CSE 521 Algorithms

Sequence Alignment

CSE421 Algorithms

Sequence Alignment

CSEP 590 A Computational Biology Autumn 2013

Lecture 2
Sequence Alignment

Tonight

Last week's "quiz" & homework
Sequence alignment
Weekly "bio" interlude - DNA replication
More sequence alignment

"HW 0" Background Poll

In your own words, what is DNA? Its main role?

What is RNA? What is its main role in the cell?

How many amino acids are there? How many are used in proteins?

Did human beings, as we know them, develop from

earlier species of animals?

What are stem cells?

What did Viterbi invent?

What is dynamic programming?

What is a likelihood ratio test?

What is the EM algorithm?

How would you find the maximum of f(x) = ax3 + bx2 + cx + d in the interval -10<x<25?

Don't worry, we'll talk about all this stuff before the course ends

Evolution & Scientific Literacy

"Human beings, as we know them, developed from earlier species of animals"

(avoiding the now politically charged word "evolution")

From 1985 to 2005, the % of Americans

rejecting: declined from 48% to 39%

accepting: also declined 45% to 40

uncertain: increased 7% to 21%

In a 2005 survey, the proportion of adults who accept evolution in 34 countries (US, Europe, Japan...), the United States ranked 33rd, just above/below Turkey.

Part I

Motivation, dynamic programming,
global alignment

What

Why

A Simple Algorithm

Complexity Analysis

A better Algorithm:

"Dynamic Programming"

What

Why

A Dynamic Programming Algorithm

Sequence Similarity: What

GGACCA

TACTAAG

TCCAAG

Sequence Similarity: What

GGACCA

Sequence Similarity: Why

Most widely used comp. tools in biology New sequence always compared to sequence data bases

Similar sequences often have similar origin or function

Recognizable similarity after 10⁸ –10⁹ yr

Sequence Similarity: Why

Bio

Most widely used comp. tools in biology New sequence always compared to data bases

Similar sequences often have similar origin or function

Recognizable similarity after 10⁸ –10⁹ yr DNA sequencing & assembly

Other

spell check/correct, diff, svn/git/..., plagiarism, ...

BLAST Demo

http://www.ncbi.nlm.nih.gov/blast/

Taxonomy Report

Try it!
pick any protein, e.g.
hemoglobin, insulin,
exportin,... BLAST to
find distant relatives.

root	64 hits	16 orgs
. Eukaryota	62 hits	14 orgs [cellular organisms]
Fungi/Metazoa group	57 hits	11 orgs
Bilateria	38 hits	7 orgs [Metazoa; Eumetazoa]
Coelomata	36 hits	6 orgs
Tetrapoda	26 hits	5 orgs [;;; Vertebrata;;;; Sarcopterygii]
Eutheria	24 hits	4 orgs [Amniota; Mammalia; Theria]
Homo sapiens	20 hits	<pre>1 orgs [Primates;; Hominidae; Homo]</pre>
Murinae	3 hits	2 orgs [Rodentia; Sciurognathi; Muridae]
Rattus norvegicus	2 hits	1 orgs [Rattus]
Mus musculus	1 hits	1 orgs [Mus]
Sus scrofa	1 hits	1 orgs [Cetartiodactyla; Suina; Suidae; Sus]
Xenopus laevis	2 hits	<pre>1 orgs [Amphibia;;;;;; Xenopodinae; Xenopus]</pre>
Drosophila melanogaster	10 hits	<pre>1 orgs [Protostomia;;;; Drosophila;;;]</pre>
Caenorhabditis elegans	2 hits	<pre>1 orgs [; Nematoda;;;;;; Caenorhabditis]</pre>
Ascomycota	19 hits	4 orgs [Fungi]
Schizosaccharomyces pombe	10 hits	<pre>1 orgs [;;;; Schizosaccharomyces]</pre>
Saccharomycetales	9 hits	<pre>3 orgs [Saccharomycotina; Saccharomycetes]</pre>
Saccharomyces	8 hits	2 orgs [Saccharomycetaceae]
Saccharomyces cerevisiae .	7 hits	1 orgs
Saccharomyces kluyveri	1 hits	1 orgs
Candida albicans	1 hits	<pre>1 orgs [mitosporic Saccharomycetales;]</pre>
Arabidopsis thaliana	2 hits	<pre>1 orgs [Viridiplantae;Brassicaceae;]</pre>
Apicomplexa	3 hits	2 orgs [Alveolata]
Plasmodium falciparum	2 hits	<pre>1 orgs [Haemosporida; Plasmodium]</pre>
Toxoplasma gondii	1 hits	<pre>1 orgs [Coccidia; Eimeriida; Sarcocystidae;]</pre>
. synthetic construct	1 hits	<pre>1 orgs [other; artificial sequence]</pre>
'mphocystis disease virus	1 hits	1 orgs [Viruses; dsDNA viruses, no RNA]

Terminology

- String: ordered list of letters TATAAG
- Prefix: consecutive letters from front empty, T, TA, TAT, ...
- Suffix: ... from end empty, G, AG, AAG, ...
- Substring: ... from ends or middle empty, TAT, AA, ...
- Subsequence: ordered, nonconsecutive TT, AAA, TAG, ...

Defn: An *alignment* of strings S, T is a pair of strings S', T' (with dashes) s.t.

(1)
$$|S'| = |T'|$$
, and ($|S| = "length of S")$

(2) removing all dashes leaves S, T

Mismatch = -1Match = 2

Alignment Scoring

a c b c d b

c a d b d

- c a d b - d -

-1 2 -1 -1 2 -1 2 -1

Value =
$$3*2 + 5*(-1) = +1$$

The *score* of aligning (characters or dashes) x & y is $\sigma(x,y)$.

Value of an alignment $\sum_{i=1}^{|S'|} \sigma(S'[i], T'[i])$

An *optimal alignment:* one of max value (Assume $\sigma(-,-) < 0$)

Optimal Alignment: A Simple Algorithm

```
for all subseqs A of S, B of T s.t. |A| = |B| do align A[i] with B[i], 1 \le i \le |A| align all other chars to spaces
```

compute its value retain the max

end

output the retained alignment

Analysis

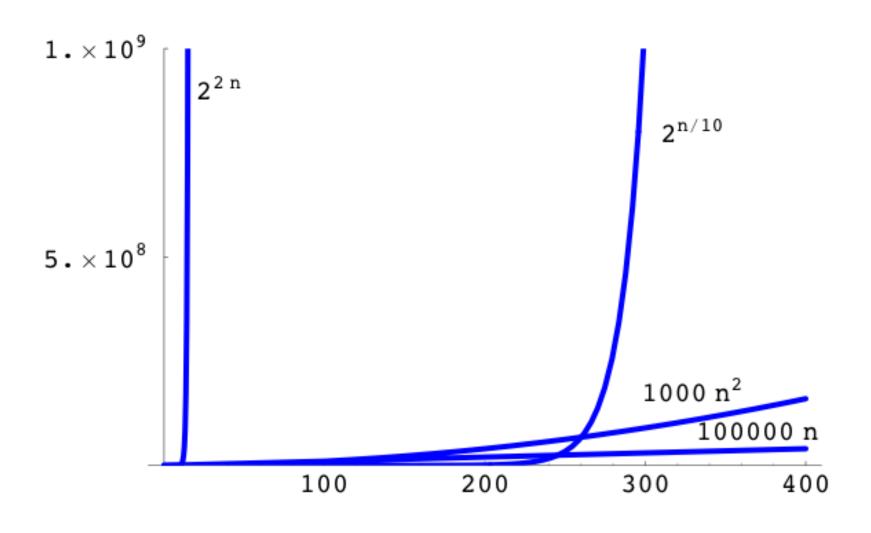
Assume |S| = |T| = nCost of evaluating one alignment: $\ge n$

How many alignments are there: $\geq \binom{2n}{n}$ pick n chars of S,T together say k of them are in S match these k to the k *un*picked chars of T

Total time:
$$\geq n \binom{2n}{n} > 2^{2n}$$
, for $n > 3$

E.g., for n = 20, time is $> 2^{40}$ operations

Polynomial vs Exponential Growth



Asymptotic Analysis

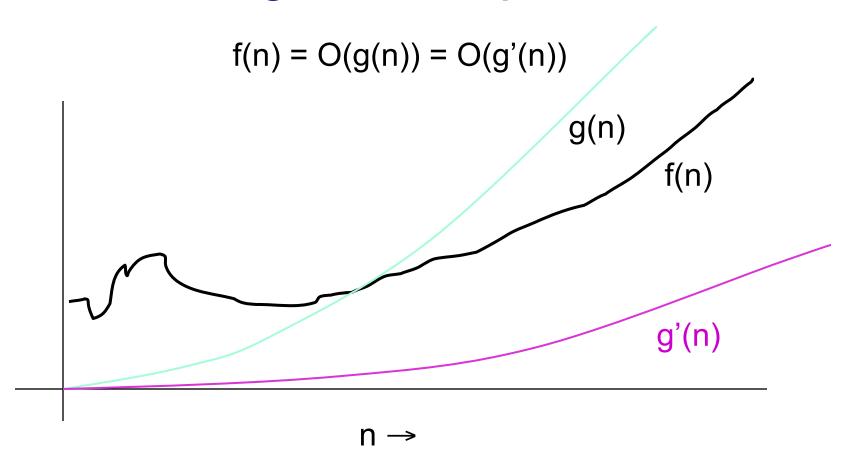
How does run time grow as a function of problem size?

```
n^2 or 100 n^2 + 100 n + 100 vs <math>2^{2n}
```

Defn: f(n) = O(g(n)) iff there is a constant c s.t. $|f(n)| \le cg(n)$ for all sufficiently large n.

100
$$n^2 + 100 n + 100 = O(n^2)$$
 [e.g. c = 101]
 $n^2 = O(2^{2n})$
 2^{2n} is *not* $O(n^2)$

Big-O Example



Utility of Asymptotics

"All things being equal," smaller asymptotic growth rate is better

All things are never equal

Even so, big-O bounds often let you quickly pick most promising candidates among competing algorithms

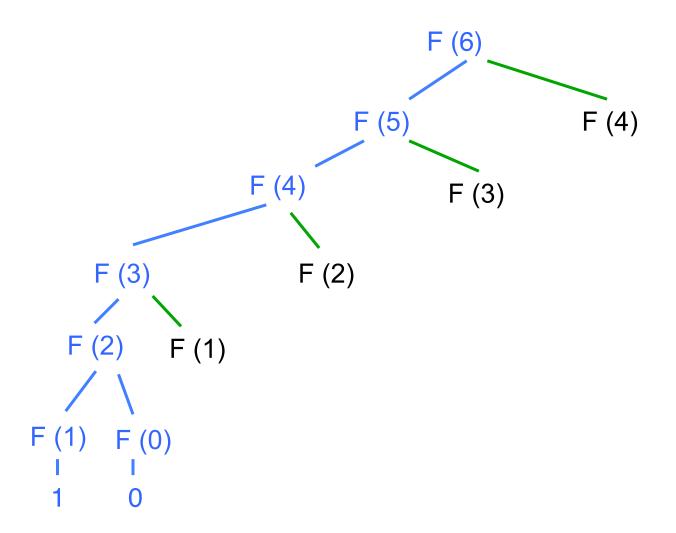
Poly time algs often practical; non-poly algs seldom are.

(Yes, there are exceptions.)

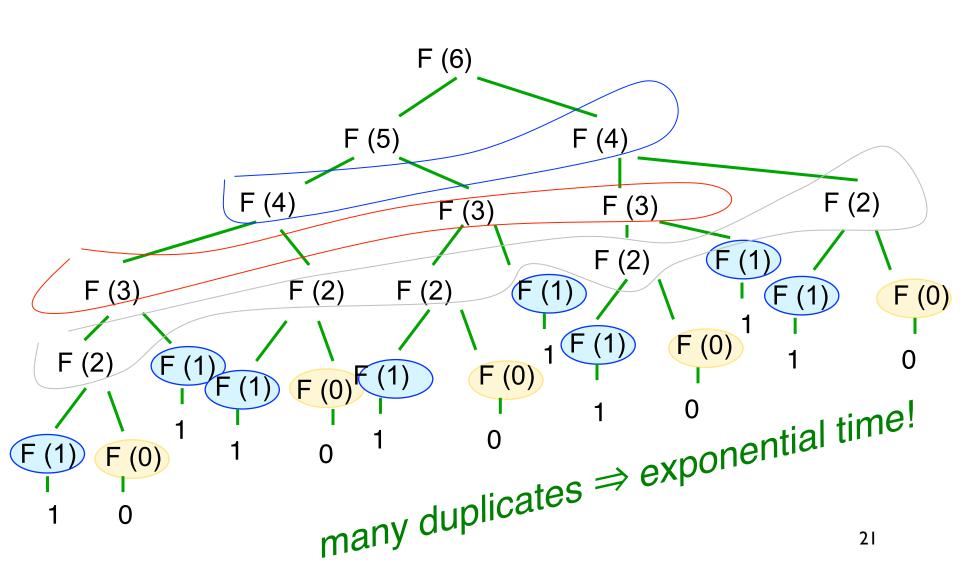
Fibonacci Numbers (recursion)

```
fibr(n) {
                                         Simple recursion,
 if (n \le 1) {
                                             but many
                                             repeated
   return 1;
                                          subproblems!!
 } else {
   return fibr(n-1) + fibr(n-2);
                                         Time = \Omega(1.61^{\rm n})
```

Call tree - start



Full call tree



Fibonacci, II (dynamic programming)

```
int fibd[n];
fibd[0] = 1;
fibd[1] = 1;
for(i=2; i<=n; i++) {
 fibd[i] = fibd[i-1] + fibd[i-2];
return fibd[n];
```

Avoid repeated subproblems by tabulating their solutions

 \Rightarrow

Time = O(n)

(in this case)

Alignment by Dynamic Programming?

Common Subproblems?

Plausible: probably re-considering alignments of various small substrings unless we're careful.

Optimal Substructure?

Plausible: left and right "halves" of an optimal alignment probably should be optimally aligned (though they obviously interact a bit at the interface).

(Both made rigorous below.)

Optimal Substructure (In More Detail)

Optimal alignment *ends* in 1 of 3 ways: last chars of S & T aligned with each other last char of S aligned with dash in T last char of T aligned with dash in S (never align dash with dash; $\sigma(-, -) < 0$)

In each case, the *rest* of S & T should be *optimally* aligned to each other

Optimal Substructure

Optimal alignment *ends* in 1 of 3 ways: last chars of S & T aligned with each other last char of S aligned with dash in T last char of T aligned with dash in S (never align dash with dash; $\sigma(-, -) < 0$)

In each case, the *rest* of S & T should be *optimally* aligned to each other

Optimal Alignment in O(n²) via "Dynamic Programming"

Input: S, T, |S| = n, |T| = m

Output: value of optimal alignment

Easier to solve a "harder" problem:

V(i,j) = value of optimal alignment of S[1], ..., S[i] with T[1], ..., T[j] for all $0 \le i \le n$, $0 \le j \le m$.

Base Cases

V(i,0): first i chars of S all match dashes

$$V(i,0) = \sum_{k=1}^{i} \sigma(S[k],-)$$

V(0,j): first j chars of T all match dashes

$$V(0,j) = \sum_{k=1}^{j} \sigma(-,T[k])$$

General Case

Opt align of S[1], ..., S[i] vs T[1], ..., T[j]:

$$\begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim T[j] \end{bmatrix}, \quad \begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim - \end{bmatrix}, \text{ or } \begin{bmatrix} \sim \sim \sim - \\ \sim \sim \sim T[j] \end{bmatrix}$$
Opt align of
$$\begin{bmatrix} V(i-1,i-1) + \sigma(S[i],T[i]) \end{bmatrix}$$

Opt align of
$$S_{1}...S_{i-1} & \\ V(i,j) = \max \begin{cases} V(i-1,j-1) + \sigma(S[i],T[j]) \\ V(i-1,j) + \sigma(S[i],-) \\ V(i,j-1) + \sigma(-,T[j]) \end{cases}$$

for all $1 \le i \le n$, $1 \le j \le m$.

Calculating One Entry

$$V(i,j) = \max \begin{cases} V(i-1,j-1) + \sigma(S[i],T[j]) \\ V(i-1,j) + \sigma(S[i], -) \\ V(i,j-1) + \sigma(-, T[j]) \end{cases}$$

$$V(i-1,j-1) \qquad V(i-1,j)$$

$$V(i-1,j-1) \qquad V(i-1,j)$$

Mismatch = -1Match = 2

Example

	j	0	1	2	3	4	5	
<u>i</u>			С	a	d	b	d	←
0		0	-1	-2	-3	-4	-5	
1	a	-1						
2	С	-2		C -	c Score(c,-) = -1			
3	b	-3						
4	O	-4						
5	d	-5						
6	b	-6						



Mismatch = -1 Match = 2

Example

	j	0	1	2	3	4	5	
<u>i</u>			С	a	d	b	d	←T
0		0	-1	-2	-3	-4	-5	
1	a	-1						
2	О	-2						
3	b	-3	- a	Score(-,a) = -				
4	O	-4						
5	d	-5						
6	b	-6						



Example

	j	0	1	2	3	4	5	
<u>i</u>			С	a	d	b	d	←T
0		0	-1	-2	-3	-4	-5	
1	a	-1						
2	С	-2						
3	Q	-3						
4	С	-4	_	- Sc	ore(-,c	c) = -1		
5	d	-5	-1		<u>,</u>			
6	b	-6						



Example

	j	0	1	2	3	4	5	
<u>i</u>			С	a	d	b	d	←T
0		0	-1	-2	-3	-4	-5	
1	а	-1	-1	1				
2	С	-2						
3	р	-3						2
4	С	-4				σ(a,	a)=+2	σ(-,a)=-1
5	d	-5				σ(a	-)=-1	1 -3 ca-
6	b	-6					>	-2 1 ca
	^ S							aa

Example

	j	0	1	2	3	4	5
<u>i</u>			С	a	d	b	d
0		0	-1	-2	-3	-4	-5
1	а	-1	-1	1			
2	С	-2	1				
3	Q	-3					
4	С	-4					
5	d	-5					
6	b	-6					

←T

Time = O(mn)



Example

	j	0	1	2	3	4	5	
<u>i</u>			С	a	d	b	d	← T
0		0	-1	-2	-3	-4	-5	
1	а	-1	-1	1	0	-1	-2	
2	С	-2	1	0	0	-1	-2	
3	b	-3	0	0	-1	2	1	
4	O	-4	-1	-1	-1	1	1	
5	р	-5	-2	-2	1	0	3	
6	b	-6	-3	-3	0	3	2	



Finding Alignments: Trace Back

Arrows = (ties for) max in V(i,j); 3 LR-to-UL paths = 3 optimal alignments

	j	0	1	2	3	4	5	
i			С	a	d	b	d	←T
0		0	—	-2	-3	-4	-5	
1	a	<u>-1</u>	-1	1	0	-1	-2	
2	С	-2		0	0	-1	-2	
3	р	-3	0	0	-1	2	1	
4	С	-4	-1	-1	-1	1	1	
5	d	-5	-2	-2	1,	0	3	
6	b	-6	-3	-3	0	3	_2	
								•

^S

Complexity Notes

Time = O(mn), (value and alignment)

Space = O(mn)

Easy to get value in Time = O(mn) and Space = O(min(m,n))

Possible to get value and alignment in Time = O(mn) and Space = O(min(m,n)) (KT section 6.7)

Complexity Notes

Time = O(mn), (value and alignment)

Space = O(mn)

Easy to get value in Time = O(mn) and Space = O(min(m,n))

Possible to get value and alignment in Time = O(mn) and Space = O(min(m,n)), but tricky (DEKM 2.6)

Significance of Alignments

Is "42" a good score?

Compared to what?

Usual approach: compared to a specific "null model", such as "random sequences"

More on this next time; a taste today, for use in next HW

Significance of Alignments

Is "42" a good score? Compared to what?

Usual approach: compared to a specific "null model", such as "random sequences"

Interesting stats problem; much is known

Overall Alignment Significance, II Empirical (via randomization)

```
You just searched with x, found "good" score for x:y Generate N random "y-like" sequences (say N = 10^3 - 10^6) Align x to each & score
```

If k of them have better score than alignment of x to y, then the (empirical) probability of a chance alignment as good as observed x:y alignment is (k+1)/(N+1)

e.g., if 0 of 99 are better, you can say "estimated p < .01"

How to generate "random y-like" seqs? Scores depend on:

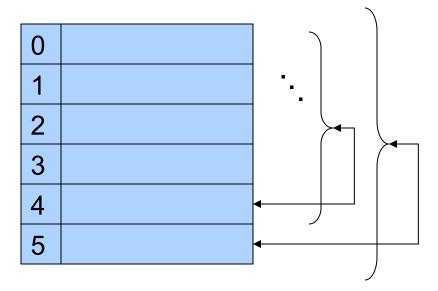
Length, so use same length as y

Sequence composition, so uniform 1/20 or 1/4 is a bad idea; even background p_i can be dangerous

Better idea: permute y N times

Generating Random Permutations

```
for (i = n-1; i > 0; i--){
    j = random(0..i);
    swap X[i] <-> X[j];
}
```

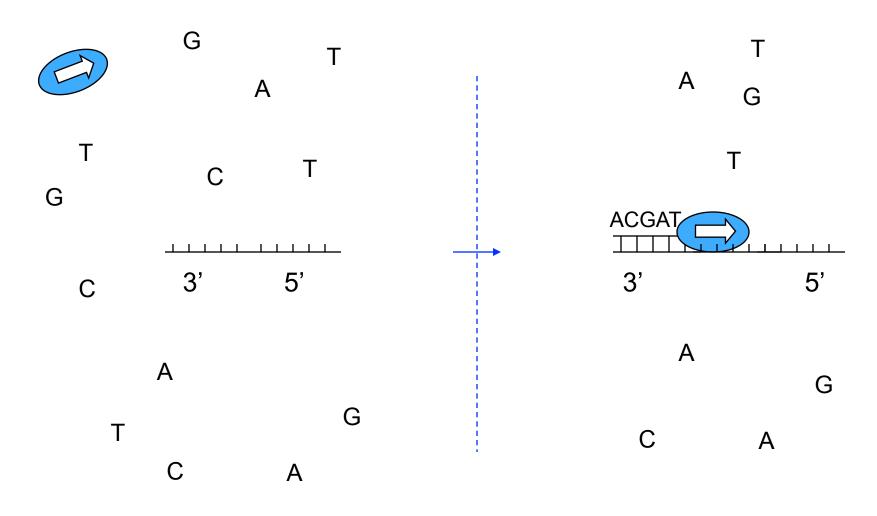


All n! permutations of the original data equally likely: A specific element will be last with prob 1/n; given that, a specific other element will be next-to-last with prob 1/(n-1), ...; overall: 1/(n!)

Weekly Bio Interlude

DNA Replication

DNA Replication: Basics

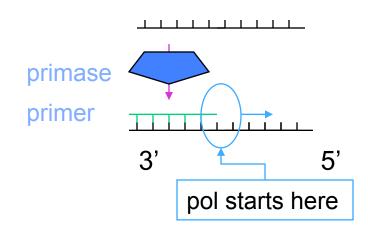


Issues & Complications, I

1st ~10 nt's added are called the *primer*In simple model, DNA pol has 2 jobs: prime & extend

Priming is error-prone

So, specialized *primase* does the priming; pol specialized for fast, accurate extension



Still doesn't solve the accuracy problem (hint: primase makes an *RNA* primer)

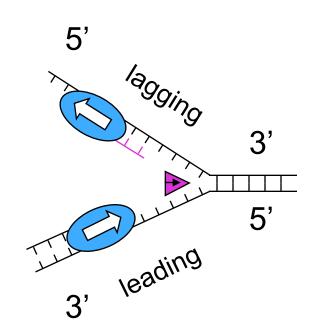
Issue 2: Rep Forks & Helices

"Replication Fork": DNA double helix is progressively unwound by a DNA helicase, and both resulting single strands are duplicated

DNA polymerase synthesizes new strand 5' -> 3'(reading its template strand 3' -> 5')

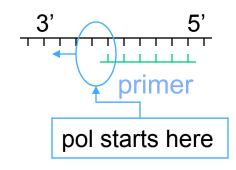
That means on one (the "leading") strand, DNA pol is chasing/pushing the replication fork

But on the other "lagging" strand, DNA pol is running away from it.



Issue 3: Fragments

Lagging strand gets a series of "Okazaki fragments" of DNA (~200nt in eukaryotes) following each primer



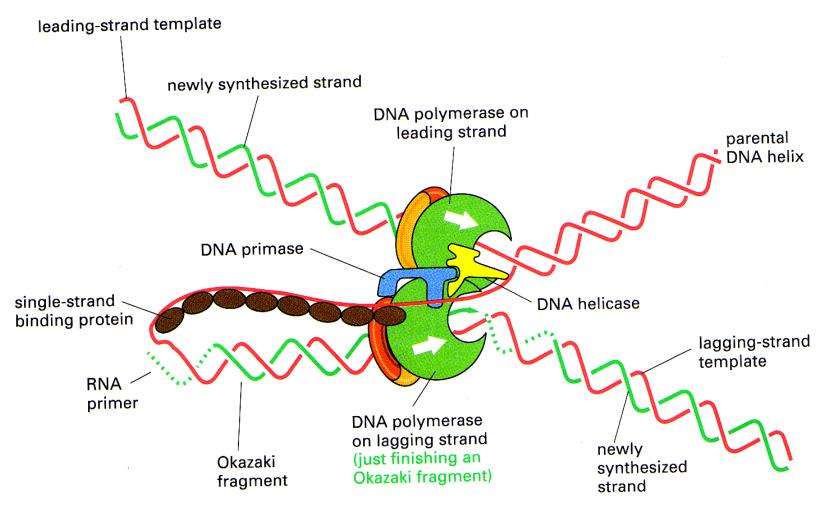
The RNA primers are later removed by a nuclease and DNA pol



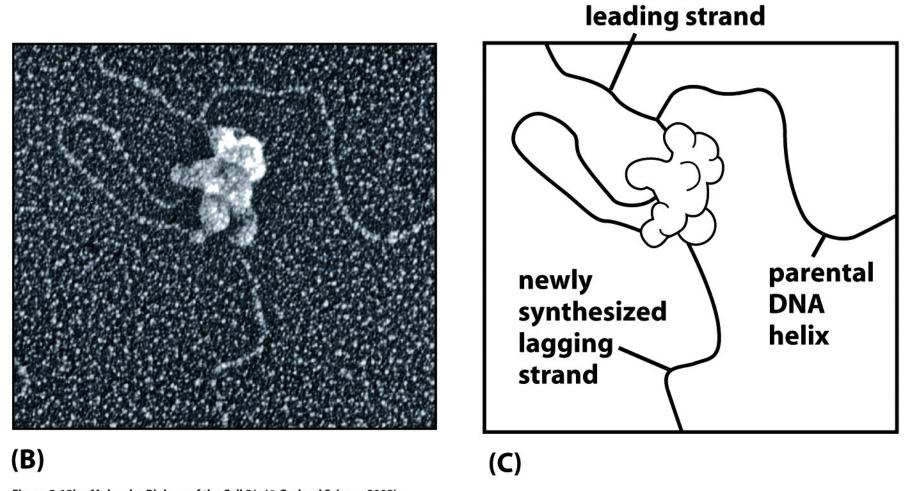
fills gaps (more accurate than primase; primed by *DNA* from adjacent Okazaki frag

Fragments joined by ligase

Issue 4: Coord of Leading/Lagging



Alberts et al., Mol. Biol. of the Cell, 3rd ed, p258



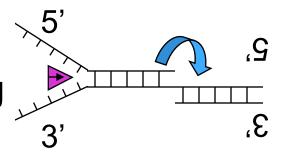
newly synthesized

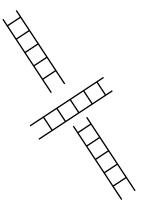
Figure 5-19bc Molecular Biology of the Cell 5/e (© Garland Science 2008)

Issue 5: Twirls & Tangles

Unwinding helix (~10 nucleotides per turn) would cause stress. Topoisomerase I cuts DNA backbone on one strand, allowing it to spin about the remaining bond, relieving stress

Topoisomerase II can cut & rejoin both strands, after allowing another double strand to pass through the gap, de-tangling it.





Issue 6: Proofreading

- Error rate of pol itself is ~10⁻⁴, but overall rate is 10⁻⁹, due to proofreading & repair, e.g.
 - pol itself can back up & cut off a mismatched base if one happens to be inserted
 - priming the new strand is hard to do accurately, hence RNA primers, later removed & replaced
 - other enzymes scan helix for "bulges" caused by base mismatch, figure out which strand is original, cut away new (faulty) copy; DNA pol fills gap
 - which strand is original? Bacteria: "methylate" some A's, eventually. Euks: strand nicking

Replication Summary

Speed: 50 (eukaryotes) to 500 (prokaryotes) bp/sec
Accuracy: 1 error per 10⁹ bp
Complex & highly optimized
Highly similar across all living cells

More info: Alberts et al., *Mol. Biol. of the Cell*

Sequence Alignment

Part II
Local alignments & gaps

Variations

Local Alignment

- Preceding gives *global* alignment, i.e. full length of both strings;
- Might well miss strong similarity of part of strings amidst dissimilar flanks

Gap Penalties

10 adjacent spaces cost 10 x one space?

Many others

Similarly fast DP algs often possible

Variations

Local Alignment

Preceding gives *global* alignment, i.e. full length of both strings;

Might well miss strong similarity of part of strings amidst dissimilar flanks

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10 adjacent spaces cost 10 x one space?

Many others

Similarly fast DP algs often possible

Local Alignment: Motivations

"Interesting" (evolutionarily conserved, functionally related) segments may be a small part of the whole

"Active site" of a protein

Scattered genes or exons amidst "junk", e.g. retroviral insertions, large deletions

Don't have whole sequence

Global alignment might miss them if flanking junk outweighs similar regions

Local Alignment

Optimal *local alignment* of strings S & T: Find substrings A of S and B of T having max value global alignment

$$S = abcxdex$$
 $A = c x d e$

$$T = xxxcde$$
 $B = c - d e$ value = 5

Local Alignment: "Obvious" Algorithm

for all substrings A of S and B of T: Align A & B via dynamic programming Retain pair with max value end;

Output the retained pair

Time: O(n²) choices for A, O(m²) for B, O(nm) for DP, so O(n³m³) total.

[Best possible? Lots of redundant work...]

Local Alignment in O(nm) via Dynamic Programming

```
Input: S, T, |S| = n, |T| = m
Output: value of optimal local alignment
Better to solve a "harder" problem
for all 0 \le i \le n, 0 \le j \le m:
 V(i,j) = \max_{i} value of opt (global)
     alignment of a suffix of S[1], ..., S[i]
     with a suffix of T[1], ..., T[j]
 Report best i,j
```

Base Cases

Assume $\sigma(x,-) \le 0$, $\sigma(-,x) \le 0$

V(i,0): some suffix of first i chars of S; all match spaces in T; best suffix is empty

$$V(i,0) = 0$$

V(0,j): similar

$$V(0,j) = 0$$

General Case Recurrences

Opt suffix align S[1], ..., S[i] vs T[1], ..., T[j]:

$$\begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim T[j] \end{bmatrix}, \quad \begin{bmatrix} \sim \sim \sim S[i] \\ \sim \sim \sim - \end{bmatrix}, \quad \begin{bmatrix} \sim \sim \sim - \\ \sim \sim \sim T[j] \end{bmatrix}, \quad \text{or} \quad \begin{bmatrix} \\ \end{bmatrix}$$

Opt align of suffix of $S_1...S_{i-1} & V(i,j) = \max \begin{cases} V(i-1,j-1) + \sigma(S[i],T[j]) \\ V(i-1,j) + \sigma(S[i],-) \\ V(i,j-1) + \sigma(-,T[j]) \end{cases}$ opt suffix alignment has: 2,1,1,0 chars of 3/T

for all $1 \le i \le n$, $1 \le j \le m$.

Scoring Local Alignments

	j	0	1	2	3	4	5	6	
i			X	X	X	С	d	е	←T
0		0	0	0	0	0	0	0	
1	a	0							
2	b	0							
3	С	0							
4	X	0							
5	d	0							
6	е	0							
7	X	0							

Finding Local Alignments

Again, arrows follow max

	j	0	1	2	3	4	5	6
i			X	X	X	С	d	е
0		0	0	0	0	0	0	0
1	a	0	0	0	0	0	0	0
2	b	0	0	0	0	0	0	0
3	С	0	0	0	0	2	1	0
4	X	0	2	2	2		1	0
5	d	0	1	1	1	1	3	2
6	е	0	0	0	0	0	2	5
7	X	0	2	2	2	1	1	4

←T

Notes

Time and Space = O(mn)

Space O(min(m,n)) possible with time
O(mn), but finding alignment is trickier

Local alignment: "Smith-Waterman"

Global alignment: "Needleman-Wunsch"

Sequence Evolution

"Nothing in Biology Makes Sense Except in the Light of Evolution" – Theodosius Dobzhansky, 1973

Changes happen at random

Deleterious/neutral/advantageous changes unlikely/ possibly/likely spread widely in a population

Changes are less likely to be tolerated in positions involved in many/close interactions, e.g.

enzyme binding pocket protein/protein interaction surface

. . .

Alignment With Gap Penalties

Gap: maximal run of spaces in S' or T'

```
ab--ddc-d
```

2 gaps in S'

1 gap in T'

(NB: KT treats "gap" and "-" as synonyms)

Motivations, e.g.:

mutation might insert/delete several or even many residues at once

matching mRNA (no introns) to genomic DNA (exons and introns)

some parts of proteins less critical

Alignment With Gap Penalties

Gap: maximal run of spaces in S' or T'

```
ab--ddc-d 2 gaps in S'
```

a---ddcbd 1 gap in T'

Motivations, e.g.:

mutation might insert/delete several or even many residues at once

matching mRNA (no introns) to genomic DNA (exons and introns)

some parts of proteins less critical

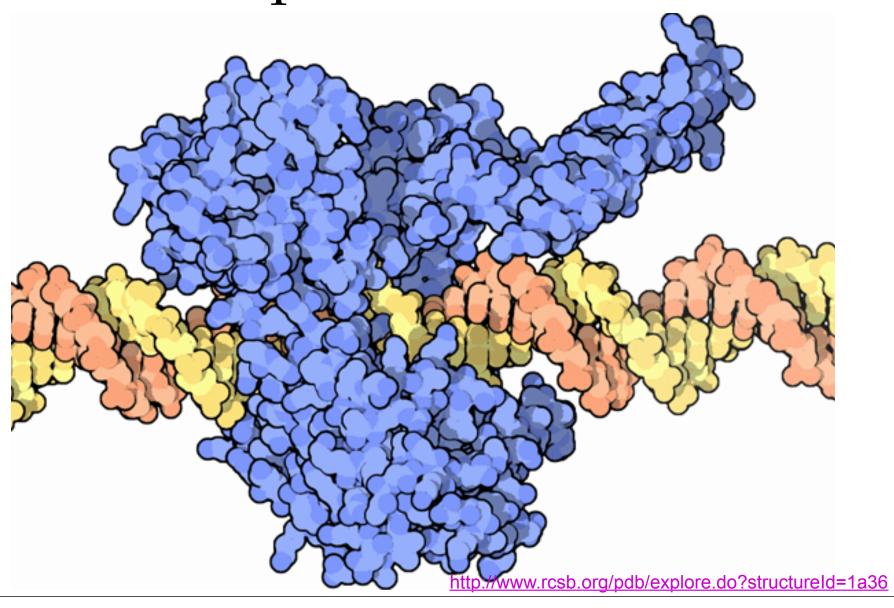
A Protein Structure: (Dihydrofolate Reductase)



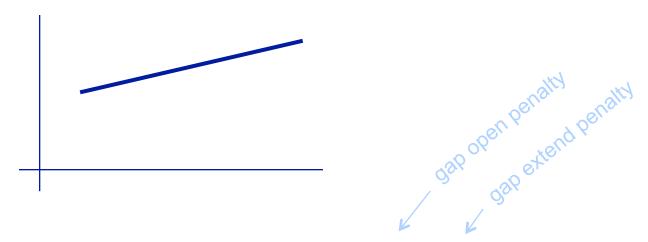
Alignment of 5 Dihydrofolate reductase proteins

mouse human chicken fly yeast	P00375 P00374 P00378 P17719 P07807	MVRPLNCIVAVSQNMGIGKNGDLPWPPLRNEFKYFQRMTTTSSVEGKQNLVIMGRKMVGSLNCIVAVSQNMGIGKNGDLPWPPLRNEFRYFQRMTTTSSVEGKQNLVIMGKKVRSLNSIVAVCQNMGIGKDGNLPWPPLRNEYKYFQRMTSTSHVEGKQNAVIMGKKMLR-FNLIVAVCENFGIGIRGDLPWR-IKSELKYFSRTTKRTSDPTKQNAVVMGRK MAGGKIPIVGIVACLQPEMGIGFRGGLPWR-LPSEMKYFRQVTSLTKDPNKKNALIMGRK : :::*** *:**:**:**:**:**:**:**:**:**:**
	P00375	TWFSIPEKNRPLKDRINIVLSRELKEP <mark></mark> PRGAHFLAKSLDDALRLIEQPELASKVDM
	P00374	TWFSIPEKNRPLKGRINLVLSRELKEP <mark></mark> PQGAHFLSRSLDDALKLTEQPELANKVDM
	P00378	TWFSIPEKNRPLKDRINIVLSRELKEA <mark></mark> PKGAHYLSKSLDDALALLDSPELKSKVDM
	P17719	TYFGVPESKRPLPDRLNIVLSTTLQESDL <mark></mark> PKG <mark>-</mark> VLLCPNLETAMKILEE <mark></mark> QNEVEN
	P07807	TWESIPPKFRPLPNRMNVIISRSFKDDFVHDKERSIVQSNSLANAIMNLESN-FKEHLER
		: .: . *** . *:*
	P00375	VWIVGGSSVYQEAMNQPGHLRLFVTRIMQEFESDTFFPEIDLGKYKLLPEYPG <mark></mark>
	P00374	VWIVGGSSVYKEAMNHPGHLKLFVTRIMQDFESDTFFPEIDLEKYKLLPEYPG <mark></mark>
	P00378	VWIVGGTAVYKAAMEKPINHRLFVTRILHEFESDTFFPEIDYKDFKLLTEYPG <mark></mark>
	P17719	IWIVGGSGVYEEAMASPRCHRLYITKIMQKFDCDTFFPAIP <mark>-</mark> DSFREVAPDSD <mark></mark>
	P07807	IYVIGGGEVYSQIFSITDHWLITKINPLDKNATPAMDTFLDAKKLEEVFSEQDPAQLKEF
	P00375	VLSEVQEEKGIKYKFEVYEKKD CLUSTAL W (1.82) multiple
	P00374	VLSDVO <mark></mark> EEKGIKYKFEVYEKND <mark> sequence alignment</mark>
	P00378	VPADIQEEDGIQYKFEVYQKSVLAQ http://pir.georgetown.edu/
	P17719	MPLGVQ EENGIKFEYKILEKHS CGi-bin/multialn.pl
	P07807	LPPKVELPETDCDQRYSLEEKGYCFEFTLYNRK 2/11/2013
		• •• ** * ••• • •

Topoisomerase I



Affine Gap Penalties



Gap penalty = $g + e^*(gaplen-1)$, $g \ge e \ge 0$

Note: no longer suffices to know just the *score* of best subproblem(s) – *state* matters: do they end with '-' or not.

Global Alignment with Affine Gap Penalties

Time: O(mn) [calculate all, O(1) each]

Affine Gap Algorithm

Gap penalty = $g + e^*(gaplen-1)$, $g \ge e \ge 0$

$$V(i,0) = E(i,0) = V(0,i) = F(0,i) = -g-(i-1)*e$$

$$V(i,j) = max(G(i,j), F(i,j), E(i,j))$$

$$G(i,j) = V(i-1,j-1) + \sigma(S[i],T[j])$$

$$F(i,j) = max(F(i-1,j)-e, V(i-1,j)-g)$$

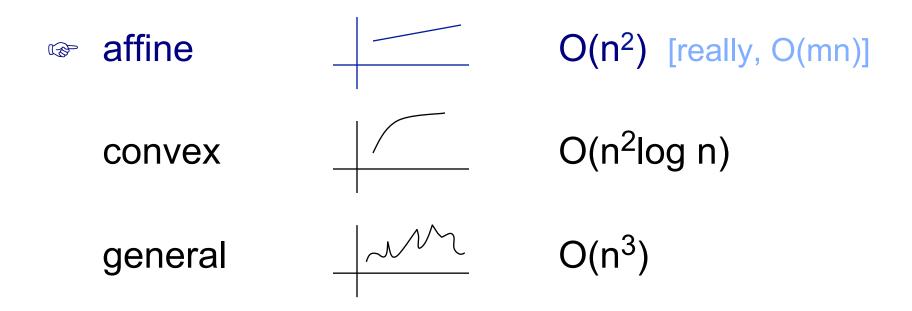
$$E(i,j) = max(E(i,j-1)-e, V(i,j-1)-g)$$

S Т x/_ x/-Χ Χ Χ old gap new gap

Q. Why is the "V" case a "new gap" when V includes E & F?

Other Gap Penalties

Score = f(gap length)
Kinds, & best known alignment time



Summary: Alignment

- Functionally similar proteins/DNA often have recognizably similar sequences even after eons of divergent evolution
- Ability to find/compare/experiment with "same" sequence in other organisms is a huge win
- Surprisingly simple scoring works well in practice: score positions separately & add, usually w/ fancier gap model like affine
- Simple dynamic programming algorithms can find *optimal* alignments under these assumptions in poly time (product of sequence lengths)
- This, and heuristic approximations to it like BLAST, are workhorse tools in molecular biology

Summary: Dynamic Programming

Keys to D.P. are to

- a) identify the subproblems (usually repeated/overlapping)
- b) solve them in a careful order so all small ones solved before they are needed by the bigger ones, and
- c) build table with solutions to the smaller ones so bigger ones just need to do table lookups (*no* recursion, despite recursive formulation implicit in (a))
- d) Implicitly, optimal solution to whole problem devolves to optimal solutions to subproblems

A really important algorithm design paradigm

Seminars

CSE 590C

"Reading and Research in Computational Biology"

Mondays, 3:30-4:30ish, EEB 026

http://www.cs.washington.edu/590c

GENOME 521

"COMBI"

Wednesdays, 1:30-2:50 Foege S060

http://www.gs.washington.edu/news/combi.htm