# CSEP 590A Computational Biology Summer 2006

Lecture 2 Sequence Alignment; DNA Replication

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#### Tonight

- Last week's "quiz" & homework
- Sequence alignment
- Weekly "bio" interlude DNA replication
- More sequence alignment

### Week 1 (anonymous) "Quiz"

- In your own words, what is DNA? Its main role?
- What is RNA? What is its main role in the cell?
- How many amino acids are there? How many are used in proteins?
- Did human beings, as we know them, develop from earlier species of animals?
- What are stem cells?
- What did Viterbi invent?
- What is dynamic programming?
- What is a likelihood ratio test?
- What is the EM algorithm?
- How would you find the maximum of f(x) = ax3 + bx2
  + cx +d in the interval -10<x<25?</li>

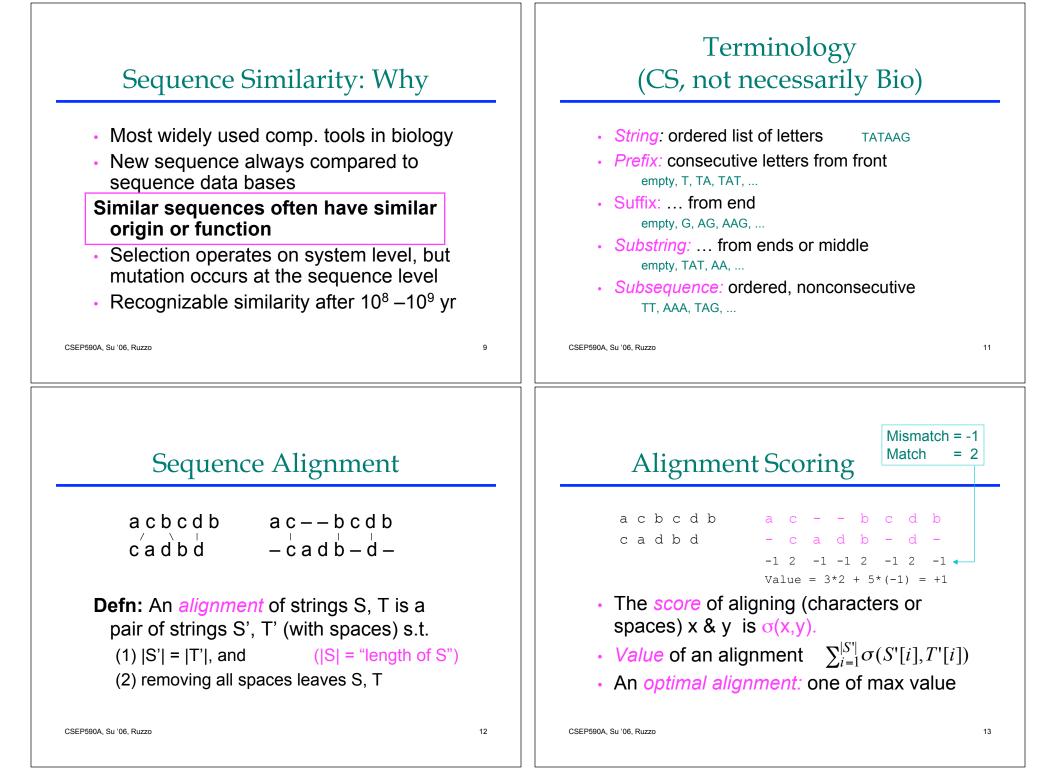
#### **Evolution & Scientific Literacy**

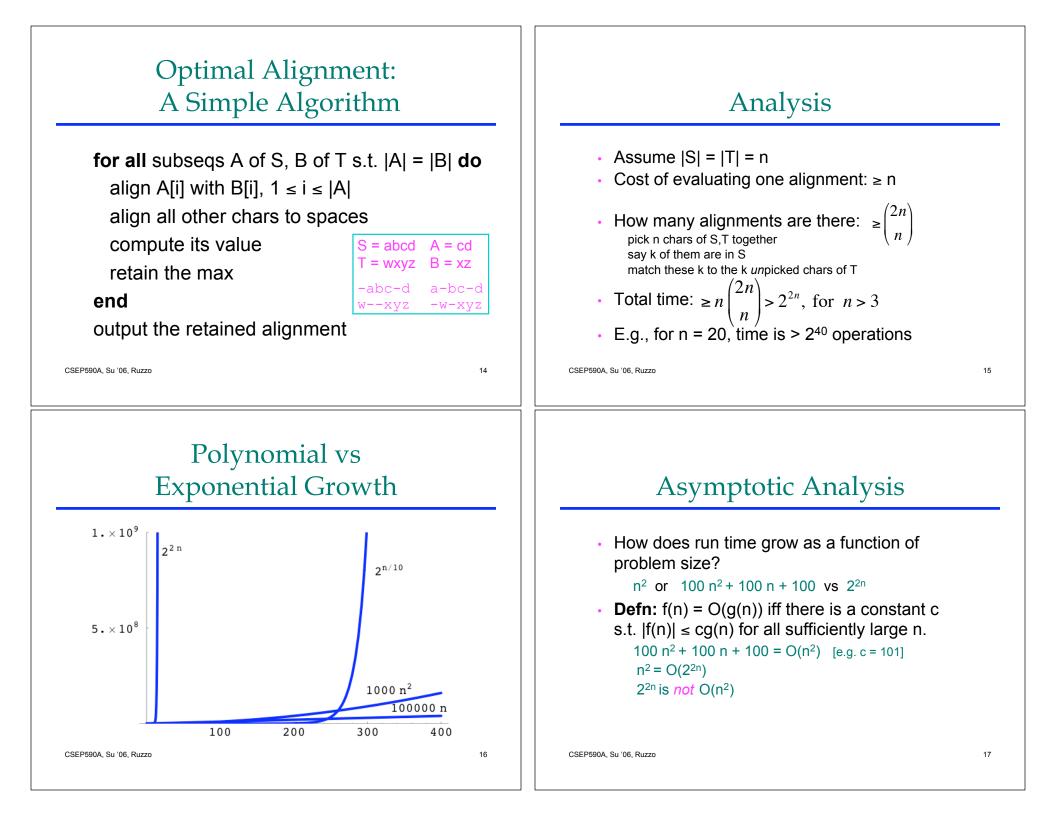
- "Human beings, as we know them, developed from earlier species of animals" (avoiding the now politically charged word "evolution")
- from 1985 to 2005, the % of Americans
  - rejecting: declined from 48% to 39%
  - accepting: also declined 45% to 40
  - uncertain: increased 7% to 21%
- In a 2005 survey, the proportion of adults who accept evolution in 34 countries (US, Europe, Japan...), the United States ranked 33rd, just above/below Turkey.
- My interpretation: The public is surprisingly malleable in the face of political agendas...

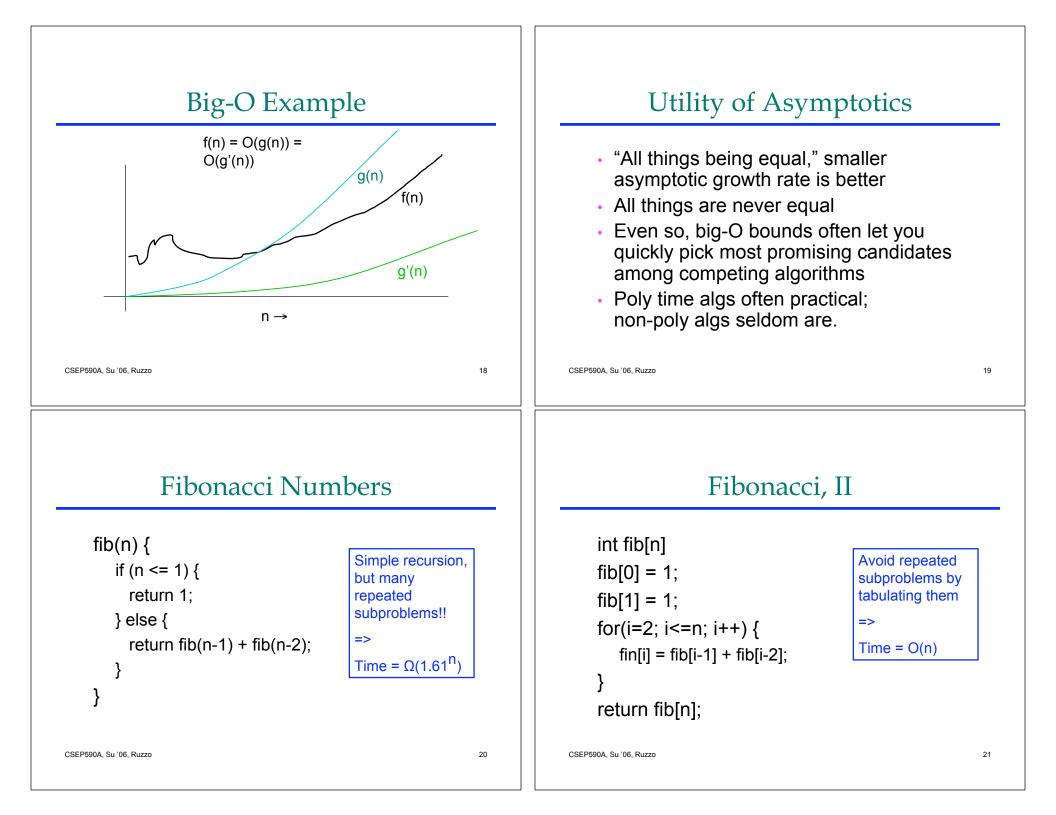
http://biology.plosjournals.org/perlserv/?request=get-document&doi=10.1371/journal.pbio.0040167

Don't worry, we'll talk about all this stuff before the course ends









## Candidate for Dynamic Programming?

- Common Subproblems?
  - Plausible: probably re-considering alignments of various small substrings unless we're careful.
- Optimal Substructure?
  - Plausible: left and right "halves" of an optimal alignment probably should be optimally aligned (though they obviously interact a bit at the interface).
- (Both made rigorous below.)

#### Optimal Substructure (In More Detail)

- Optimal alignment ends in 1 of 3 ways:
  - last chars of S & T aligned with each other
  - last char of S aligned with space in T
  - last char of T aligned with space in S
  - ( never align space with space;  $\sigma(-,-) < 0$  )
- In each case, the rest of S & T should be optimally aligned to each other

Optimal Alignment in O(n<sup>2</sup>) via "Dynamic Programming"

- Input: S, T, |S| = n, |T| = m
- Output: value of optimal alignment

Easier to solve a "harder" problem:

V(i,j) = value of optimal alignment ofS[1], ..., S[i] with T[1], ..., T[j] for all  $0 \le i \le n, 0 \le j \le m$ . iret i chare of

V(i,0): first i chars of S all match spaces

**Base Cases** 

$$V(i,0) = \sum_{k=1}^{i} \sigma(S[k], -)$$

• V(0,j): first j chars of T all match spaces  $V(0, j) = \sum_{k=1}^{j} \sigma(-, T[k])$ 

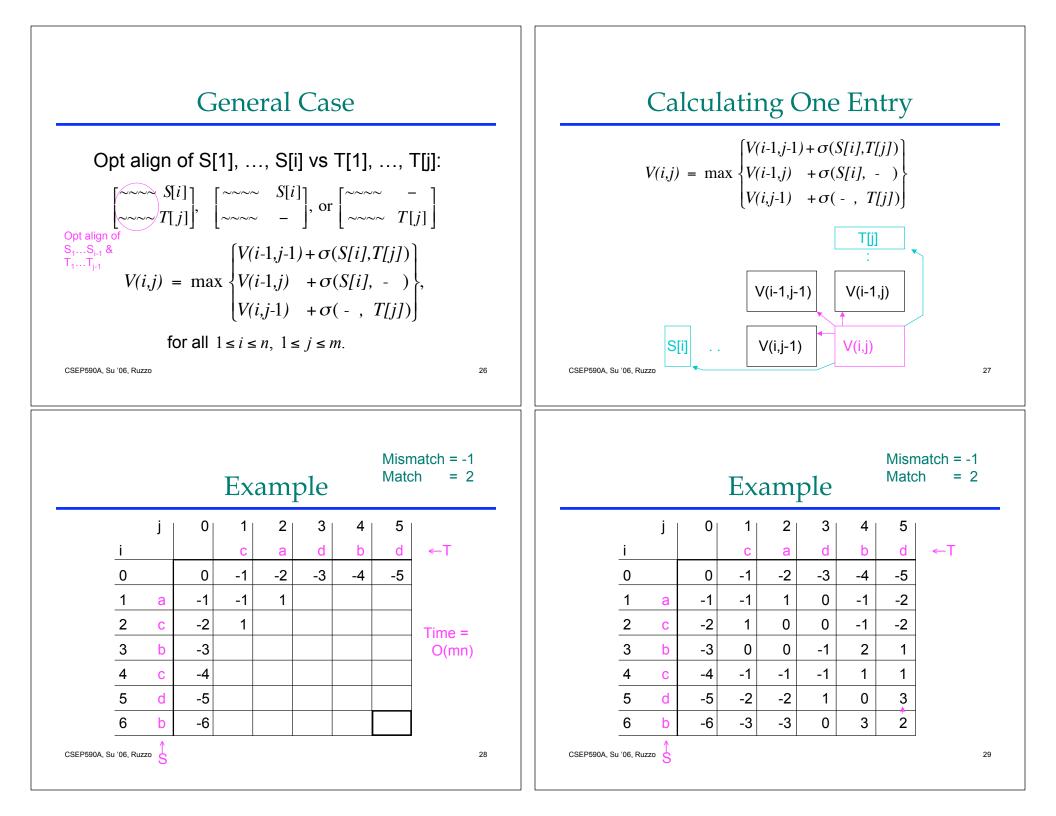
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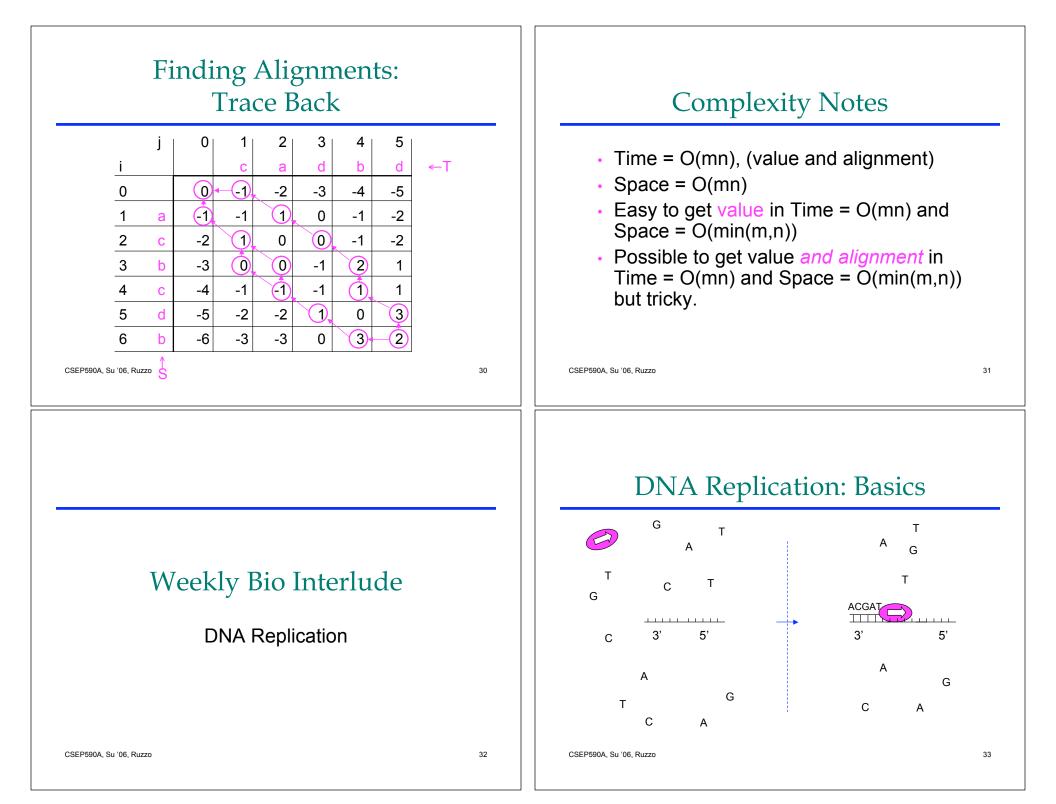
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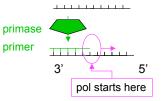
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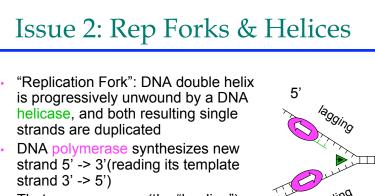
#### Issues & Complications, I

- 1st ~10 nt's added are called the *primer*
- In simple model, DNA pol has 2 jobs: prime & extend
- Priming is error-prone
- So, specialized primase does the priming; pol specialized for fast, accurate extension



Still doesn't solve the accuracy problem (hint: primase makes an RNA primer)

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- That means on one (the "leading") strand, DNA pol is chasing/pushing the replication fork
- But on the other "lagging" strand, DNA pol is running away from it.

3' 5' leading

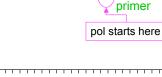
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### Issue 3: Fragments

primer

Lagging strand gets a series of "Okazaki fragments" of DNA (~200nt in eukaryotes) following each primer



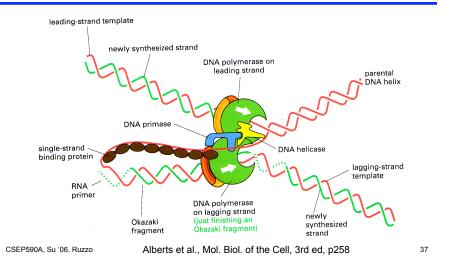
Okazaki

The RNA primers are later removed by a *nuclease* and DNA pol fills gaps (more accurate than primase)



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## Issue 4: Coord Lead/Lag



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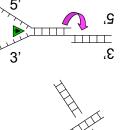
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5'

primer

#### Issue 5: Twirls & Tangles

 Unwinding helix (~10 nucleotides per turn) would cause stress.
 *Topoisomerase I* cuts DNA backbone on *one* strand, allowing it to spin about the remaining bond, relieving stress



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*Topoisomerase II* can cut & rejoin *both* strands, after allowing another double strand to pass through the gap, de-tangling it.

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#### **Replication Summary**

- Speed: 50 (eukaryotes) 500 (prokaryotes) bp/sec
- Accuracy: 1 error per 10<sup>9</sup> bp
- Complex & highly optimized
- · Highly similar across all living cells
- More info: Alberts et al., Mol. Biol. of the Cell

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#### Issue 6: Proofreading

- Error rate of pol itself is ~10<sup>-4</sup>, but overall rate is 10<sup>-9</sup>, due to proofreading & repair, e.g.
  - pol itself can back up & cut off a mismatched base if one happens to be inserted
  - priming the new strand is hard to do accurately, hence RNA primers, later removed & replaced
  - other enzymes scan helix for "bulges" caused by base mismatch, figure out which strand is original, cut away new (faulty) copy; DNA pol fills gap
  - which strand is original? In bacteria, some A's are "methylated", but not immediately after replication

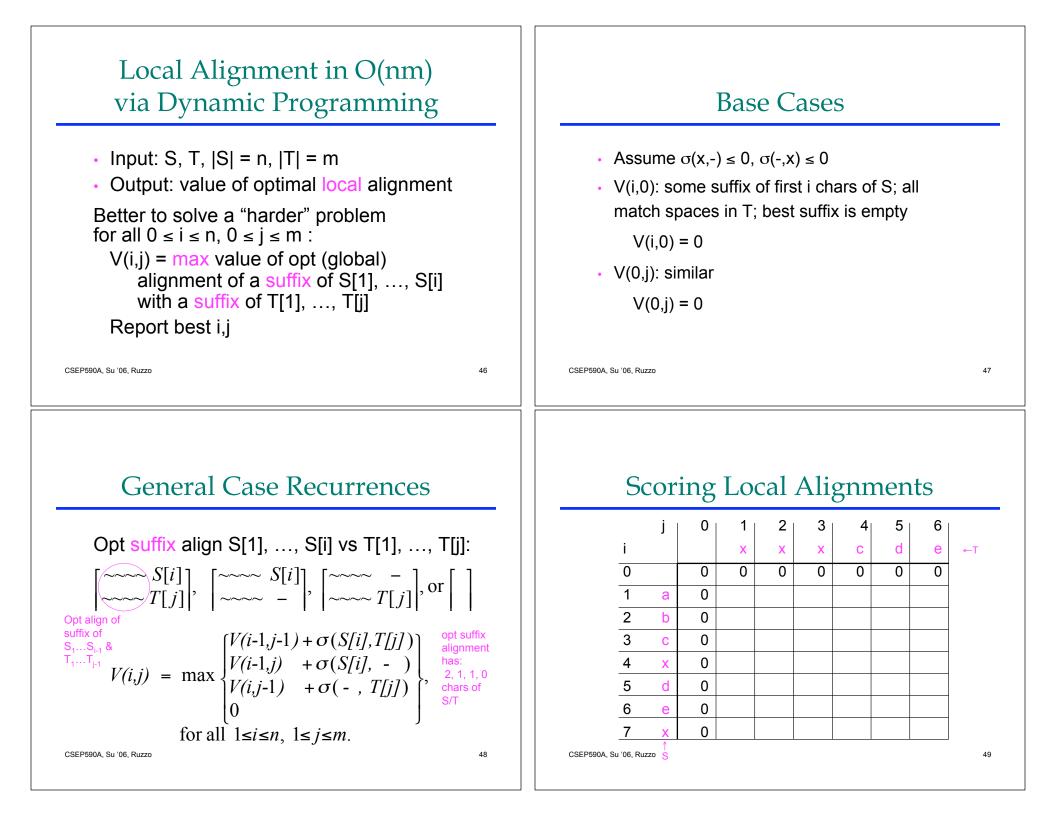
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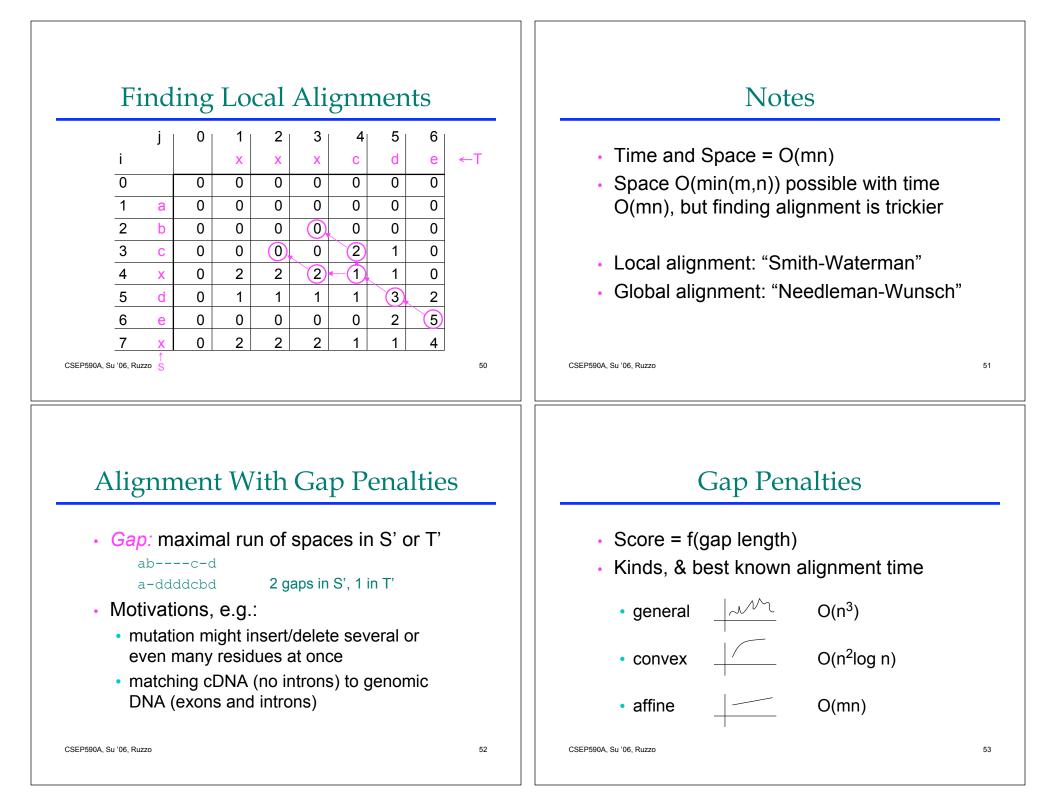
#### Sequence Alignment

#### Part II Local alignments & gaps

#### Variations Local Alignment: Motivations Local Alignment "Interesting" (evolutionarily conserved, functionally related) segments may be a small Preceding gives global alignment, i.e. full part of the whole length of both strings; · Might well miss strong similarity of part of · "Active site" of a protein strings amidst dissimilar flanks Scattered genes or exons amidst "junk", e.g. retroviral insertions, large deletions **Gap Penalties** Don't have whole sequence 10 adjacent spaces cost 10 x one space? Global alignment might miss them if flanking Many others junk outweighs similar regions CSEP590A, Su '06, Ruzzo 42 CSEP590A, Su '06, Ruzzo 43 The "Obvious" Local Local Alignment Alignment Algorithm for all substrings A of S and B of T Optimal *local alignment* of strings S & T: Align A & B via dynamic programming Find substrings A of S and B of T Retain pair with max value having max value global alignment end : Output the retained pair A = c x d eS = abcxdexTime: $O(n^2)$ choices for A, $O(m^2)$ for B, B = c - d e value = 5 T = xxxcdeO(nm) for DP, so $O(n^3m^3)$ total. [Best possible? Lots of redundant work...] 44

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## Global Alignment with Affine Gap Penalties

 $\begin{array}{l} \mathsf{V}(\mathsf{i},\mathsf{j}) = \mathsf{value} \ \mathsf{of} \ \mathsf{opt} \ \mathsf{alignment} \ \mathsf{of} \\ & \mathsf{S}[1], \ \ldots, \ \mathsf{S}[\mathsf{i}] \ \mathsf{with} \ \mathsf{T}[\mathsf{i}], \ \ldots, \ \mathsf{T}[\mathsf{j}] \\ & \mathsf{G}(\mathsf{i},\mathsf{j}) = \ldots, \ \mathsf{s.t.} \ \mathsf{last} \ \mathsf{pair} \ \mathsf{matches} \ \mathsf{S}[\mathsf{i}] \ \& \ \mathsf{T}[\mathsf{j}] \\ & \mathsf{F}(\mathsf{i},\mathsf{j}) = \ldots, \ \mathsf{s.t.} \ \mathsf{last} \ \mathsf{pair} \ \mathsf{matches} \ \mathsf{S}[\mathsf{i}] \ \& - \\ & \mathsf{E}(\mathsf{i},\mathsf{j}) = \ldots, \ \mathsf{s.t.} \ \mathsf{last} \ \mathsf{pair} \ \mathsf{matches} \ - \ \& \ \mathsf{T}[\mathsf{j}] \\ \end{array}$ 

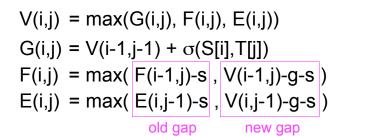
Time: O(mn) [calculate all, O(1) each]

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## Affine Gap Algorithm

Gap penalty =  $g + s^*(gap length), g, s \ge 0$ 

$$V(i,0) = E(i,0) = V(0,i) = F(0,i) = -g-i*s$$



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#### Summary

- Functionally similar proteins/DNA often have recognizably similar sequences even after eons of divergent evolution
- Ability to find/compare/experiment with "same" sequence in other organisms is a huge win
- Surprisingly simple scoring model works well in practice: score each position separately & add, possibly w/ fancier gap model like affine
- Simple "dynamic programming" algorithms can find optimal alignments under these assumptions in poly time (product of sequence lengths)
- This, and heuristic approximations to it like BLAST, are workhorse tools in molecular biology

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