GENOME 560, Spring 2012 Problem Set #4

(Due May 31th 9:00am)

1. [20 points] ANOVA Table

Complete the ANOVA table above from the values given. The sample size is N=20. (Hint: See slide 21 of lecture note 7.)

| Source of Variation | Sum of Squares | $\mathbf{d}\mathbf{f}$ | Mean Square | \mathbf{F} |
|---------------------|----------------|------------------------|-------------|--------------|
| Group | 56.7 | | | |
| Error | | 14 | 13.5 | |
| Total | | | | |

2. [80 points] Chi-Square Test

An expensive private school also asks for donations. Here are (actual) data (we have anonymized the school) on how many of the parents in each of its graduating classes have donated to the school's fund drive. The school is K-12. These are from the same year (2009) so the 2009 class means current 12-th graders, 2010 means current 11th graders, and so on.

| Year | Donated | Total Parents |
|------|---------|---------------|
| 2009 | 35 | 51 |
| 2010 | 42 | 56 |
| 2011 | 39 | 70 |
| 2012 | 37 | 60 |
| 2013 | 38 | 53 |
| 2014 | 35 | 54 |
| 2015 | 32 | 53 |
| 2016 | 19 | 27 |
| 2017 | 22 | 31 |
| 2018 | 20 | 30 |
| 2019 | 17 | 32 |
| 2020 | 34 | 34 |
| 2021 | 28 | 32 |

- (a) Do a Chi-square analysis (be careful to set up the table correctly) to find out whether there is any sign of parent burnout are donations equally likely in all grades?
- (b) Is this to be done as one-tailed or two-tailed? Why? (Does a low Chi-square mean a departure from the expected proportions?)
- (c) Think of some way to lump parts of the table to make the test focus more on the question at issue, and not waste effort on detecting whether there are differences that do not represent a long term trend. Carry it out and describe the results. Note that you can sum column 2 of rows 1 to 8 of a table by the R command sum(a[1:8,2])
- (d) What is the effect on the Chi-square test, on average, if some of the parents have two (or more) children in more than one grade, and thus are listed as donating (or not) in both of those grades on the basis of the same donation or the same non-donation?