# Multiview Alignment and Sparse SFM <br> CSE P576 

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## Multiview + Sparse SFM

- Multiview Image Alignment, Residuals, Error Function
- Structure from Motion (SFM)
- Bundle Adjustment, Pose Estimation,Triangulation


## Multiview Image Alignment

- Align a set of images given a motion model (e.g., planar affine)

[ Szeliski 9.2 ]


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Step I: Find all matches between images using SIFT

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## RANSAC recap

- RANSAC solution for Similarity Transform (2 points)



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4 inliers (red, yellow, orange, brown),
4 outliers (blue, light blue, purple, pink)

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cbberlentingraibligetancese $\#$ inliers $=2$


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cheblowaspolmaligelaneces
\#inliers = 2


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clatrdobrapcimadigeargies
\#inliers $=4$


## RANSAC recap

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## Planar Image Alignment

- Given a clean set of correspondences, align all images




## Planar Mapping Residuals

- Residual $=$ vector between observed feature and projection



## Multiview Image Alignment

- Minimize squared projection errors between images with respect to planar transform parameters (H matrices)
$4(4.5$


## Panorama Recognition



## Panorama Recognition



## Panorama Recognition



## Panorama Recognition




## Panorama Stitching

- We can concatenate pairwise homographies, but over time multiple pairwise mappings accumulate errors
- We use global alignment (bundle adjustment) to close the gap


## Structure from Motion



Given an (unordered) set of input images, compute cameras and 3D structure of the scene

## Structure from Motion



## 2-view Structure from Motion

- We can use the combination of SIFT/RANSAC and triangulation to compute 3D structure from 2 views


Raw SIFT matches


RANSAC for $F$


Extract R, t
Triangulate to 3D Point Cloud

## Global Alignment

- Concatenation of pairwise R, $t$ estimates results in drift, e.g.,


Pairwise alignment


Global alignment

## Global Alignment

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Pairwise alignment


Global alignment

## Global Alignment

- In robotic navigation frame-frame alignment also causes drift


We can use bundle adjustment to close the gap
[ Kaess Dellaert 2010]

## RANSAC for $F$



Raw feature matches (after ratio test filtering)


Solved for $F$ and RANSAC inliers

## Feature Tracking

- Form feature tracks by combining pairwise feature matches

- Tracked features become individual 3D points in the reconstruction
- Features matched across 3 or more views provide strong constraints on the 3D reconstruction


## Bundle Adjustment

- Minimise errors projecting 3D points into all images

[ Szeliski 7.4 ]
$\mathbf{K}_{i}, \mathbf{R}_{i}, \mathbf{t}_{i}$


## Bundle Adjustment

- Initialization with 3 views


Joint optimization of cameras and structure

## Bundle Adjustment

- Add camera 4


Estimate camera pose, add new 3D points, jointly optimize

## Bundle Adjustment

- Add camera 5


Estimate camera pose, add new 3D points, jointly optimize

## Bundle Adjustment

- Add camera 6


Estimate camera pose, add new 3D points, jointly optimize

## Bundle Adjustment

- Add remaining cameras in same way



## Structure from Motion



## Why "Bundle" Adjustment?

- Can think of bundles of light rays emanating from each 3D point


Adjust camera + 3D point positions so that bundles match measured positions (feature points)

## SFM recap

- Match features, e.g., SIFT, between all views
- Use RANSAC to reject outliers and estimate F matrices
- Form feature tracks by linking multiview matches
- Select an initialization set, e.g., 3 images with lots of matches and good baseline (parallax)
- Jointly optimize cameras $\mathrm{R}, \mathrm{t}$ and structure X for this set
- Repeat for each camera:
- Estimate pose R, t by minimising projection errors with existing $X$
- Add 3D points corresponding to the new view and optimize
- Bundle adjust optimizing over all cameras and structure


## Visual SFM



## Application: 3D from Internet Images

- Reconstruct 3D from unordered photo collections

[ Building Rome in a Day, S.Agarwal et al 2009 ]



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## Next Lecture

## - Dense matching and reconstruction

