

# Multiview Alignment and Sparse SFM

CSE P576

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These slides were developed by Dr. Matthew Brown for CSEP576 Spring 2020 and adapted (slightly) for Fall 2021  
credit → Matt  
blame → Vitaly

# Multiview + Sparse SFM

- Multiview Image Alignment, Residuals, Error Function
- Structure from Motion (SFM)
- Bundle Adjustment, Pose Estimation, Triangulation

[ Szeliski 7, 9 ]

# Multiview Image Alignment

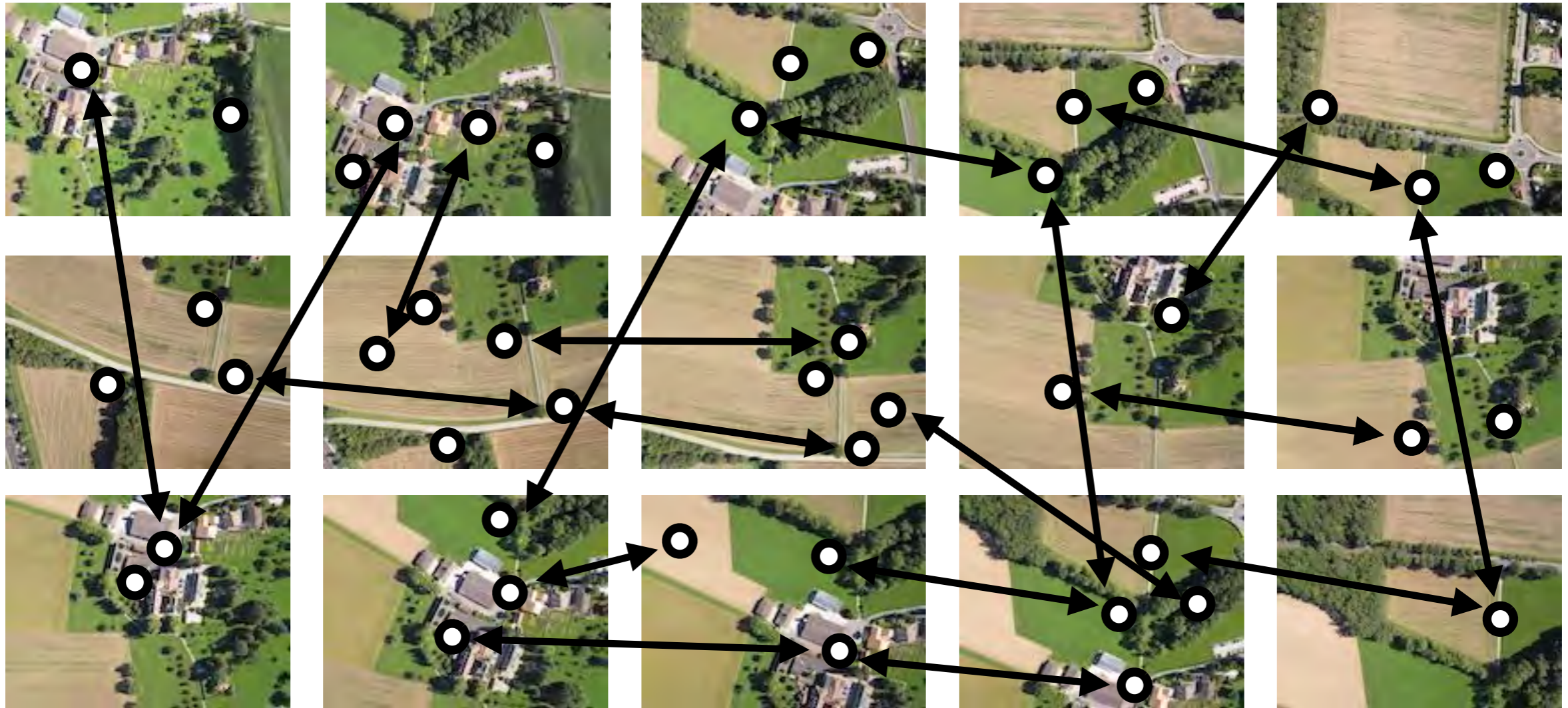
- Align a set of images given a motion model (e.g., planar affine)



[ Szeliski 9.2 ]

# Multiview Image Alignment

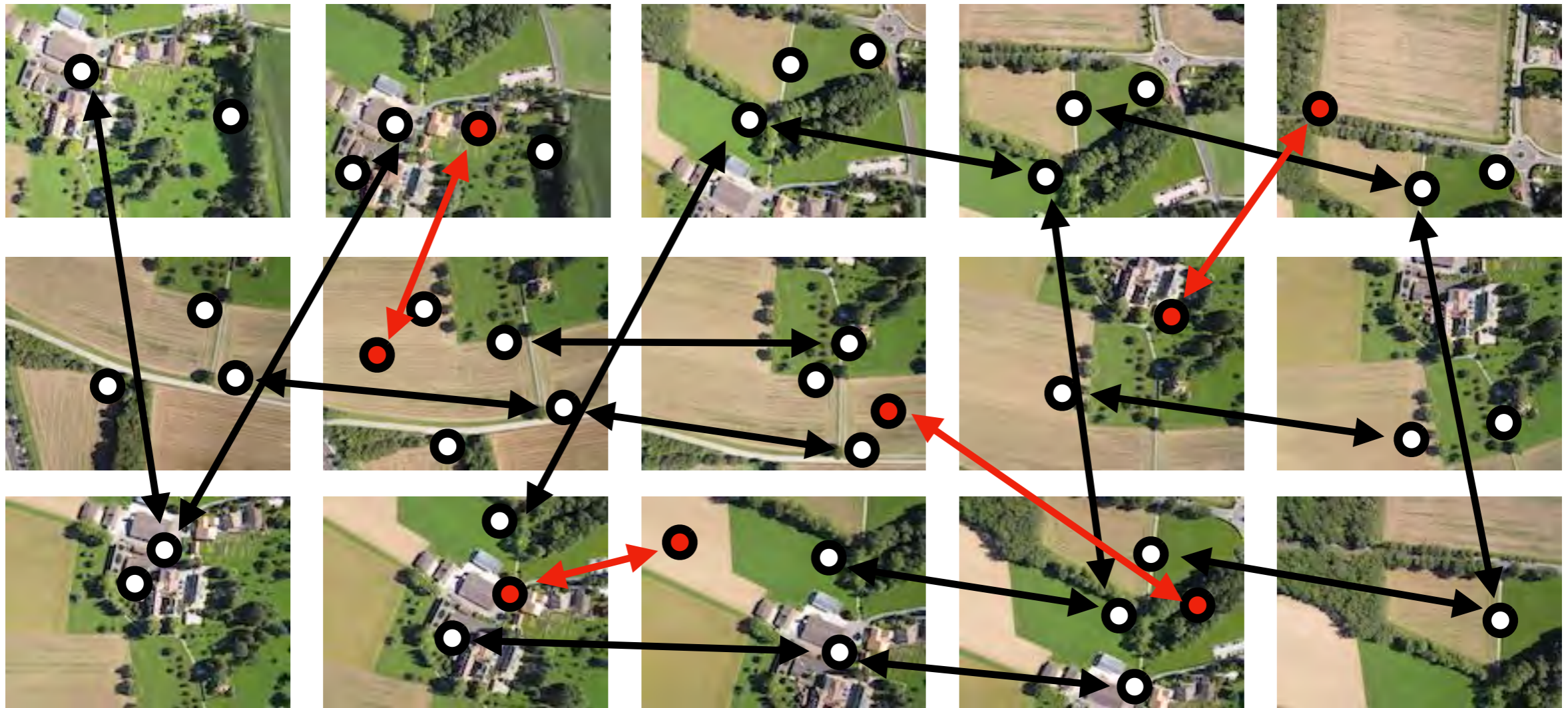
- Align a set of images given a motion model (e.g., planar affine)



Step 1: Find all matches between images using SIFT

# Multiview Image Alignment

- Align a set of images given a motion model (e.g., planar affine)



Step 1: Find all matches between images using SIFT

Step 2: Remove incorrect matches using RANSAC

# Multiview Image Alignment

- Align a set of images given a motion model (e.g., planar affine)

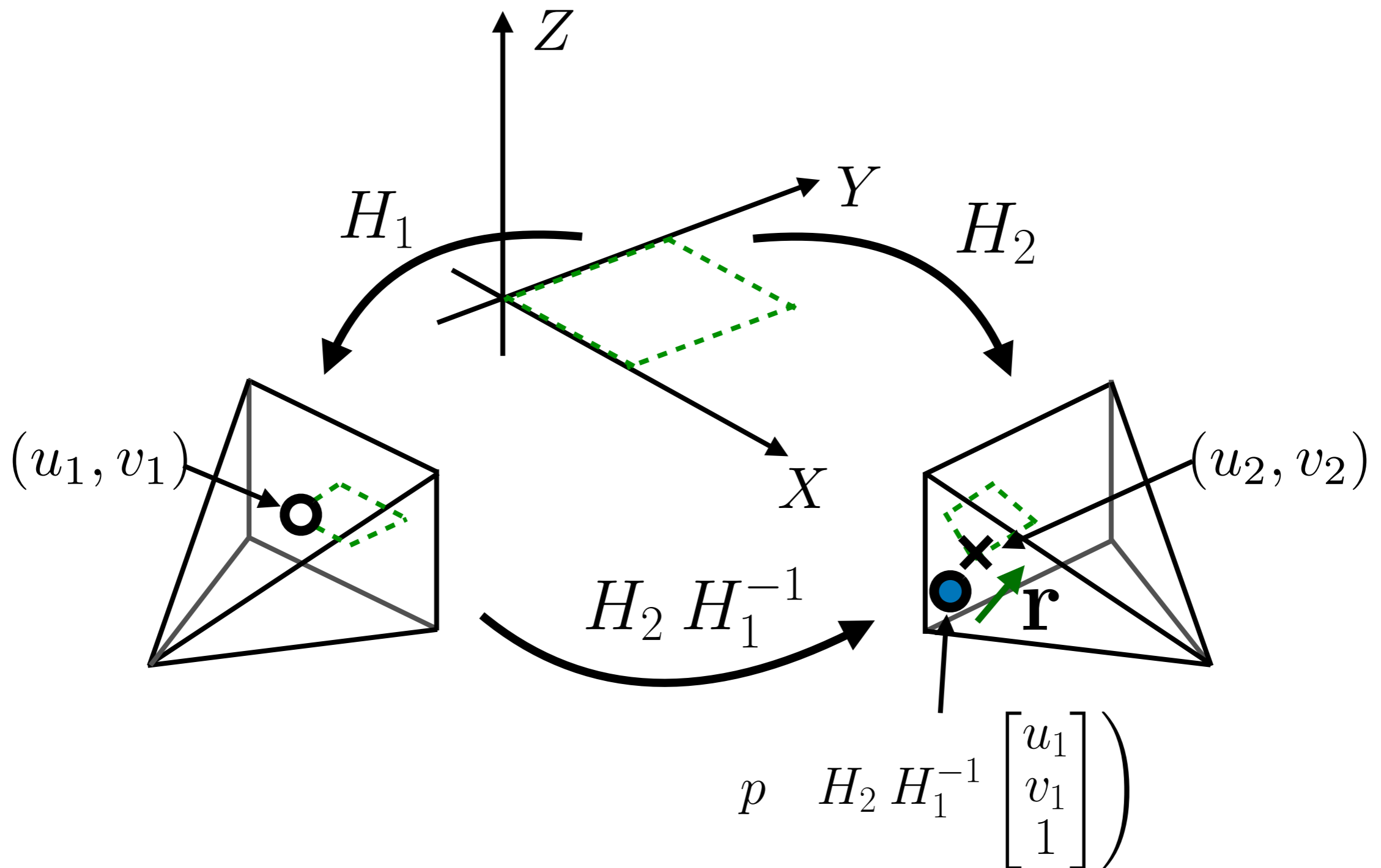


Step 1: Find all matches between images using SIFT

Step 2: Remove incorrect matches using RANSAC

# Planar Mapping Residuals

- Residual = vector between observed feature and projection

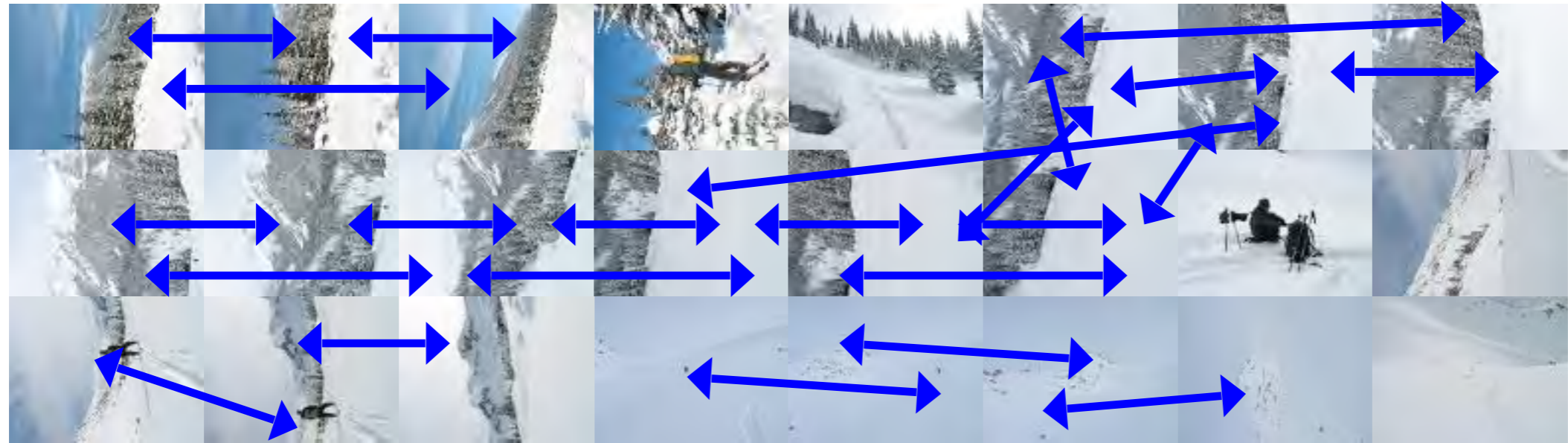


# Multiview Image Alignment

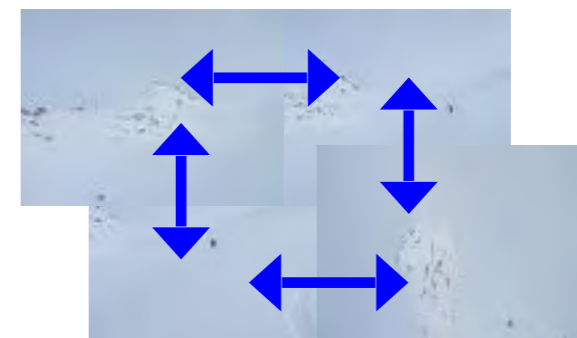
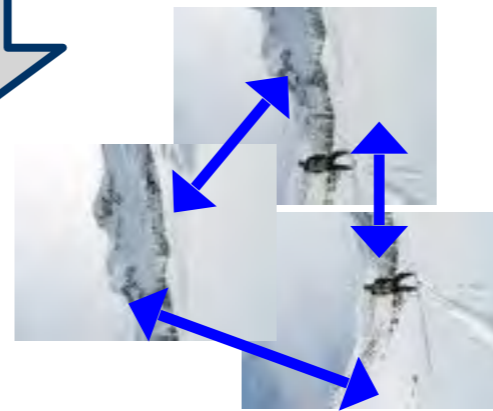
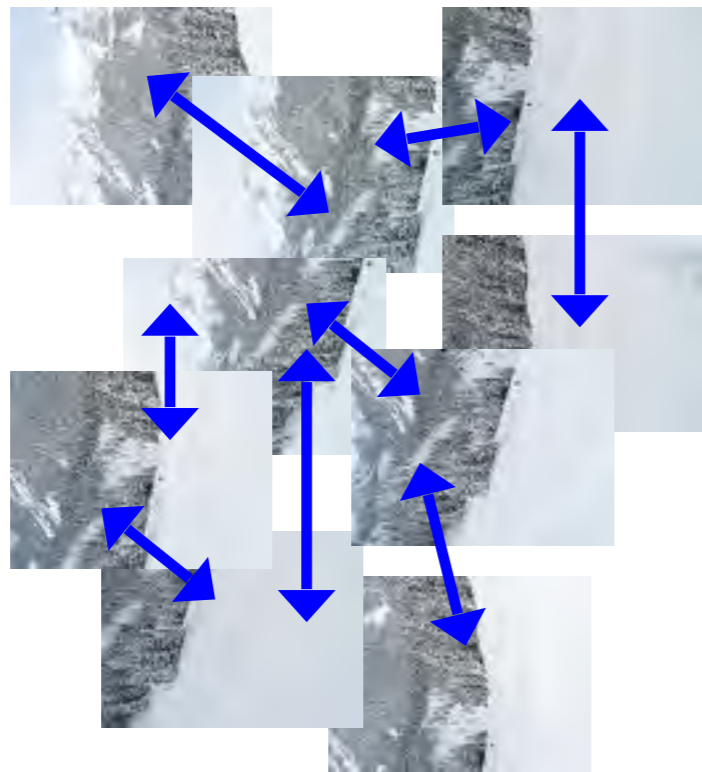
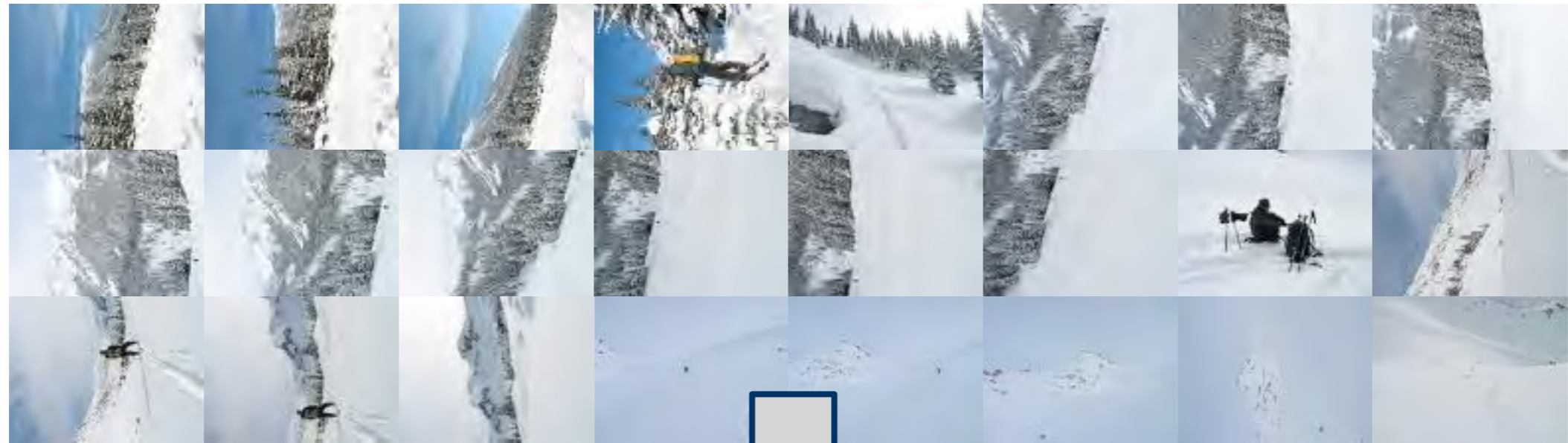
- Minimize squared projection errors between images with respect to planar transform parameters (H matrices)



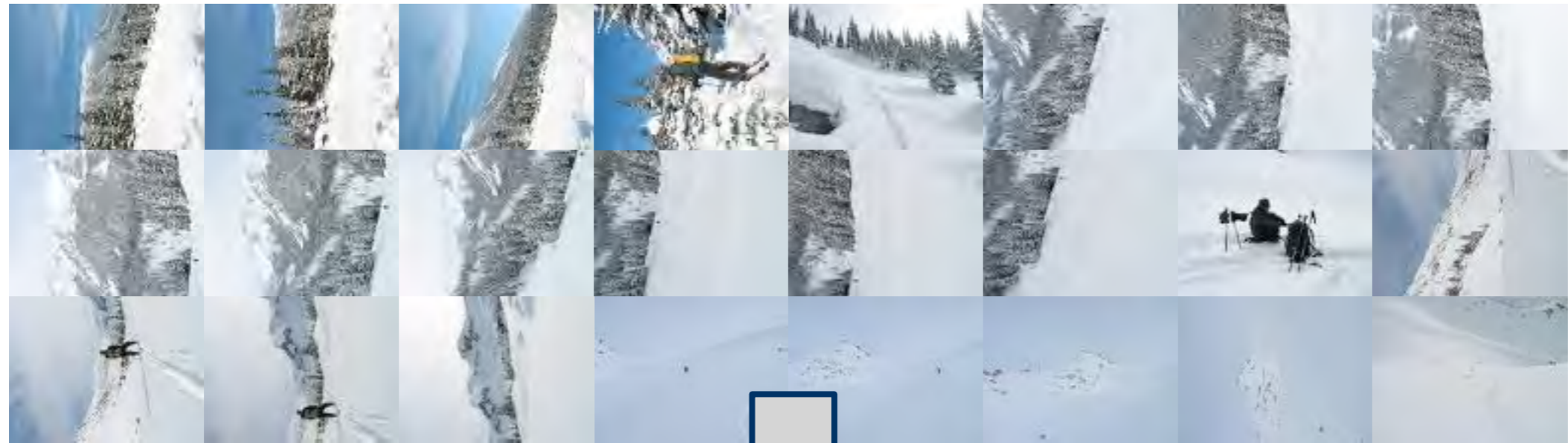
# Panorama Recognition



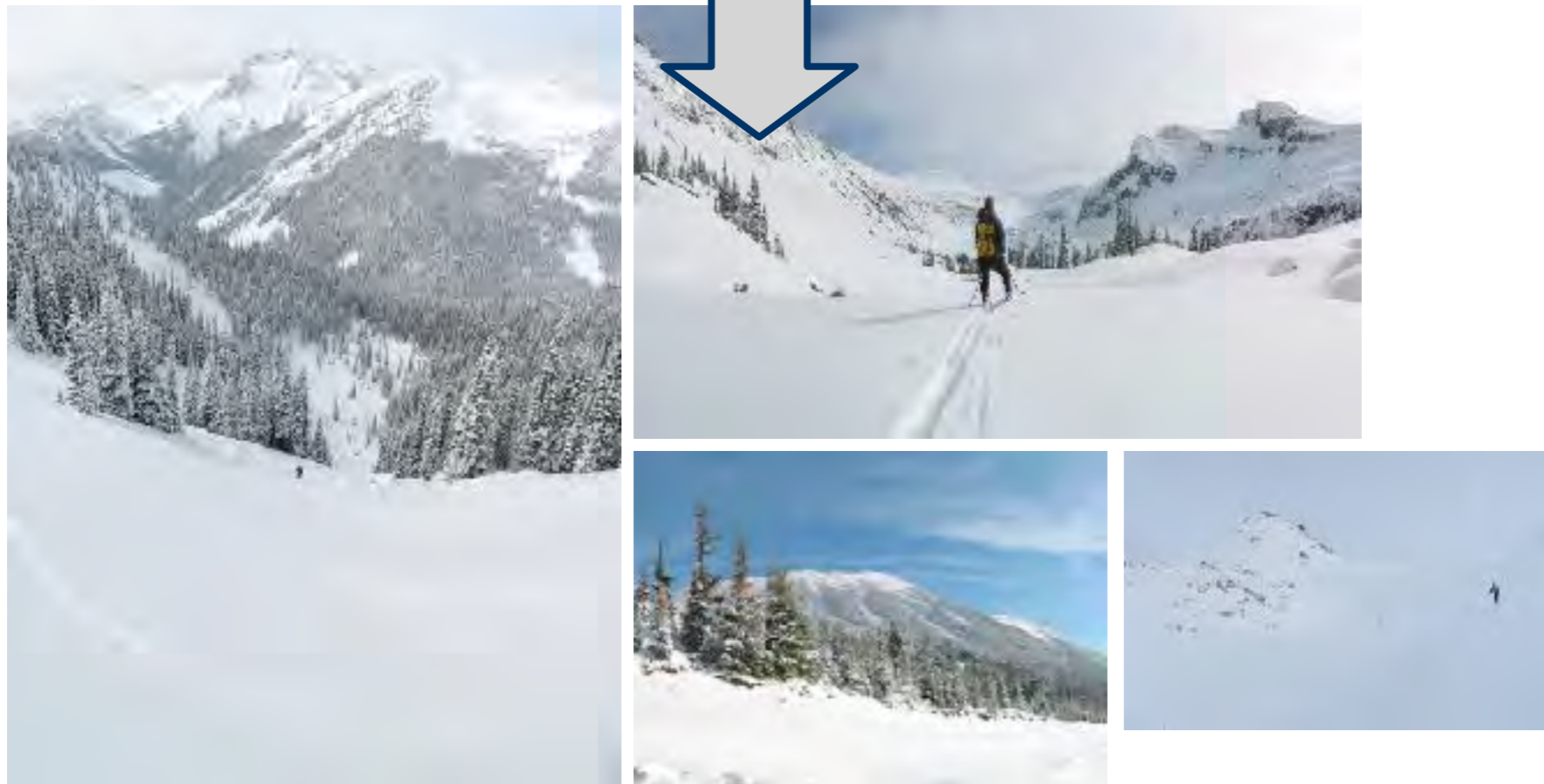
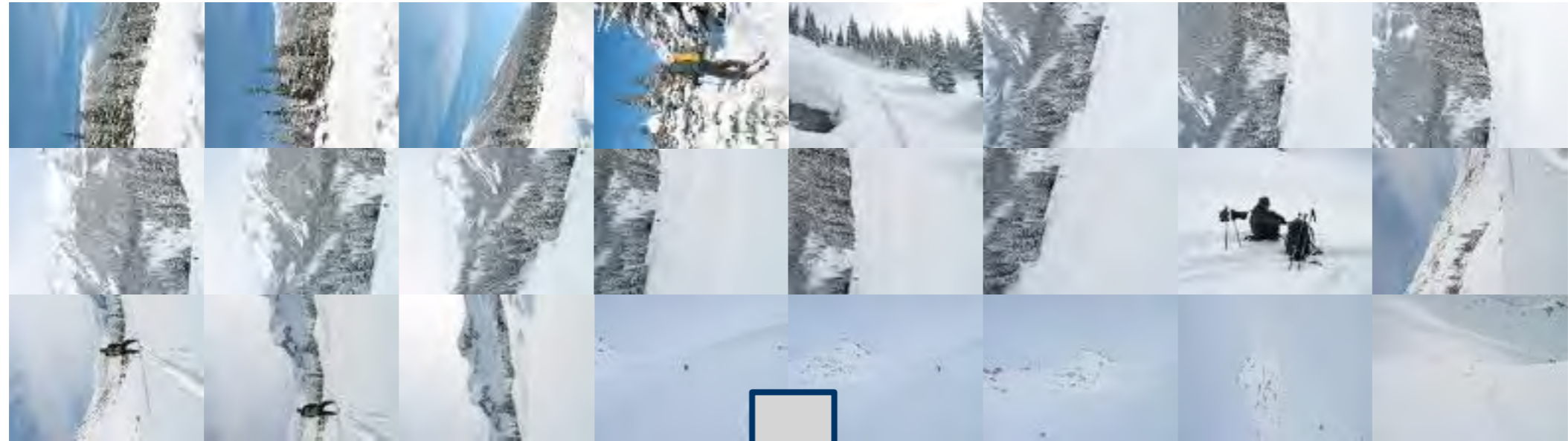
# Panorama Recognition



# Panorama Recognition



# Panorama Recognition

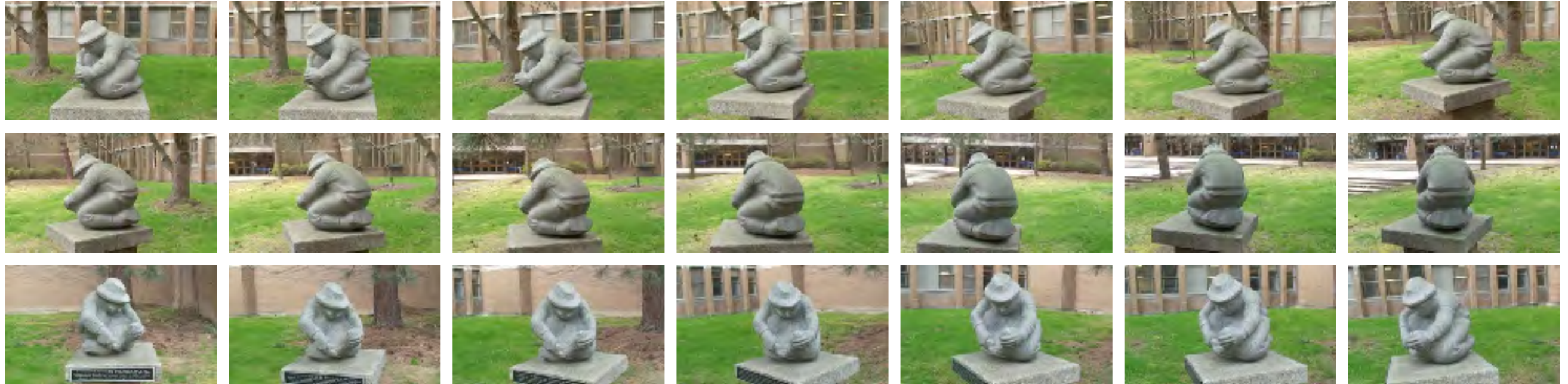


# Panorama Stitching

- We can concatenate pairwise homographies, but over time multiple pairwise mappings accumulate errors
- We use global alignment (bundle adjustment) to close the gap



# Structure from Motion



Given an (unordered) set of input images, compute cameras and 3D structure of the scene

# Structure from Motion



# 2-view Structure from Motion

- We can use the combination of SIFT/RANSAC and triangulation to compute 3D structure from 2 views

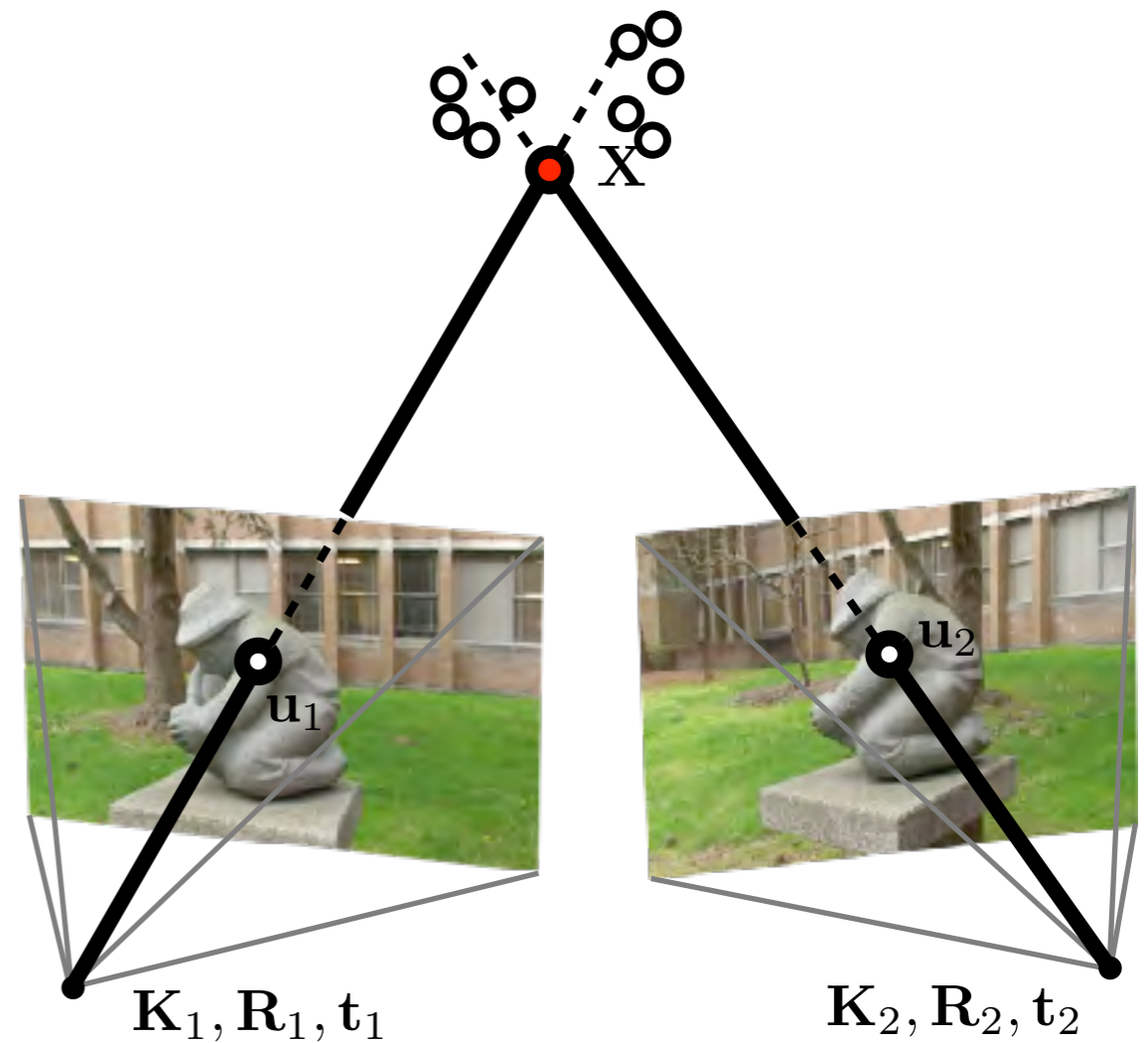


Raw SIFT matches



RANSAC for F

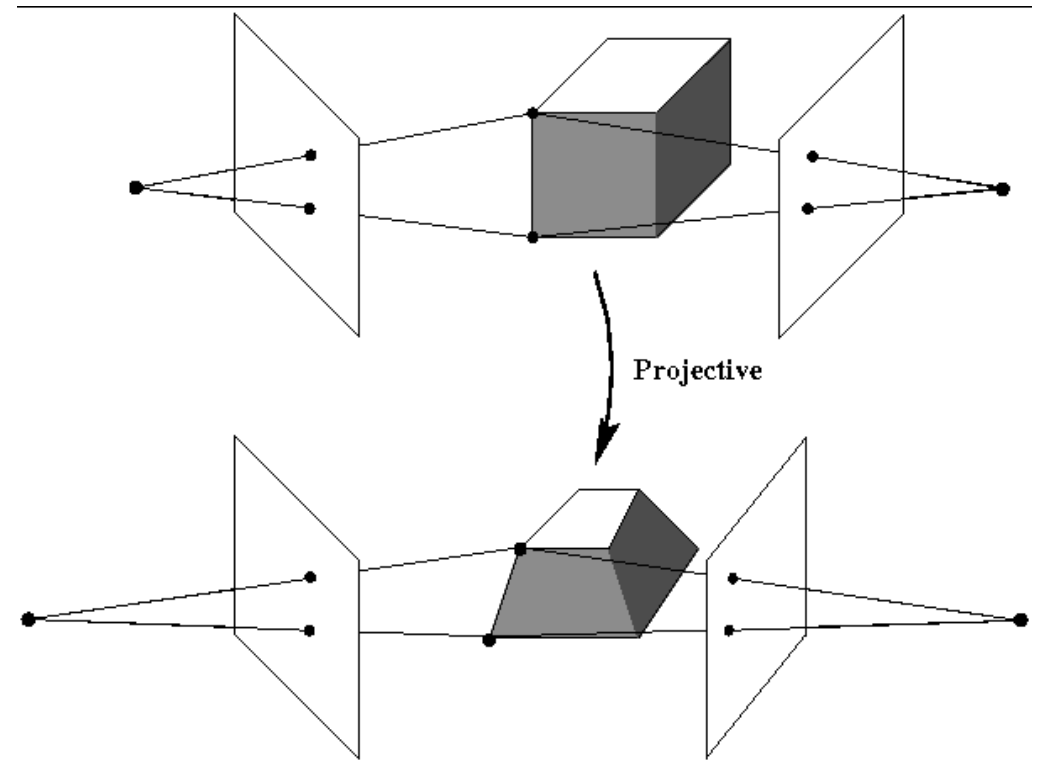
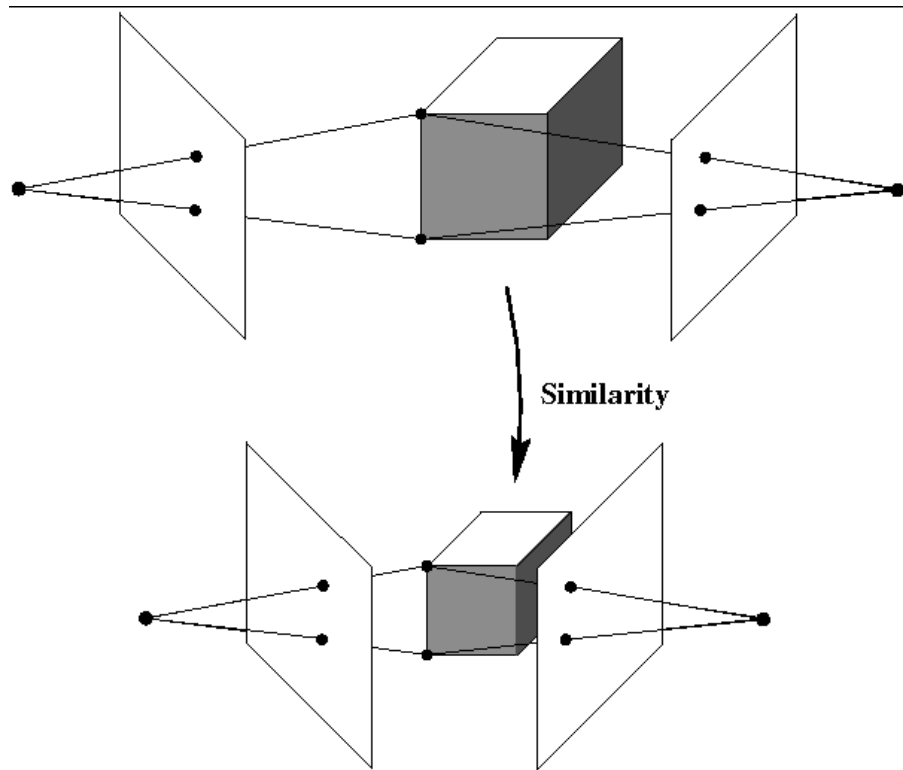
Extract  $R, t$



Triangulate to 3D Point Cloud



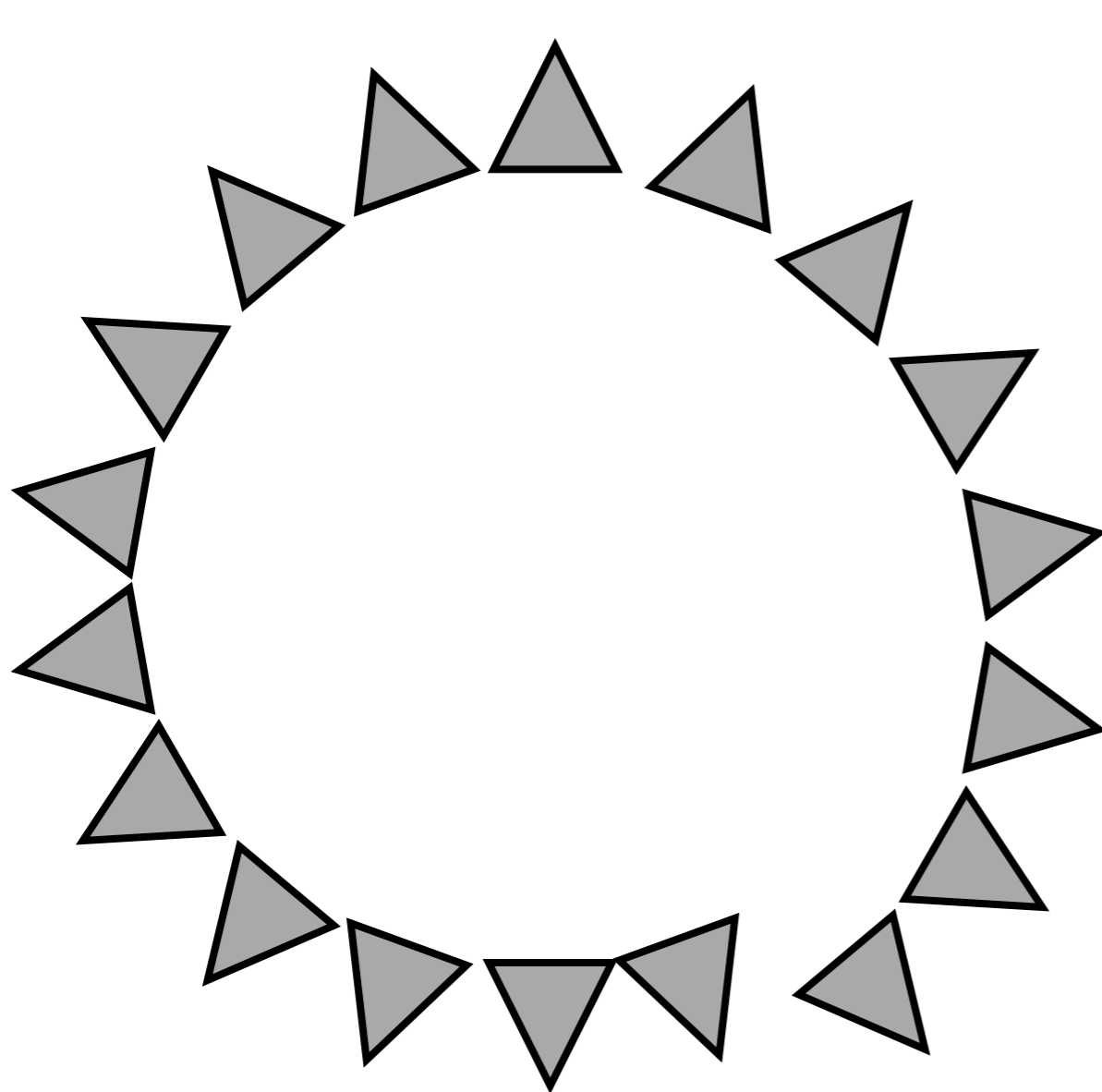
# Ambiguities in 2-view Reconstruction



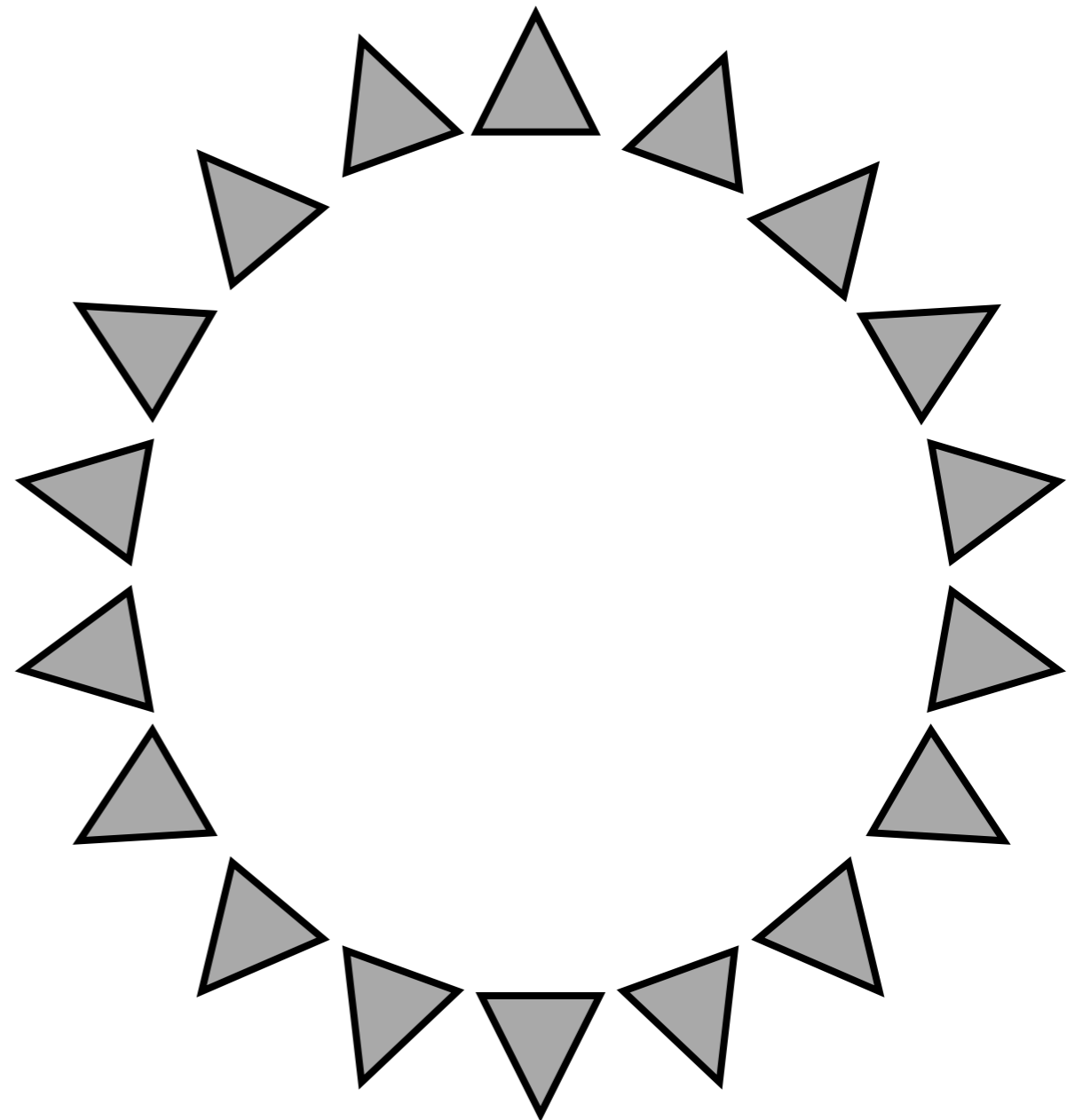
[ Hartley and Zisserman, Ch. 10 ]

# Global Alignment

- Concatenation of pairwise  $R, t$  estimates results in drift, e.g.,



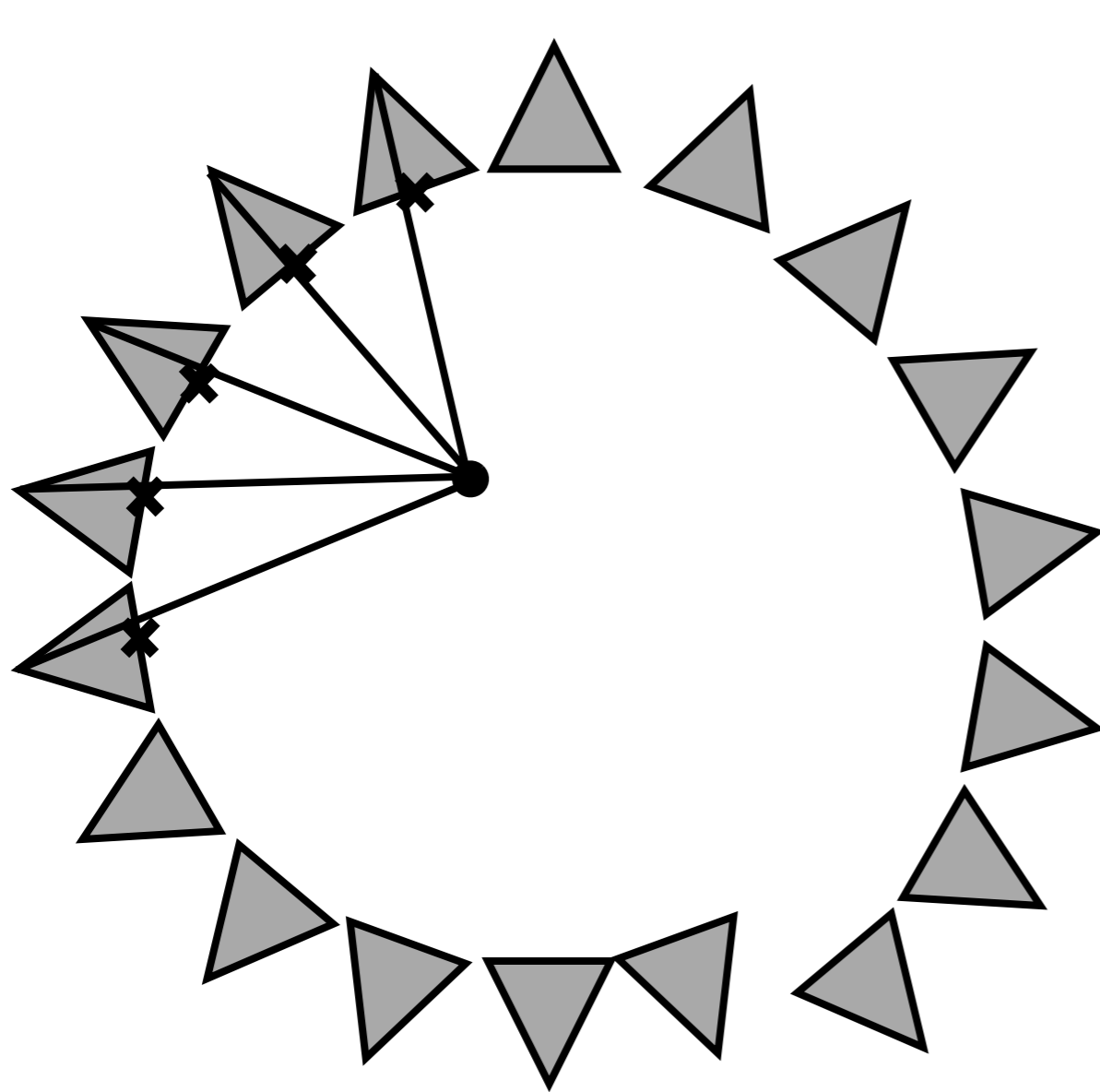
Pairwise alignment



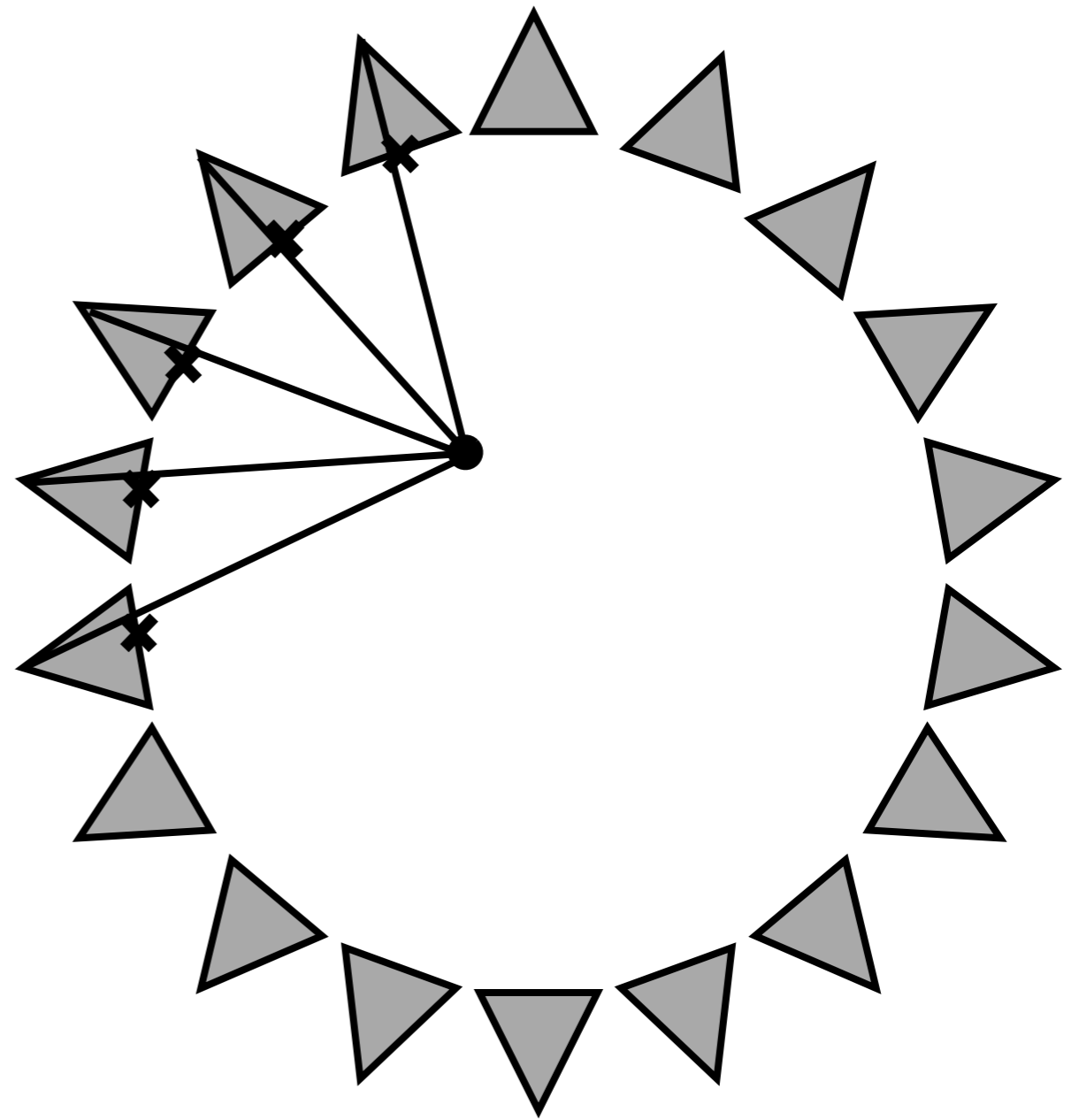
Global alignment

# Global Alignment

- Concatenation of pairwise  $R, t$  estimates results in drift, e.g.,



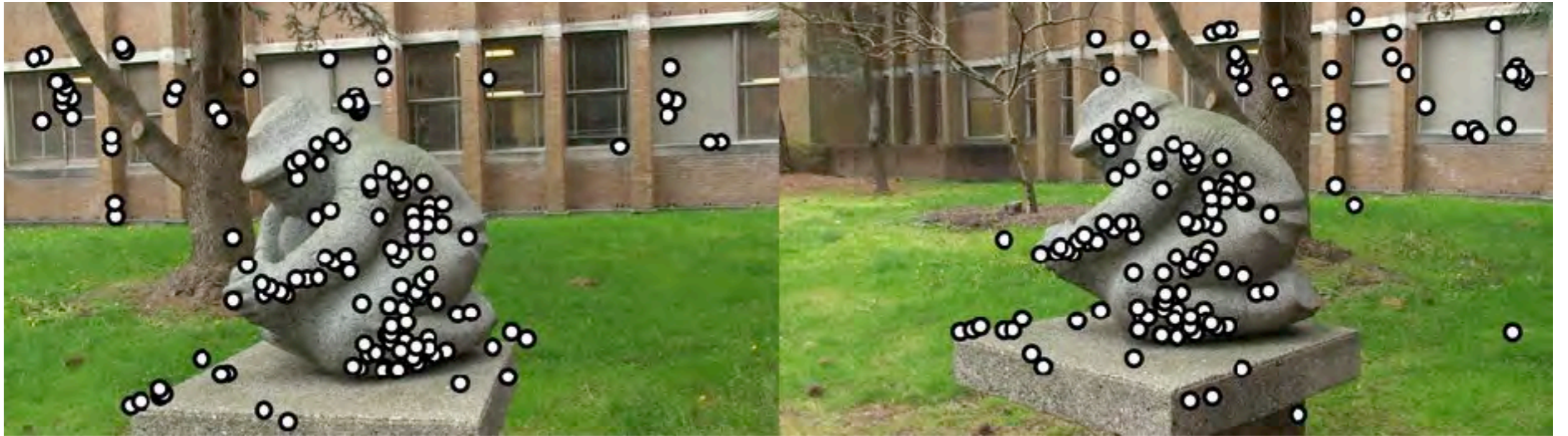
Pairwise alignment



Global alignment



# RANSAC for F



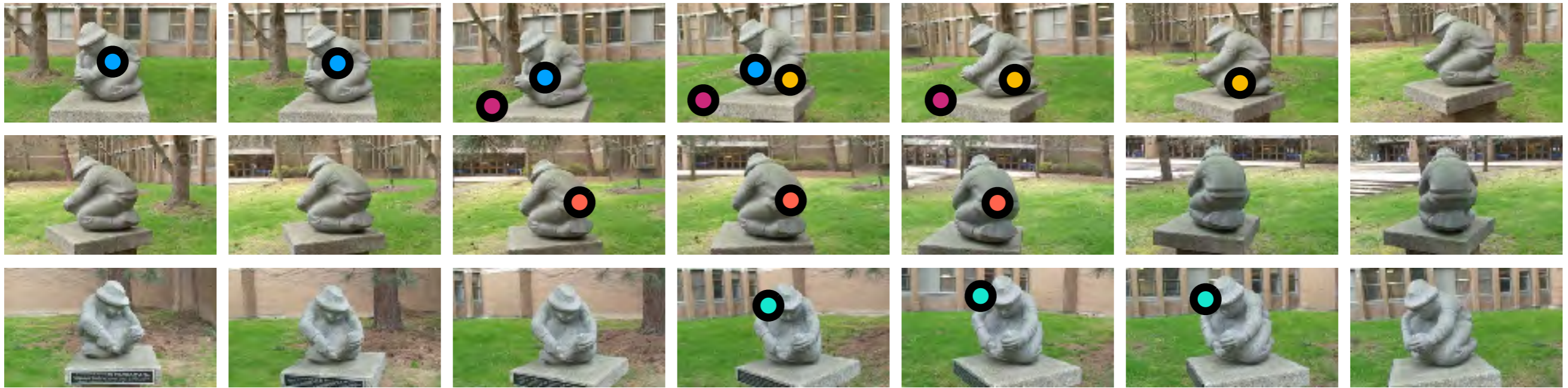
Raw feature matches (after ratio test filtering)



Solved for F and RANSAC inliers

# Feature Tracking

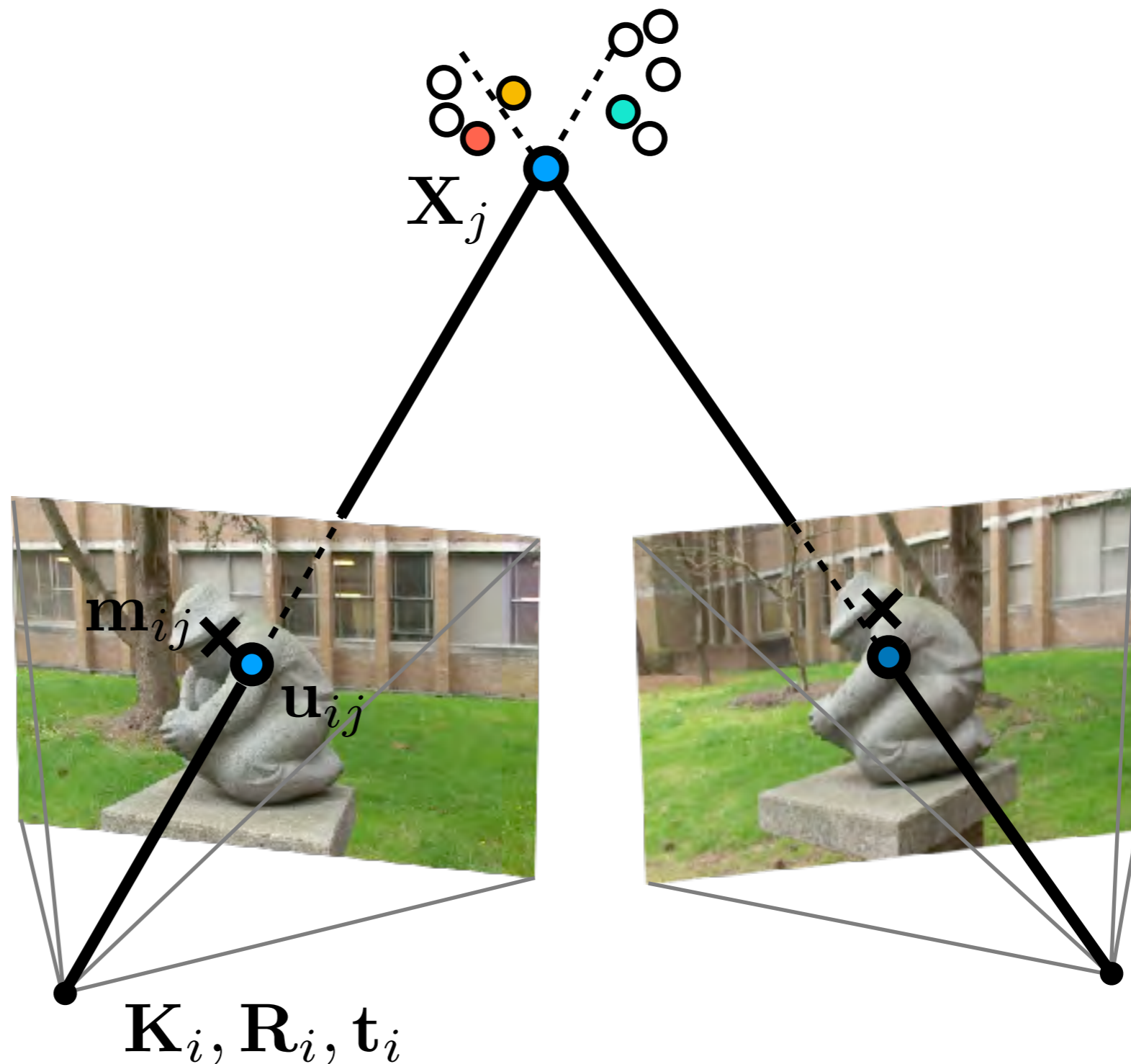
- Form feature tracks by combining pairwise feature matches



- Tracked features become individual 3D points in the reconstruction
- Features matched across 3 or more views provide strong constraints on the 3D reconstruction

# Bundle Adjustment

- Minimise errors projecting 3D points into all images



[ Szeliski 7.4 ]

# Bundle Adjustment

- Initialization with 3 views

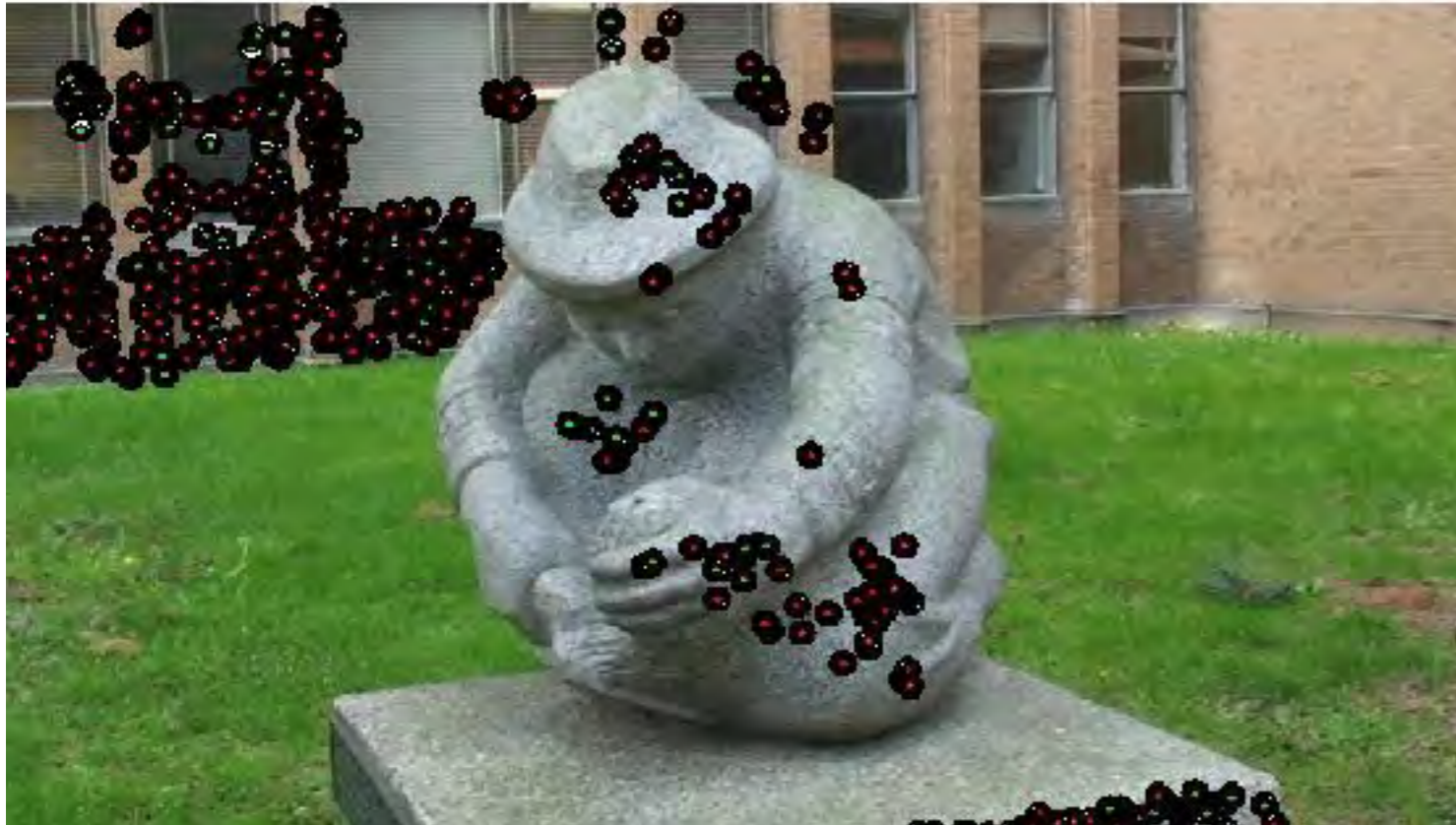


Joint optimization of cameras and structure



# Bundle Adjustment

- Add camera 4



Estimate camera pose, add new 3D points, jointly optimize

# Bundle Adjustment

- Add camera 5



Estimate camera pose, add new 3D points, jointly optimize

# Bundle Adjustment

- Add camera 6



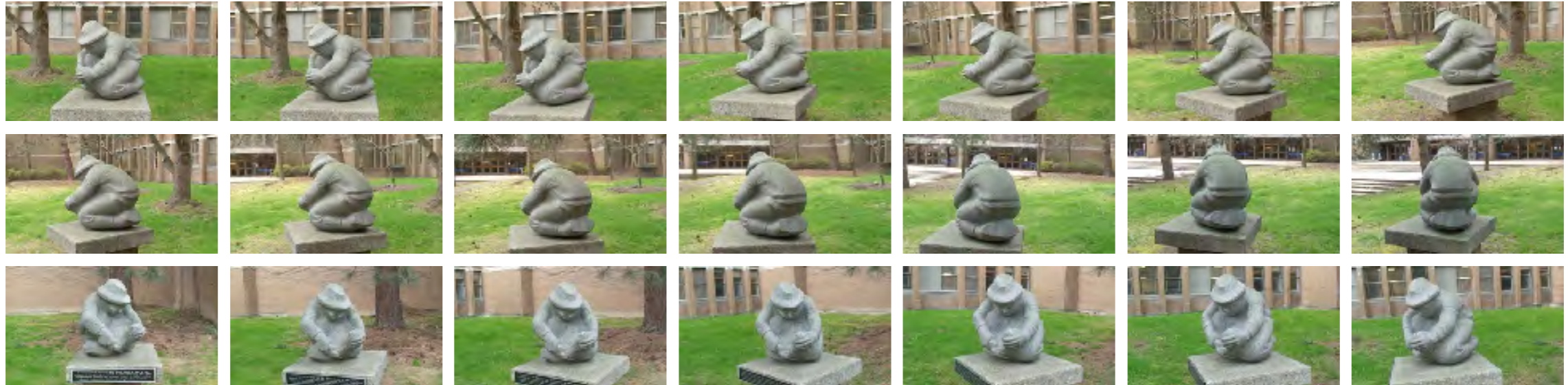
Estimate camera pose, add new 3D points, jointly optimize

# Bundle Adjustment

- Add remaining cameras in same way

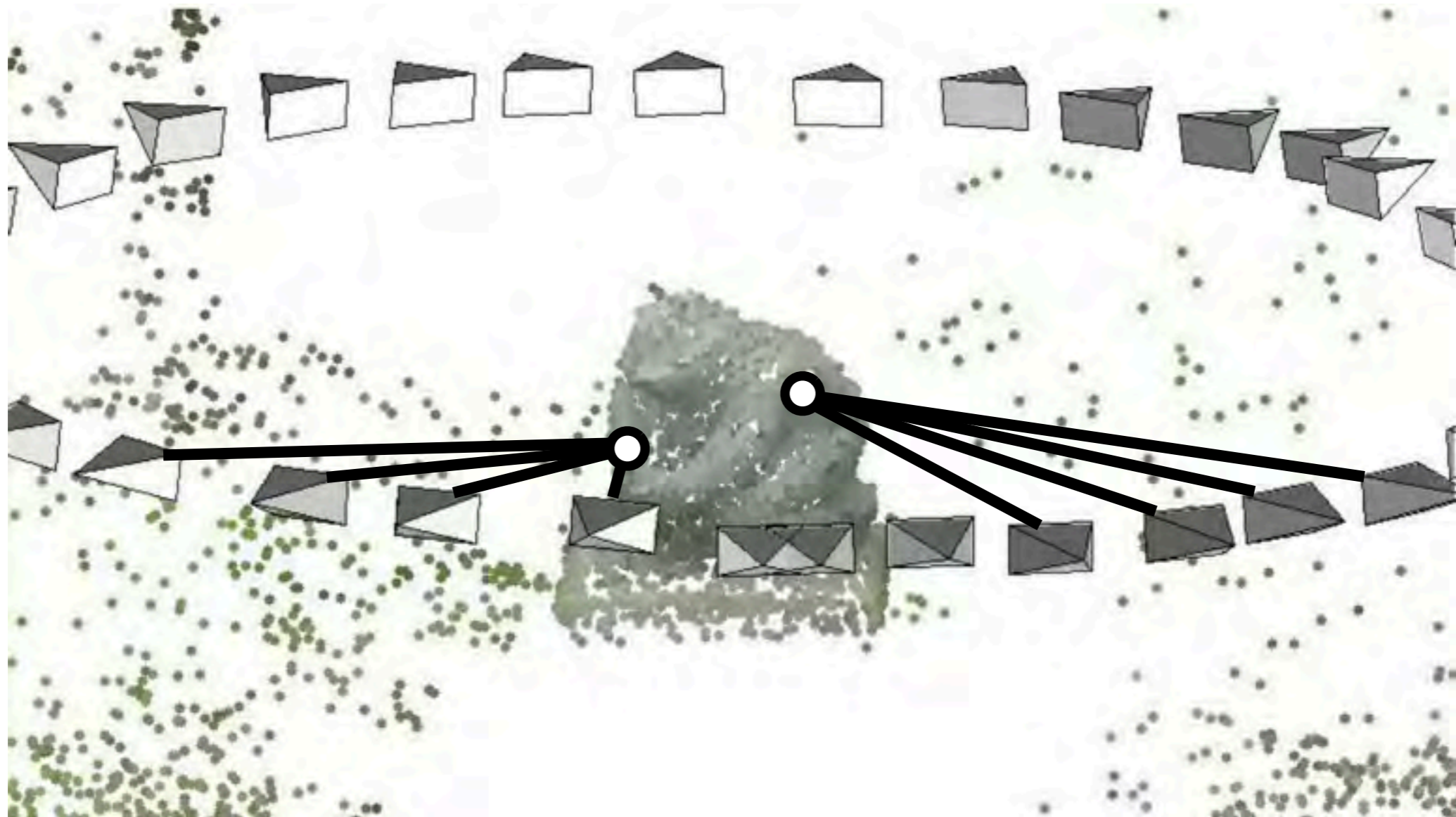


# Structure from Motion



# Why “Bundle” Adjustment?

- Can think of bundles of light rays emanating from each 3D point

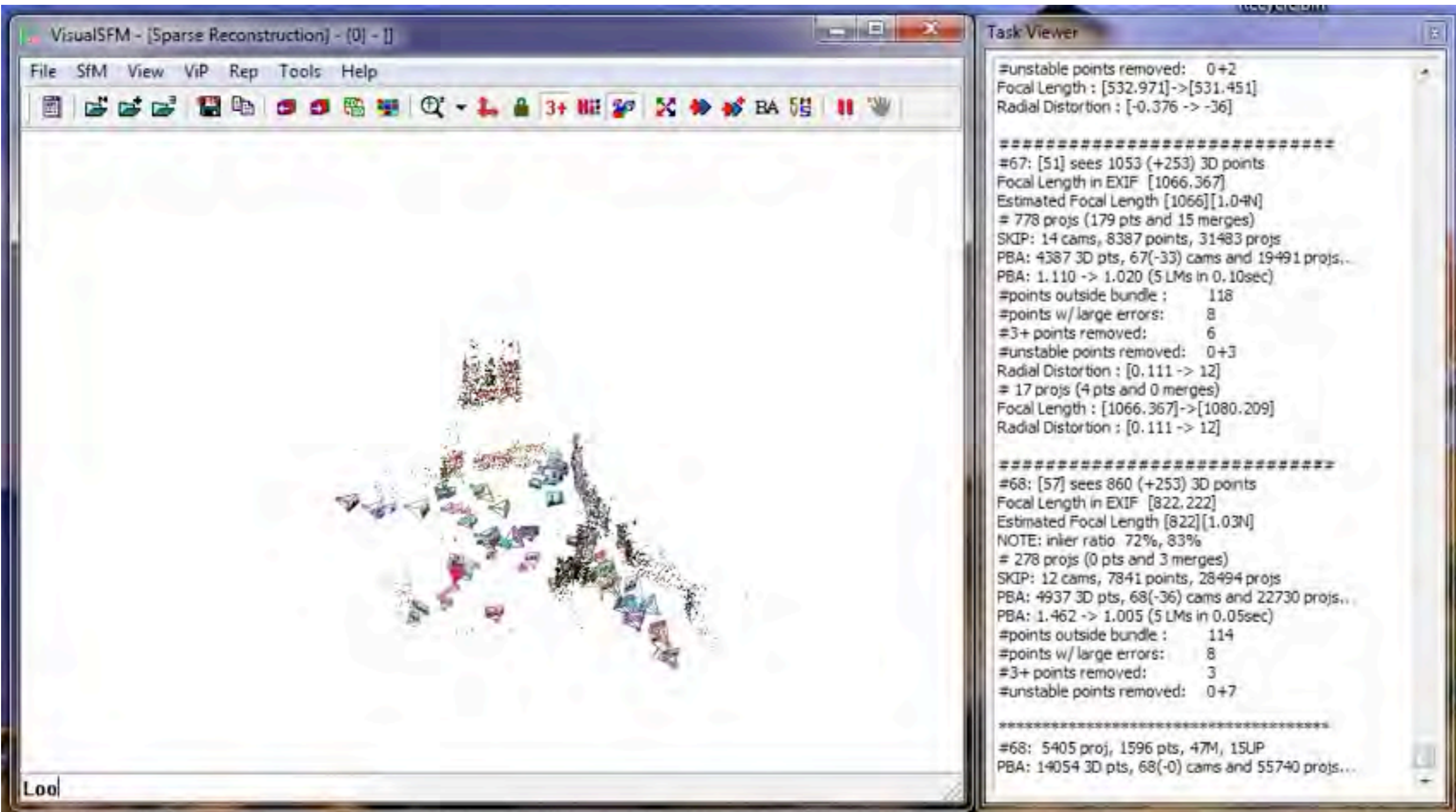


Adjust camera + 3D point positions so that bundles match measured positions (feature points)

# SFM recap

- Match features, e.g., SIFT, between all views
- Use RANSAC to reject outliers and estimate  $F$  matrices
- Form feature tracks by linking multiview matches
- Select an initialization set, e.g., 3 images with lots of matches and good baseline (parallax)
- Jointly optimize cameras  $R, t$  and structure  $X$  for this set
- Repeat for each camera:
  - Estimate pose  $R, t$  by minimising projection errors with existing  $X$
  - Add 3D points corresponding to the new view and optimize
  - Bundle adjust optimizing over all cameras and structure

# Visual SFM





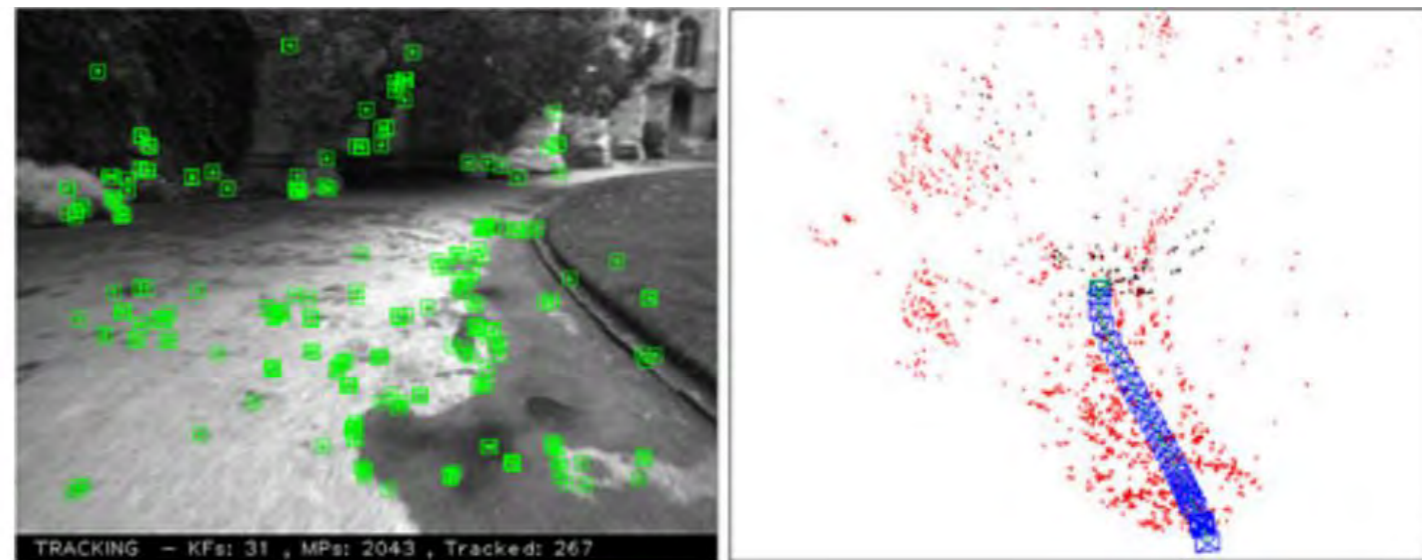
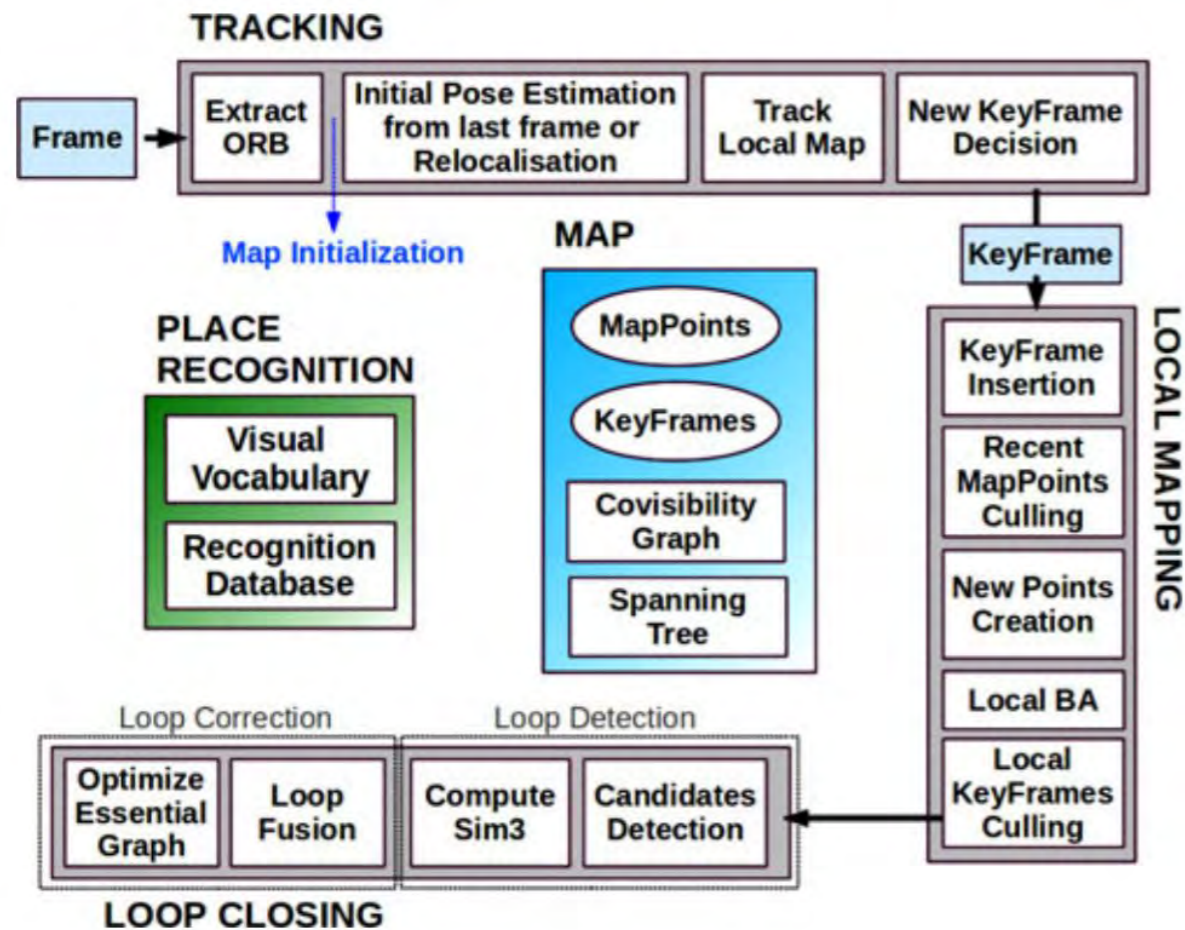
# Application: 3D from Internet Images

- Reconstruct 3D from unordered photo collections



[ Building Rome in a Day, S. Agarwal et al 2009 ]

# Simultaneous Localization and Mapping



[ R. Mur-Artal et al., "ORB-SLAM: A Versatile and Accurate Monocular SLAM System", IEEE Transactions on Robotics, 2015 ]

# Next Lecture

- Dense matching and reconstruction