

# Binocular Photometric Stereo

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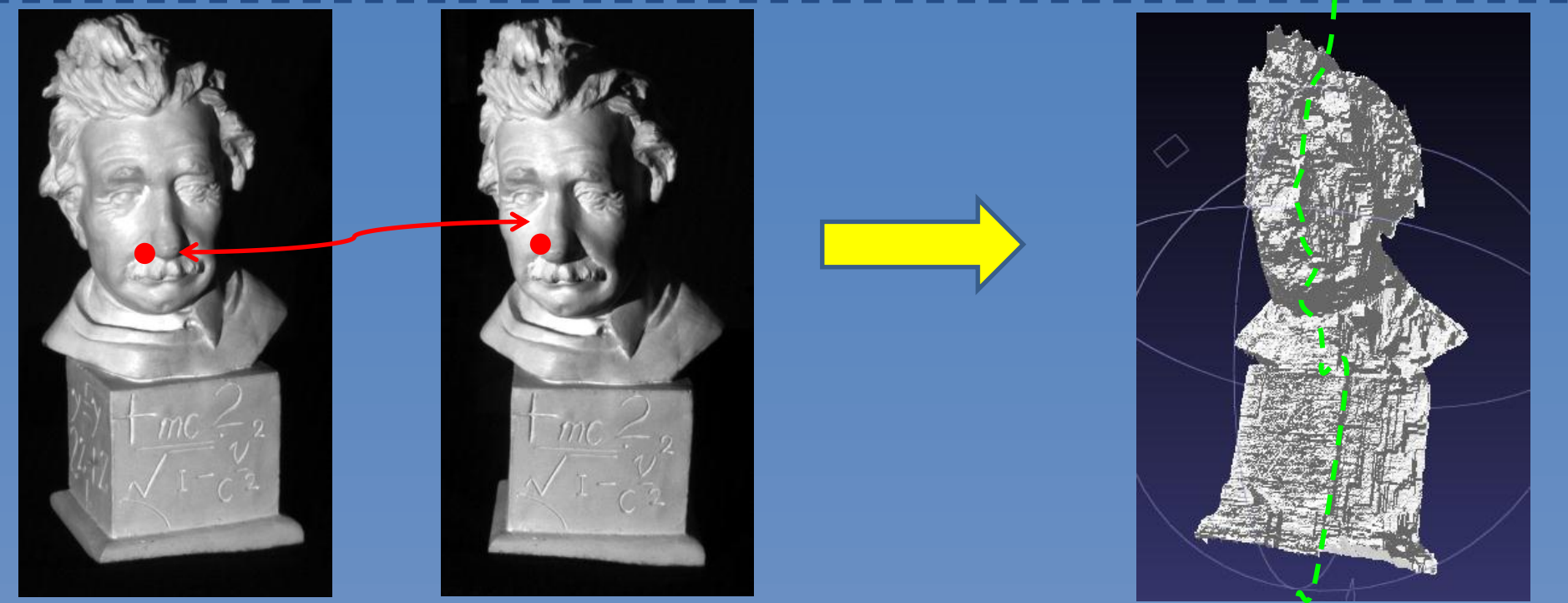
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## Motivation

### Binocular Stereo



- Pros.
- Metric depths
- Cons.
- Limited surface quality at texture-less areas

Principle

### Photometric Stereo



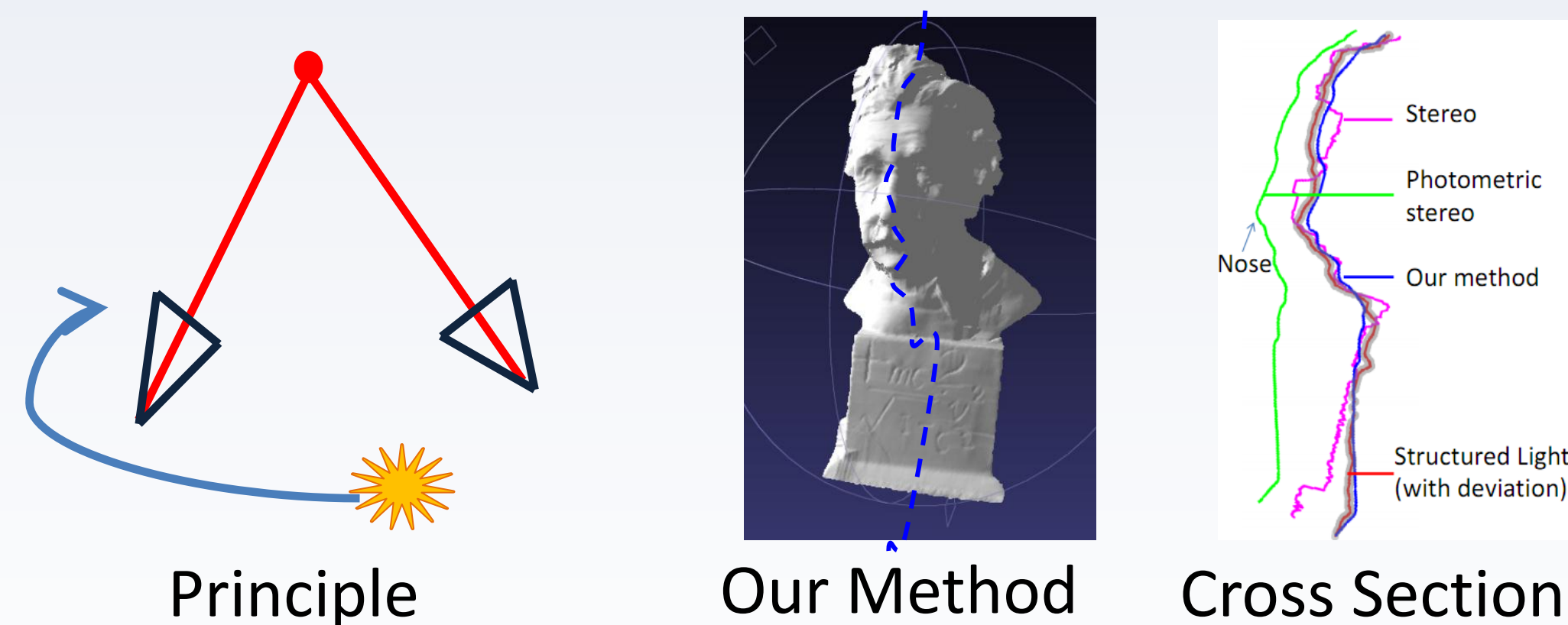
- Pros.
- Detailed surface normals
- Cons.
- Only relative depths;
  - Handles discontinuities poorly

Principle

## Our Work

### Binocular Photometric Stereo

To achieve the best of both worlds!



Principle

Our Method

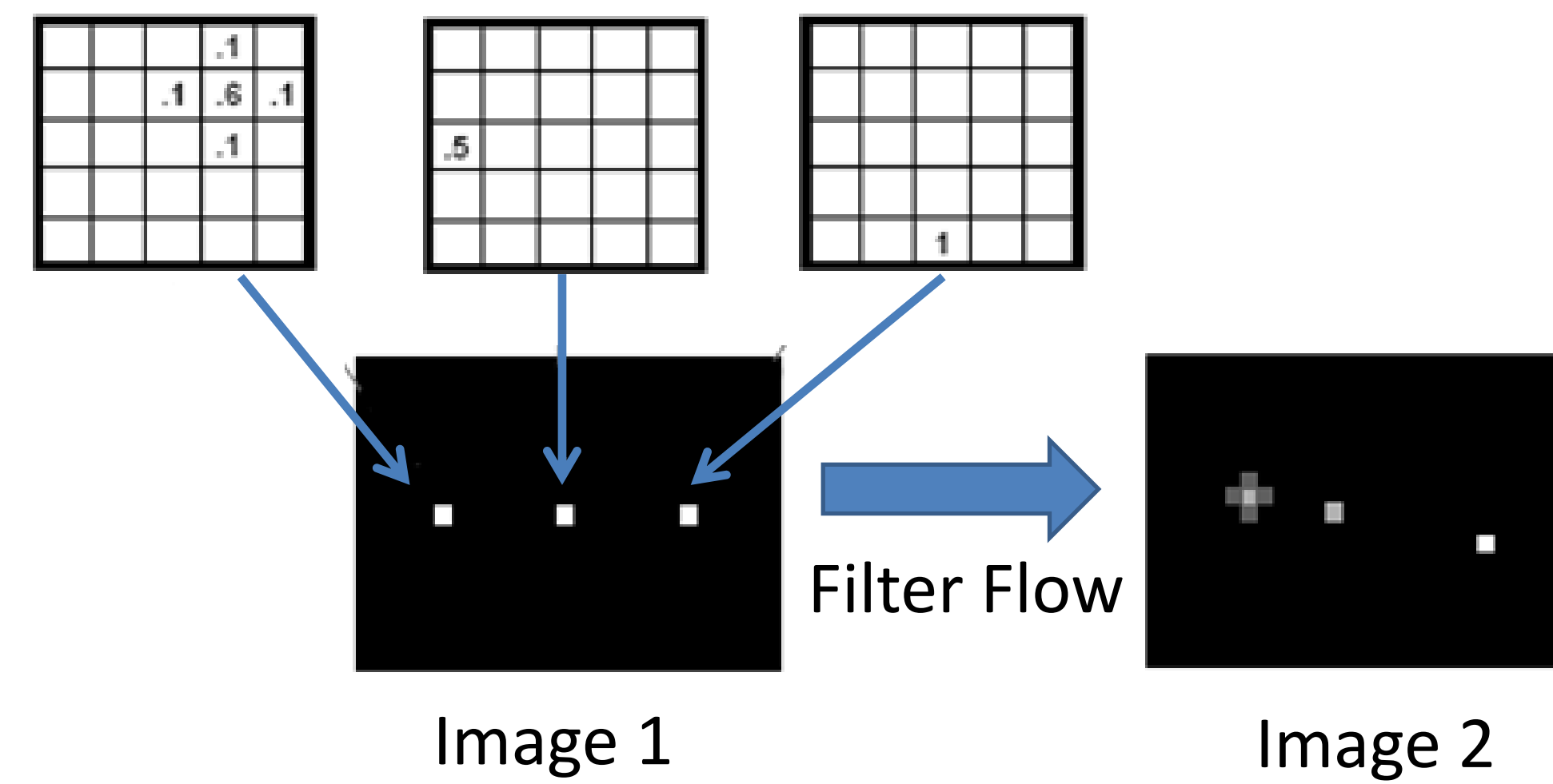
Cross Section

- # Setting: Add a **second** camera for photometric stereo
- # Formulation: A single **convex** optimization

## Filter Flow

### Filter Flow Background

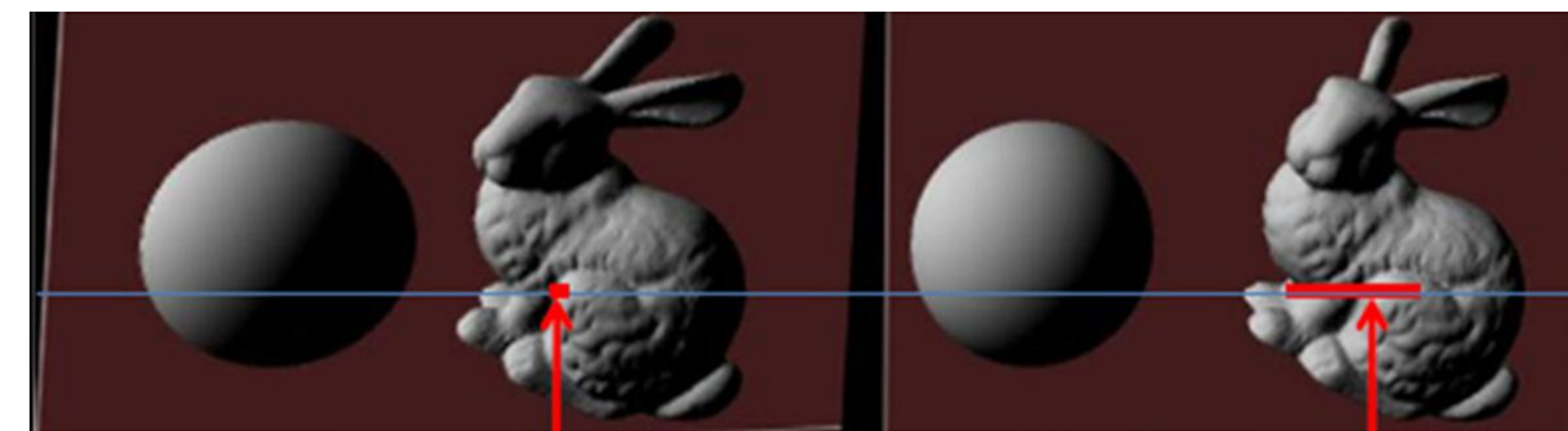
S. Seitz and S. Baker, 2009  
- A framework to model image transformation



Filter flow models each pixel as a filtered version of the other image, with constraints on the entries of the filter kernel.

## Modeling Stereo with Filter Flow

### 1D Filters



$\mathbf{u} = (u, v)$

$M^u$

1.9 Pixel shift to the left

### Disparity is the centroid of filter kernel.

- Disparity and depth are nonlinearly related.
- Normal and depth are linearly related.

### Linear Optimization Objectives

- **Data Objective (DO):** (Stereo intensity match)

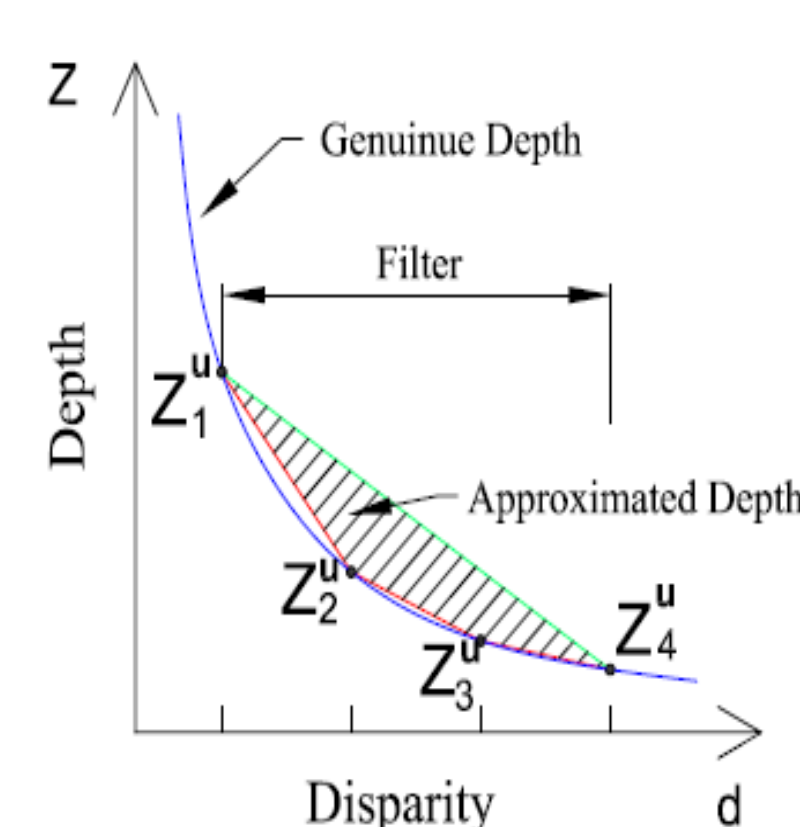
$$\sum_{\mathbf{u}} \left\| I_i^i(u, v) - \sum_j M_j^u I_r^i(u + j, v) \right\|_1$$

- **Normal Objective (NO):** (Normal match)

$$\| \hat{T}_u^u \cdot N^u \|_1 + \| \hat{T}_v^u \cdot N^u \|_1,$$

where

- Tangents:  $\hat{T}_u^u = \frac{\partial \hat{P}^u}{\partial u}$   $\hat{T}_v^u = \frac{\partial \hat{P}^u}{\partial v}$
- 3D Pos.:  $\hat{P}^u = (\hat{X}^u, \hat{Y}^u, \hat{Z}^u)$
- Depth  $\hat{Z}^u = \sum_j M_j^u Z_j^u = \sum_j M_j^u \frac{f_b}{j}$



## Constraints

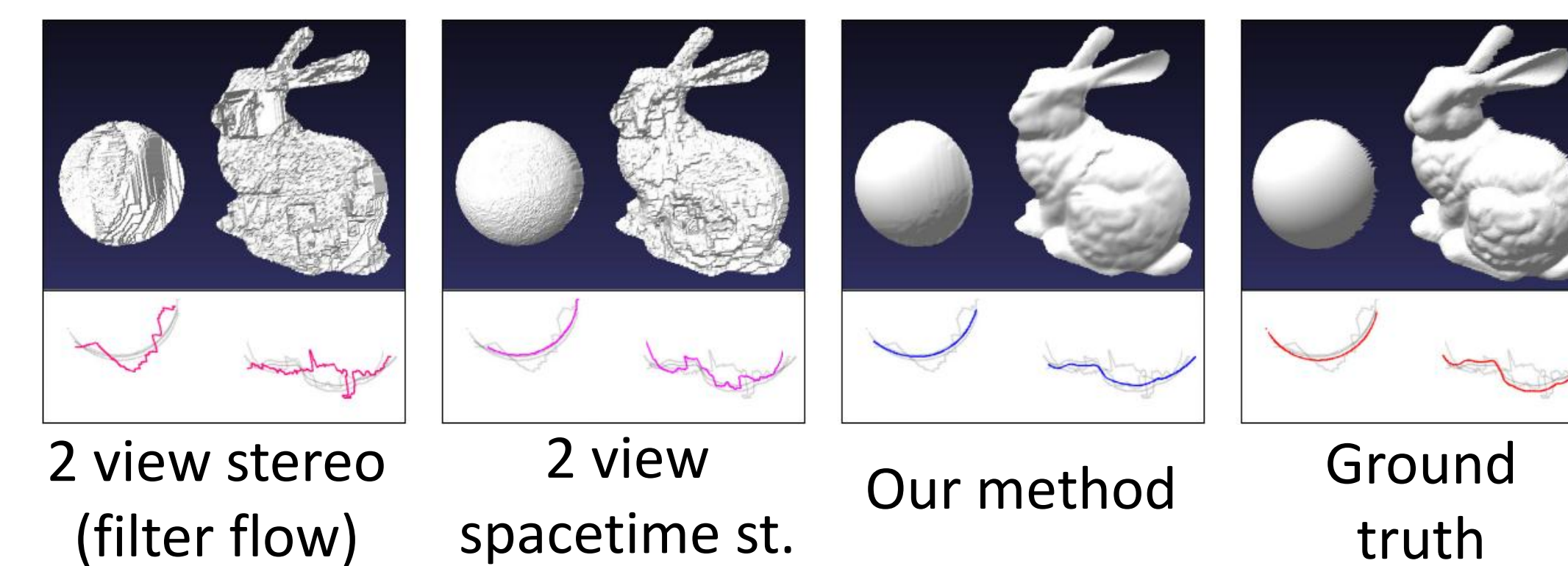
- Intensity preservation
- Non-negative:  $M_j^u \geq 0 \forall j$  (POS-M)
- Sum-to-one:  $\sum M_j^u = 1$  (SUM1-M)

## The Convex Optimization

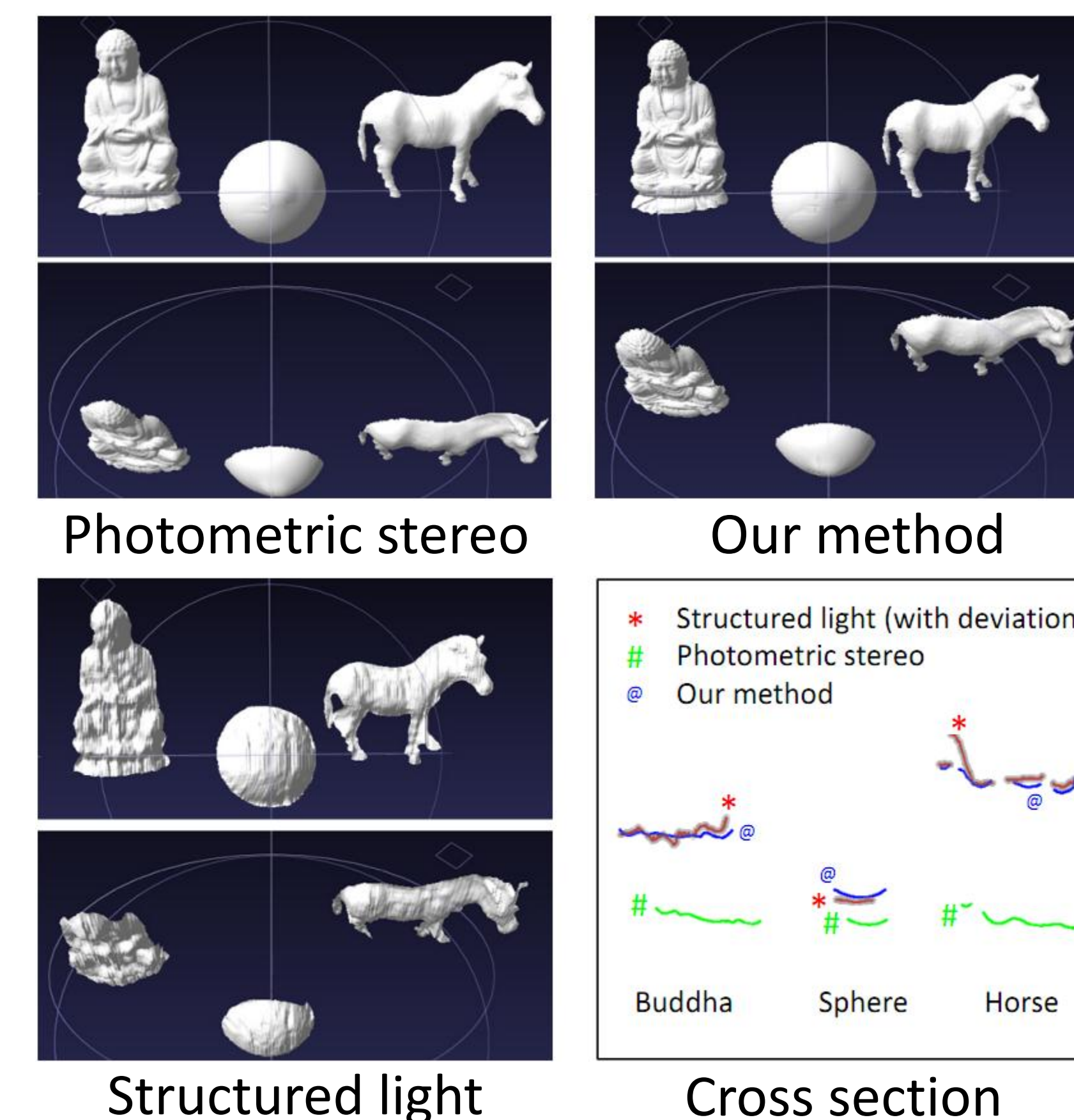
- DO + NO s.t. POS-M and SUM1-M
- Solve for filter entries  $M_j^u$
  - Recover depths according to the approximation

## Results

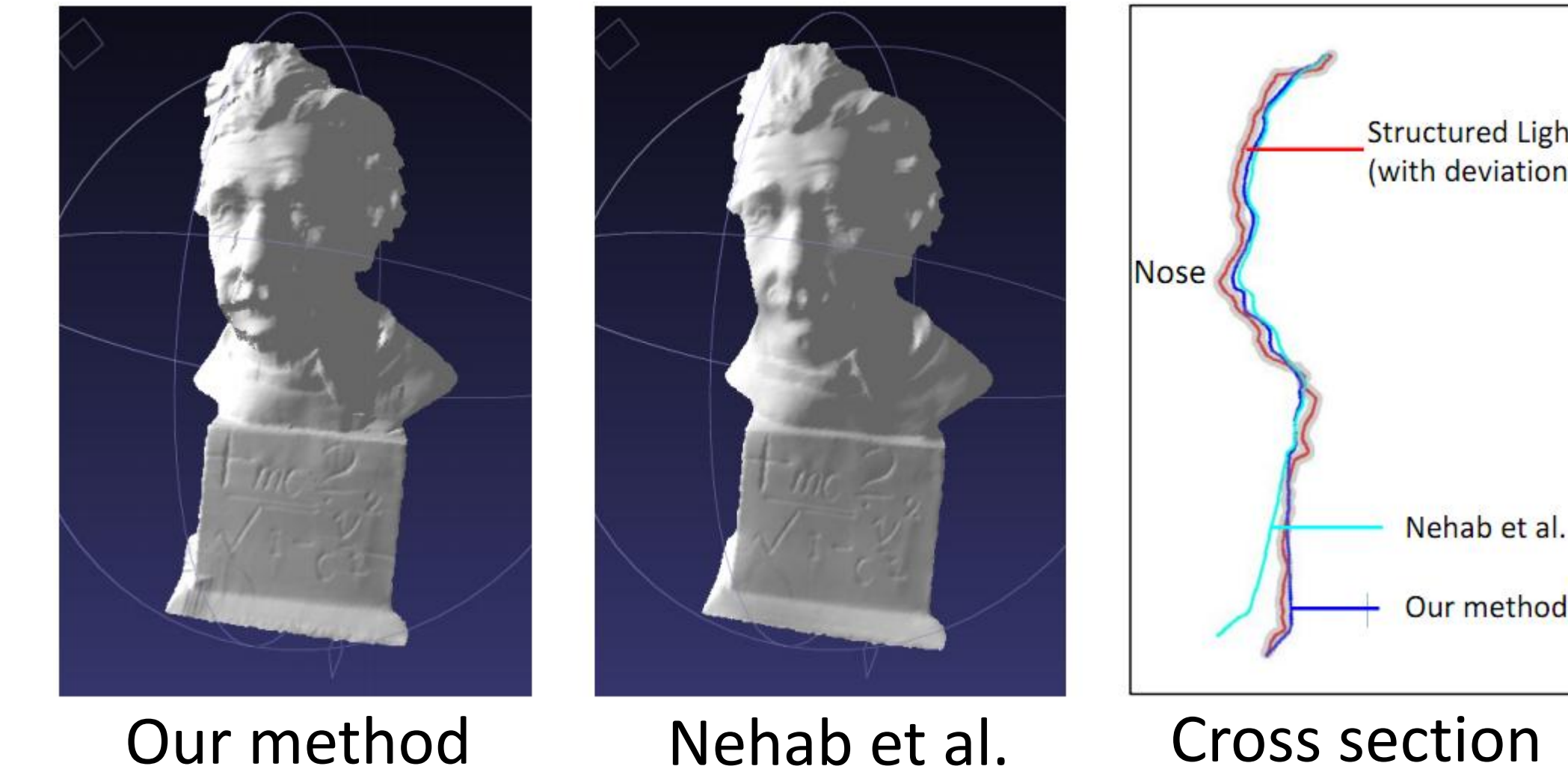
### Simulated Data - Comparing with Binocular Stereo



### Real Data - Comparing with Photometric Stereo



### Real Data - Comparing with [Nehab'05].

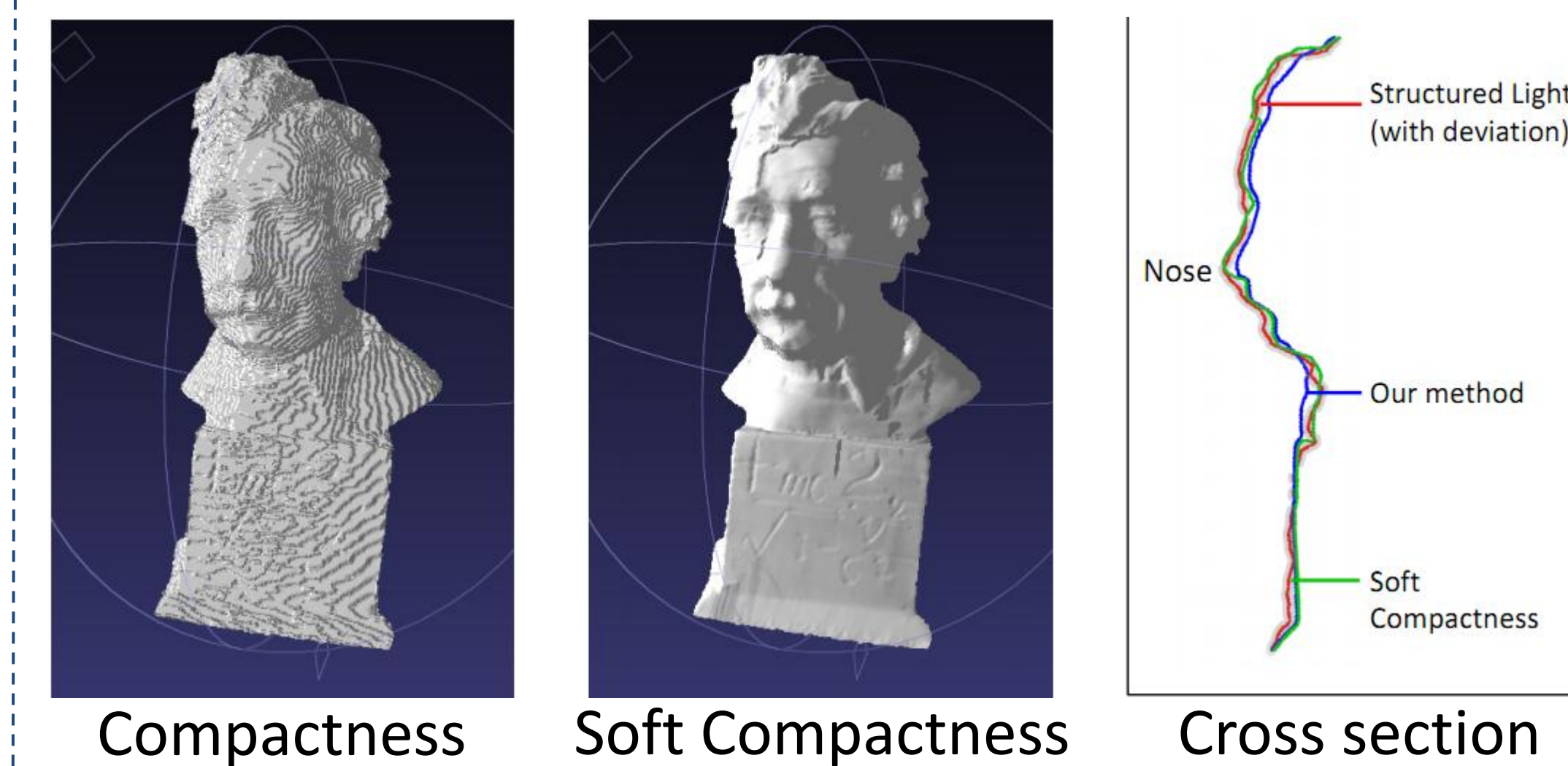


Our method simultaneously optimizes correspondence and normal cues, therefore it operates effectively at low textured flat areas.

### Optional Compactness Objective (non-linear)

$$\sum_j M_j^u \|j - \bar{M}^u\|_2^2 \quad \text{Compactness Obj.}$$

$$\sum_j M_j^u [\max(0, \|j - \bar{M}^u\|_2^2 - c^2)] \quad \text{Soft-Compactness Obj.}$$



	Our method	Compactness	Soft-CP
Bunny	0.199	0.191	0.112
Einstein	0.184	0.182	0.136
Three Objects	0.253	0.244	0.138
Dinosaur	0.170	0.170	0.083

Metric errors (in unit length)

## Related Methods

### Integrating with sparse stereo samples

These methods compute shape from photometric stereo as a separate step. [e.g. Lee 91]

### Integrating with dense scanned shape

These methods use a laser scanned shape as input. [e.g. Neheb 05]

### Multiview photometric stereo

These methods do not use surface appearance cues, and use multiview [e.g. Hernandez 08, Vlastic 09]

