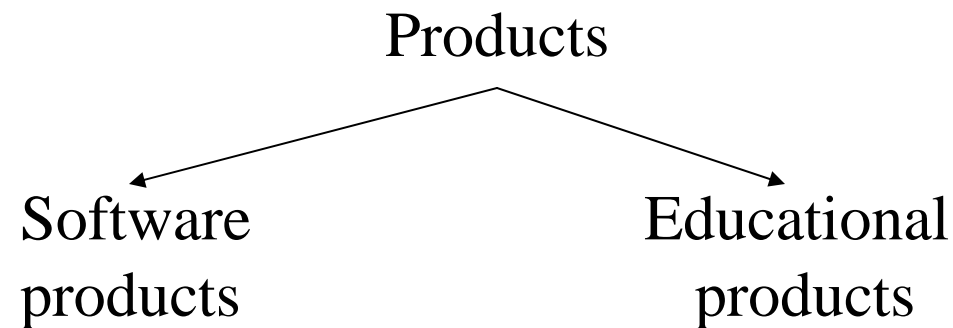




# Modeling Subclasses

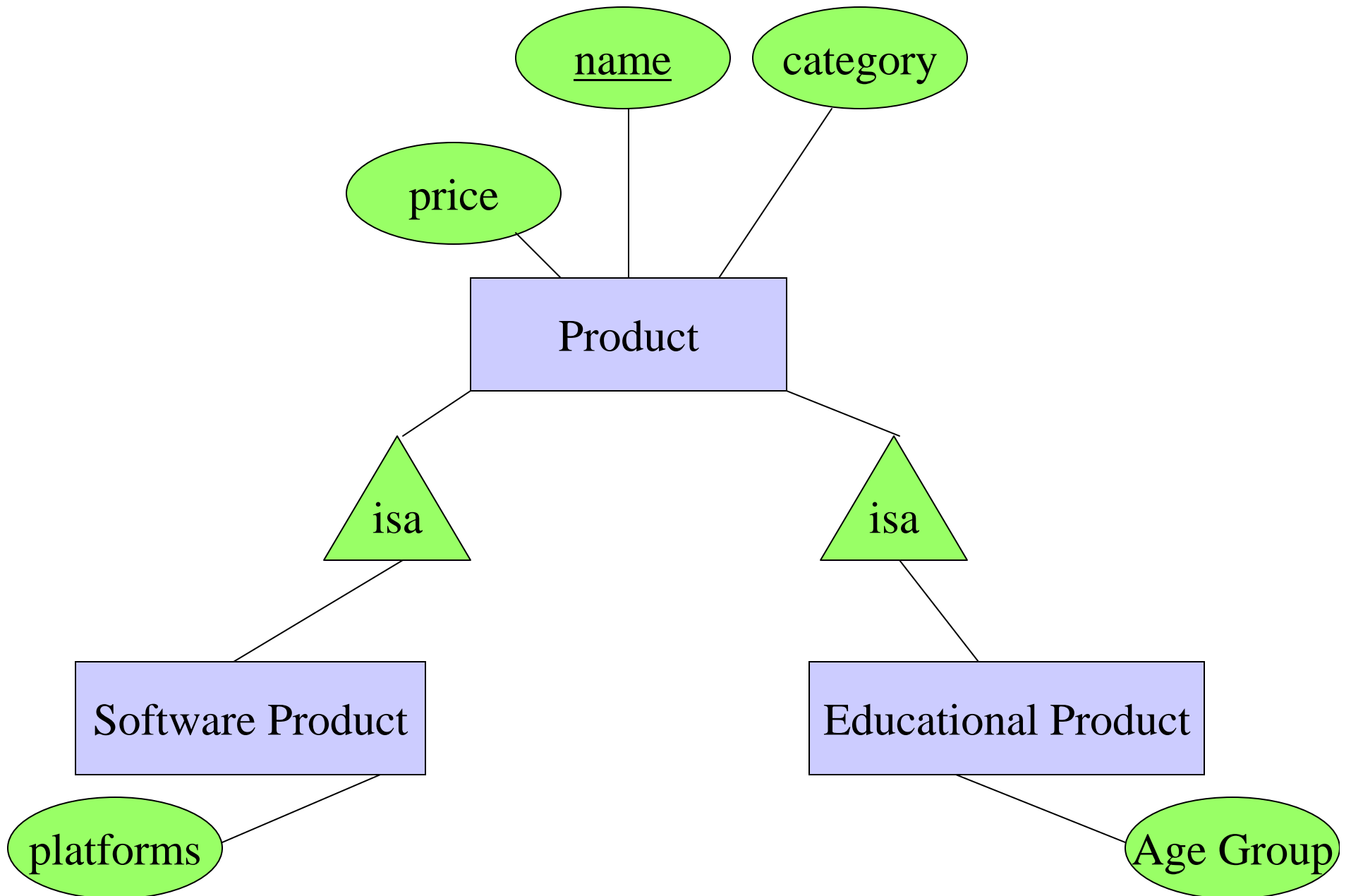
Some objects in a class may be special

- define a new class
- better: define a *subclass*



So --- we define subclasses in E/R

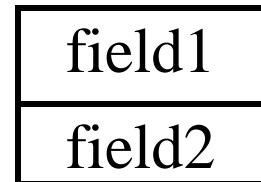
# Subclasses



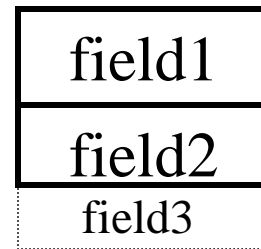
# Understanding Subclasses

- Think in terms of records:

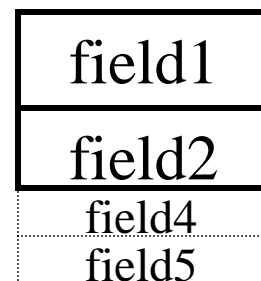
- Product



- SoftwareProduct



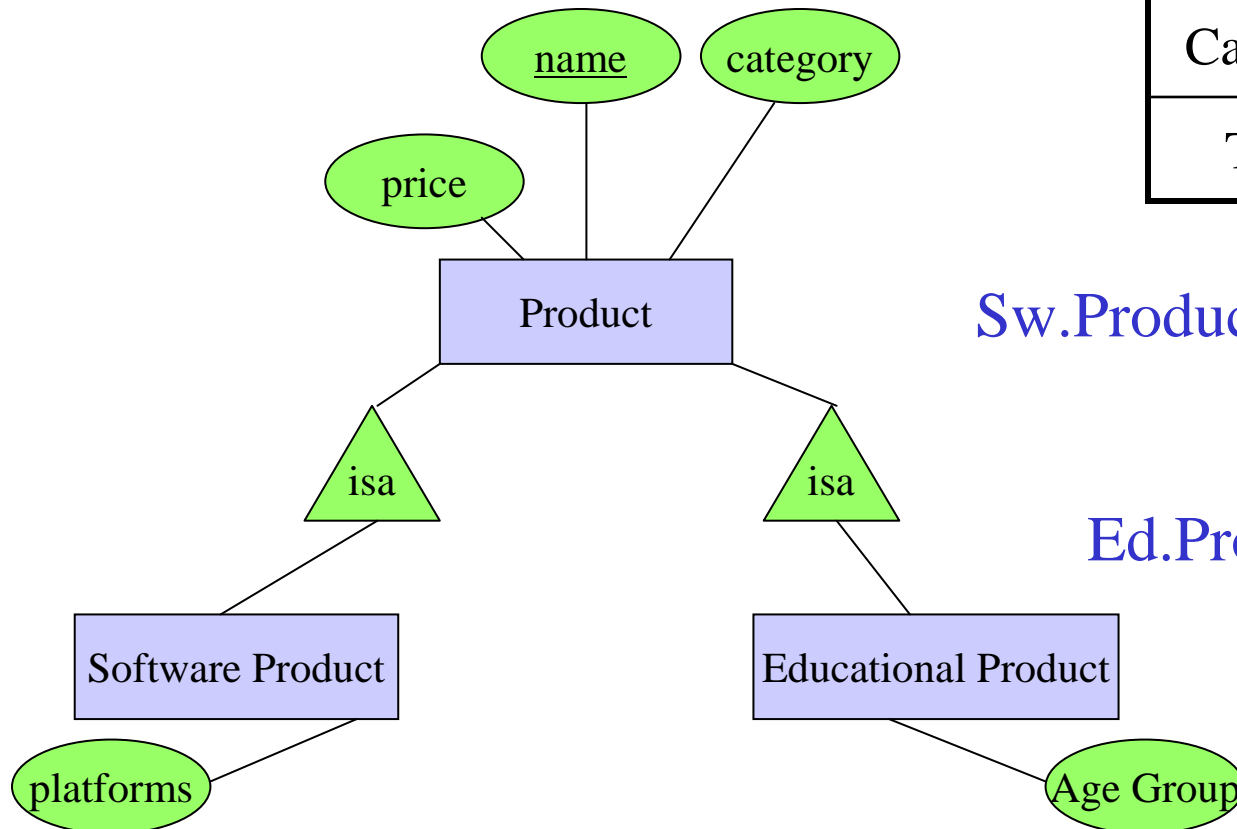
- EducationalProduct



# Subclasses to Relations

## Product

<u>Name</u>	Price	Category
Gizmo	99	gadget
Camera	49	photo
Toy	39	gadget



## Sw.Product

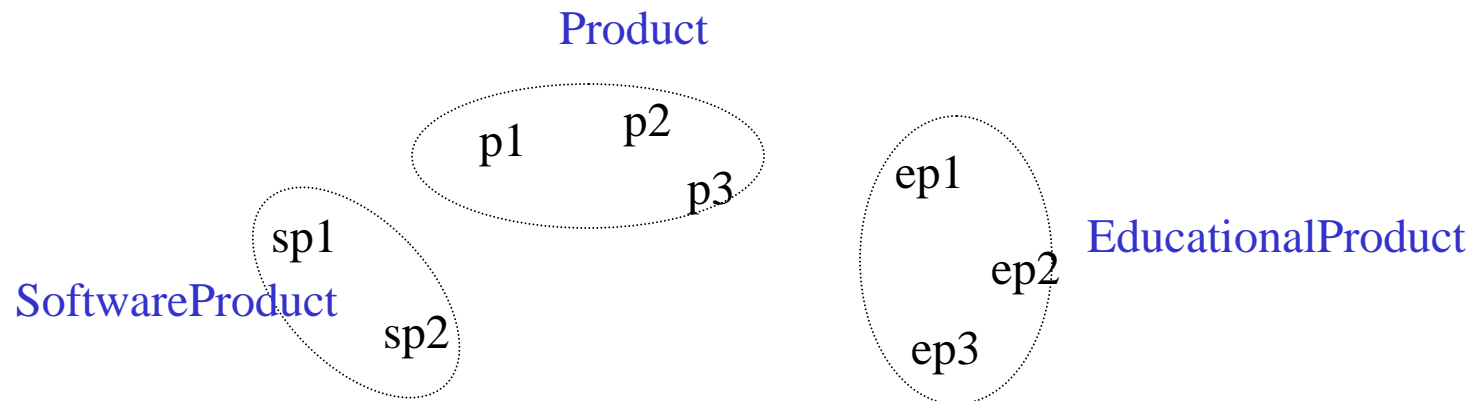
<u>Name</u>	platforms
Gizmo	unix

## Ed.Product

<u>Name</u>	Age Group
Gizmo	todler
Toy	retired

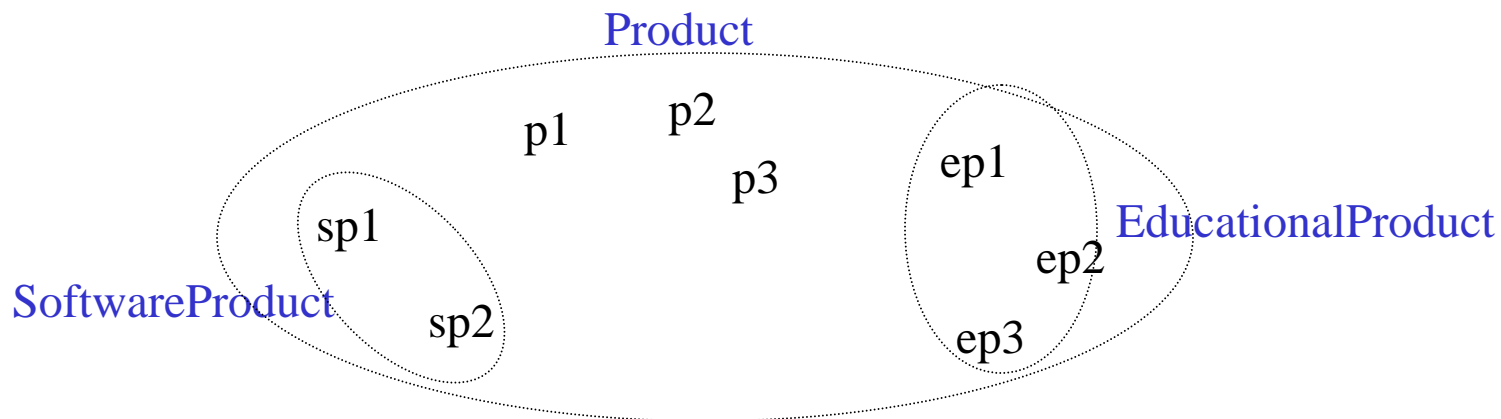
# Difference between OO and E/R inheritance

- OO: classes are disjoint (same for Java, C++)

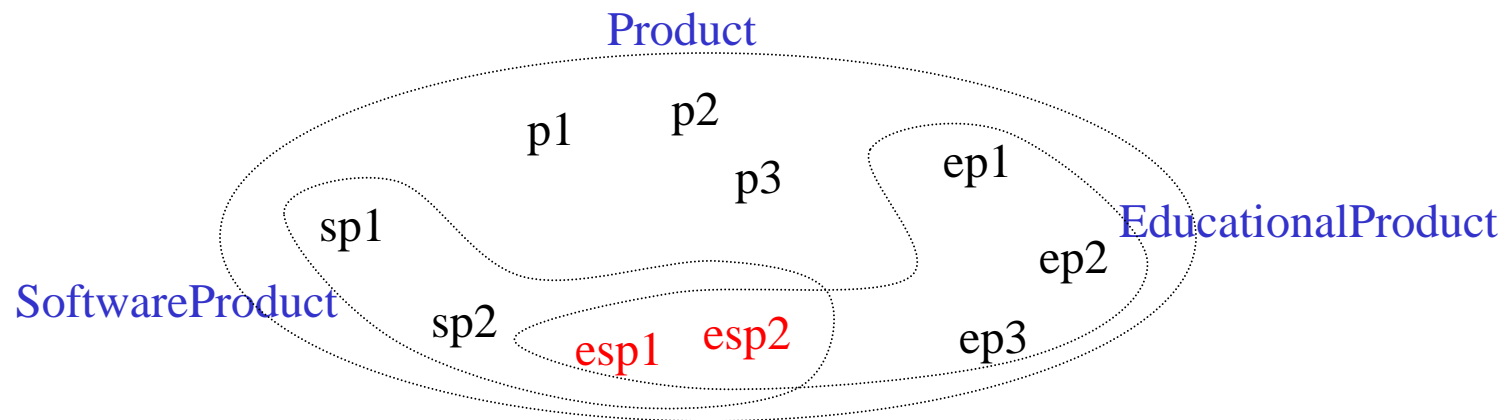


# Difference between OO and E/R inheritance

- E/R: entity sets overlap

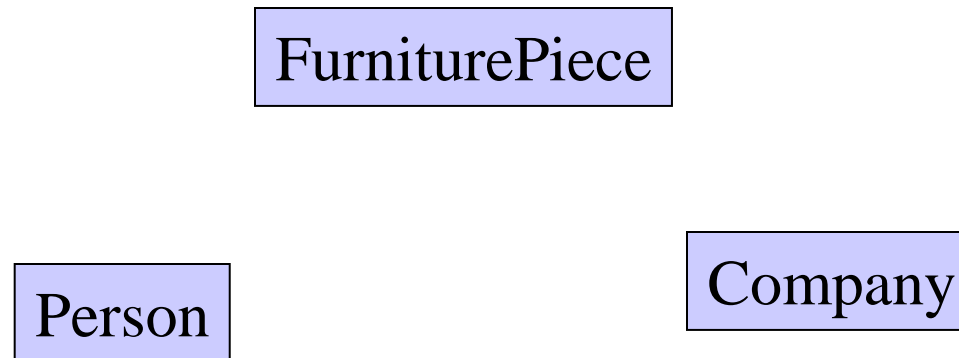


No need for multiple inheritance in E/R



We have three entity sets, but four different kinds of objects.

# Modeling UnionTypes With Subclasses



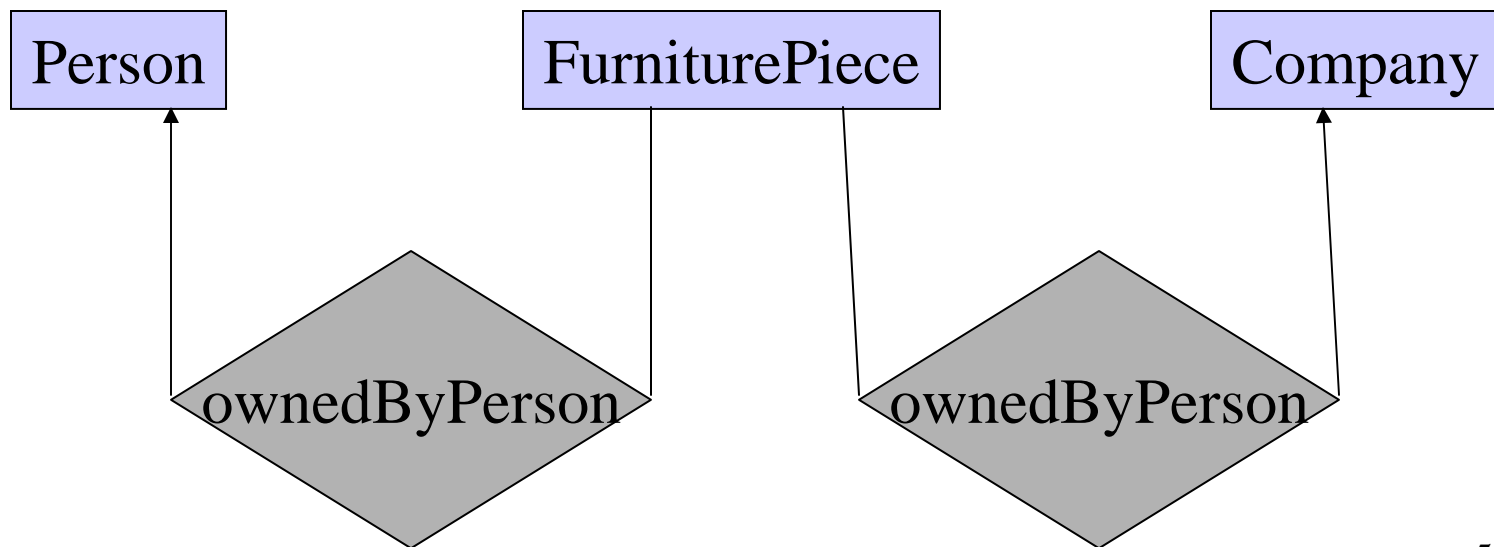
Say: each piece of furniture is owned either by a person, or by a company



# Modeling Union Types with Subclasses

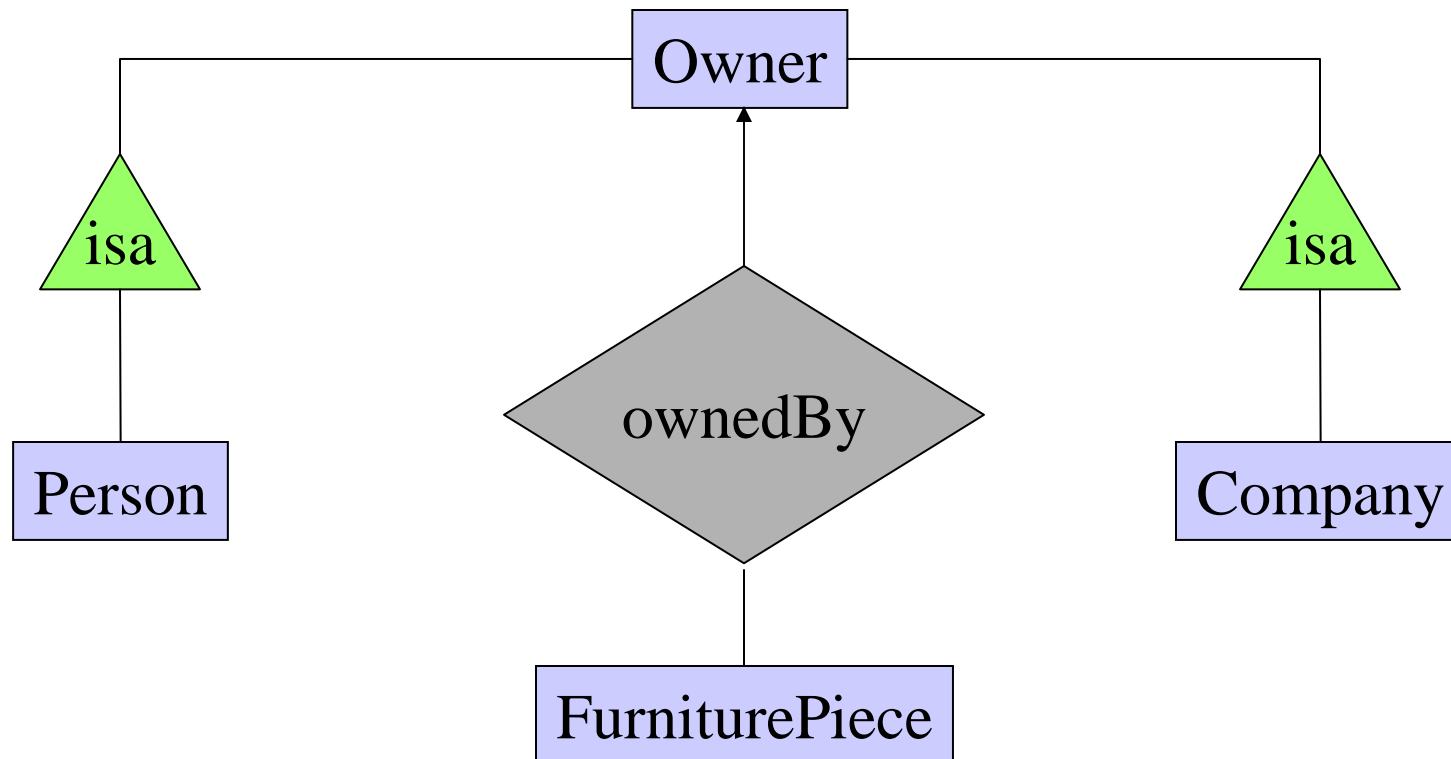
Say: each piece of furniture is owned either by a person, or by a company

Solution 1. Acceptable, imperfect (What's wrong ?)



# Modeling Union Types with Subclasses

Solution 2: better, more laborious



# Constraints in E/R Diagrams

Finding constraints is part of the modeling process.

Commonly used constraints:

**Keys:** social security number uniquely identifies a person.

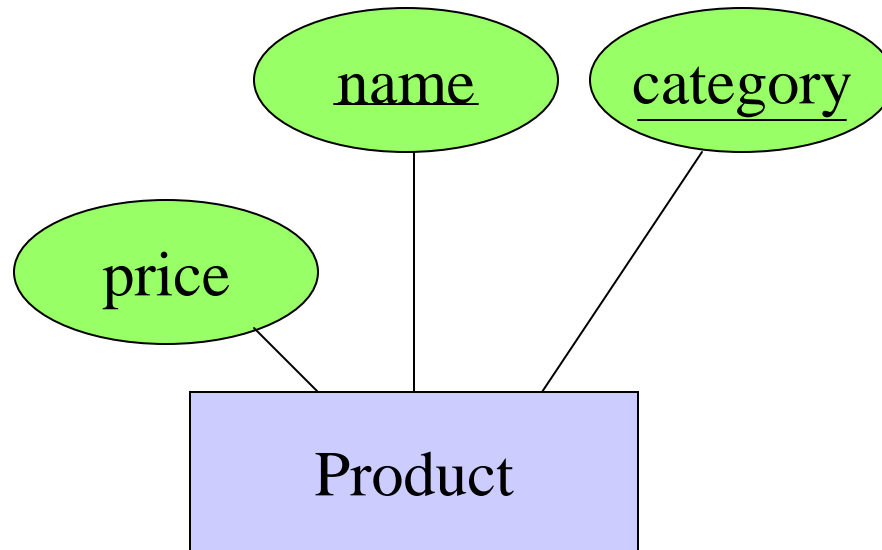
**Single-value constraints:** a person can have only one father.

**Referential integrity constraints:** if you work for a company, it must exist in the database.

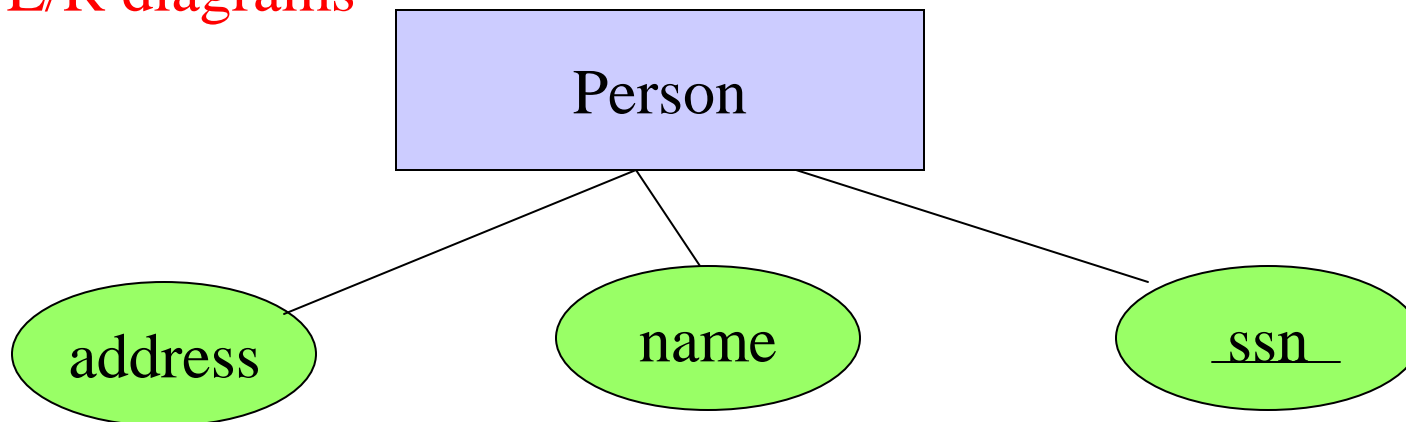
**Other constraints:** peoples' ages are between 0 and 150.

# Keys in E/R Diagrams

Underline:



No formal way  
to specify multiple  
keys in E/R diagrams



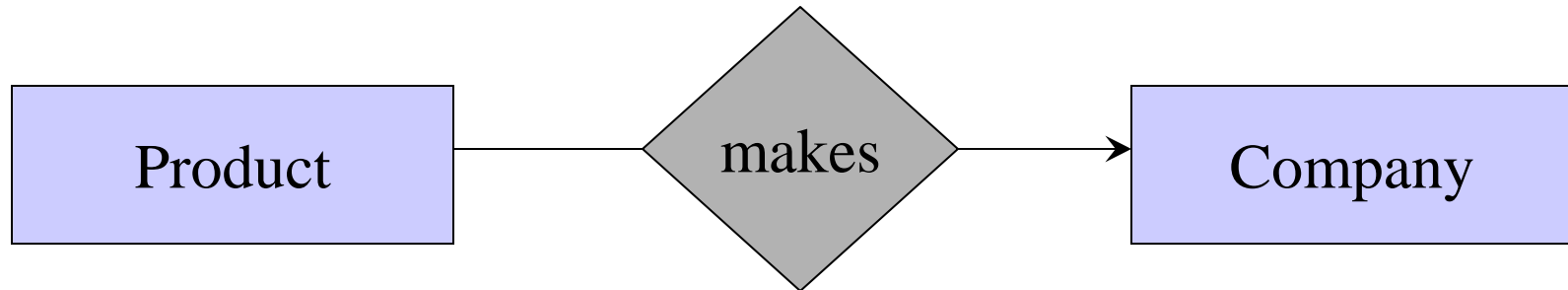
# Single Value Constraints



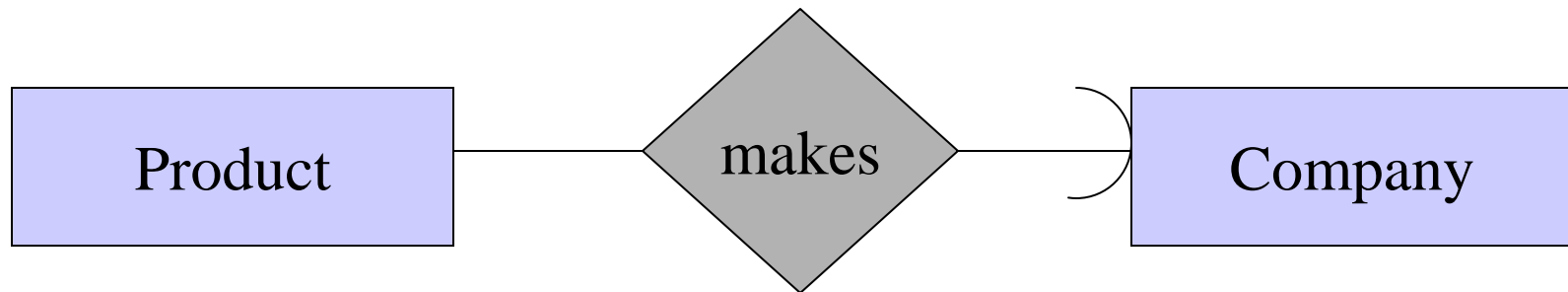
v. s.



# Referential Integrity Constraints

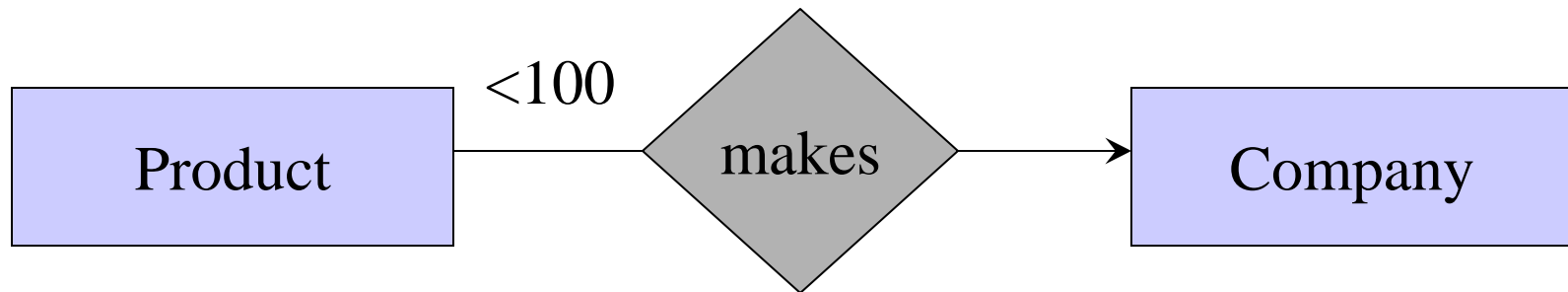


Each product made by at most one company.  
Some products made by no company



Each product made by exactly one company.

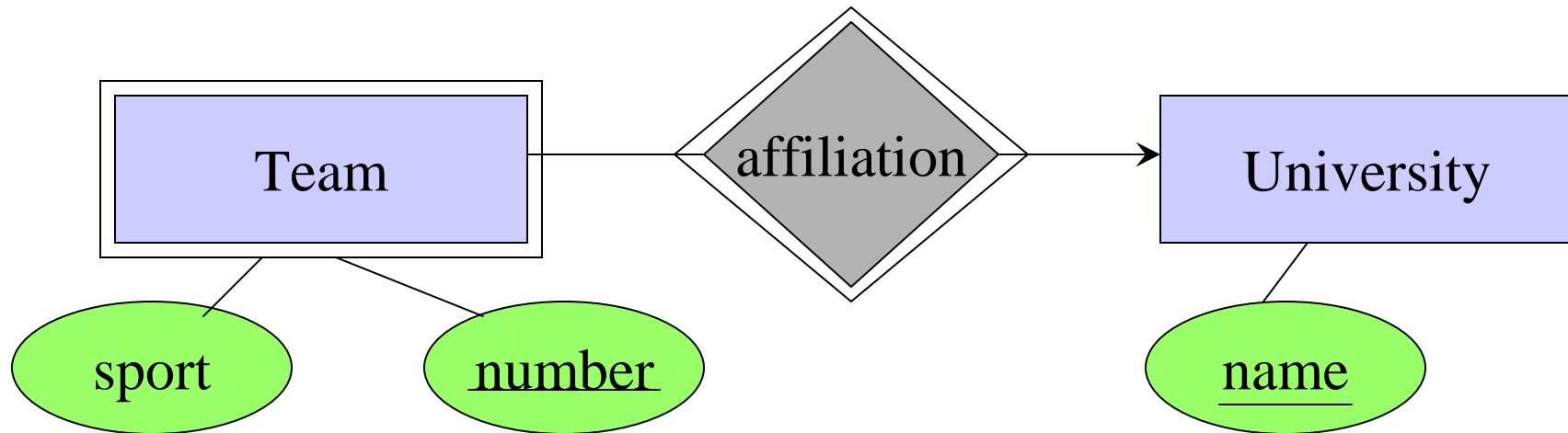
# Other Constraints



What does this mean ?

# Weak Entity Sets

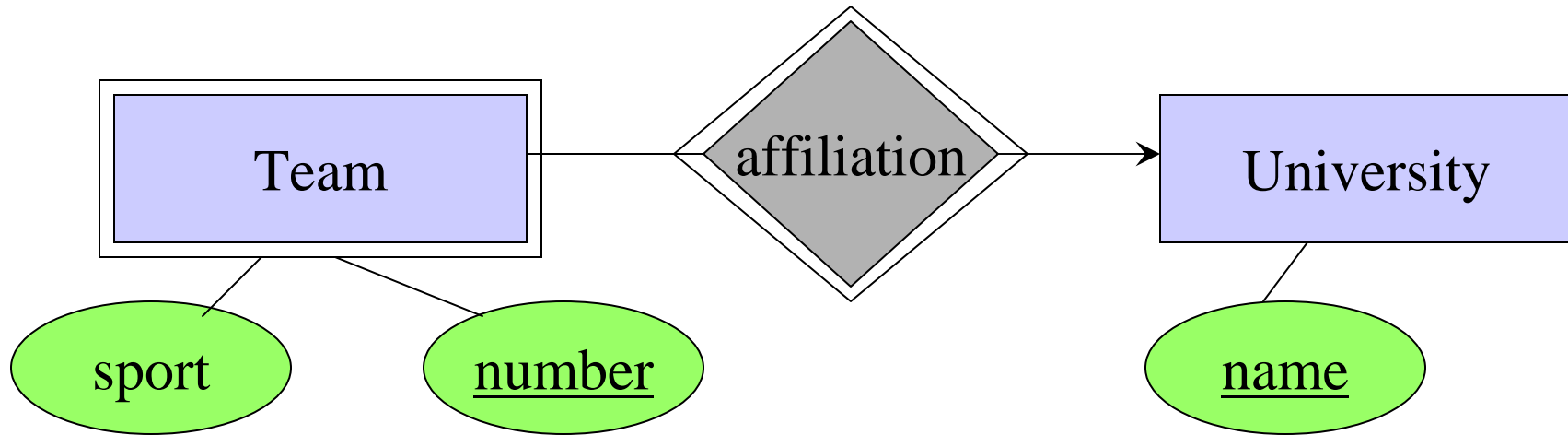
Entity sets are weak when their key comes from other classes to which they are related.



Notice: we encountered this when converting multiway relationships to binary relationships (last lecture) <sup>64</sup>



# Handling Weak Entity Sets



Convert to a relational schema (in class)

# Schema Refinements = Normal Forms

- 1st Normal Form = all tables are flat
- 2nd Normal Form = obsolete
- Boyce Codd Normal Form = will study
- 3rd Normal Form = see book

# First Normal Form (1NF)

- A database schema is in First Normal Form if all tables are flat

Student

Name	GPA	Courses			
Alice	3.8	<table border="1"><tr><td>Math</td></tr><tr><td>DB</td></tr><tr><td>OS</td></tr></table>	Math	DB	OS
Math					
DB					
OS					
Bob	3.7	<table border="1"><tr><td>DB</td></tr><tr><td>OS</td></tr></table>	DB	OS	
DB					
OS					
Carol	3.9	<table border="1"><tr><td>Math</td></tr><tr><td>OS</td></tr></table>	Math	OS	
Math					
OS					

Student

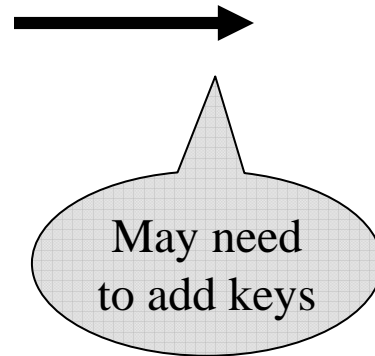
Name	GPA
Alice	3.8
Bob	3.7
Carol	3.9

Takes

Student	Course
Alice	Math
Carol	Math
Alice	DB
Bob	DB
Alice	OS
Carol	OS

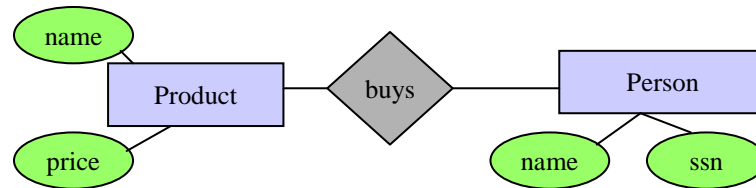
Course

Course
Math
DB
OS

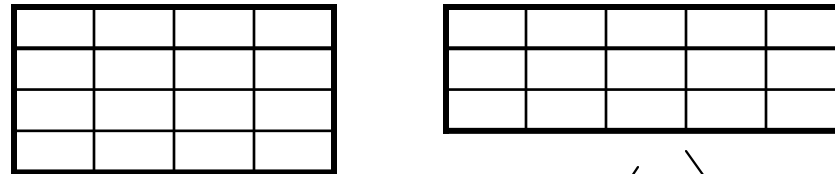


# Relational Schema Design

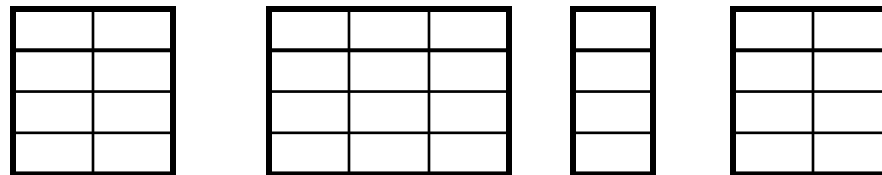
Conceptual Model:



Relational Model:  
plus FD's



Normalization:  
Eliminates anomalies



# Data Anomalies

When a database is poorly designed we get anomalies:

**Redundancy**: data is repeated

**Updated anomalies**: need to change in several places

**Delete anomalies**: may lose data when we don't want

# Relational Schema Design

Recall set attributes (persons with several phones):

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

## Anomalies:

- Redundancy = repeat data
- Update anomalies = Fred moves to “Bellevue”
- Deletion anomalies = Joe deletes his phone number:  
what is his city ?

# Relation Decomposition

**Break the relation into two:**

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121

**Anomalies have gone:**

- No more repeated data
- Easy to move Fred to “Bellevue” (how ?)
- Easy to delete all Joe’s phone number (how ?)

# Relational Schema Design (or Logical Design)

Main idea:

- Start with some relational schema
- Find out its *functional dependencies*
- Use them to design a better relational schema



# Functional Dependencies

- A form of constraint
  - hence, part of the schema
- Finding them is part of the database design
- Also used in normalizing the relations

# Functional Dependencies

## Definition:

If two tuples agree on the attributes

$$A_1, A_2, \dots, A_n$$

then they must also agree on the attributes

$$B_1, B_2, \dots, B_m$$

## Formally:

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

# When Does an FD Hold

Definition:  $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$  holds in R if:

$$\forall t, t' \in R, (t.A_1=t'.A_1 \wedge \dots \wedge t.A_m=t'.A_m \Rightarrow t.B_1=t'.B_1 \wedge \dots \wedge t.B_n=t'.B_n)$$

R

	$A_1$	...	$A_m$		$B_1$	...	$B_m$		
t									
t'									

if t, t' agree here      then t, t' agree here

# Examples

An FD holds, or does not hold on an instance:

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

EmpID  $\rightarrow$  Name, Phone, Position

Position  $\rightarrow$  Phone

but not Phone  $\rightarrow$  Position

# Example

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876 ←	Salesrep
E1111	Smith	9876 ←	Salesrep
E9999	Mary	1234	Lawyer

Position → Phone

# Example

EmpID	Name	Phone	Position
E0045	Smith	1234 →	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234 →	Lawyer

but not Phone → Position

# Example

FD's are constraints:

- On some instances they hold
- On others they don't

name  $\rightarrow$  color  
category  $\rightarrow$  department  
color, category  $\rightarrow$  price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99

Does this instance satisfy all the FDs ?

# Example

name  $\rightarrow$  color  
category  $\rightarrow$  department  
color, category  $\rightarrow$  price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Black	Toys	99
Gizmo	Stationary	Green	Office-supp.	59

What about this one ?



# An Interesting Observation

If all these FDs are true:

name  $\rightarrow$  color  
category  $\rightarrow$  department  
color, category  $\rightarrow$  price

Then this FD also holds:

name, category  $\rightarrow$  price

Why ??

# Goal: Find ALL Functional Dependencies

- Anomalies occur when certain “bad” FDs hold
- We know some of the FDs
- Need to find *all* FDs, then look for the bad ones

# Armstrong's Rules (1/3)

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

Is equivalent to

$$\begin{array}{l} A_1, A_2, \dots, A_n \rightarrow B_1 \\ A_1, A_2, \dots, A_n \rightarrow B_2 \\ \dots \dots \dots \\ A_1, A_2, \dots, A_n \rightarrow B_m \end{array}$$

**Splitting rule  
and  
Combing rule**

	A1	...	Am		B1	...	Bm	

# Armstrong's Rules (1/3)

$$A_1, A_2, \dots, A_n \rightarrow A_i$$

**Trivial Rule**

where  $i = 1, 2, \dots, n$

Why ?

	$A_1$	...	$A_m$	

# Armstrong's Rules (1/3)

## Transitive Closure Rule

If

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

and

$$B_1, B_2, \dots, B_m \rightarrow C_1, C_2, \dots, C_p$$

then

$$A_1, A_2, \dots, A_n \rightarrow C_1, C_2, \dots, C_p$$

Why ?

	$A_1$	...	$A_m$		$B_1$	...	$B_m$		$C_1$	...	$C_p$	

# Example (continued)

Start from the following FDs:

1. name  $\rightarrow$  color
2. category  $\rightarrow$  department
3. color, category  $\rightarrow$  price

Infer the following FDs:

Inferred FD	Which Rule did we apply ?
4. name, category $\rightarrow$ name	
5. name, category $\rightarrow$ color	
6. name, category $\rightarrow$ category	
7. name, category $\rightarrow$ color, category	
8. name, category $\rightarrow$ price	

# Example (continued)

Answers:

1. name  $\rightarrow$  color
2. category  $\rightarrow$  department
3. color, category  $\rightarrow$  price

Inferred FD	Which Rule did we apply ?
4. name, category $\rightarrow$ name	Trivial rule
5. name, category $\rightarrow$ color	Transitivity on 4, 1
6. name, category $\rightarrow$ category	Trivial rule
7. name, category $\rightarrow$ color, category	Split/combine on 5, 6
8. name, category $\rightarrow$ price	Transitivity on 3, 7

THIS IS TOO HARD ! Let's see an easier way.



# Closure of a set of Attributes

**Given** a set of attributes  $A_1, \dots, A_n$

The **closure**,  $\{A_1, \dots, A_n\}^+$  = the set of attributes B  
s.t.  $A_1, \dots, A_n \rightarrow B$

Example:

name  $\rightarrow$  color  
category  $\rightarrow$  department  
color, category  $\rightarrow$  price

Closures:

name<sup>+</sup> = {name, color}

{name, category}<sup>+</sup> = {name, category, color, department, price}

color<sup>+</sup> = {color}

# Closure Algorithm

$X = \{A_1, \dots, A_n\}$ .

**Repeat until**  $X$  doesn't change **do:**

**if**  $B_1, \dots, B_n \rightarrow C$  is a FD **and**  
 $B_1, \dots, B_n$  are all in  $X$   
**then** add  $C$  to  $X$ .

Example:

$\text{name} \rightarrow \text{color}$   
 $\text{category} \rightarrow \text{department}$   
 $\text{color, category} \rightarrow \text{price}$

$\{\text{name, category}\}^+ =$   
 $\{\text{name, category, color, department, price}\}$

Hence:  $\text{name, category} \rightarrow \text{color, department, price}$

# Example

In class:

$R(A,B,C,D,E,F)$

$A, B$	$\rightarrow$	$C$
$A, D$	$\rightarrow$	$E$
$B$	$\rightarrow$	$D$
$A, F$	$\rightarrow$	$B$

Compute  $\{A,B\}^+$   $X = \{A, B, \quad \}$

Compute  $\{A, F\}^+$   $X = \{A, F, \quad \}$

# Why Do We Need Closure

- With closure we can find all FD's easily
- To check if  $X \rightarrow A$ 
  - Compute  $X^+$
  - Check if  $A \in X^+$

# Using Closure to Infer ALL FDs

Example:

$A, B \rightarrow C$
$A, D \rightarrow B$
$B \rightarrow D$

Step 1: Compute  $X^+$ , for every  $X$ :

$A^+ = A, B^+ = BD, C^+ = C, D^+ = D$

$AB^+ = ABCD, AC^+ = AC, AD^+ = ABCD,$

$BC^+ = BCD, BD^+ = BD, CD^+ = CD$

$ABC^+ = ABD^+ = ACD^+ = ABCD$  (no need to compute— why ?)

$BCD^+ = BCD, ABCD^+ = ABCD$

Step 2: Enumerate all FD's  $X \rightarrow Y$ , s.t.  $Y \subseteq X^+$  and  $X \cap Y = \emptyset$ :

$AB \rightarrow CD, AD \rightarrow BC, ABC \rightarrow D, ABD \rightarrow C, ACD \rightarrow B$

# Another Example

- Enrollment(student, major, course, room, time)  
student  $\rightarrow$  major  
major, course  $\rightarrow$  room  
course  $\rightarrow$  time

What else can we infer ? [in class, or at home]

# Keys

- A **superkey** is a set of attributes  $A_1, \dots, A_n$  s.t. for any other attribute  $B$ , we have  $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
  - I.e. set of attributes which is a superkey and for which no subset is a superkey

# Computing (Super)Keys

- Compute  $X^+$  for all sets  $X$
- If  $X^+ = \text{all attributes}$ , then  $X$  is a key
- List only the minimal  $X$ 's



# Example

Product(name, price, category, color)

name, category  $\rightarrow$  price  
category  $\rightarrow$  color

What is the key ?

# Example

Product(name, price, category, color)

name, category  $\rightarrow$  price  
category  $\rightarrow$  color

What is the key ?

(name, category) + = name, category, price, color

Hence (name, category) is a key

# Examples of Keys

Enrollment(student, address, course, room, time)

student → address

room, time → course

student, course → room, time

(find keys at home)

# Eliminating Anomalies

Main idea:

- $X \rightarrow A$  is OK if  $X$  is a (super)key
- $X \rightarrow A$  is not OK otherwise

# Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

SSN  $\rightarrow$  Name, City

What the key?

{SSN, PhoneNumber}

Hence SSN  $\rightarrow$  Name, City  
is a “bad” dependency

# Key or Keys ?

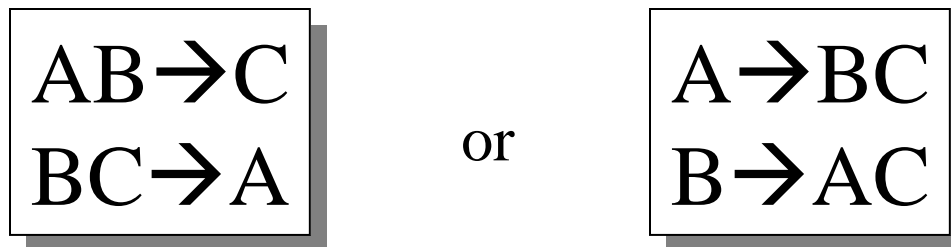
Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more keys

# Key or Keys ?

Can we have more than one key ?

Given  $R(A,B,C)$  define FD's s.t. there are two or more keys



what are the keys here ?

Can you design FDs such that there are *three* keys ?

# Boyce-Codd Normal Form

A simple condition for removing anomalies from relations:

A relation  $R$  is in BCNF if:

If  $A_1, \dots, A_n \rightarrow B$  is a non-trivial dependency in  $R$ , then  $\{A_1, \dots, A_n\}$  is a superkey for  $R$

In other words: there are no “bad” FDs

Equivalently:

$\forall X$ , either  $(X^+ = X)$  or  $(X^+ = \text{all attributes})$



# BCNF Decomposition Algorithm

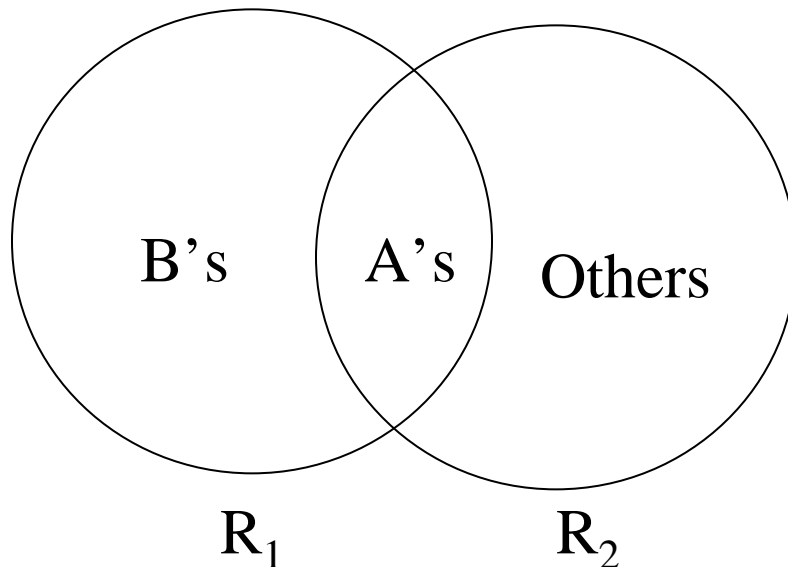
**repeat**

choose  $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$  that violates BCNF

split  $R$  into  $R_1(A_1, \dots, A_m, B_1, \dots, B_n)$  and  $R_2(A_1, \dots, A_m, [\text{others}])$

continue with both  $R_1$  and  $R_2$

**until** no more violations



Is there a  
2-attribute  
relation that is  
not in BCNF ?

In practice, we have  
a better algorithm (coming<sup>105</sup> up)

# Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

SSN → Name, City

What the key?

{SSN, PhoneNumber}

use SSN → Name, City  
to split

# Example

<u>Name</u>	<u>SSN</u>	<u>City</u>
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

SSN → Name, City

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

Let's check anomalies:

- Redundancy ?
- Update ?
- Delete ?

# Example Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN  $\rightarrow$  name, age

age  $\rightarrow$  hairColor

Decompose in BCNF (in class):

# BCNF Decomposition Algorithm

BCNF\_Decompose(R)

find  $X$  s.t.:  $X \neq X^+ \neq$  [all attributes]

**if** (not found) **then** “R is in BCNF”

**let**  $Y = X^+ - X$

**let**  $Z =$  [all attributes]  $- X^+$

decompose R into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$

continue to decompose recursively  $R_1$  and  $R_2$

Find  $X$  s.t.:  $X \neq X^+ \neq$  [all attributes]

# Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

SSN  $\rightarrow$  name, age

age  $\rightarrow$  hairColor

Iteration 1: Person

SSN<sup>+</sup> = SSN, name, age, hairColor

Decompose into: P(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Iteration 2: P

age<sup>+</sup> = age, hairColor

Decompose: People(SSN, name, age)

Hair(age, hairColor)

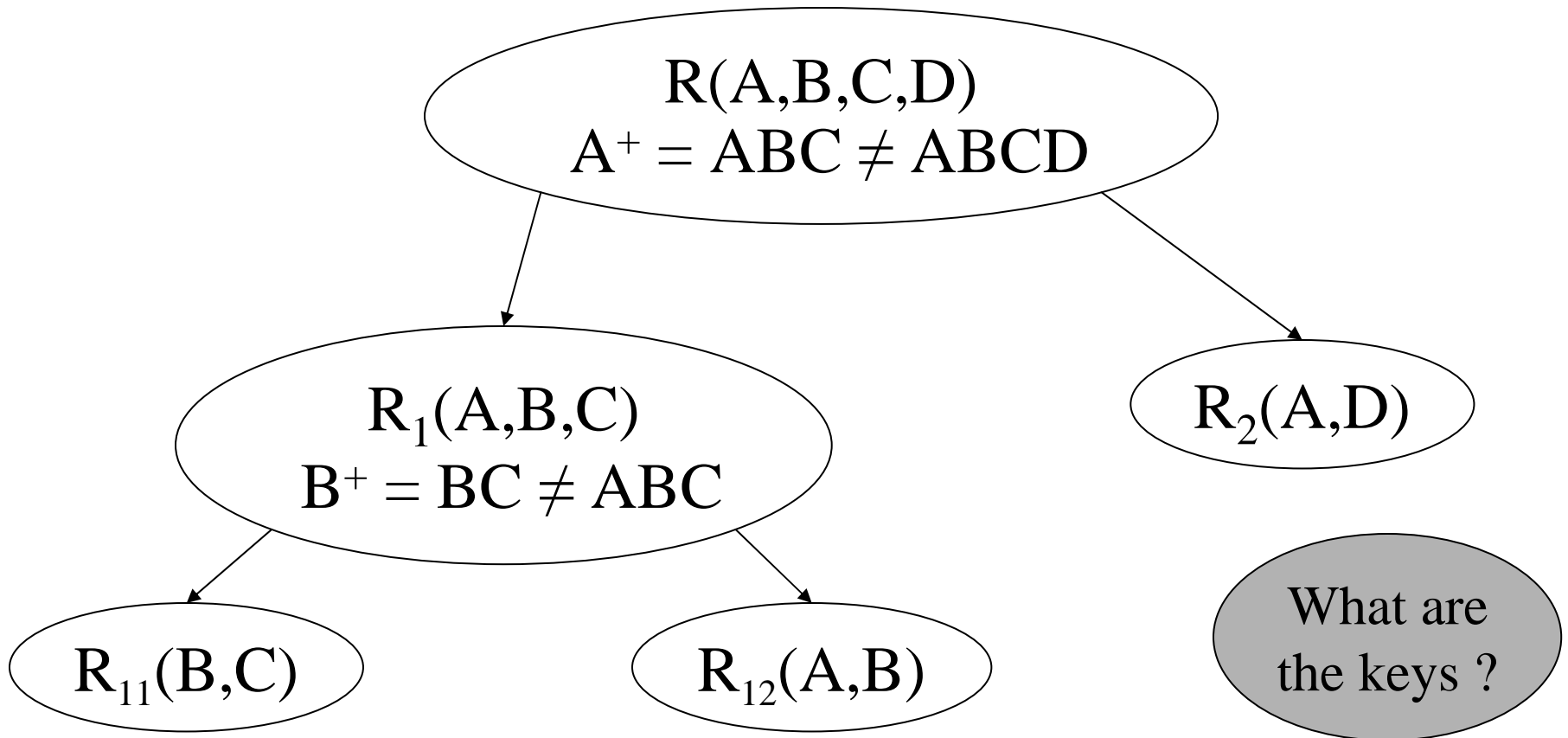
Phone(SSN, phoneNumber)

What are  
the keys ?

$R(A,B,C,D)$

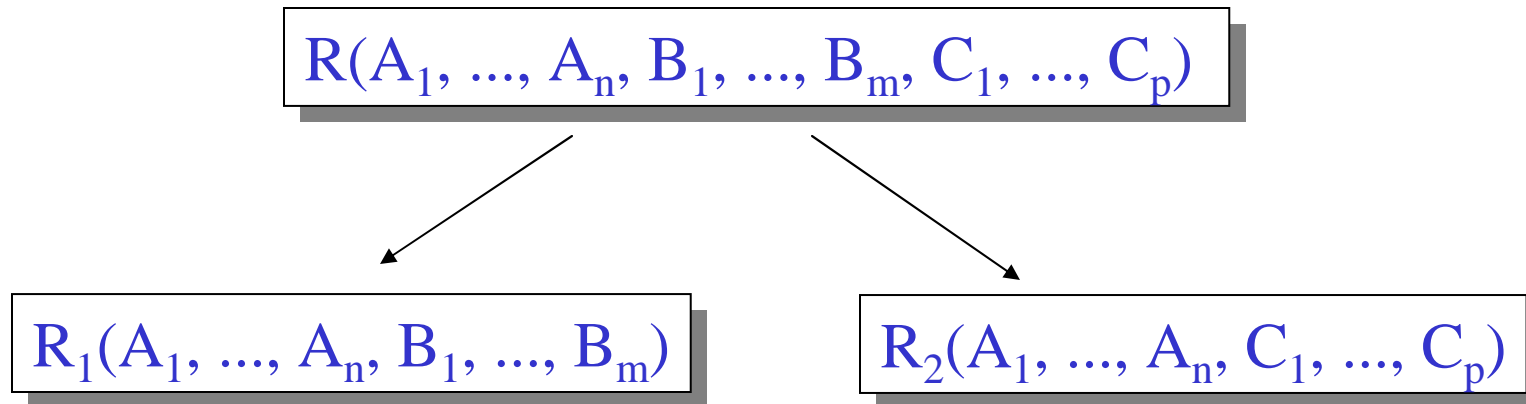
$A \rightarrow B$   
 $B \rightarrow C$

# Example



What happens if in R we first pick  $B^+$  ? Or  $AB_{111}^+$  ?

# Decompositions in General



$R_1$  = projection of  $R$  on  $A_1, \dots, A_n, B_1, \dots, B_m$


$R_2$  = projection of  $R$  on  $A_1, \dots, A_n, C_1, \dots, C_p$



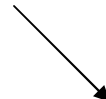
# Theory of Decomposition

- Sometimes it is correct:

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
Gizmo	19.99	Camera



Name	Price
Gizmo	19.99
OneClick	24.99
<del>Gizmo</del>	<del>19.99</del>



Name	Category
Gizmo	Gadget
OneClick	Camera
Gizmo	Camera

Lossless decomposition

# Incorrect Decomposition

- Sometimes it is not:

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
Gizmo	19.99	Camera

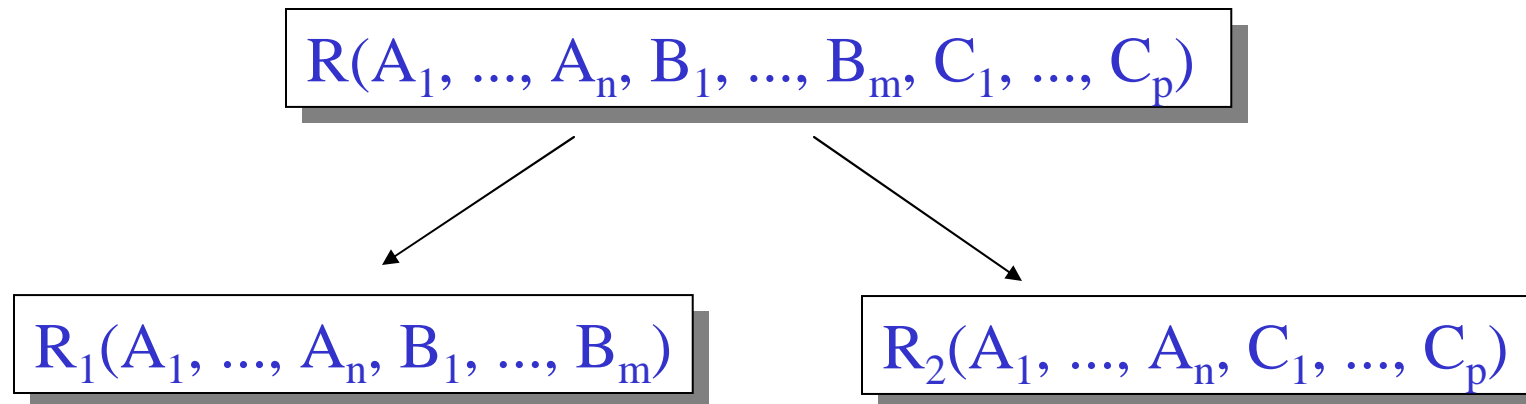
What's incorrect ??

Name	Category
Gizmo	Gadget
OneClick	Camera
Gizmo	Camera

Price	Category
19.99	Gadget
24.99	Camera
19.99	Camera

Lossy decomposition

# Decompositions in General



If  $A_1, \dots, A_n \rightarrow B_1, \dots, B_m$   
Then the decomposition is lossless

Note: don't need  $A_1, \dots, A_n \rightarrow C_1, \dots, C_p$

BCNF decomposition is always lossless. WHY ?