## CSEP 546: Data Mining

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## Program for Today

- Rule induction – Propositional – First-order
- First project

**Rule Induction** 

#### Learning Sets of Rules

Rules are very easy to understand; popular in data mining. • Variable Size. Any boolean function can be represented.

- Deterministic.
- Discrete and Continuous Parameters.

Learning algorithms for rule sets can be described as

- Constructive Search. The rule set is built by adding rules; each rule is constructed by adding conditions.
- Eager.
- Batch.

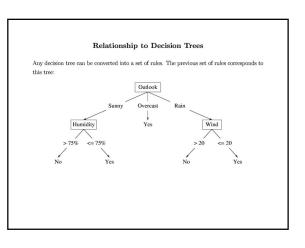


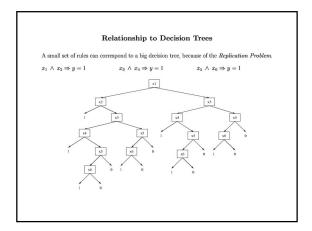
• Each rule is a conjunction of tests. Each test has the form  $x_j=v,\,x_j\leq v,$  or  $x_j\geq v,$  where v is a value for  $x_j$  that appears in the training data.

 $x_1 = Sunny \ \land \ x_2 \leq 75\% \Rightarrow y = 1$ 

 A rule set is a disjunction of rules. Typically all of the rules are for one class (e.g., y = 1). An example is classified into y = 1 if any rule is satisfied.

 $\begin{array}{l} x_1 = Sunny \, \wedge \, x_2 \leq 75\% \, \Rightarrow \, y = 1 \\ \\ x_1 = Overcast \, \Rightarrow \, y = 1 \\ \\ x_1 = Rain \, \wedge \, x_3 \leq 20 \, \Rightarrow \, y = 1 \end{array}$ 





#### Learning a Single Rule

We grow a rule by starting with an empty rule and adding tests one at a time until the rule "covers" only positive examples.

GROWRULE(S)  $R = \{ \}$ repeat

choose best test  $x_j \Theta v$  to add to R, where  $\Theta \in \{=, \neq, \leq, \geq\}$ S := S - all examples that do not satisfy  $R \cup \{x_j \Theta v\}$ . **until** S contains only positive examples.

#### Choosing the Best Test

• Current rule R covers  $m_0$  negative examples and  $m_1$  positive examples. Let  $p = \frac{m_1}{m_0+m_1}$ .

• Proposed rule  $R \cup \{x_j \ominus v\}$  covers  $m'_0$  and  $m'_1$  examples.

Let  $p' = \frac{m'_1}{m'_0 + m'_1}$ .

• Gain =  $m'_1\left[(-p\lg p) - (-p'\lg p')\right]$ 

We want to reduce our surprise (to the point where we are *certain*), but we also want the rule to cover many examples. This formula tries to implement this tradeoff.

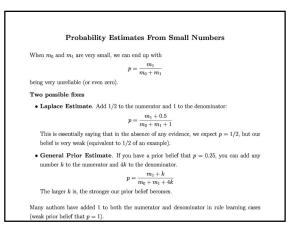
#### Learning a Set of Rules (Separate-and-Conquer)

 $\begin{array}{l} \operatorname{GrowRuleSet}(S) \\ A = \left\{ \right. \right\} \\ repeat \\ R := \operatorname{GrowRule}(S) \\ \operatorname{Add} R \ \text{to} \ A \\ S := S - \ \text{all positive examples that satisfy } R. \\ \textbf{until } S \ \text{is empty.} \\ return \ A \end{array}$ 

#### More Thorough Search Procedures

All of our algorithms so far have used greedy algorithms. Finding the smallest set of rules is NP-Hard. But there are some more thorough search procedures that can produce better rule sets.

- Round-Robin Replacement. After growing a complete rule set, we can delete the first rule, compute the set S of training examples not covered by any rule, and one or more new rules, to cover S. This can be repeated with each of the original rules. This process allows a later rule to "capture" the positive examples of a rule that was learned earlier.
- Backfitting. After each new rule is added to the rule set, we perform a few iterations
  of Round-Robin Replacement (it typically converges quickly). We repeat this process
  of growing a new rule and then performing Round-Robin Replacement until all positive
  examples are covered.
- Beam Search. Instead of growing one new rule, we grow B new rules. We consider adding each possible test to each rule and keep the best B resulting rules. When no more tests can be added, we choose the best of the B rules and add it to the rule set.



### Learning Rules for Multiple Classes

What if rules for more than one class?

Two possibilities:

- Order rules (decision list)
- Weighted vote (e.g., weight = accuracy  $\times$  coverage)

### Learning First-Order Rules

#### Why do that?

- Can learn sets of rules such as  $\begin{aligned} Ancestor(x,y) \leftarrow Parent(x,y) \\ Ancestor(x,y) \leftarrow Parent(x,z) \land Ancestor(z,y) \end{aligned}$
- The PROLOG programming language: programs are sets of such rules

#### First-Order Rule for Classifying Web Pages

[Slattery, 1997]

 $\begin{array}{l} \operatorname{course}(A) \leftarrow \\ & \operatorname{has-word}(A, \operatorname{instructor}), \\ & \neg \operatorname{has-word}(A, \operatorname{good}), \\ & \operatorname{link-from}(A, B), \\ & \operatorname{has-word}(B, \operatorname{assign}), \\ & \neg \operatorname{link-from}(B, C) \end{array}$ 

Train: 31/31, Test: 31/34

#### FOIL (First-Order Inductive Learner)

- Same as propositional separate-and-conquer, except:
- Different candidate specializations (literals)
- Different evaluation function

#### Specializing Rules in FOIL

Learning rule:  $P(x_1, x_2, \ldots, x_k) \leftarrow L_1 \ldots L_n$ 

Candidate specializations add new literal of form:

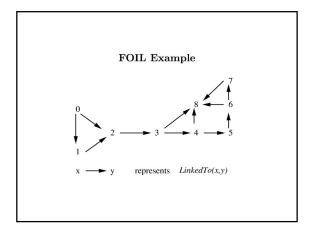
- $Q(v_1, \ldots, v_r)$ , where at least one of the  $v_i$  in the created literal must already exist as a variable in the rule.
- $Equal(x_j, x_k),$  where  $x_j$  and  $x_k$  are variables already present in the rule
- The negation of either of the above forms of literals

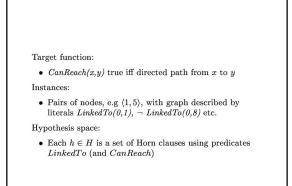
#### Information Gain in FOIL

Foil\_Gain(L, R) 
$$\equiv t \left( \log_2 \frac{p_1}{p_1 + n_1} - \log_2 \frac{p_0}{p_0 + n_0} \right)$$

Where

- L is the candidate literal to add to rule R
- $p_0$  = number of positive bindings of R
- $n_0$  = number of negative bindings of R
- $p_1$  = number of positive bindings of R + L
- $n_1$  = number of negative bindings of R + L
- t = no. of positive bindings of R also covered by R + L





#### Induction as Inverted Deduction

Induction is finding  $\boldsymbol{h}$  such that

 $(\forall \langle x_i, f(x_i) \rangle \in D) \ B \wedge h \wedge x_i \vdash f(x_i)$ 

where

- $x_i$  is *i*th training instance
- $f(x_i)$  is the target function value for  $x_i$
- B is other background knowledge

So let's design inductive algorithm by inverting operators for automated deduction.

#### Induction as Inverted Deduction

"Pairs of people  $\langle u,v\rangle$  such that child of u is v "

- $f(x_i)$ : Child(Bob, Sharon)
- $\begin{array}{lll} x_i: & Male(Bob), Female(Sharon), Father(Sharon, Bob) \\ B: & Parent(u,v) \leftarrow Father(u,v) \end{array}$

What satisfies  $(\forall \langle x_i, f(x_i) \rangle \in D) \ B \land h \land x_i \vdash f(x_i)$ ?

- $h_1: Child(u, v) \leftarrow Father(v, u)$
- $h_2: Child(u, v) \leftarrow Parent(v, u)$

#### Induction as Inverted Deduction

We have mechanical *deductive* operators F(A, B) = C, where  $A \land B \vdash C$ 

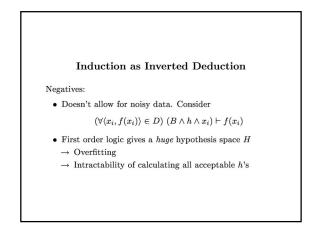
Need *inductive* operators

O(B,D) = h where  $(\forall \langle x_i, f(x_i) \rangle \in D) \ (B \land h \land x_i) \vdash f(x_i)$ 

#### Induction as Inverted Deduction

Positives:

- Subsumes earlier idea of finding h that "fits" training data
- Domain theory B helps define meaning of "fit" the data  $B \wedge h \wedge x_i \vdash f(x_i)$
- Suggests algorithms that search  ${\cal H}$  guided by  ${\cal B}$



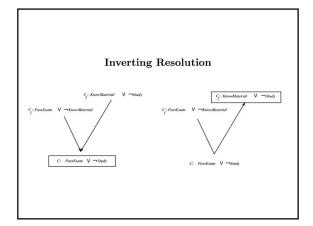
#### **Deduction: Resolution Rule**

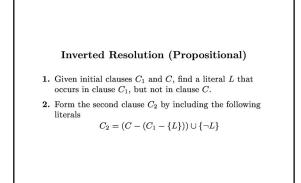
$$\begin{array}{cccc} P & \lor & L \\ \neg L & \lor & R \\ \hline P & \lor & R \end{array}$$

- 1. Given initial clauses  $C_1$  and  $C_2$ , find a literal L from clause  $C_1$  such that  $\neg L$  occurs in clause  $C_2$
- Form the resolvent C by including all literals from C<sub>1</sub> and C<sub>2</sub>, except for L and ¬L. More precisely, the set of literals occurring in the conclusion C is

 $C = (C_1 - \{L\}) \cup (C_2 - \{\neg L\})$ 

where  $\cup$  denotes set union, and "-" is set difference





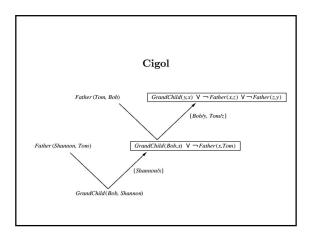
#### **First-Order Resolution**

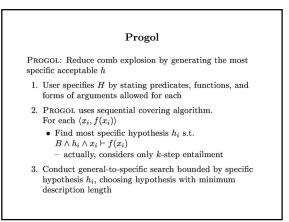
- 1. Find a literal  $L_1$  from clause  $C_1$ , literal  $L_2$  from clause  $C_2$ , and substitution  $\theta$  such that  $L_1\theta = \neg L_2\theta$
- Form the resolvent C by including all literals from C<sub>1</sub>θ and C<sub>2</sub>θ, except for L<sub>1</sub>θ and ¬L<sub>2</sub>θ. More precisely, the set of literals occurring in the conclusion C is

$$C = (C_1 - \{L_1\})\theta \cup (C_2 - \{L_2\})\theta$$

### **Inverting First-Order Resolution**

 $C_2 = (C - (C_1 - \{L_1\})\theta_1)\theta_2^{-1} \cup \{\neg L_1\theta_1\theta_2^{-1}\}$ 





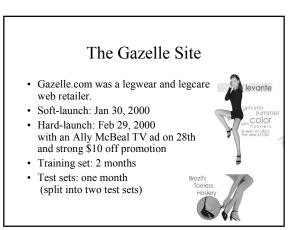
#### **Rule Induction: Summary**

- Rule grown by adding one antecedent at a time
- Rule set grown by adding one rule at a time
- Propositional or first-order
- Alternative: inverse resolution

## First Project: Clickstream Mining

## Overview

- The Gazelle site
- Data collection
- · Data pre-processing
- KDD Cup
- · Hints and findings



## Data Collection

- Site was running Blue Martini's Customer Interaction System version 2.0
- Data collected includes:

#### - Clickstreams

- Session: date/time, cookie, browser, visit count, referrer
- Page views: URL, processing time, product, assortment (assortment is a collection of products, such as back to school)
- Order information
  - · Order header: customer, date/time, discount, tax, shipping.
  - Order line: quantity, price, assortment
- Registration form: questionnaire responses

## Data Pre-Processing

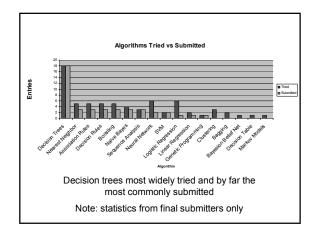
- Acxiom enhancements: age, gender, marital status, vehicle type, own/rent home, etc.
- Keynote records (about 250,000) removed. They hit the home page 3 times a minute, 24 hours.
- Personal information removed, including: Names, addresses, login, credit card, phones, host name/IP, verification question/answer. Cookie, e-mail obfuscated.
- Test users removed based on multiple criteria (e.g., credit card) not available to participants
- Original data and aggregated data (to session level) were provided

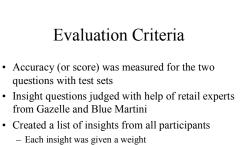
## **KDD** Cup Questions

- 1. Will visitor leave after this page?
- 2. Which brands will visitor view?
- 3. Who are the heavy spenders?
- 4. Insights on Question 1
- 5. Insights on Question 2

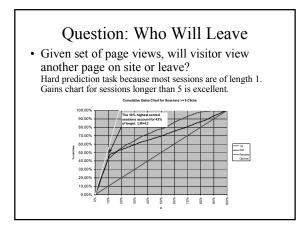
## **KDD** Cup Statistics

- 170 requests for data
- 31 submissions
- 200 person/hours per submission (max 900)
- Teams of 1-13 people (typically 2-3)

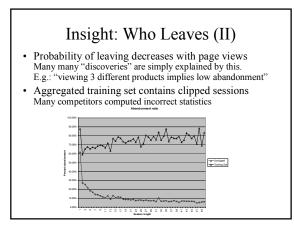


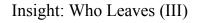


- Each insight was given a weight
   Each participant was scored on all insights
- Additional factors: presentation quality, correctness

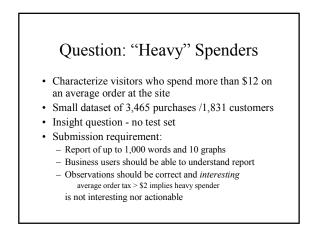


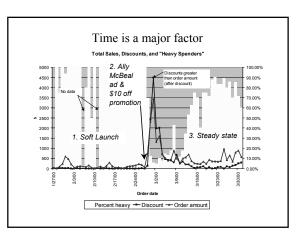




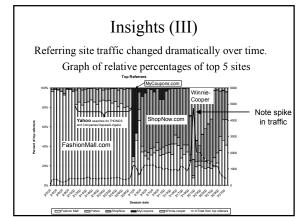


- People who register see 22.2 pages on average compared to 3.3 (3.7 without crawlers)
- Free Gift and Welcome templates on first three pages encouraged visitors to stay at site
- Long processing time (> 12 seconds) implies high abandonment Actionable
- Users who spend less time on the first few pages (session time) tend to have longer session lengths









#### Insights (IV) · Referrers - establish ad policy based on conversion rates, not clickthroughs - Overall conversion rate: 0.8% (relatively low) - MyCoupons had 8.2% conversion rate, but low spenders - FashionMall and ShopNow brought 35,000 visitors Only 23 purchased (0.07% conversion rate!) What about Winnie-Cooper? Winnie Cooper is a 31-year-old guy who wears pantyhose and has a pantyhose site.

8,700 visitors came from his site (!). · Make him a celebrity, interview him about

how hard it is for men to buy in stores Personalize for XL sizes

Actions:

•

40.00

30.00 20.00



# **Common Mistakes**

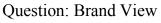
- Insights need support Rules with high confidence are meaningless when they apply to 4 people
- Dig deeper Many "interesting" insights with interesting explanations were simply identifying periods of the site. For example:
  - "93% of people who responded that they are purchasing for others are heavy purchasers. True, but simply identifying people who registered prior

to 2/28, before the form was changed. Similarly, "presence of children" (registration form)

implies heavy spender.



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- · Given set of page views, which product brand will visitor view in remainder of the session? (Hanes, Donna Karan, American Essentials, or none)
- Good gains curves for long sessions (lift of 3.9, 3.4, and 1.3 for three brands at 10% of data).
- Referrer URL is great predictor
  - Karan different population segments reach these sites MyCoupons, Tripod, DealFinder are referrers for American
- Essentials AE contains socks, excellent for coupon users · Previous views of a product imply later views
- Few realized Donna Karan only available > Feb 26

- - FashionMall, Winnie-Cooper are referrers for Hanes, Donna

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# Project

- Implement decision tree learner
- Apply to first question (Who leaves?)
- Improve accuracy by refining data
- Report insights
- Good luck and have fun!