CSE P 573 Artificial Intelligence Spring 2014

Ali Farhadi Problem Spaces and Search

slides from Dan Klein, Stuart Russell, Andrew Moore, Dan Weld, Pieter Abbeel, Luke Zettelmoyer

Outline

- Agents that Plan Ahead
- Search Problems
- Uninformed Search Methods (part review for some)
 - Depth-First Search
 - Breadth-First Search
 - Uniform-Cost Search
- Heuristic Search Methods (new for all)
 - Best First / Greedy Search

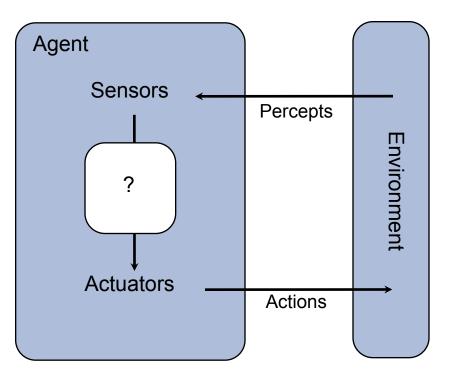
Review: Agents

An agent:

- Perceives and acts
- Selects actions that maximize its utility function
- Has a goal

Environment:

• Input and output to the agent



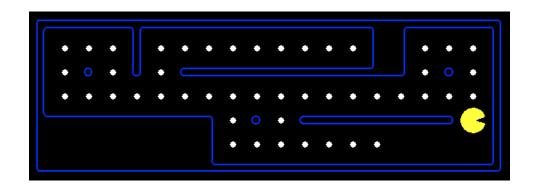
Search -- the environment is: fully observable, single agent, deterministic, static, discrete

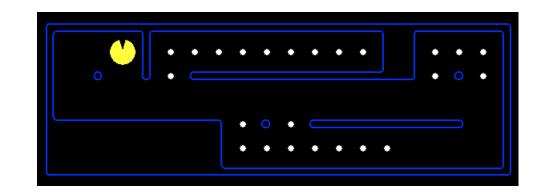


Reflex Agents

Reflex agents:

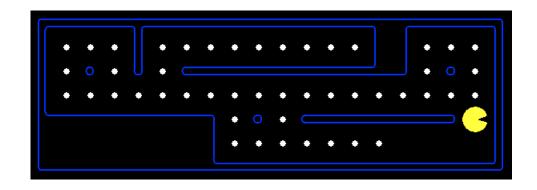
- Choose action based on current percept (and maybe memory)
- Do not consider the future consequences of their actions
- Act on how the world IS
- Can a reflex agent achieve goals?

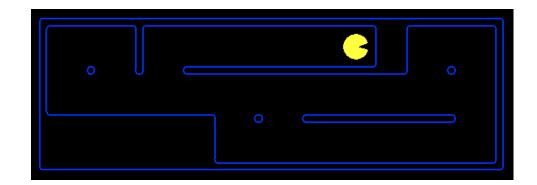




Goal Based Agents

- Goal-based agents:
 - Plan ahead
 - Ask "what if"
 - Decisions based on (hypothesized) consequences of actions
 - Must have a model of how the world evolves in response to actions
 - Act on how the world WOULD BE





Search thru a Problem Space / State Space

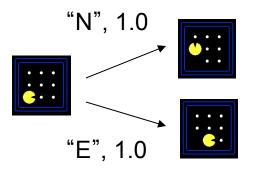
- Input:
 - Set of states
 - Successor Function [and costs default to 1.0]
 - Start state
 - Goal state [test]
 - Output:
 - Path: start \Rightarrow a state satisfying goal test
 - [May require shortest path]
 - [Sometimes just need state passing test]

Example: Simplified Pac-Man

- Input:
 - A state space



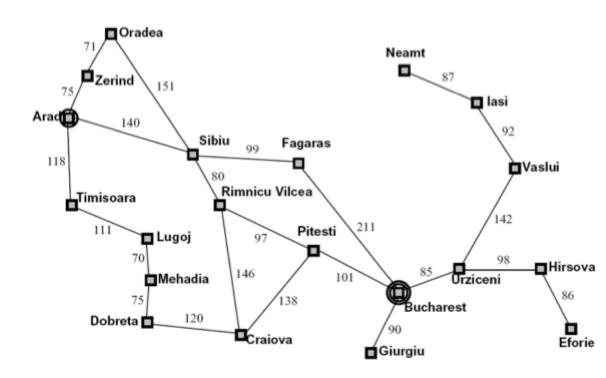
A successor function



- A start state
- A goal test
- Output:

Ex: Route Planning: Romania \rightarrow Bucharest

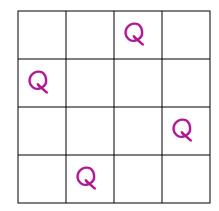
- Input:
 - Set of states
 - Operators [and costs]
 - Start state
 - Goal state (test)
- Output:



Example: N Queens

Input:

- Set of states
- Operators [and costs]
- Start state
- Goal state (test)
- Output



Algebraic Simplification

 $\partial_r^2 u = -\left[E' - \frac{l(l+1)}{r^2} - r^2\right] u(r)$ $e^{-2s} \left(\partial_s^2 - \partial_s\right) u(s) = -\left[E' - l(l+1)e^{-2s} - e^{2s}\right] u(s)$ $e^{-2s} \left[e^{\frac{1}{2}s} \left(e^{-\frac{1}{2}s}u(s)\right)'' - \frac{1}{4}u\right] = -\left[E' - l(l+1)e^{-2s} - e^{2s}\right] u(s)$ $e^{-2s} \left[e^{\frac{1}{2}s} \left(e^{-\frac{1}{2}s}u(s)\right)''\right] = -\left[E' - \left(l + \frac{1}{2}\right)^2 e^{-2s} - e^{2s}\right] u(s)$ $v'' = -e^{2s} \left[E' - \left(l + \frac{1}{2}\right)^2 e^{-2s} - e^{2s}\right] v$

Input:

Introducing

Παρουσιάζουμε το Featuring a new generation of

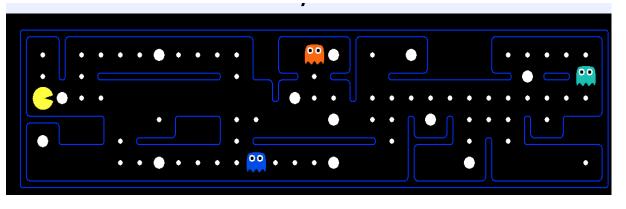
advanced algorithms with unparalleled

speed, scope, and scalability .

- Set of states
- Operators [and costs]
- Start state
- Goal state (test)
- Output:

What is in State Space?

A world state includes every details of the environment



A search state includes only details needed for planning
 Problem: Pathing
 Problem: Eat-all-dots

States: {x,y} locations Actions: NSEW moves Successor: update location Goal: is (x,y) End? States: {(x,y), dot booleans}

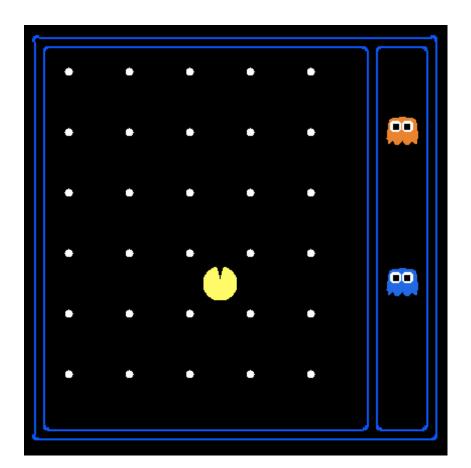
Actions: NSEW moves

Successor: update location and dot boolean

Goal: dots all false?

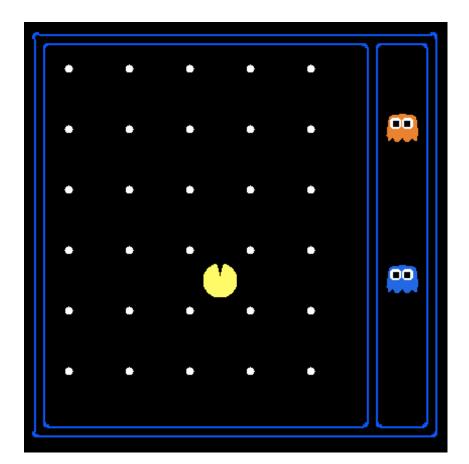
State Space Sizes?

- World states:
- Pacman positions:
 10 x 12 = 120
- Pacman facing: up, down, left, right
- Food Count: 30
- Ghost positions: 12

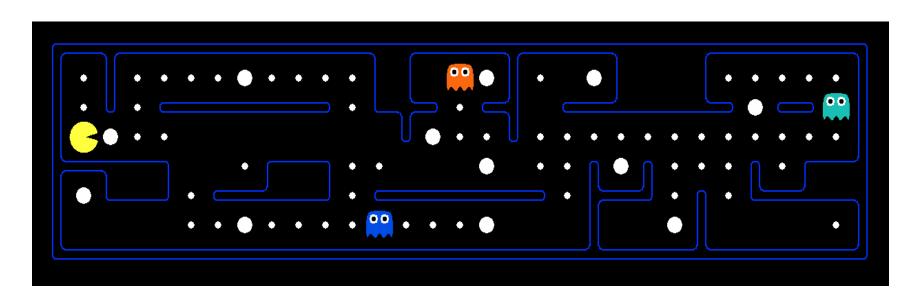


State Space Sizes?

- How many?
- World State:
 - 120*(230)*(122)*4
- States for Pathing:
 - 120
- States for eat-all-dots: 120*(2³⁰)



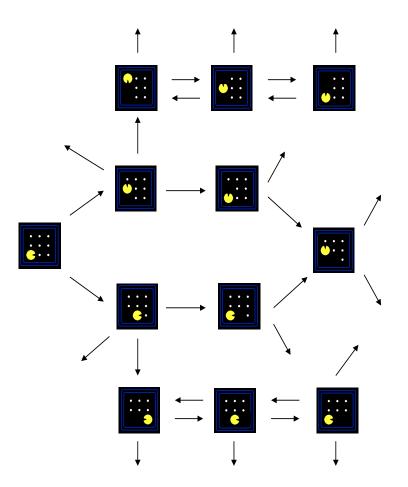
Quiz: Safe Passage



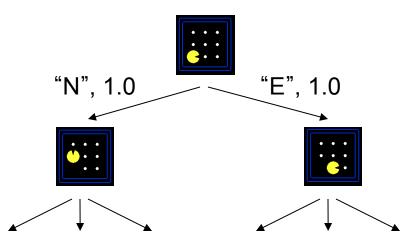
- Problem: eat all dots while keeping the ghosts perma-scared
- What does the state space have to specify?

State Space Graphs

- State space graph:
 - Each node is a state
 - The successor function is represented by arcs
 - Edges may be labeled with costs
- We can rarely build this graph in memory (so we don't)



Search Trees

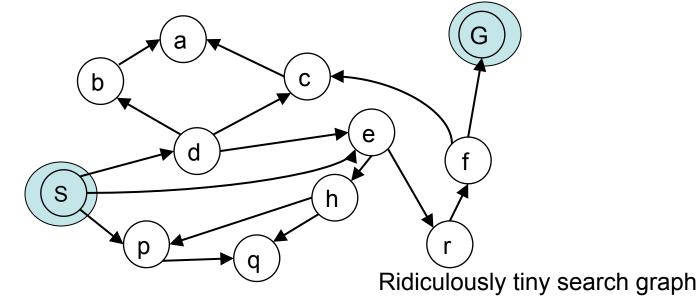


A search tree:

- Start state at the root node
- Children correspond to successors
- Nodes contain states, correspond to PLANS to those states
- Edges are labeled with actions and costs
- For most problems, we can never actually build the whole tree

Example: Tree Search

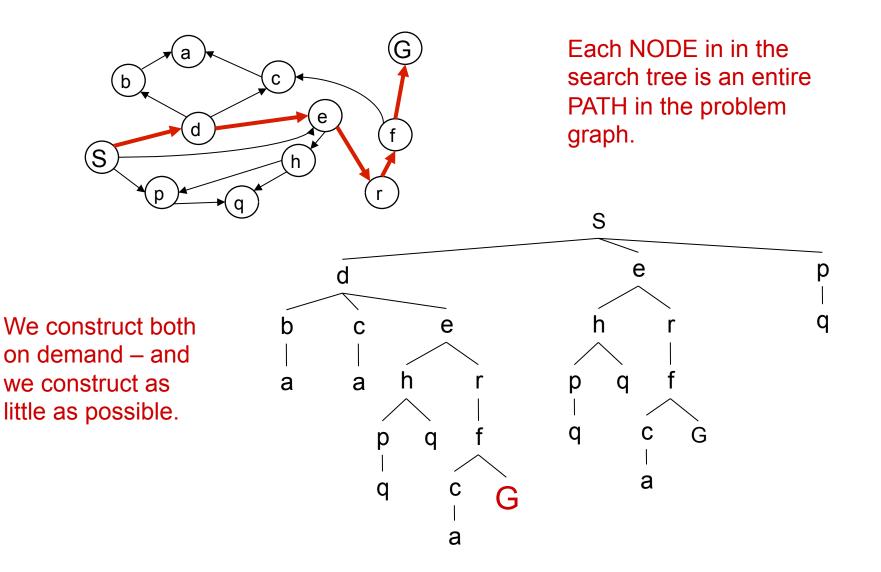
State Graph:



for a tiny search problem

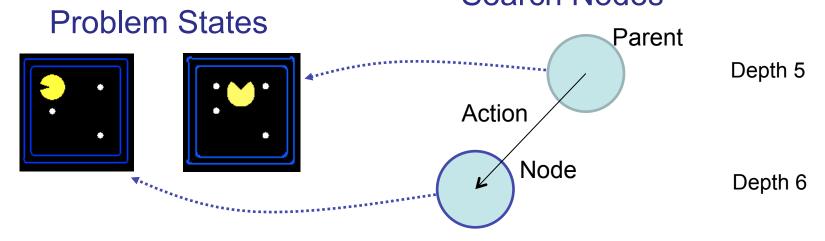
What is the search tree?

State Graphs vs. Search Trees



States vs. Nodes

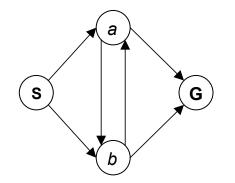
- Nodes in state space graphs are problem states
 - Represent an abstracted state of the world
 - Have successors, can be goal / non-goal, have multiple predecessors
- Nodes in search trees are plans
 - Represent a plan (sequence of actions) which results in the node's state
 - Have a problem state and one parent, a path length, a depth & a cost
 - The same problem state may be achieved by multiple search tree nodes
 Search Nodes



Quiz: State Graphs vs. Search Trees

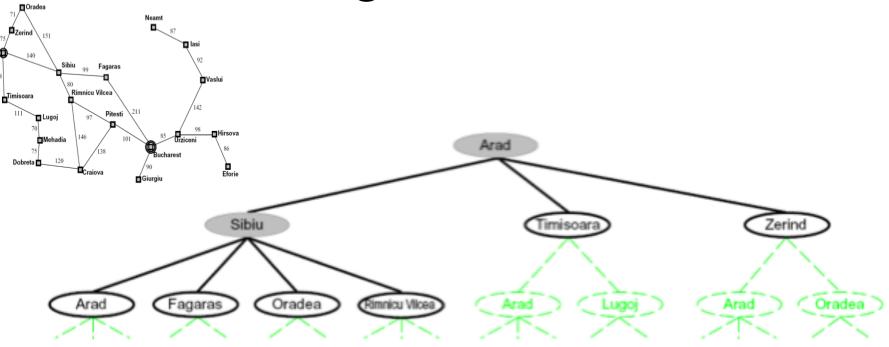
Consider this 4-state graph:

How big is its search tree (from S)?



Important: Lots of repeated structure in the search tree!

Building Search Trees



Search:

- Expand out possible plans
- Maintain a fringe of unexpanded plans
- Try to expand as few tree nodes as possible

General Tree Search

function TREE-SEARCH(problem, strategy) returns a solution, or failure
initialize the search tree using the initial state of problem
loop do
 if there are no candidates for expansion then return failure
 choose a leaf node for expansion according to strategy
 if the node contains a goal state then return the corresponding solution
 else expand the node and add the resulting nodes to the search tree
end

- Important ideas:
 - Fringe
 - Expansion
 - Exploration strategy

Main question: which fringe nodes to explore?

Detailed pseudocode is in the book!

Search Methods

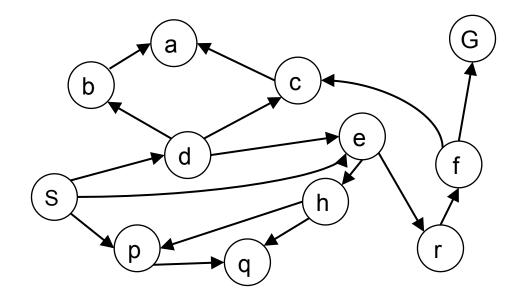
Uninformed Search Methods (part review for some)

- Depth-First Search
- Breadth-First Search
- Uniform-Cost Search
- Heuristic Search Methods (new for all)
 - Best First / Greedy Search

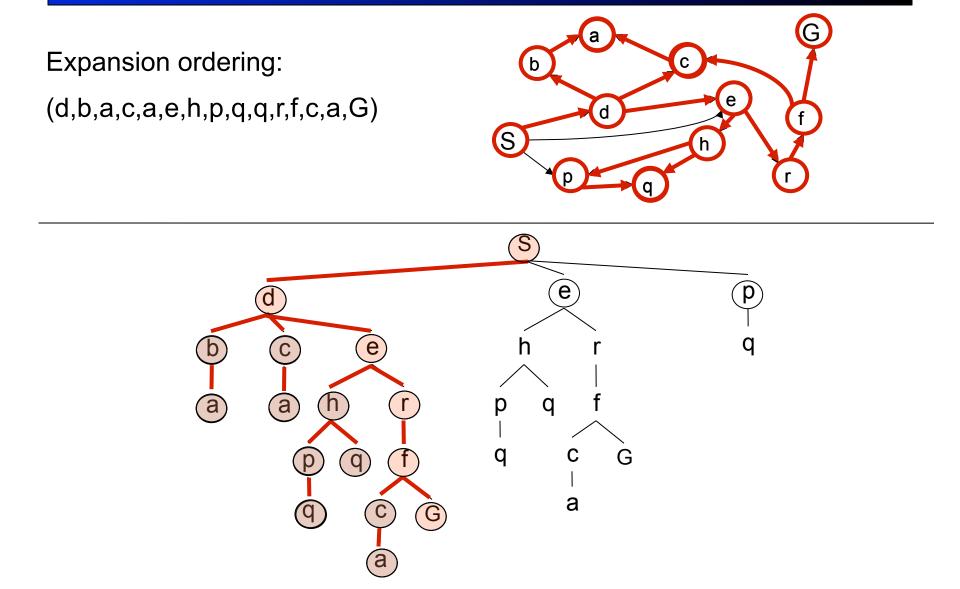
Review: Depth First Search

Strategy: expand deepest node first

Implementation: Fringe is a LIFO queue (a stack)



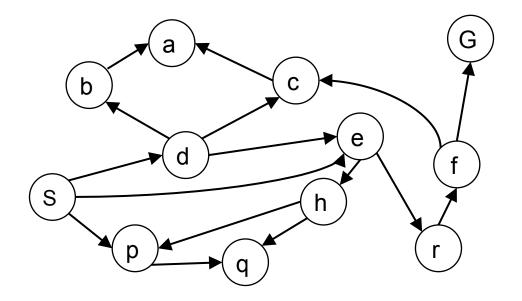
Review: Depth First Search



Review: Breadth First Search

Strategy: expand shallowest node first

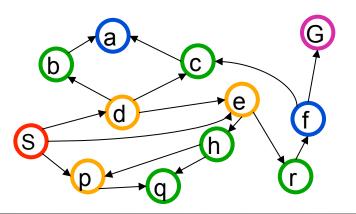
Implementation: Fringe is a FIFO queue

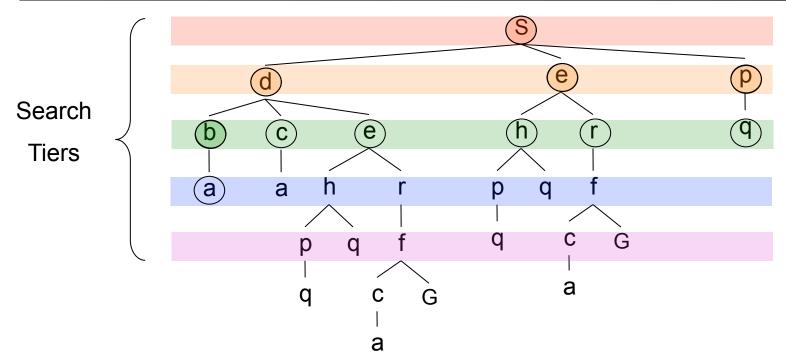


Review: Breadth First Search

Expansion order:

(S,d,e,p,b,c,e,h,r,q,a,a ,h,r,p,q,f,p,q,f,q,c,G)





Search Algorithm Properties

- Complete? Guaranteed to find a solution if one exists?
- Optimal? Guaranteed to find the least cost path?
- Time complexity?
- Space complexity?

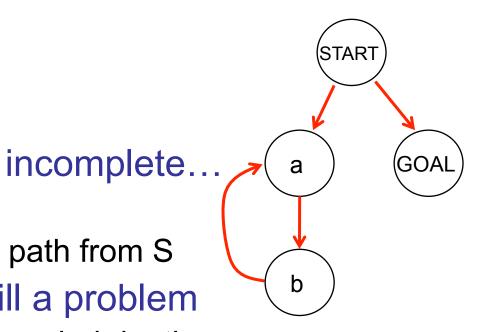
Variables:

n	Number of states in the problem
b	The maximum branching factor B (the maximum number of successors for a state)
C*	Cost of least cost solution
d	Depth of the shallowest solution
m	Max depth of the search tree

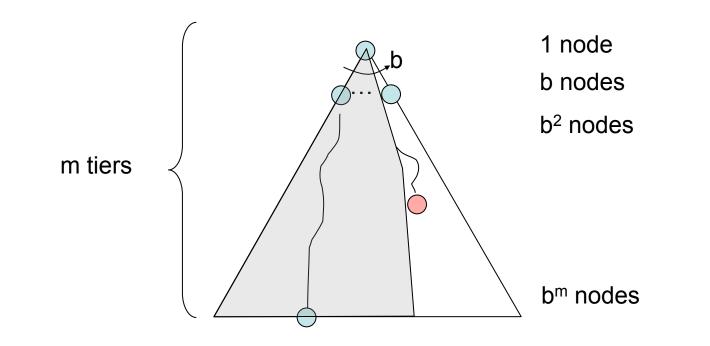
DFS

Algorith	m	Complete	Optimal	Time	Space
	Depth First Search	No	No	Infinite	Infinite

- Infinite paths make DFS incomplete...
 - How can we fix this?
 - Check new nodes against path from S
- Infinite search spaces still a problem
 - If the left subtree has unbounded depth



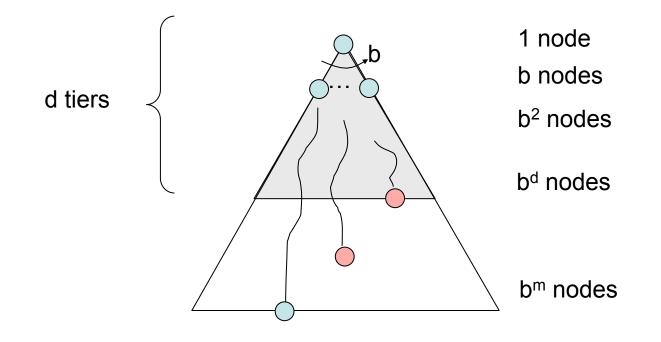
DFS



Algorith	m	Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y if finite	N	O(b ^m)	O(bm)

BFS

Algorithm		Complete	Optimal	Time	Space
	w/ Path Checking	Y	N	O(b ^m)	O(bm)
BFS		Y	Y*	O(b ^d)	O(b ^d)



Comparisons

When will BFS outperform DFS?

When will DFS outperform BFS?

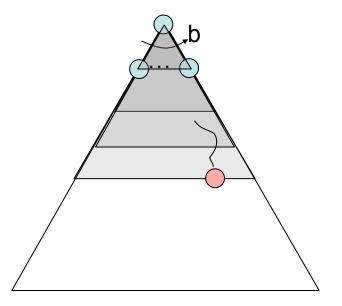
7% Search Strategies Demo	

Iterative Deepening

Iterative deepening uses DFS as a subroutine:

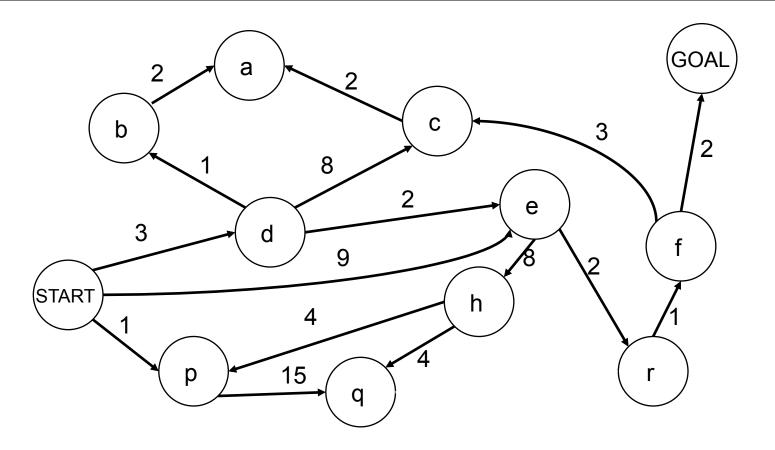
- 1. Do a DFS which only searches for paths of length 1 or less.
- 2. If "1" failed, do a DFS which only searches paths of length 2 or less.
- 3. If "2" failed, do a DFS which only searches paths of length 3 or less.

....and so on.



Algorithm		Complete	Optimal	Time	Space
	w/ Path Checking	Y	N	O(b ^m)	O(bm)
BFS		Y	Y*	O(b ^d)	O(b ^d)
ID		Y	Y*	O(b ^d)	O(bd)

Costs on Actions



Notice that BFS finds the shortest path in terms of number of transitions. It does not find the least-cost path.

Best-First Search

- Generalization of breadth-first search
- Priority queue of nodes to be explored
- Cost function f(n) applied to each node

Add initial state to priority queue While queue not empty Node = head(queue) If goal?(node) then return node Add children of node to queue

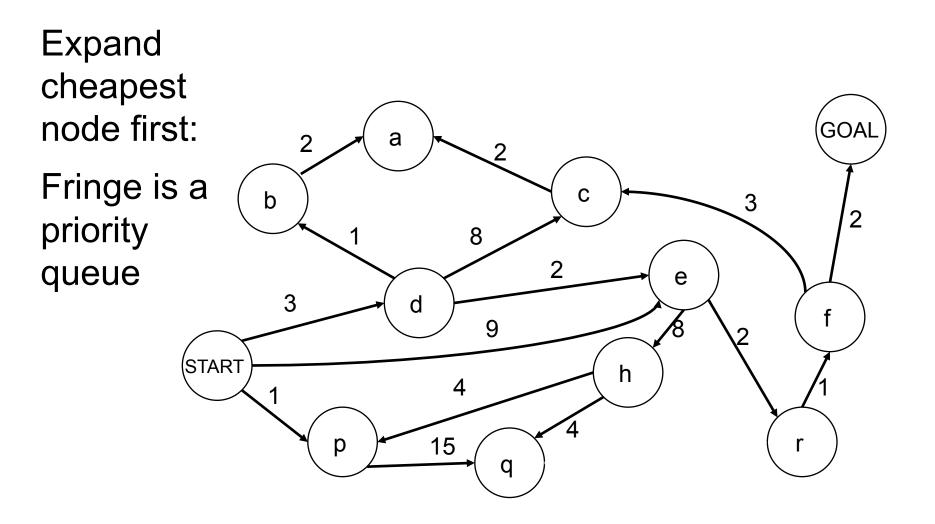


A priority queue is a data structure in which you can insert and retrieve (key, value) pairs with the following operations:

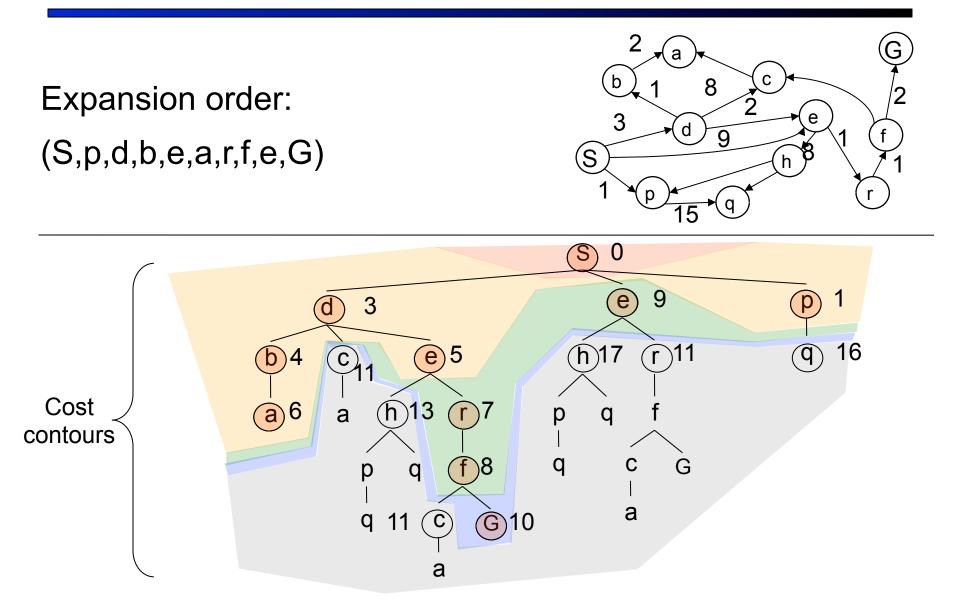
pq.push(key, value)	inserts (key, value) into the queue.	
pq.pop()	returns the key with the lowest value, and removes it from the queue.	

- You can decrease a key's priority by pushing it again
- Unlike a regular queue, insertions aren't constant time, usually O(log n)
- We'll need priority queues for cost-sensitive search methods

Uniform Cost Search

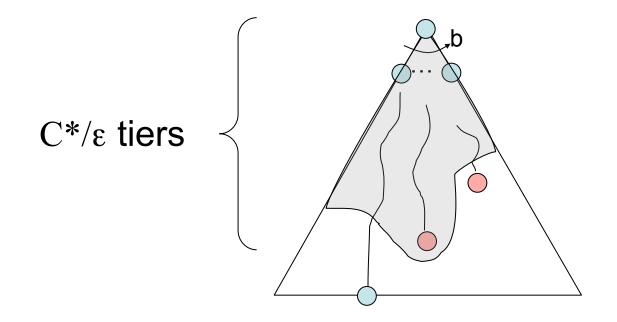


Uniform Cost Search



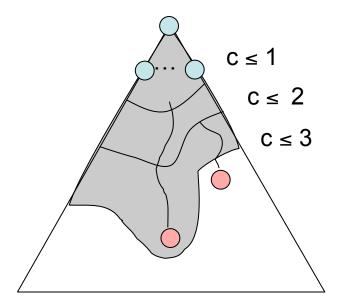
Uniform Cost Search

Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y	N	O(b ^m)	O(bm)
BFS		Y	Y*	O(b ^d)	O(b ^d)
UCS		Y*	Y	$O(b^{C^{*/\epsilon}})$	$O(b^{C^{*/\epsilon}})$

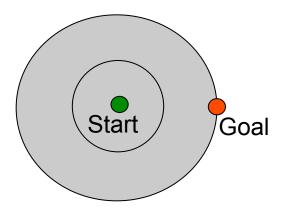


Uniform Cost Issues

- Remember: explores increasing cost contours
- The good: UCS is complete and optimal!

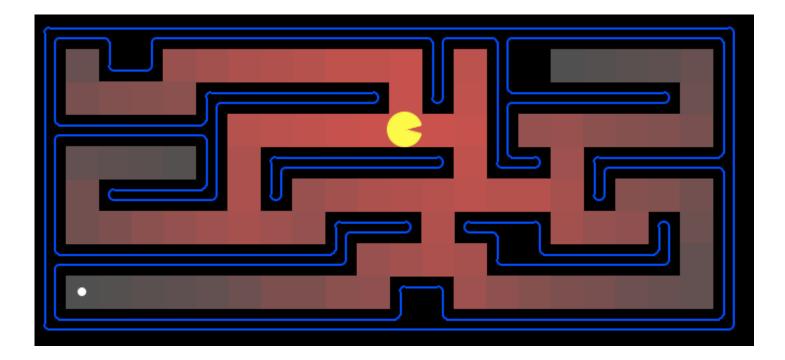


- The bad:
 - Explores options in every "direction"
 - No information about goal location



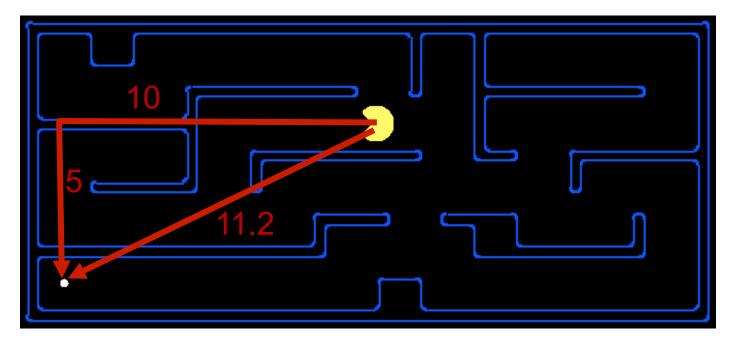
Uniform Cost: Pac-Man

- Cost of 1 for each action
- Explores all of the states, but one



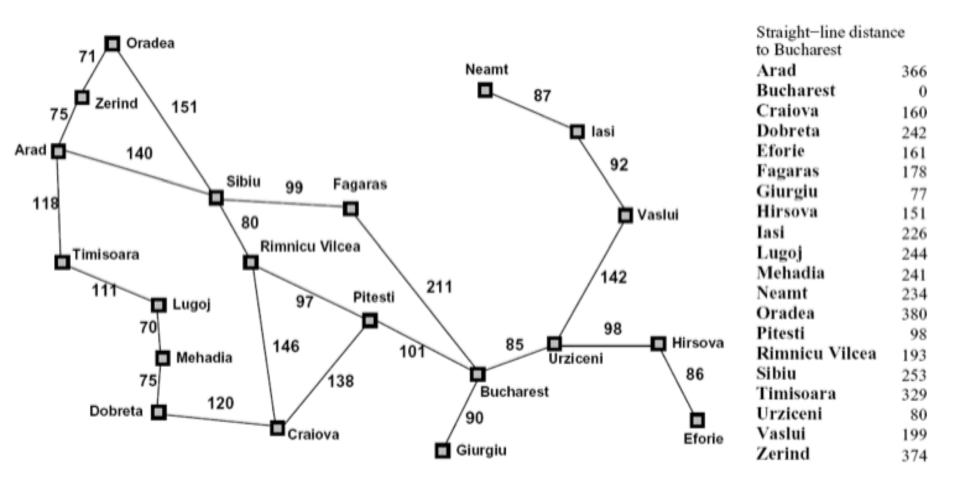
Search Heuristics

- Any estimate of how close a state is to a goal
- Designed for a particular search problem



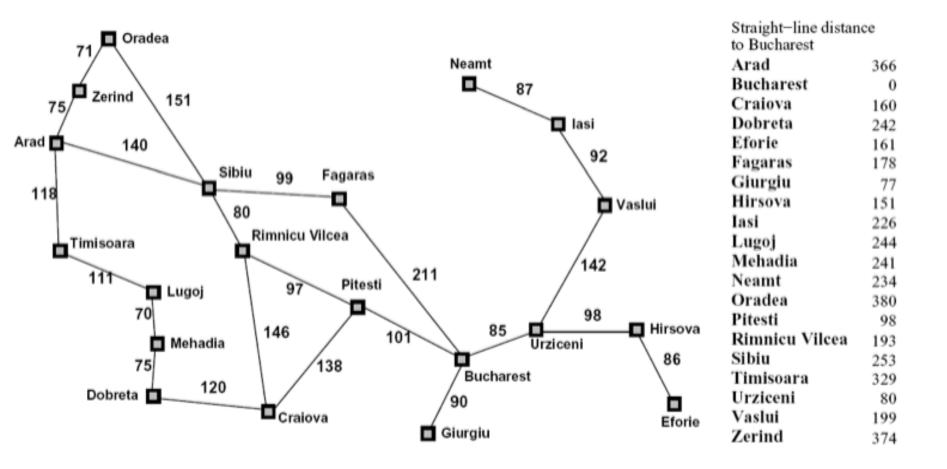
Examples: Manhattan distance, Euclidean distance

Heuristics



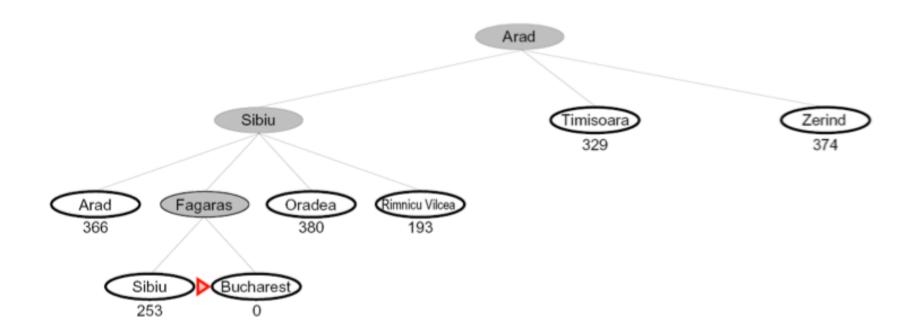
Best First / Greedy Search

Best first with f(n) = heuristic estimate of distance to goal



Best First / Greedy Search

Expand the node that seems closest...



What can go wrong?

Best First / Greedy Search

- A common case:
 - Best-first takes you straight to the (wrong) goal
- Worst-case: like a badlyguided DFS in the worst case
 - Can explore everything
 - Can get stuck in loops if no cycle checking
- Like DFS in completeness (finite states w/ cycle checking)

