

# CSE 369 QUIZ 3

Name: \_\_\_\_\_

Student ID  
Number: \_\_\_\_\_

**Please do not turn the page until 11:40.**

## Instructions

- This quiz contains 4 pages, including this cover page.
- Show scratch work for partial credit, but put your final answers in the boxes and blanks provided.
- The quiz is closed book and closed notes.
- Please silence and put away all cell phones and other mobile or noise-making devices.
- Remove all hats, headphones, and watches.
- You have 50 minutes to complete this quiz.

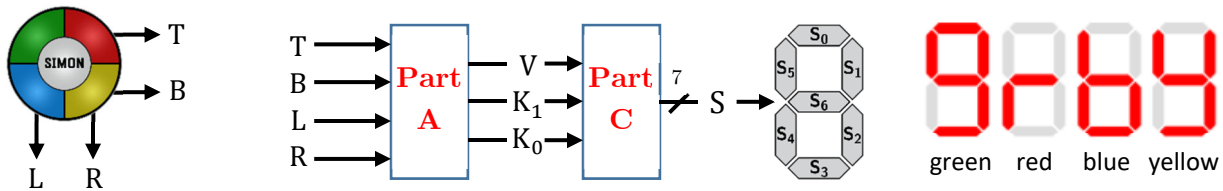
## Advice

- Read questions carefully before starting. Read *all* questions first and start where you feel the most confident to maximize the use of your time.
- There may be partial credit for incomplete answers; please show your work.
- Relax. You are here to learn.

Question	Points	Score
(1) Decoders	12	
(2) Shift Registers	11	
(3) Cryptography	9	
<b>Total:</b>	<b>32</b>	

**Question 1: Decoders [12 pts]**

We are building a **7-seg decoder circuit** for Simon, a color-based memory game with 4 buttons. The signals T(op), B(ottom), L(eft), and R(right) are high (1) only if a button in the corresponding column or row is being pushed. The 2-bit bus K represents which color is recognized (green = 00, red = 01, blue = 10, yellow = 11). The Valid signal (V) is high when at least one *button* is being pressed.



- (A) Complete the truth table. We give priority to T and L. [4 pt]
- (B) In the space below, solve for the minimal logical expression for  $K_0$ . [4 pt]

T	B	L	R	V	K <sub>1</sub>	K <sub>0</sub>
0	0	0	0			X
0	0	0	1			X
0	0	1	0			X
0	0	1	1			X
0	1	0	0			X
0	1	0	1			1
0	1	1	0			0
0	1	1	1			0
1	0	0	0			X
1	0	0	1			1
1	0	1	0			0
1	0	1	1			0
1	1	0	0			X
1	1	0	1			1
1	1	1	0			0
1	1	1	1			0

- (C) For the 7-seg signal numbering and outputs shown above (lit/red = 1), draw the minimal logic for  $S_2$  in terms of V, K<sub>1</sub>, and K<sub>0</sub>. All signals should be off when V = 0. [4 pt]

V

K<sub>1</sub>

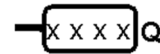
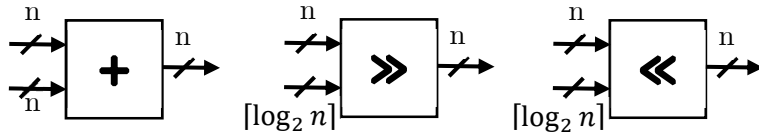
K<sub>0</sub>

S<sub>2</sub>

## Question 2: Routing Elements [11 pts]

We are creating a sequential circuit with 1-bit inputs  $E$  (enable),  $A$  (action), and  $D$  (direction) and  $n$ -bit output  $Q$ . When not enabled,  $Q$  stays constant, otherwise, the circuit will either count ( $A=0$ ) or shift ( $A=1$ ) each cycle.  $D=0$  indicates to *decrement* when counting or *right-shift* when shifting and  $D=1$  indicates the opposites. The circuit always shifts in a  $\theta$  bit.

- (A) Draw out the circuit below. You can freely use registers, constants, 2:1 MUXes, and the following logic blocks. Make sure you label the corresponding selector bits for ports of routing elements. [8 pt]



- (B) Now assume that we instantiate our circuit with  $n = 3$ . In the Verilog testbench below, fill in the blanks to indicate how the output of our sequential circuit updates. [3 pt]

```

initial begin
    D <= 1; A <= 0; E <= 1; // Q: 000
    @(posedge clk);        A <= 1; // Q: _____
    @(posedge clk);        E <= 0; // Q: _____
    @(posedge clk); D <= 0; A <= 0; E <= 1; // Q: _____
    @(posedge clk);        A <= 1; // Q: _____
    @(posedge clk);        A <= 0; // Q: _____
    @(posedge clk); $stop(); // Q: _____
end

```

**Question 3: Cryptography [9 pts]**

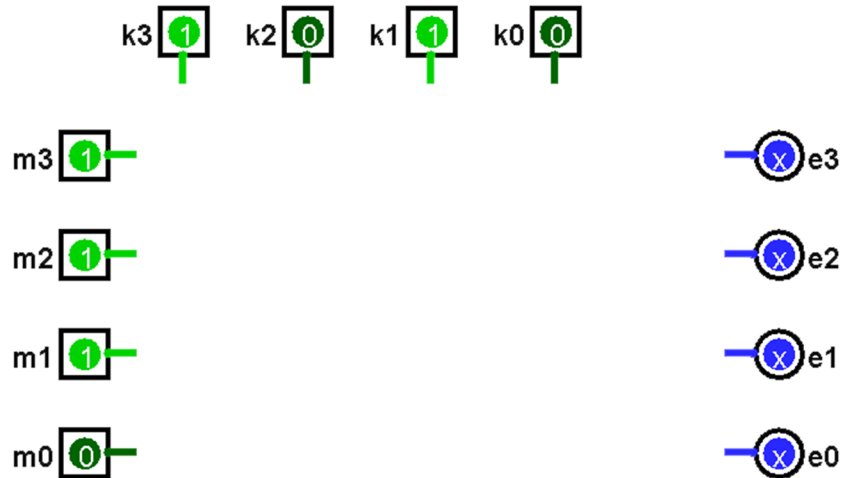
In cryptography, we wish to encode a message to apparent nonsense in a *reversible* manner so that the intended recipient can decode it and recover the original message. We can build a simple encoder using logic gates and a special “key”!

Example: With the message  $0b1110$ , and key  $0b1010$ , we get the encrypted message  $0b0100$ , from which we can recover the original message using the same key.

(A) (Circle one) Which type of gate will allow us to reversibly encrypt and decrypt? [1 pt]

AND                  NAND                  NOR                  OR                  XNOR                  XOR

(B) Below, implement a 4-bit **encryption circuit** that computes the encrypted message  $e$  from the original message  $m$  and key  $k$ . You may only use a *single type of 2-input logic gate*. [3 pt]



(C) Assume  $t_{\text{NOT}} = 10 \text{ ns}$ ,  $t_{\text{AND}} = t_{\text{OR}} = 25 \text{ ns}$ , and  $t_{\text{XOR}} = 40 \text{ ns}$ . Now we want to implement a **decryption circuit** that reverses the encryption. How much slower, if at all, would this decryption circuit be than the encryption circuit from Part B? [2 pt]

\_\_\_\_\_ ns

(D) Outline (in writing) a possible solution to handling messages of any length (*e.g.*, ones that are much longer than the key), assuming that we only have one instance of the encryption circuit (*i.e.*, we can't spawn extra circuitry on the fly). [3 pt]