# CS-XXX: Graduate Programming Languages

## Lecture 14 — Efficient Lambda Interpreters

#### Dan Grossman 2012

## Where are we

#### Done<sup>.</sup>

- Formal definition of evaluation contexts and first-class continuations
- Continuation-passing style as a programming idiom
- The CPS transform

#### Now:

- Implement an efficent lambda-calculus interpreter using little more than malloc and a single while-loop
  - Explicit evaluation contexts (i.e., continuations) is essential
  - Key novelty is maintaining the current context incrementally
  - letcc and throw can be O(1) operations (homework problem)

### See the code

See lec14code.ml for four interpreters where each is:

- More efficient than the previous one and relies on less from the meta-language
- Close enough to the previous one that equivalence among them is tractable to prove

#### The interpreters:

- 1. Plain-old small-step with substitution
- 2. Evaluation contexts, re-decomposing at each step
- 3. Incremental decomposition, made efficient by representing evaluation contexts (i.e., continuations) as a linked list with "shallow end" of the stack at the beginning of the list

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4. Replacing substitution with environments

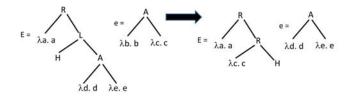
The last interpreter is trivial to port to assembly or C

## Example

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Decomposition (second interpreter):



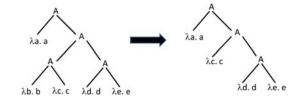
Decomposition rewritten with linked list (hole implicit at *front*):

 $c = L(A(\lambda d. d, \lambda e. e)) :: R(\lambda a. a) :: []$  $c = R(\lambda c. c) :: R(\lambda a. a) :: []$  $e = A(\lambda b. b, \lambda c. c)$ e = A(λd. d, λe. e)

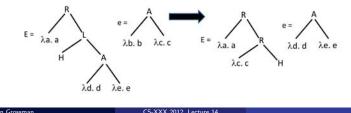
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### Example





Decomposition (second interpreter):



#### Example

Decomposition rewritten with linked list (hole implicit at *front*):

 $c = L(A(\lambda d. d, \lambda e. e)) :: R(\lambda a. a) :: []$  $e = A(\lambda b. b, \lambda c. c)$ 

 $c = R(\lambda c. c) :: R(\lambda a. a) :: []$ e = A(λd. d, λe. e)

Some loop iterations of third interpreter:

e = A(λb. b, λc. c)	$c = L(A(\lambda d. d, \lambda e. e)) :: R(\lambda a. a) :: []$
$e = \lambda b. b$	$c=L(\lambdac.\ c)::L(A(\lambdad.\ d,\lambdae.\ e))::R(\lambdaa.\ a)::[]$
e = λc. c	c = R( $\lambda$ b. b) :: L(A( $\lambda$ d. d, $\lambda$ e. e)) :: R( $\lambda$ a. a) :: []
e = λc. c	c = L(A(λd. d, λe. e)) :: R(λa. a) :: []
e = A(λd. d, λe. e)	c = R(λc. c) :: R(λa. a) :: []

Fourth interpreter: replace substitution with environment/closures CS-XXX 2012, Lecture 14

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# The end result

The last interpreter needs just:

- ► A loop
- Lists for contexts and environments
- Tag tests

Moreover:

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- Function calls execute in O(1) time
- Variable look-ups don't, but that's fixable
  (e.g., de Bruijn indices and arrays for environments)
- Other operations, including pairs, conditionals, letcc, and
  - throw also all work in O(1) time • Need new kinds of contexts and values
    - Left as a homework exercise as a way to understand the code

Making evaluation contexts explicit data structures was key

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