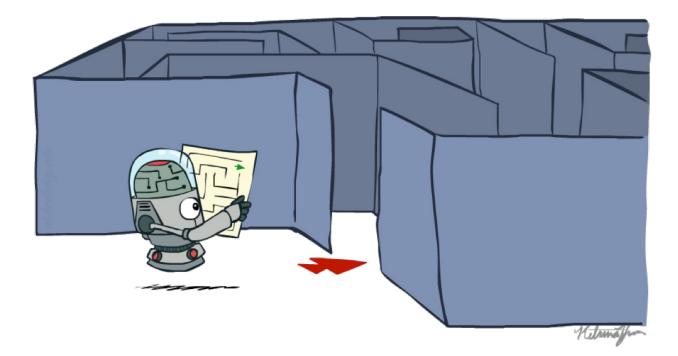
CSEP 573: Artificial Intelligence

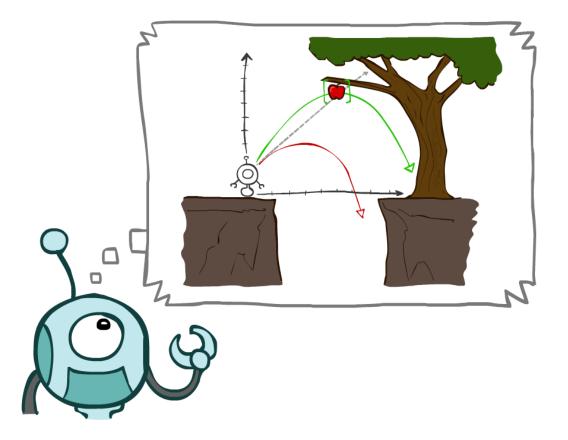
Search



slides adapted from Stuart Russel, Dan Klein, Pieter Abbeel from ai.berkeley.edu And Hanna Hajishirzi, Jared Moore, Dan Weld

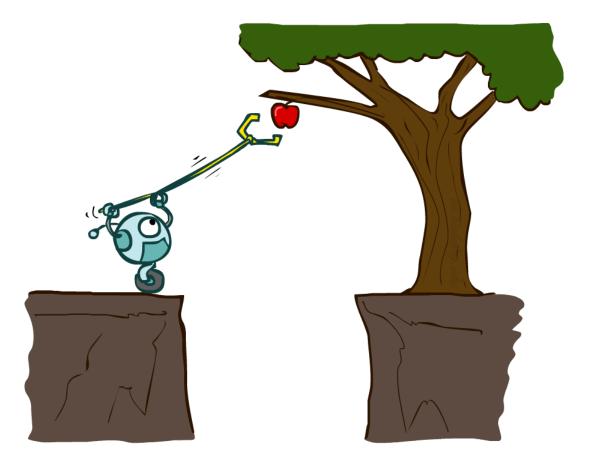
Today

- Agents that Plan Ahead
 - goal-based
- Search Problems
- Uninformed Search Methods
 - Depth-First Search
 - Breadth-First Search
 - Uniform-Cost Search

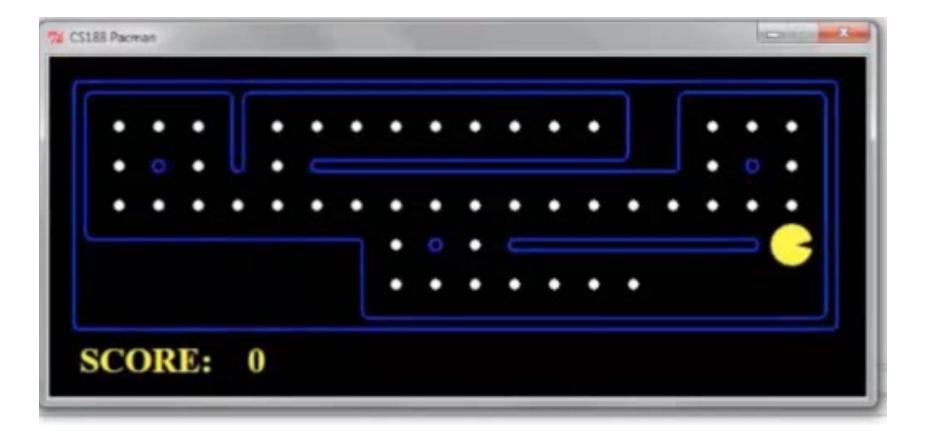


Planning Agents

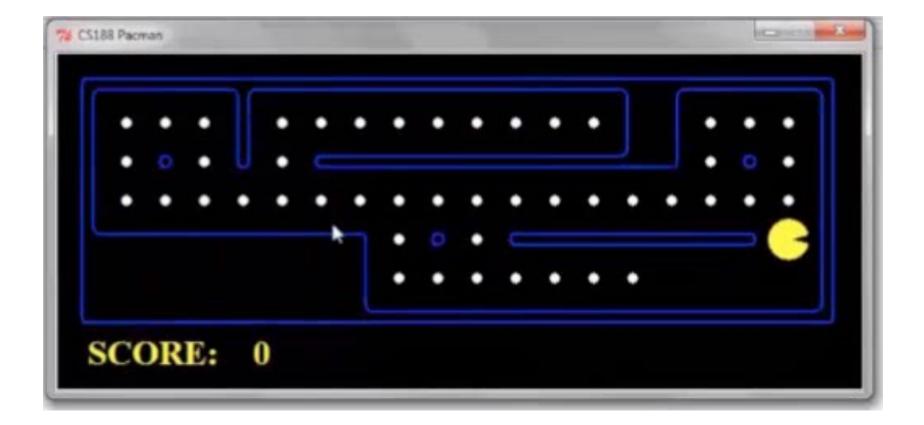
- Planning agents decide based on evaluating future action sequences
- Must have a model of how the world evolves in response to actions
- Usually have a definite goal
- Optimal: Achieve goal at least cost



Optimal?



Precompute optimal plan, execute it



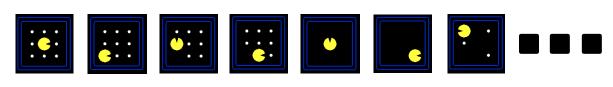
Search Problems

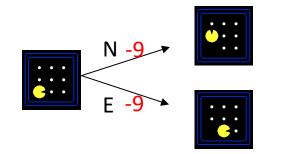


Search Problems

A search problem consists of:

- A state space S
- An initial state s₀
- Actions A(s) in each state
- Transition model Result(s,a)
- A goal test G(s)
 - S has no dots left
- Action cost c(s,a,s')
 - +1 per step; -10 food; -500 win; +500 die; -200 eat ghost
- A solution is an action sequence that reaches a goal state
- An optimal solution has least cost among all solutions





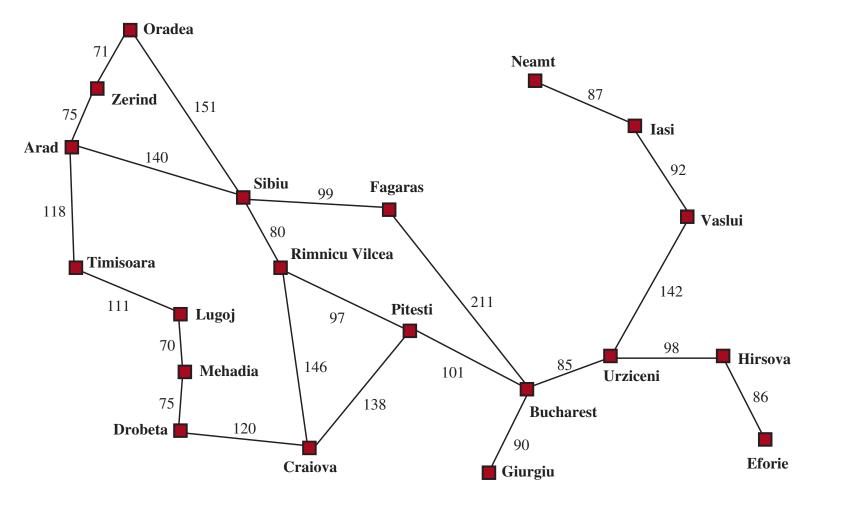
Search Problems Are Models



Example: Traveling in Romania

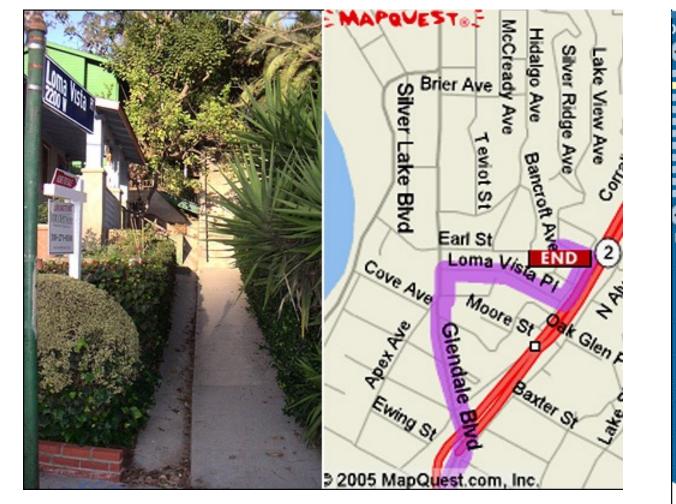


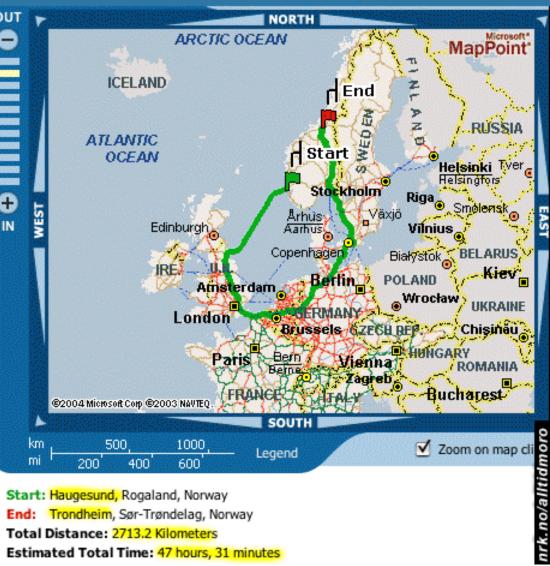
Example: Traveling in Romania



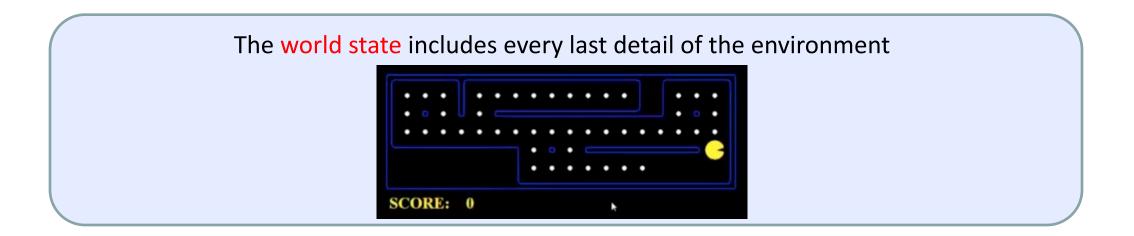
- State space:
 - Cities
- Initial state:
 - Arad
- Actions:
 - Go to adjacent city
- Transition model:
 - Reach adjacent city
- Goal test:
 - s = Bucharest?
- Action cost:
 - Road distance from s to s'
- Solution?

Models are almost always wrong





What's in a State Space?



A search state keeps only the details needed for planning (abstraction)

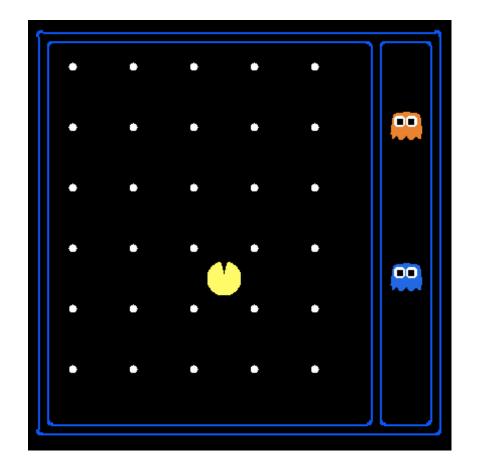
- Problem: Pathing (= path finding)
 - States: (x,y); location
 - Actions: NSEW
 - Transition: update x,y value
 - Goal test: is (x,y)=destination

- Problem: Eat-All-Dots
 - States: pacman location, boolean for each food
 - Actions: NSEW
 - Transition: update x,y and possibly a dot Boolean
 - Goal test: dots all false

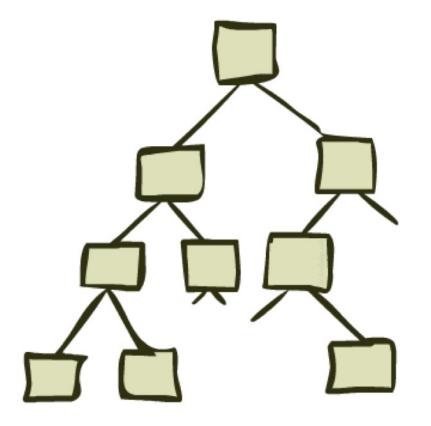
State Space Sizes

World state:

- Agent positions: 120
- Food count: 30
- Ghost positions: 12
- Agent facing: NSEW
- How many
 - World states?
 120x(2³⁰)x(12²)x4
 - States for pathing (path finding)?
 120
 - States for eat-all-dots?
 120x(2³⁰)

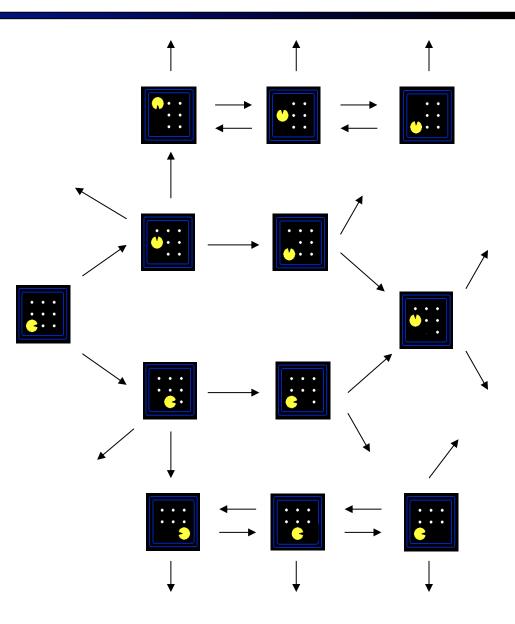


State Space Graphs and Search Trees



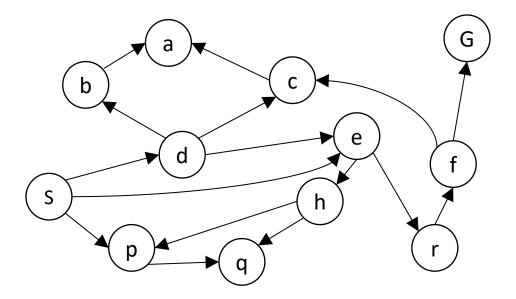
State Space Graphs

- State space graph: A mathematical representation of a search problem
 - Nodes are (abstracted) world configurations
 - Arcs represent successors (action results)
 - The goal test is a set of goal nodes (maybe only one)
- In a state space graph, each state occurs only once!
- We can rarely build this full graph in memory (it's too big), but it's a useful idea

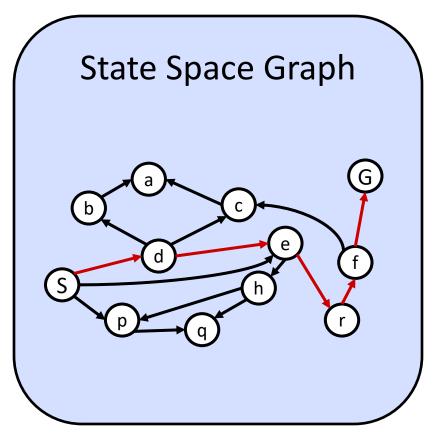


State Space Graphs

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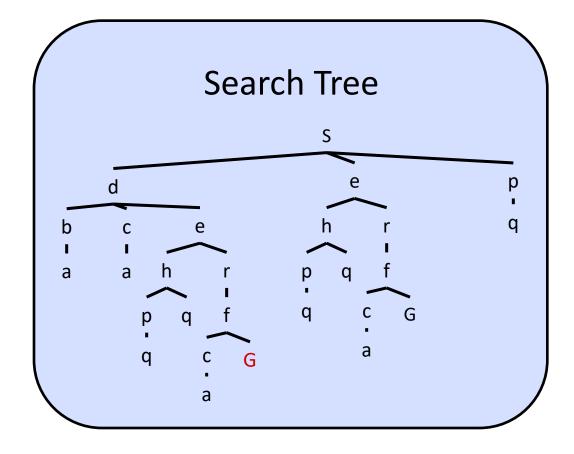


Tiny state space graph for a tiny search problem



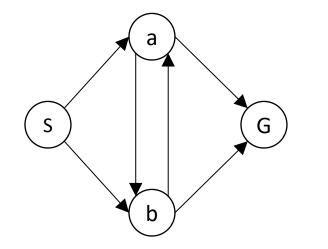
Each NODE in in the search tree is an entire PATH in the state space graph.

We construct the tree on demand – and we construct as little as possible.



Consider this 4-state graph:

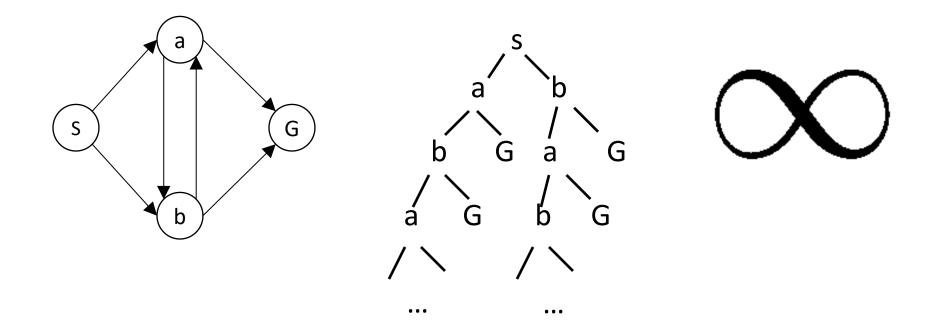
How big is its search tree (from S)?



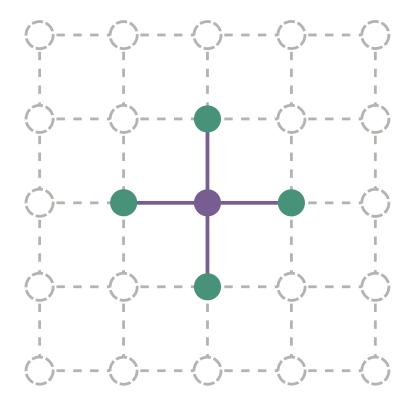


Consider this 4-state graph:

How big is its search tree (from S)?



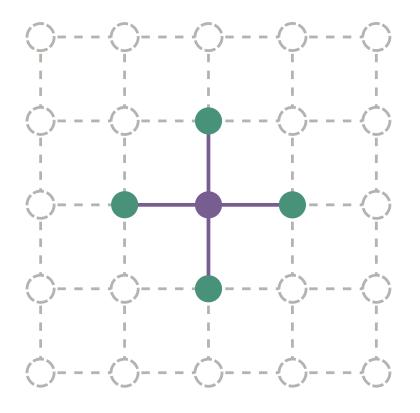
Consider a rectangular grid:



How many unique states within d steps of start?

How many states in search tree of depth d?

Consider a rectangular grid:



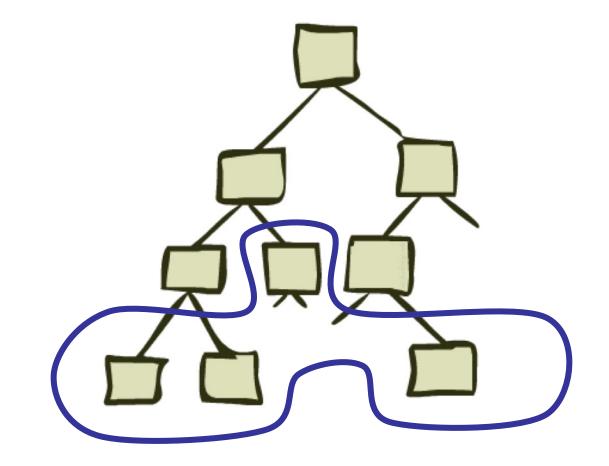
How many unique states within d steps of start?

Enumerate after step 1: {4, 4 + 8, 4 + 8 + 12, ...}

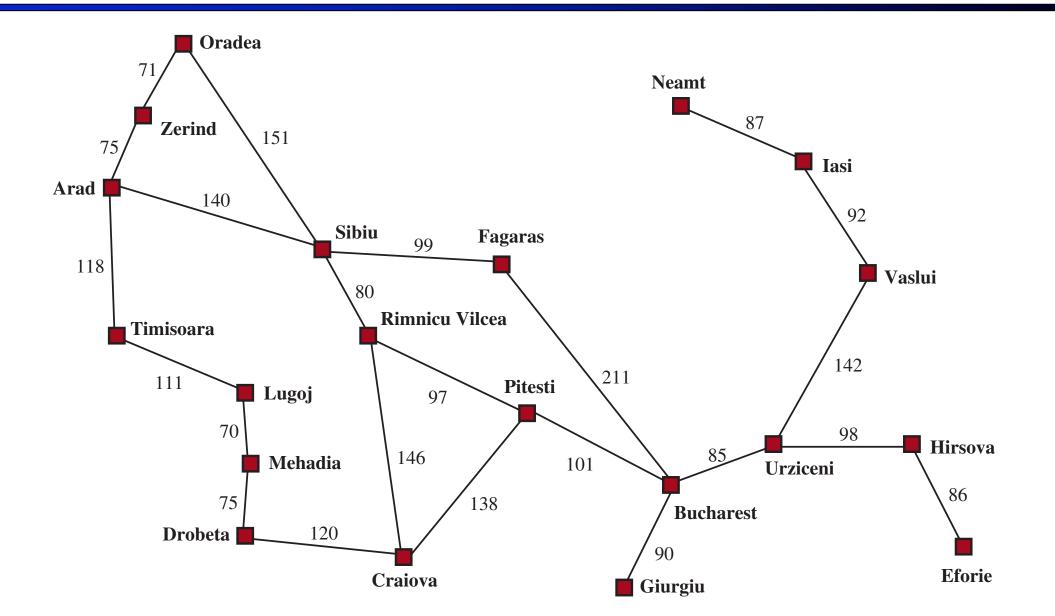
How many states in search tree of depth d?

 $= O(4^d)$

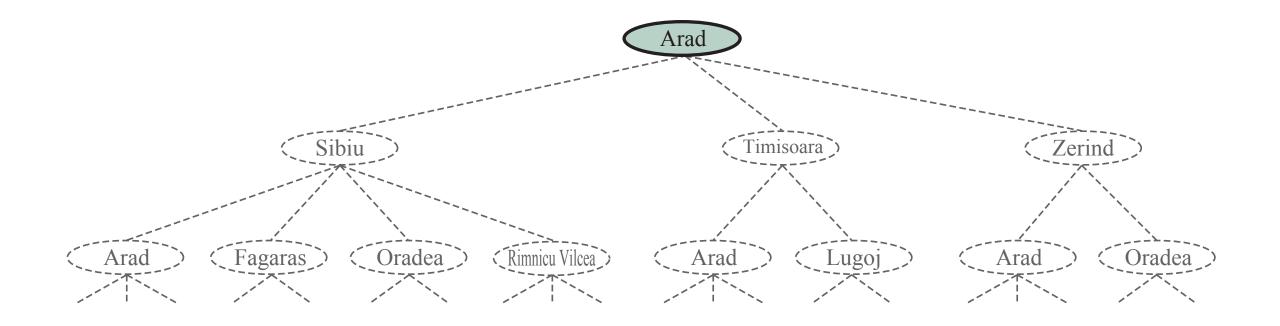
Tree Search



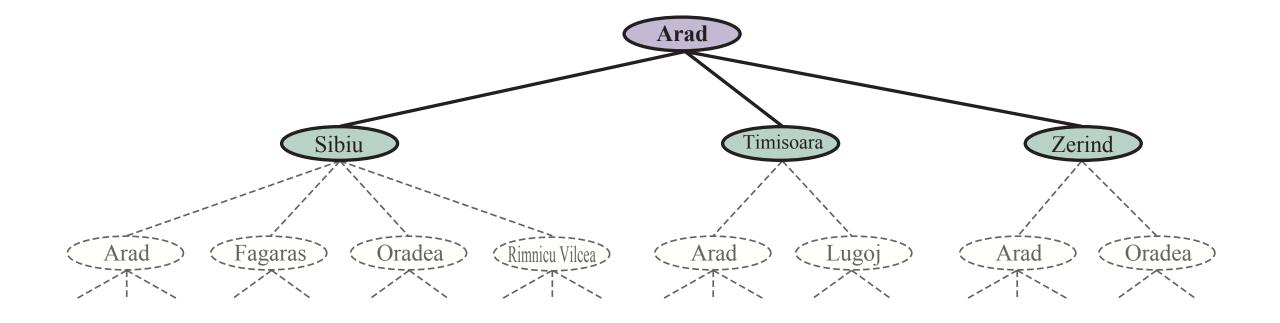
Search Example: Romania



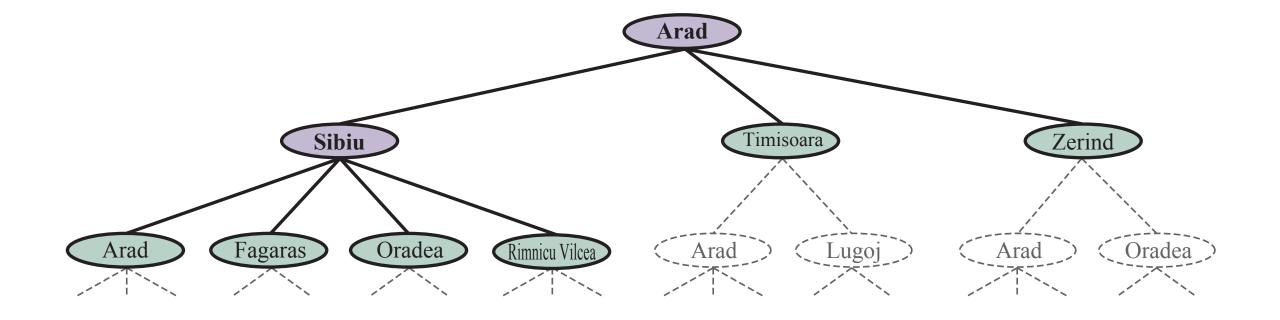
Creating the search tree



Creating the search tree



Creating the search tree



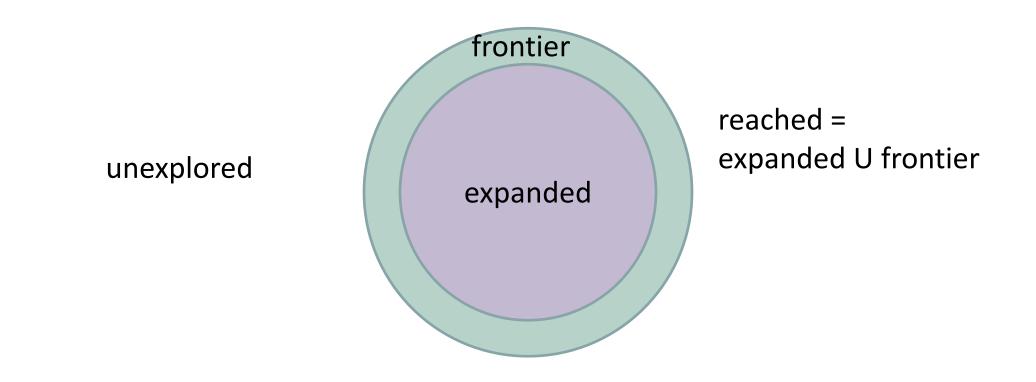
General Tree Search

function TREE-SEARCH(problem, strategy) returns a solution, or failure initialize the search tree using the initial state of problem loop do

if there are no candidates for expansion then return failure choose a leaf node for expansion according to *strategy* if the node contains a goal state then return the corresponding solution else expand the node and add the resulting nodes to the search tree end

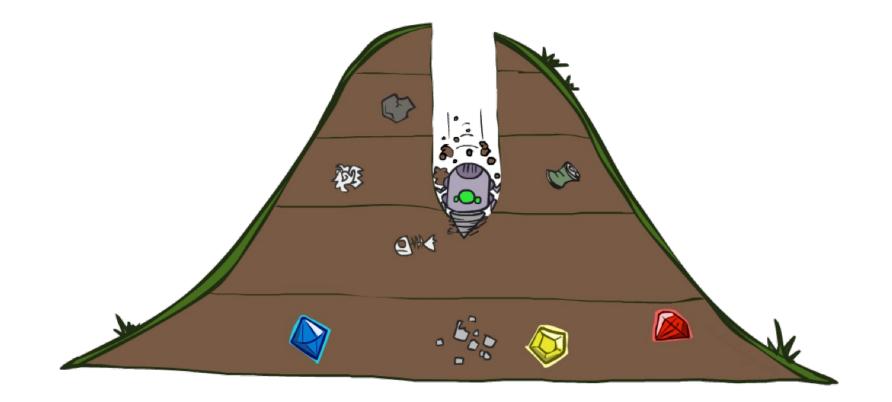
- Main variations:
 - Which leaf node to expand next
 - Whether to check for repeated states
 - Data structures for frontier, expanded nodes

Systematic search



- 1. Frontier separates expanded from unexplored region of state-space graph
- 2. Expanding a frontier node:
 - a. Moves a node from frontier into expanded
 - b. Adds nodes from unexplored into frontier, maintaining property 1

Depth-First Search

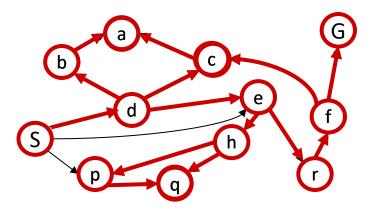


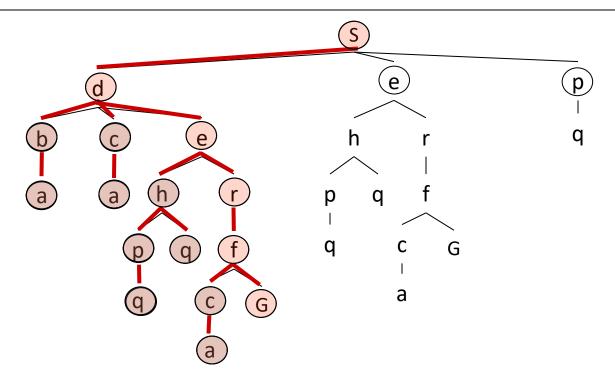
Depth-First Search

Strategy: expand a deepest node first

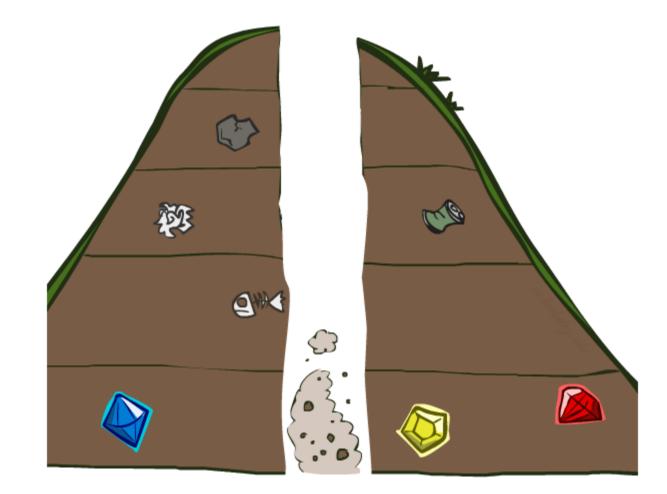
Implementation: Frontier is a LIFO stack

(last in first out)





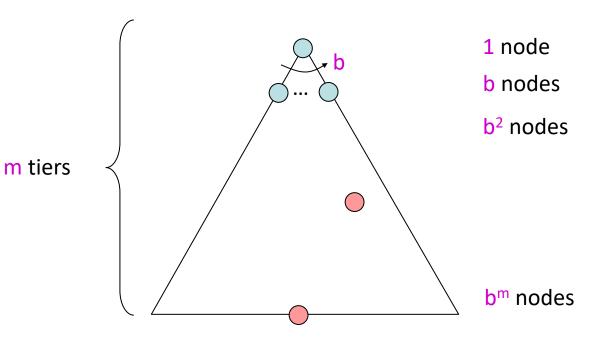
Search Algorithm Properties



Search Algorithm Properties

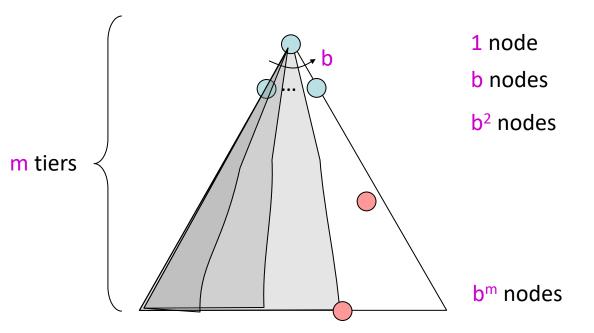
- **Complete:** Guaranteed to find a solution if one exists?
- **Optimal:** Guaranteed to find the least cost path?
- Time complexity?
- Space complexity?
- Cartoon of search tree:
 - **b** is the branching factor
 - m is the maximum depth
 - solutions at various depths
- Number of nodes in entire tree?
 - $1 + b + b^2 + \dots b^m = O(b^m)$



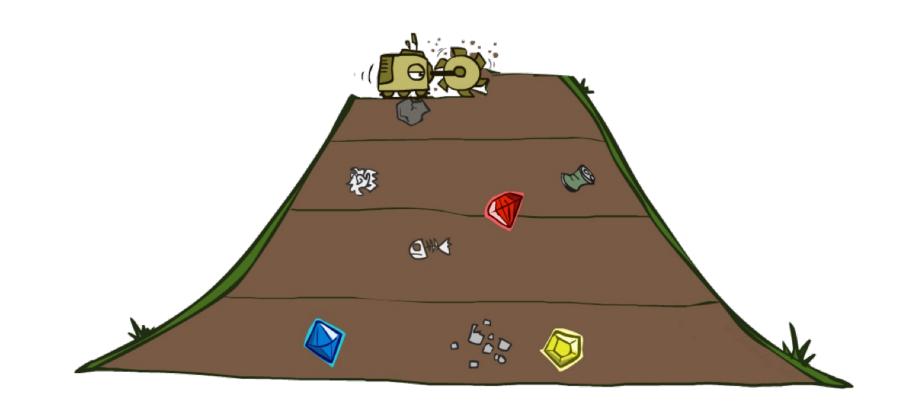


Depth-First Search (DFS) Properties

- What nodes does DFS expand?
 - Some left prefix of the tree down to depth *m*.
 - Could process the whole tree!
 - If m is finite, takes time O(b^m)
- How much space does the frontier take?
 - Only has siblings on path to root, so O(bm)
- Is it complete?
 - *m* could be infinite
 - preventing cycles may help (more later)
- Is it optimal?
 - No, it finds the "leftmost" solution, regardless of depth or cost



Breadth-First Search

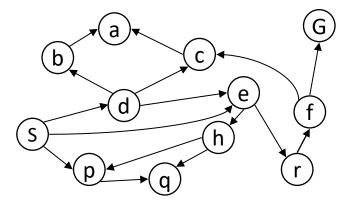


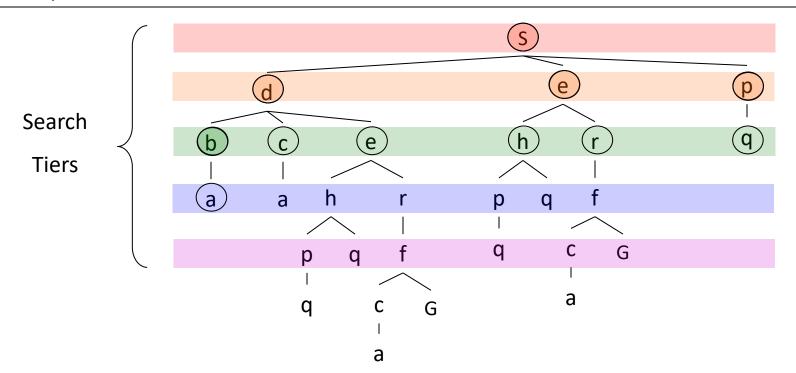
Breadth-First Search

Strategy: expand a shallowest node first

Implementation: Frontier is a FIFO queue

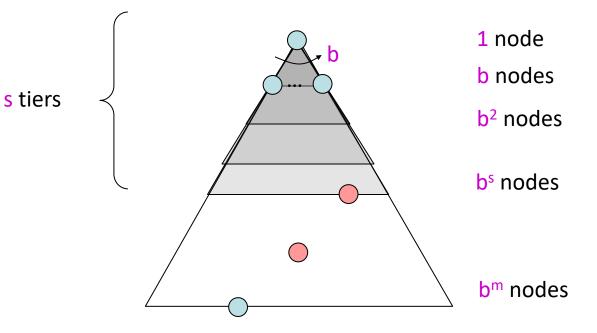
(first in first out)



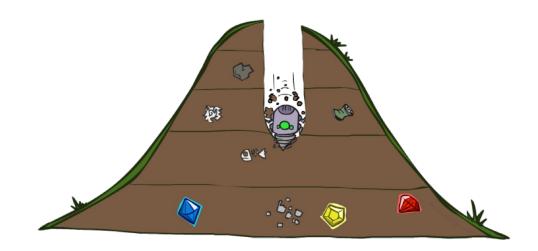


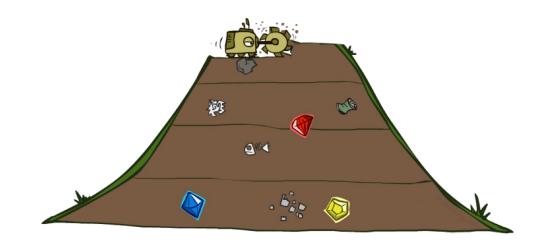
Breadth-First Search (BFS) Properties

- What nodes does BFS expand?
 - Processes all nodes above shallowest solution
 - Let depth of shallowest solution be s
 - Search takes time O(b^s)
- How much space does the frontier take?
 - Has roughly the last tier, so O(b^s)
- Is it complete?
 - s must be finite if a solution exists, so yes!
- Is it optimal?
 - If costs are equal (e.g., 1)



Quiz: DFS vs BFS





Quiz: DFS vs BFS

(In terms of S, the depth of the shallowest solution and M, the maximum depth)

When will BFS outperform DFS?

When will DFS outperform BFS?

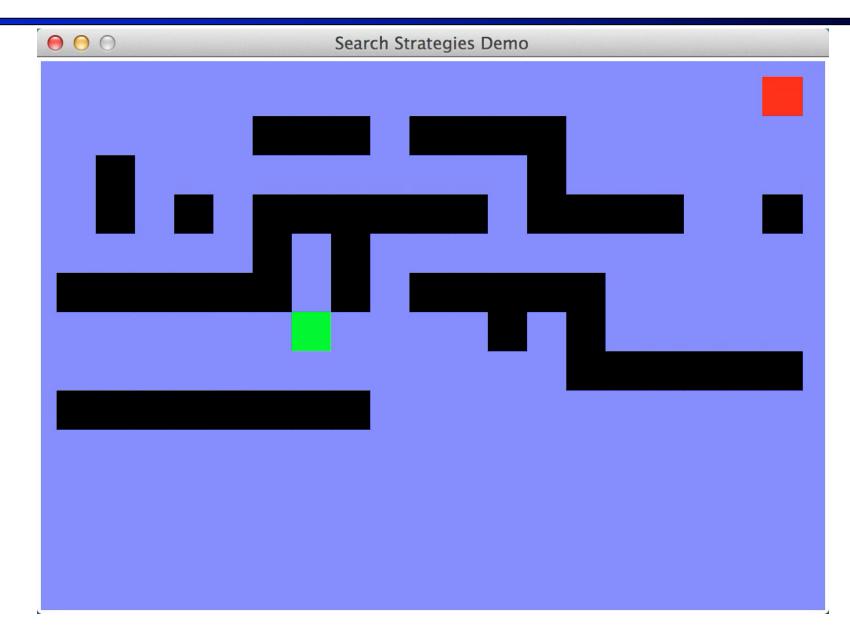
Quiz: DFS vs BFS

(In terms of S, the depth of the shallowest solution and M, the maximum depth)

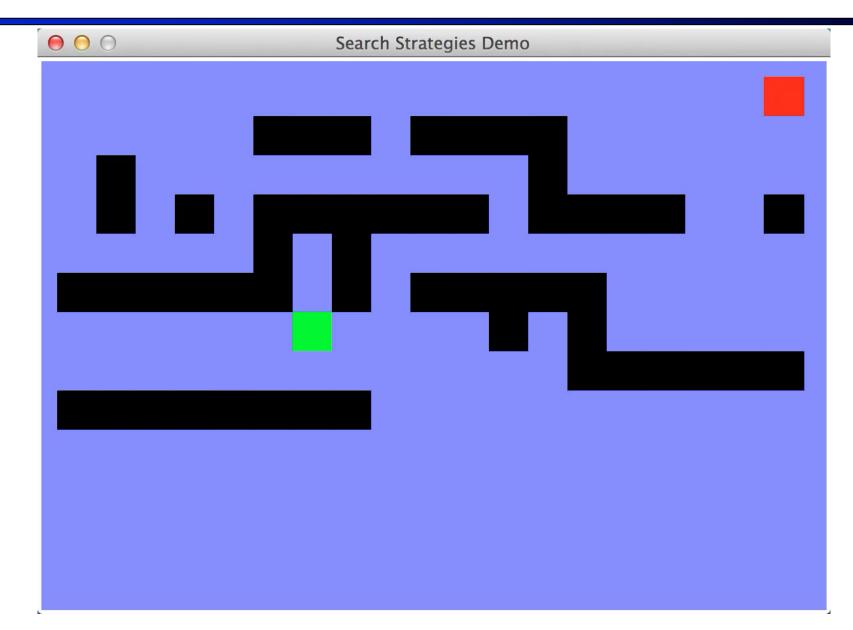
- When will BFS outperform DFS?
 - S << M

- When will DFS outperform BFS?
 - S ~= M

Example: Maze Water DFS/BFS (part 1)

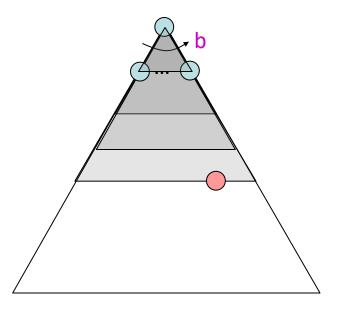


Example: Maze Water DFS/BFS (part 2)

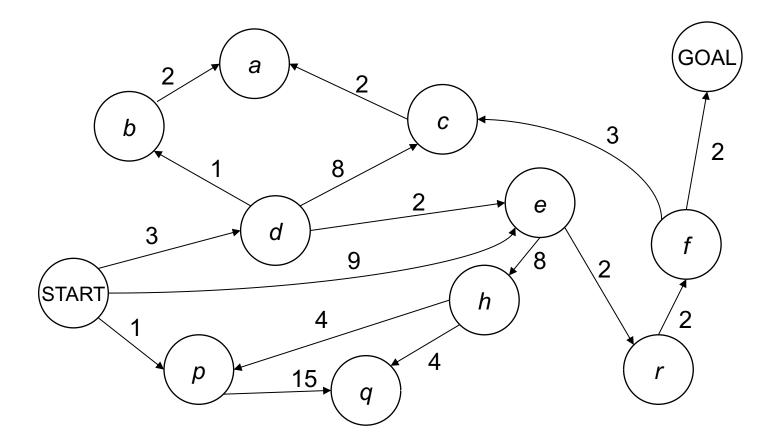


Iterative Deepening

- Idea: get DFS's space advantage with BFS's time / shallow-solution advantages
 - Run a DFS with **depth limit** 1. If no solution...
 - Run a DFS with depth limit 2. If no solution...
 - Run a DFS with depth limit 3.
- Isn't that wastefully redundant?
 - Generally most work happens in the lowest level searched, so not so bad!
 - Also useful for the meta data

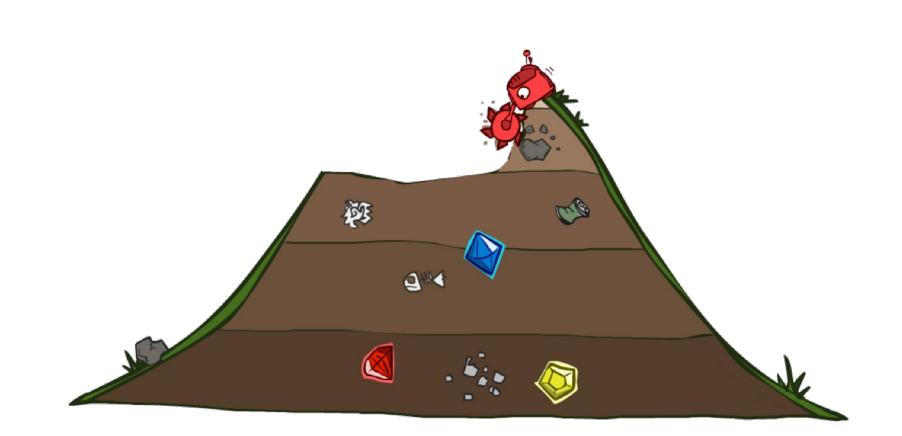


Cost-Sensitive Search



BFS finds the shortest path in terms of number of actions. It does not find the least-cost path. We will now cover a similar algorithm which does find the least-cost path.

Uniform Cost Search

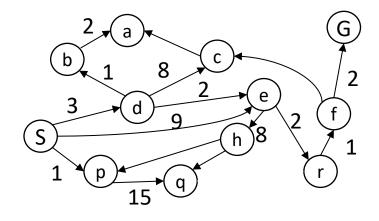


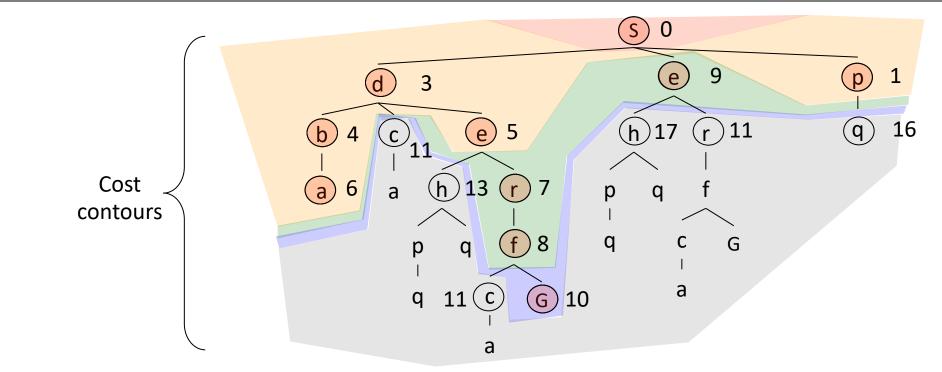
Uniform Cost Search

g(n) = cost from root to n

Strategy: expand lowest g(n)

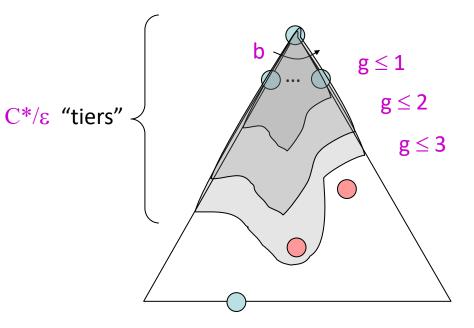
Frontier is a priority queue sorted by g(n)



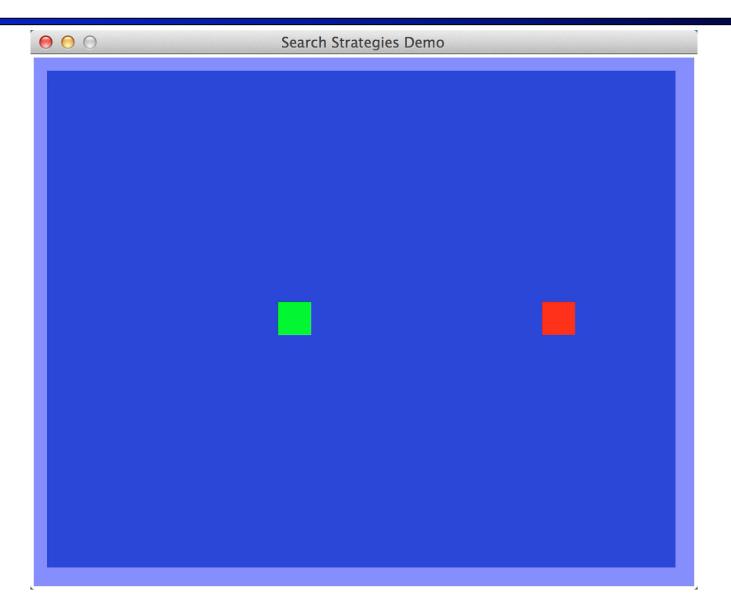


Uniform Cost Search (UCS) Properties

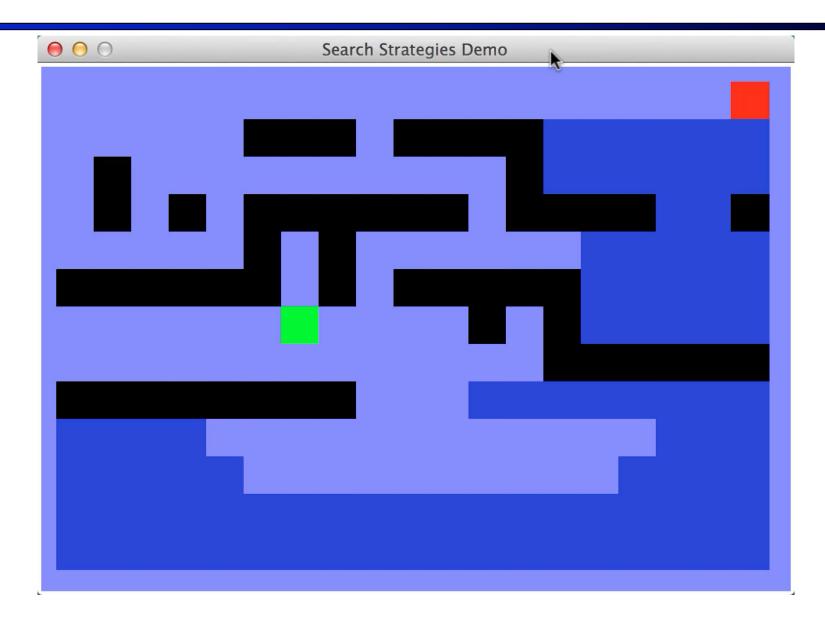
- What nodes does UCS expand?
 - Processes all nodes with cost less than cheapest solution!
 - If solution costs C* and arcs cost at least *ε*, then C*/*ε* is effective depth (upper bound on depth of solution)
 - Takes time O(b^{C*/ɛ}) (exponential in effective depth)
- How much space does the frontier take?
 - Has roughly the last tier, so O(b^{C*/ε})
- Is it complete?
 - Assuming C* is finite and E > 0, yes!
- Is it optimal?
 - Yes! (Proof next lecture via A*)



Video of Demo Empty UCS



Video of Demo Maze with Deep/Shallow Water --- BFS or UCS? (part 1)



Video of Demo Maze with Deep/Shallow Water --- BFS or UCS? (part 2)

