## Time, Clocks, and the Ordering of Events in a Distributed System

Motivating example: a distributed compilation service

- FTP server storing source files, object files, executable file
- stored files have timestamps, set by client and preserved by server
- basic procedure to depcheck(A)
- consider file A that depends on file B
- if timestamp (A) < timestamp (B)
- compile B
- compile:
- depcheck of B
- fetch file
- compile file
- store result
- does this work?
- need client clocks to be tightly synchronized
- offset must be less than time to fetch/compile a file
- alternative is to use logical clocks, obviously


## Basic idea behind causal ordering



- Three concepts we have to pin down: process, events, and messages
- what is a process?
- threads on a multiprocessor? Processes on OS? Etc.
- three kinds of events in a distributed system
- local computation
- $\operatorname{send}(\mathrm{M})$
- receive(M)
- what is a message?
- shared memory communication?

Lamport's happens before (" $\rightarrow$ ") relation

- within a process, if P1 comes before P2, then P1 $\rightarrow$ P2
- why?
- can we have P1, P2 concurrent with each other?
- across processes: message has two events, $a=\operatorname{send}(m), b=\operatorname{receive}(m)$
- $\mathrm{a} \rightarrow \mathrm{b}$
- why?
- in shared memory, aren't $\mathrm{a}, \mathrm{b}$ at the same time? (No!)
- transitivity
- if $\mathrm{a} \rightarrow \mathrm{b}$ and $\mathrm{b} \rightarrow \mathrm{c}$, then $\mathrm{a} \rightarrow \mathrm{c}$
- why?
- interpretation of happens before as "could have influenced", i.e., causality
- Physical interpretation: $\mathrm{a} \rightarrow \mathrm{b}$ if you can move from a to b in the diagram by following time within a process or message lines across processes
- two different events $\mathrm{a}, \mathrm{b}$ are concurrent if neither $\mathrm{a} \rightarrow \mathrm{b}$ nor $\mathrm{b} \rightarrow \mathrm{a}$
- interpretation as "could not have influenced"


## Abstract logical clock

We want to build a system of clocks that respect causality

- each process Pi has a local clock Ci
- time of an event "a" at Pi is $\mathrm{Ci}(a)$
- we want to logically synchronize the clocks, so that there is a global notion of time $\mathrm{C}(\mathrm{a})=\mathrm{Ci}(\mathrm{A})$
- for this to be meaningful, the global clock C must respect lamport's "clock condition"
- for any events $\mathrm{a}, \mathrm{b}$ : if $\mathrm{a} \rightarrow \mathrm{b}$ then $\mathrm{C}(\mathrm{a})<\mathrm{C}(\mathrm{b})$
- so, an event that happens before is earlier in global logical time
- there are two subconditions that, if they are respected, imply the clock condition
- C1: if $\mathrm{a}, \mathrm{b}$ are events in Pi and a is before b , then $\mathrm{Ci}(\mathrm{a})<\mathrm{Ci}(\mathrm{b})$
- C2: if $a=\operatorname{send}(m)$ and $b=$ receive $(m)$, then $\mathrm{Ci}(a)<\mathrm{Cj}(\mathrm{b})$

Imposes a series of tickpoints on the diagram

- C 1 : at least one tick between any two events on a process line
- C2: at least one tick between the send and receive of a message

and then straighten the lines:



## Implementing logical clocks

There are many different implementations of logical clocks that are consistent with Lamport's clock conditions. He gives one:

- Each process Pi maintains a local counter Ci
- IR1:
- Each process Pi increments Ci between any two successive events
- IR2:
- Each process piggybacks timestamp Tm on a message it sents, where Tm is Ci at the time of sending m
- If $\mathrm{a}=\operatorname{send}(\mathrm{m})$ by Pi , then m contains $\mathrm{Tm}=\mathrm{Ci}(\mathrm{a})$
- On receiving $\mathrm{m}, \mathrm{Pj}$ sets Cj to $\max (\mathrm{Cj}, \mathrm{Tm}+1)$
- The receipt of $m$ is a separate event that then separately advances Cj
- Properties of this implementation?
- Respects causality
- If a $\rightarrow$ b, then $\mathrm{C}(\mathrm{a})<\mathrm{C}(\mathrm{b})$
- But, converse is not true
- If $\mathrm{C}(\mathrm{a})<\mathrm{C}(\mathrm{b})$, don't know that $\mathrm{a} \rightarrow \mathrm{b}$
- Why? Both cases are possible
- Could be concurrent
- Could be causally preceeding


## Global ordering

- Use logical clock to set order
- If tie, use process IDs as tiebreaker
- i.e., global order is (Logical timestamp) . (process ID)

Problems with causal ordering

- There could be events outside of the system that have causal influence on the evolution of the system
- e.g., users telephoning each other. System could choose to order events in way that breaks the telephone causality, since it doesn't know the events are causally related.
- Is there a way to implement a system that captures all forms of causality?
- Hypothetically, yes - this is the Einstein relativity and physical clocks
- Need to keep clocks in tight synchronization with each other, in particular, any pair of clocks' offsets must be less than min transmission time between them
- Hard question:
- If all you can do to synchronize clocks is use the messages inherent in the system, can you synchronize tightly enough to meet this bound?
- Lamport argues yes
- Causal ordering doesn't actually imply influence, just potential influence
- Causal consistency algorithms tend to overconstrain as a result

Q: how far from physical time can logical time diverge? I.e., if logical time says two events are concurrent, how far apart in time could they actually occur?

- Arbitrarily far, as clocks can run at independent rates until interaction occurs
- Depends on clock synchronization, depends on how long until interaction (or transitive interaction) occurs.


## Alternate system of logical clocks: vector timestamps, a.k.a. version vectors

Remember that with Lamport clocks, if a $\rightarrow \mathrm{b}$, then $\mathrm{C}(\mathrm{a})<\mathrm{C}(\mathrm{b})$, but the converse is not true.

We can build a logical clock that satisfies the clock condition, but for which the converse is true: a vector clock.

- Each node maintains a vector of counters, one for each node in the system
- IR1:
- If two events a and b in Pi , and b is after a , then Pi sets $\operatorname{VCi}[\mathrm{i}]=\mathrm{VCi}[\mathrm{i}]+1$
- IR2:
- If $a$ is "Pi sends $m$ " and $b$ is " $P j$ receives $m$ ", then:
- Pi increments $\mathrm{VCi}[\mathrm{i}]$ and copies its full vector clock into $m$
- For each $\mathrm{k}, \mathrm{VCj}[\mathrm{k}]=\max (\mathrm{VCj}[\mathrm{k}]$, timestamp $[\mathrm{k}])$

Need to know how to compare vector clocks:
$\mathrm{VCi}<\mathrm{VCj}$ iff for all $\mathrm{k}, \mathrm{VCi}[\mathrm{k}]<=\operatorname{VCj}[\mathrm{k}]$ and there is one k s.t. $\mathrm{VCi}[\mathrm{k}]<\mathrm{VCj}[\mathrm{k}]$
It's basically the partial order captured perfectly.

Back to distributed make

- How to fix?
- Use different ordering: causal ordering
- Make clocks more strongly synchronized
- Physical clock ordering is consistent with "happens-before" relationship if and only if length $($ event +msg transmit $)>\mathrm{d}$
- Makes sure timestamps cannot go backwards
- How tight? If clocks $|\mathrm{Ci}-\mathrm{Cj}|<\mathrm{d}$ for all $\mathrm{I}, \mathrm{j}$ then need length (compilation + msg transmit) $>\mathrm{d}$
- Not always true, especially as compiles get faster
- Or, change timestamps at file server!!
- Why does this work?

