## CSE P 590 A

## Markov Models and Hidden Markov Models


http://upload.wikimedia.org/wikipedia/commons/b/ba/Calico_cat

## Dosage Compensation and $X$-Inactivation

2 copies (mom/dad) of each chromosome I-23
Mostly, both copies of each gene are expressed
E.g., A B O blood group defined by 2 alleles of I gene

Women ( XX ) get double dose of $X$ genes (vs XY )?
So, early in embryogenesis:

- One $X$ randomly inactivated in each cell
- Choice maintained in daughter cells

Calico: a major coat color gene is on $X$

## Reminder: Proteins "Read" DNA



## Down in the Groove

Different patterns of hydrophobic methyls, potential H bonds, etc. at edges of different base pairs. They're accessible, esp. in major groove


Figure 7-7 Molecular Biology of the Cell 5/e (© Garland Science 2008)

## DNA Methylation

CpG - 2 adjacent nts, same strand (not Watson-Crick pair; " $p$ " mnemonic for the phosphodiester bond of the DNA backbone)

cytosine


Figure 7-7 Molecular Biology of the Cell 5/e (© Garland Science 2008)

## DNA Methylation-Why

In vertebrates, it generally silences transcription
(Epigenetics) X -inactivation, imprinting, repression of mobile elements, cancers, aging, and developmental differentiation
E.g., if a stem cell divides, one daughter fated
to be liver, other kidney, need to

(a) turn off liver genes in kidney \& vice versa,
(b) remember that through subsequent divisions

How? One way:
(a) Methylate genes, esp. promoters, to silence them
(b) after $\div$, DNA methyltransferases convert hemi- to fully-methylated (\& deletion of methyltransferase is embrionic-lethal in mice)
Major exception: promoters of housekeeping genes

## "CpG Islands"

Methyl-C mutates to T relatively easily
Net: CpG is less common than expected genome-wide:

$$
f(C p G)<f(C) * f(G)
$$


cytosine

thymine

## CpG Islands

## CpG Islands

More CpG than elsewhere (say, $\mathrm{CpG} / \mathrm{GpC}>50 \%$ )
More C \& G than elsewhere, too (say, C+G>50\%)
Typical length: few 100 to few 1000 bp
Questions
Is a short sequence (say, 200 bp ) a CpG island or not?
Given long sequence (say, IO-IO0kb), find CpG islands?

## Markov \& Hidden Markov Models

References (see also online reading page):
Eddy, "What is a hidden Markov model?" Nature Biotechnology, 22, \#I0 (2004) I3I5-6.
Durbin, Eddy, Krogh and Mitchison, "Biological Sequence Analysis", Cambridge, 1998 (esp. chs 3, 5)
Rabiner, "A Tutorial on Hidden Markov Models and Selected Application in Speech Recognition," Proceedings of the IEEE, v 77 \#2,Feb 1989, 257-286

## Independence

A key issue: Previous models we've talked about assume independence of nucleotides in different positions - definitely unrealistic.

## Markov Chains

A sequence $x_{1}, x_{2}, \ldots$ of random variables is a $k$-th order Markov chain if, for all $i, i^{\text {th }}$ value is independent of all but the previous $k$ values:

$$
P\left(x_{i} \mid \underset{\text { i-i }}{x_{1}, x_{2}, \ldots, x_{i-1}} \longleftrightarrow \stackrel{L}{\longleftrightarrow}\right)=P\left(x_{i} \mid \underset{\text { k typically }<\mathrm{i}-1}{x_{i-k}, x_{i-k+1}, \ldots, x_{i-1}}\right)
$$

Example I: Uniform random ACGT
Example 2: Weight matrix model
Example 3: ACGT, but $\downarrow \operatorname{Pr}($ G following C)


## A Markov Model (Ist order)



States: A,C,G,T
Emissions: corresponding letter
Transitions: $a_{s t}=P\left(x_{i}=t \mid x_{i-1}=s\right) \longleftarrow$ Ist order

## A Markov Model (Ist order)



States: A,C,G,T
Emissions: corresponding letter
Transitions: $a_{s t}=P\left(x_{i}=t \mid x_{i-1}=s\right)$ Begin/End states

## Pr of emitting sequence $x$

$$
\begin{aligned}
& x \quad=x_{1} x_{2} \ldots x_{n}
\end{aligned}
$$

$$
\begin{aligned}
& =P\left(x_{1}\right) \cdot P\left(x_{2} \mid x_{1}\right) \cdots P\left(x_{n} \mid x_{n-1}, \ldots, x_{1}\right) \\
& \left.=P\left(x_{1}\right) \cdot P\left(x_{2} \mid x_{1}\right) \cdots P\left(x_{n} \mid x_{n-1}\right)\right\rangle_{\text {if } 1 \text { ster }^{t} M C}^{\text {order }} \\
& =P\left(x_{1}\right) \prod_{i=1}^{n-1} a_{x_{i}, x_{i+1}} \\
& =\prod_{i=0}^{n-1} a_{x_{i}, x_{i+1}} \quad \text { (with Begin state) }
\end{aligned}
$$

## Training

Max likelihood estimates for transition probabilities are just the frequencies of transitions when emitting the training sequences
E.g., from 48 CpG islands in 60 kbp :

| + | A | C | G | T | - | A | C | G | T |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 0.180 | 0.274 | 0.426 | 0.120 | A | 0.300 | 0.205 | 0.285 | 0.210 |
| C | 0.171 | 0.368 | 0.274 | 0.188 | C | 0.322 | 0.298 | 0.078 | 0.302 |
| G | 0.161 | 0.339 | 0.375 | 0.125 | G | 0.248 | 0.246 | 0.298 | 0.208 |
| T | 0.079 | 0.355 | 0.384 | 0.182 | T | 0.177 | 0.239 | 0.292 | 0.292 |

## Discrimination/Classification

Log likelihood ratio of $\mathrm{CpG}_{\mathrm{p}}$ model vs background model

## CpG Island Scores



Figure 3.2 Histogram of length-normalized scores.

# What does a 2nd order Markov Model look like? 

3rd order?

## Questions

Q1: Given a short sequence, is it more likely from feature model or background model? Above
Q2: Given a long sequence, where are the features in it (if any)

Approach I: score 100 bp (e.g.) windows
Pro: simple
Con: arbitrary, fixed length, inflexible
Approach 2: combine $+/$ models.

## Combined Model



Emphasis is "Which (hidden) state?" not "Which model?"

## Hidden Markov Models (HMMs; Claude Shannon, I948)

States:
Paths:
Transitions:
Emissions:
Observed data: emission sequence
Hidden data: state/transition sequence

## The Occasionally Dishonest Casino

1 fair die, 1 "loaded" die, occasionally swapped


| Rolls |  |
| :---: | :---: |
| Die | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLLLLL |
| Viterbi | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLL |
| Rolls | 651166453132651245636664631636663162326455236266666625151631 |
| Die | LLLLLLFFFFFFFFFFFFLLLLLLLLLLLLLLLLFFFLLLLLLLLLLLLLLFFFFFFFFF |
| Viterbi | LLLLLLFFFFFFFFFFFFLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLFFFFFFFF |
| Rolls | 222555441666566563564324364131513465146353411126414626253356 |
| Die | FFFFFFFFLLLLLLLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLL |
| Viterbi | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFL |
| Rolls | 366163666466232534413661661163252562462255265252266435353336 |
| Die | LLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF |
| Viterbi | LLLLLLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF |
| Rolls | 233121625364414432335163243633665562466662632666612355245242 |
| Die | FFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLLLLLLLLLLLLEFFFFFFFFFF |
| Fite |  |

## Figure 3.5

Rolls: Visible data-300 rolls of a die as described above.
Die: Hidden data-which die was actually used for that roll ( $F=$ fair, $L=$ loaded). Viterbi: the prediction by the Viterbi algorithm is shown.

## Inferring hidden stuff

Joint probability of a given path $\pi \&$ emission sequence $x$ :

$$
P(x, \pi)=a_{0, \pi_{1}} \prod_{i=1}^{n} e_{\pi_{i}}\left(x_{i}\right) \cdot a_{\pi_{i}, \pi_{i+1}}
$$

But $\pi$ is hidden; what to do? Some alternatives:
Most probable single path

$$
\pi^{*}=\arg \max _{\pi} P(x, \pi)
$$

Sequence of most probable states

$$
\hat{\pi}_{i}=\arg \max _{k} P\left(\pi_{i}=k \mid x\right)
$$

Etc.

## The Viterbi Algorithm: The most probable path

Viterbi finds: $\quad \pi^{*}=\arg \max _{\pi} P(x, \pi)$
Possibly there are $10^{99}$ paths of prob $10^{-99}$ (If so, non-Viterbi approaches may be preferable.)
More commonly, one path (+ slight variants) dominate others; Viterbi finds that

Key problem: exponentially many paths $\pi$

## Unrolling an HMM



Conceptually, sometimes convenient
Note exponentially many paths

## Viterbi

$v_{l}(i)=$ probability of the most probable path emitting $x_{1}, x_{2}, \ldots, x_{i}$ and ending in state $l$

Initialize:
$v_{l}(0)= \begin{cases}1 & \text { if } l=B \text { egin state } \\ 0 & \text { otherwise }\end{cases}$
(1) ${ }^{1} \cdot .$.


General case:
$v_{l}(i+1)=e_{l}\left(x_{i+1}\right) \cdot \max _{k}\left(v_{k}(i) a_{k, l}\right)$


## HMM Casino Example


(Excel spreadsheet on web; download \& play...)

## HMM Casino Example


(Excel spreadsheet on web; download \& play...)

## Viterbi Traceback

Above finds probability of best path
To find the path itself, trace backward to the state $k$ attaining the max at each stage


| Rolls |  |
| :---: | :---: |
| Die | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLLLLL |
| Viterbi | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLL |
| Rolls | 651166453132651245636664631636663162326455236266666625151631 |
| Die | LLLLLLFFFFFFFFFFFFLLLLLLLLLLLLLLLLFFFLLLLLLLLLLLLLLFFFFFFFFF |
| Viterbi | LLLLLLFFFFFFFFFFFFLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLFFFFFFFF |
| Rolls | 222555441666566563564324364131513465146353411126414626253356 |
| Die | FFFFFFFFLLLLLLLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLL |
| Viterbi | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFL |
| Rolls | 366163666466232534413661661163252562462255265252266435353336 |
| Die | LLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF |
| Viterbi | LLLLLLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF |
| Rolls | 233121625364414432335163243633665562466662632666612355245242 |
| Die | FFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLLLLLLLLLLLLEFFFFFFFFFF |
| Fite |  |

## Figure 3.5

Rolls: Visible data-300 rolls of a die as described above.
Die: Hidden data-which die was actually used for that roll ( $F=$ fair, $L=$ loaded). Viterbi: the prediction by the Viterbi algorithm is shown.

## Most probable path $\neq$ Sequence of most probable states

Another example, based on casino dice again
Suppose p(fair $\leftrightarrow$ loaded) transitions are $10^{-99}$ and roll sequence is IIIII...66666; then fair state is more likely all through I's \& well into the run of 6 's, but eventually loaded wins, and the improbable $\mathrm{F} \rightarrow \mathrm{L}$ transitions make Viterbi $=$ all L .


$$
\begin{aligned}
* & =\text { max prob } \\
\square & =\text { Viterbi }
\end{aligned}
$$

## Is Viterbi "best"?

Viterbi finds $\pi^{*}=\arg \max _{\pi} P(x, \pi)$


Most probable (Viterbi) path goes through 5, but most probable state at 2 nd step is 6 (l.e., Viterbi is not the only interesting answer.)

## An HMM (unrolled)



Emissions/sequence positions $\longrightarrow$

## Viterbi: best path to each state



Viterbi score:
Viterbi path ${ }^{R}$ :

$$
v_{l}(i+1)=e_{l}\left(x_{i+1}\right) \cdot \max _{k}\left(v_{k}(i) a_{k, l}\right)
$$

$$
\operatorname{back}_{l}(i+1)=\arg \max _{k}\left(v_{k}(i) a_{k, l}\right)
$$

## The Forward Algorithm

For each state/time, want total probability of all paths leading to it, with given emissions


$$
\begin{aligned}
f_{k}(i) & \triangleq P\left(x_{1} \ldots x_{i}, \pi_{i}=k\right) \\
f_{l}(i+1) & =e_{l}\left(x_{i+1}\right) \sum_{k} f_{k}(i) a_{k, l} \\
P(x) & =\sum_{\pi} P(x, \pi)=\sum_{k} f_{k}(n) a_{k, 0}
\end{aligned}
$$

## The Backward Algorithm

Similar: for each state/time, want total probability of all paths from it, with given emissions, conditional on that state.


## In state $k$ at step $i$ ?

$$
\begin{aligned}
& P\left(x, \pi_{i}=k\right) \\
& \quad=P\left(x_{1}, \ldots, x_{i}, \pi_{i}=k\right) \cdot P\left(x_{i+1}, \ldots, x_{n} \mid x_{1}, \ldots, x_{i}, \pi_{i}=k\right) \\
& \quad=P\left(x_{1}, \ldots, x_{i}, \pi_{i}=k\right) \cdot P\left(x_{i+1}, \ldots, x_{n} \mid \pi_{i}=k\right) \\
& \quad=f_{k}(i) \cdot b_{k}(i) \\
& P\left(\pi_{i}=k \mid x\right)=\frac{P\left(x, \pi_{i}=k\right)}{P(x)}=\frac{f_{k}(i) \cdot b_{k}(i)}{P(x)}
\end{aligned}
$$

## Posterior Decoding,

Alternative 1: what's the most likely state at step i?

$$
\hat{\pi}_{i}=\arg \max _{k} P\left(\pi_{i}=k \mid x\right)
$$

Note: the sequence of most likely states $\neq$ the most likely sequence of states. May not even be legal!


## The Occasionally Dishonest Casino

1 fair die, 1 "loaded" die, occasionally swapped


| Rolls |  |
| :---: | :---: |
| Die | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLLLLL |
| Viterbi | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLL |
| Rolls | 651166453132651245636664631636663162326455236266666625151631 |
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| Viterbi | LLLLLLFFFFFFFFFFFFLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLLFFFFFFFF |
| Rolls | 222555441666566563564324364131513465146353411126414626253356 |
| Die | FFFFFFFFLLLLLLLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFLL |
| Viterbi | FFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFL |
| Rolls | 366163666466232534413661661163252562462255265252266435353336 |
| Die | LLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF |
| Viterbi | LLLLLLLLLLLLFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFFF |
| Rolls | 233121625364414432335163243633665562466662632666612355245242 |
| Die | FFFFFFFFFFFFFFFFFFFFFFFFFFFLLLLLLLLLLLLLLLLLLLLLLEFFFFFFFFFF |
| Fite |  |

## Figure 3.5

Rolls: Visible data-300 rolls of a die as described above.
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## Posterior Decoding



Figure 3.6 The posterior probability of being in the state corresponding to the fair die in the casino example. The $x$ axis shows the number of the roll. The shaded areas show when the roll was generated by the loaded die.

## Posterior Decoding, II

Alternative 1: what's most likely state at step $i$ ?

$$
\hat{\pi}_{i}=\arg \max _{k} P\left(\pi_{i}=k \mid x\right)
$$

Alternative 2: given some function $g(k)$ on states, what's its expectation. E.g., what's probability of " + " model in CpG HMM ( $g(k)=1$ iff $k$ is " + " state)?

$$
G(i \mid x)=\sum_{k} P\left(\pi_{i}=k \mid x\right) \cdot g(k)
$$

## CpG Islands again

Data: 4 I human sequences, totaling 60 kbp , including 48 CpG islands of about Ikbp each

Viterbi:
Found 46 of 48
plus I2I "false positives"
Posterior Decoding: same 2 false negatives plus 236 false positives

Post-process: 46/48
67 false pos

46/48
83 false pos

Post-process: merge within
500; discard < 500

## Training

Given model topology \& training sequences, learn transition and emission probabilities

If $\pi$ known, then MLE is just frequency observed in training data

$$
\begin{array}{ll}
a_{k, l} & =\quad \frac{\text { count of } k \rightarrow l \text { transitions }}{\text { count of } k \rightarrow \text { anywhere transitions }} \\
e_{k}(b) & =\ldots
\end{array}
$$

If $\pi$ hidden, then use EM :
given $\pi$, estimate $\theta$; given $\theta$ estimate $\pi$; repeat $\}^{2}$ ways

## Viterbi Training <br> given $\pi$, estimate $\theta$; given $\theta$ estimate $\pi$; repeat

Make initial estimates of parameters $\theta$
Find Viterbi path $\pi$ for each training sequence
Count transitions/emissions on those paths, getting new $\theta$
Repeat
Not rigorously optimizing desired likelihood, but still useful \& commonly used.
(Arguably good if you're doing Viterbi decoding.)

## Baum-Welch Training namems backward alg"

EM: given $\theta$, estimate $\pi$ ensemble; then re-estimate $\theta$

$$
\begin{aligned}
& P\left(\pi_{i}=k, \pi_{i+1}=l \mid x, \theta\right) \\
& \quad=\frac{f_{k}(i \mid \theta) a_{k, l} e_{l}\left(x_{i+1}\right) b_{l}(i+1 \mid \theta)}{P(x \mid \theta)}
\end{aligned}
$$

Estimated \# of $k \rightarrow l$ transitions $\hat{A}_{k, l}$

$$
=\sum_{\text {training seqs } x^{j}} \sum_{i} P\left(\pi_{i}=k, \pi_{i+1}=l \mid x^{j}, \theta\right)
$$

New estimate $\hat{a}_{k, l}=\frac{\hat{A}_{k, l}}{\sum_{l} \hat{A}_{k, l}}$
Emissions: similar


Log-odds (vs all F) per roll True model 0.101 bits 300-roll est. 0.097 bits 30k-roll est. 0.100 bits (NB: overestimated)


B-W Learned Model


From DEKM

## HMMs in Action: Pfam http://pfam.sanger.ac.uk/

Proteins fall into families, both across \& within species
Ex: Globins, GPCRs, Zinc fingers, Leucine zippers,...
Identifying family very useful: suggests function, etc.

So, search \& alignment are both important One very successful approach: profile HMMs

Helix HBA_HUMAN HBB_HUMAN MYG_PHYCA GLB3_CHITP GLB5_PETMA LGB2_LUPLU GLB1_GLYDI Consensus

Helix
HBA_HUMAN HBB_HUMAN MYG_PHYCA GLB3_CHITP GLB5_PETMA LGB2__LUPLU GLB1_GLYDI Consensus

Helix
HBA_HUMAN HBB__HUMAN MYG_PHYCA GLB3_CHITP GLB5_PETMA LGB2_LUPLU GLB1_GLYDI Consensus

AAAAAAAAAAAAAAAA BBBBBBBBBBBBBBBBCCCCCCCCCCC ----------VLSPADKTNVKAAWGKVGA--HAGEYGAEALERMFLSFPTTKTYFPHF
---------VHLTPEEKSAVTALWGKV----NVDEVGGEALGRLLVVYPWTQRFFESF
---------VLSEGEWQLVLHVWAKVEA--DVAGHGQDILIRLFKSHPETLEKFDRF
----------LSADQISTVQASFDKVKG------DPVGILYAVFKADPSIMAKFTQF PIVDTGSVAPLSAAEKTKIRSAWAPVYS--TYETSGVDILVKFFTSTPAAQEFFPKF -------GALTESQAALVKSSWEEFNA--NIPKHTHRFFILVLEIAPAAKDLFS-F ---------GLSAAQRQVIAATWKDIAGADNGAGVGKDCLIKFLSAHPQMAAVFG-F Ls... v a W kv . . g . L. . f. P . F F

DDDDDDDEEEEEEEEEEEEEEEEEEEEE
FFFFFFFFFFFF -DLS-----HGSAQVKGHGKKVADALTNAVAHV---D--DMPNALSALSDLHAHKL-GDLSTPDAVMGNPKVKAHGKKVLGAFSDGLAHL---D--NLKGTFATLSELHCDKL-KHLKTEAEMKASEDLKKHGVTVLTALGAILKK----K-GHHEAELKPLAQSHATKH-AG-KDLESIKGTAPFETHANRIVGFFSKIIGEL--P---NIEADVNTFVASHKPRG-K̈GLTTADQLKKSADVRWHAERIINAVNDAVASM--DDTEKMSMKLRDLSGKHAKSF-LK-GTSEVPQNNPELQAHAGKVFKLVYEAAIQLQVTGVVVTDATLKNLGSVHVSKG-SG----AS---DPGVAALGAKVLAQIGVAVSHL--GDEGKMVAQMKAVGVRHKGYGN
t .. . v..Hg kv. a a...l d . a 1. 1 H
FFGGGGGGGGGGGGGGGGGGG
нНннннНннннНнннннннннннннн


# Alignment of 7 globins. A-H mark 8 alpha helices. Consensus line: upper case $=6 / 7$, lower $=4 / 7$, dot $=3 / 7$. Could we have a profile (aka weight matrix) w/ indels? 

## Profile Hmm Structure



Figure 5.2 The transition structure of a profile HMM.
$\mathrm{M} \mathrm{j}: \quad$ Match states ( 20 emission probabilities)
l : $\quad$ Insert states (Background emission probabilities)
$\mathrm{D}_{\mathrm{j}}: \quad$ Delete states (silent - no emission)

## Silent States

Example: chain of states, can skip some


Problem: many parameters.
A solution: chain of "silent" states; fewer parameters (but less detailed control)


Algorithms: basically the same.

## Using Profile HMM's

## Search

Forward or Viterbi
Scoring
Log likelihood (length adjusted)
Log odds vs background
$Z$ scores from either


Alignment
Viterbi

## Likelihood vs Odds Scores




Figure 5.5 To the left the length-normalized LL score is shown as a function of sequence length. The right plot shows the same for the log-odds score.

## Z-Scores



Figure 5.6 The Z-score calculated from the LL scores (left) and the log-odds (right).

## Pfam Model Building

Hand-curated "seed" multiple alignments
Train profile HMM from seed alignment Hand-chosen score threshold(s)
Automatic classification/alignment of all other protein sequences
Pfam 25.0 (March 20II, I2273 families; covers
~75\% of human proteins)
Pfam 27.0 (March 2013, I483I families; $\approx 90 \%$ )

## Model-building refinements

Pseudocounts (count $=0$ common when training with 20 aa's)

$$
e_{i}(a)=\frac{C_{i, a}+A \cdot q_{a}}{\sum_{a} C_{i, a}+A}, \quad A \sim 20, q_{a}=\text { background }
$$

Pseudocount "mixtures", e.g. separate pseudocount vectors for various contexts (hydrophobic regions, buried regions,...)
(~10-20 training sequences)

## More refinements

Weighting: may need to down weight highly similar sequences to reflect phylogenetic or sampling biases, etc.
Match/insert assignment: Simple threshold, e.g. " $>50 \%$ gap $\Rightarrow$ insert", may be suboptimal. Can use forward-algorithm-like dynamic programming to compute max a posteriori assignment.

## Numerical Issues

Products of many probabilities $\rightarrow 0$
For Viterbi: just add logs
For forward/backward: also work with logs, but you need sums of products, so need "log-of-sum-of-product-of-exp-of-logs", e.g., by table/interpolation

Keep high precision and perhaps scale factor Working with log-odds also helps.

## Model structure

Define it as well as you can.
In principle, you can allow all transitions and hope to learn their probabilities from data, but it usually works poorly - too many local optima

# Duration Modeling 

Self-loop duration: geometric $p^{n}(1-p)$
min, then geometric

"negative binomial"


More general: possible (but slower)

## HMM Summary

Inference
Viterbi - best single path
Forward - sum over all paths
Backward - similar
Posterior decoding
Model building
Semi-supervised - typically fix architecture (e.g. profile HMM), then learn parameters
Baum-Welch - training via EM and forward/backward (aka the forward/backward algorithm)
Viterbi training - also "EM", but Viterbi-based

## HMM Summary (cont.)

Search:
Viterbi or forward
Scoring:
Odds ratio to background
Z-score
E-values, etc., too
Excellent tools available (SAM, HMMer, Pfam, ...)
A very widely used tool for biosequence analysis

## Caenorhabditis elegans



## Cell Fate /

## Differentiation



## Differentiation

Once a cell differentiates, how does it know to stay that way?
"Epigenetics"
Methylation is a large part of the story
Chromatin modification is another part

## Chromatin



Figure 4-22 Molecular Biology of the Cell 5/e (© Garland Science 2008)


side view
histone H2A $\square$ histone H2Bhistone H3 $\square$ histone H4

Figure 4-24 Molecular Biology of the Cell 5/e (© Garland Science 2008)


## Histone Codes



Figure 4-44a Molecular Biology of the Cell 5/e ( $\odot$ Garland Science 2008)
modification state


## Differentiation

Once a cell differentiates, how does it know to stay that way?
Methylation is a large part of the story
Chromatin modification is another part
Positive autoregulation of genes is another TF A turns self on (+ others) maintaining A identity
Consequences:
Can't regrow body parts (but salamanders can...)
Can't clone (easily)

## Stem Cells

Reservoirs of partially undifferentiated cells in many tissues in the body
Replenish/replace dead/damaged cells
Huge therapeutic potential
Best source? Embryonic tissue
$\Rightarrow$ ethical issues
What about cell cultures
$\Rightarrow$ many are basically tumors

## Cloning

Need to "undo" all the epigenetic marking added during differentiation, quench the feedback markers, etc.
Dolly the sheep

OCT 3/4 (Octamer binding transcription factor 3/4)
Transcription factor that binds to the octamer motif ( 5 '-ATTTGCAT-3'). Forms a trimeric complex with SOX2 on DNA and controls the expression of a number of genes involved in embryonic development such as YESI, FGF4, UTFI and ZFP206. Critical for early embryogenesis and for embryonic stem cell pluripotency.
http://www.uniprot.org/uniprot/Q01860

SOX2 (SRY-related high-mobility-group (HMG)-box protein 2)
Transcription factor that forms a trimeric complex with OCT4 on DNA and controls the expression of a number of genes involved in embryonic development such as YESI, FGF4, UTFI and ZFP206. Critical for early embryogenesis and for embryonic stem cell pluripotency
http://www.uniprot.org/uniprot/P4843I


Klf4 (kruppel-like factor 4)


Zinc-finger transcription factor. Contains 3 C 2 H 2 -type zinc fingers. May act as a transcriptional activator. Binds the CACCC core sequence. May be involved in the differentiation of epithelial cells and may also function in the development of the skeleton and kidney.
http://www.uniprot.org/uniprot/O43474

MYC (Myc proto-oncogene)
Basic helix-loop-helix transcription factor. Binds DNA both in a non-specific manner and also specifically recognizes the core sequence 5'-CAC[GA]TG-3'. Seems to activate the transcription of growth-related genes. Efficient DNA binding requires dimerization with another bHLH protein. Binds DNA as a heterodimer with MAX. Interacts with TAFIC, SPAG9, PARPI0, JARIDIA and JARIDIB.
http://www.uniprot.org/uniprot/POI IO6

## Stem Cells Again

Great recent progress in making equiv of embryonic stem cells from adult tissues

Takahashi \& Yamanaka, Cell, 2006

Key? Transfect genes for those 4 transcription factors!

## Issues

Myc is a proto-oncogene
Long term stability of derived cells with unnatural expression of these genes is unclear
Delivery: Retro virus
may do damage during integration

## Recent Progress

2007: Some other gene combinations work, without Myc

2008: Can use adenoviruses
E.g., Stadtfeld, Nagaya, Utikal, Weir, Hochedlinger, Science, Sept 2008.


Coat color pattern reflects "chimeric" animals otherwise normal, but mosaic of "induced pluripotent stem cells" \& normal cells, grown from embryonic fusion

Stadtfeld, et al.,


Ditto in brain section

