

# CS-XXX: Graduate Programming Languages

## Lecture 24 — Bounded Polymorphism

Dan Grossman  
2012

### Revenge of Type Variables

Sorted lists in ML (partial):

```
type 'a slist
make : ('a -> 'a -> int) -> 'a slist
cons : 'a slist -> 'a -> 'a slist
find : 'a slist -> 'a -> 'a option
```

Getting by with OOP subtyping:

```
interface Cmp { Int f(Object, Object); }
class SList {
  ... some field definitions ...
  constructor (Cmp x) {...}
  Slist cons(Object x) {...}
  Object find(Object x) {...}
}
```

Dan Grossman CS-XXX 2012, Lecture 24

2

### Wanting Type Variables

Will downcast (potential run-time exception) the arguments to `f` and the result of `find`

We are not enforcing list-element type-equality

OOP-style subtyping is no replacement for parametric polymorphism; we can have both:

```
interface Cmp<'a> { Int f('a, 'a); } // Cmp not a type
class SList<'a> { // SList not a type (SList<Int> e.g. is)
  ... some field definitions (can use type 'a) ...
  constructor (Cmp<'a> x) {...}
  Slist<'a> cons('a x) {...}
  'a find('a x) {...}
}
```

Dan Grossman

CS-XXX 2012, Lecture 24

3

### Same Old Story

- ▶ Interface and class declarations are *parameterized*; they produce types
- ▶ The constructor is polymorphic
  - ▶ For all T, given a Cmp<T>, it makes a SList<T>
- ▶ If o has type SList<T>, its cons method:
  - ▶ Takes a T
  - ▶ Returns a SList<T>

No more downcasts; the best of both worlds

Dan Grossman CS-XXX 2012, Lecture 24

4

### Complications

"Interesting" interaction with overloading and multimethods

```
class B {
  unit f(C<Int> x) {...}
  unit f(C<String> x) {...}
}
class C<'a> { unit g(B x) { x.f(self); } }
```

For C<T> where T is neither Int nor String, can have no match

- ▶ Cannot resolve static overloading at compile-time without code duplication and no abstraction (C++)
- ▶ To resolve overloading or multimethods at run-time, need run-time type information *including the instantiation T* (C#)
- ▶ Could disallow such overloading (Java)
- ▶ Or could just reject this sort of call as unresolvable (?)

Dan Grossman

CS-XXX 2012, Lecture 24

5

### Wanting bounds

There are compelling reasons to *bound* the instantiation of type variables

Simple example: Use at supertype without losing that it's a subtype

```
interface I { unit print(); }
class Logger<'a <: I> { // must apply to subtype of I
  'a item;
  'a get_it() { syslog(item.print()); item }
}
```

Without polymorphism or downcasting, client could only use `get_it` result for printing

Without bound or downcasting, Logger could not print

Issue isn't special to OOP

Dan Grossman CS-XXX 2012, Lecture 24

6

## Fancy Example from "A Theory of Objects" Abadi/Cardelli

With forethought, bounds can avoid some subtyping limitations

```
interface Omnivore { unit eat(Food); }
interface Herbivore { unit eat(Veg); } // Veg <= Food
```

Allowing  $\text{Herbivore} \leq \text{Omnivore}$  could make a vegetarian eat meat (unsound)! But this works:

```
interface Omnivore<'a <: Food> { unit eat('a); }
interface Herbivore<'a <: Veg> { unit eat('a); }
```

If  $\text{Herbivore}<\text{T}>$  is legal, then  $\text{Omnivore}<\text{T}>$  is legal *and*  $\text{Herbivore}<\text{T}> \leq \text{Omnivore}<\text{T}>$ !

Useful for unit feed('a food, Omnivore<'a> animal) {...}

## Bounded Polymorphism

This "bounded polymorphism" is useful in any language with universal types and subtyping. Instead of  $\forall \alpha.\tau$  and  $\Delta\alpha.e$ , we have  $\forall \alpha < \tau'.\tau$  and  $\Delta\alpha < \tau'.e$ :

- ▶ Change  $\Delta$  to be a list of bounds ( $\alpha < \tau$ ) instead of a set of type variables
- ▶ In  $e$  you can subsume from  $\alpha$  to  $\tau'$
- ▶  $e_1[\tau_1]$  typechecks when  $\tau_1$  "satisfies the bound" in type of  $e_1$

One limitation: When is  $(\forall \alpha_1 < \tau_1.\tau_2) \leq (\forall \alpha_2 < \tau_3.\tau_4)$ ?

- ▶ Contravariant bounds and covariant bodies assuming bound are sound, but makes subtyping undecidable
- ▶ Requiring invariant bounds and covariant bodies regains decidability, but obviously allows less subtyping