Design of Digital Circuits and Systems Pipelining

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Teaching Assistants:

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Relevant Course Information

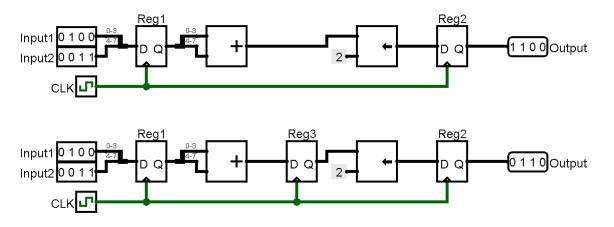
- Quiz 3 starts at 11:50 am
- Lab 4 due Friday (5/3), demos next week
- Homework 5 released today, due next Friday (5/10)
 - Static Timing Analysis and Pipelining
- Lab 5 released today, due in two weeks (5/17)
 - Hardest lab for many students
 - You will need to use the VGA interface on LabsLand
 - There's a creative component and opportunity for extra credit

Review: Timing Closure

- Fixing hold violations: caused by fast data path and destination register's clock latency
 - Add delay in the data path with buffers or pairs of inverters (done automatically by Quartus)
- Fixing setup violations: data arrives too late compared to the destination register's clock speed
 - Slow down the clock (undesirable)
 - Tell fitter to try harder or confine logic to a smaller area
 - Rewrite code to simplify logic
 - Add pipelining (today!)

Pipelining

- Pipelining is a set of data processing elements connected in series with buffer storage inserted between
 - In digital systems, the buffer storage are FFs & registers and data processing elements are stages of combinational logic
 - In its simplest form, can be thought of as adding registers in the middle of a computation to reduce our clock period



Performance

- What does it mean to say X performs better than Y?
- Silly example: a Tesla vs. a school bus
 - 2015 Tesla Model S P90D
 - 5 passengers, 2.8 secs in quarter mile
 - 2011 Type D school bus
 - Up to 90 passengers, quarter mile time?



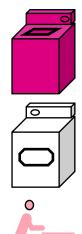
Measurements of Performance

- Latency (or response time or execution time)
 - Time to complete one task
- Throughput (or bandwidth)
 - Tasks completed per unit time

Analogy: Doing Laundry

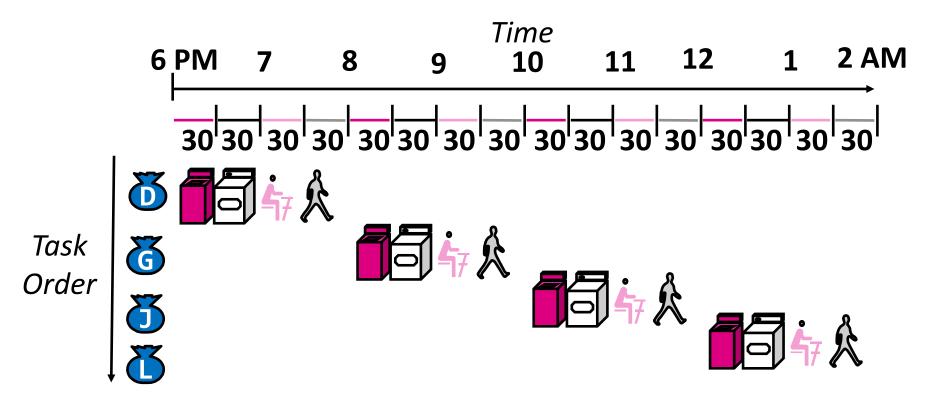
- Deepti, Gayathri, Jared, and Lancelot each have one load of clothes to wash, dry, fold, and put away
 - Washer takes 30 minutes
 - Dryer takes 30 minutes
 - "Folder" takes 30 minutes
 - "Stasher" takes 30 minutes to put clothes into drawers





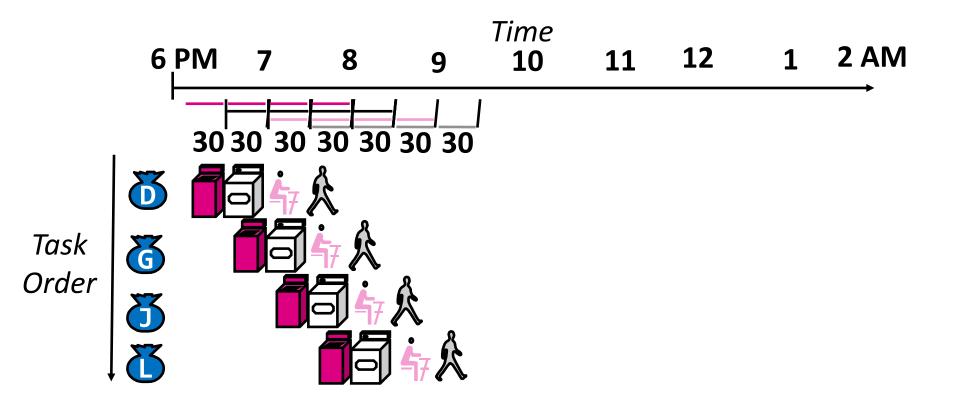


Sequential Laundry



Sequential laundry takes 8 hours for 4 loads

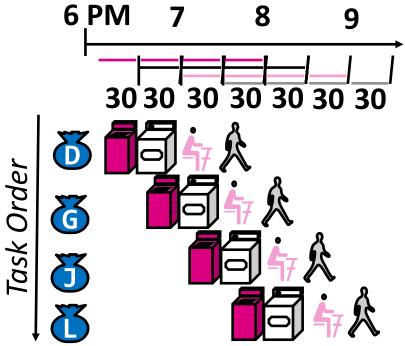
Pipelined Laundry



Pipelined laundry takes 3.5 hours for 4 loads!

Pipelining Notes

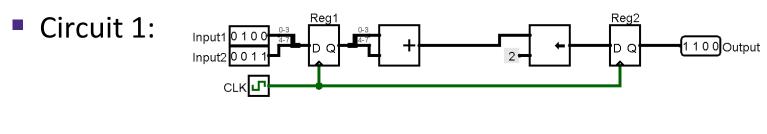
- Pipelining helps <u>throughput</u> of overall workload, but not <u>latency</u> of single task
 - Reduction in critical pathway allows for shorter clock period

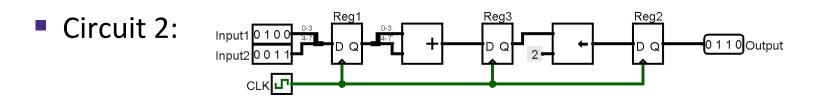


- Multiple tasks operating
 simultaneously using different resources
 - Executing different parts of multiple computations at the same time using the same hardware – like an assembly line
 - Greater utilization of logic resources

Pipelined Performance Example

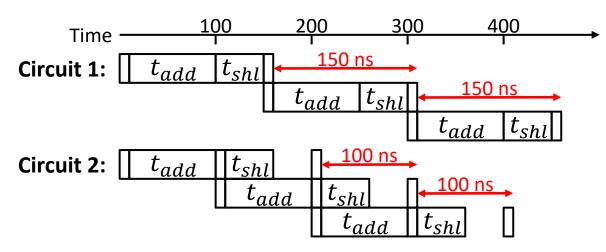
- * Assume t_{CO} = 10 ns, t_{add} = 90 ns, t_{shl} = 50 ns
 - For simplicity, assume $t_{clk} = t_{wire} = t_h = t_{su} = 0$
- Solve for the minimum clock period for each circuit
 - Given this minimum clock period, solve for the latency and throughput of each circuit





Pipeline Performance

- In theory, can measure "speedup" as the ratio in time per completion (TC) of computations
 - speedup = $\frac{TC_{original}}{TC_{pipelined}}$
 - speedup_{max} = # of pipeline stages
 - Speedup is reduced by unbalanced stages (and t_{CO}):

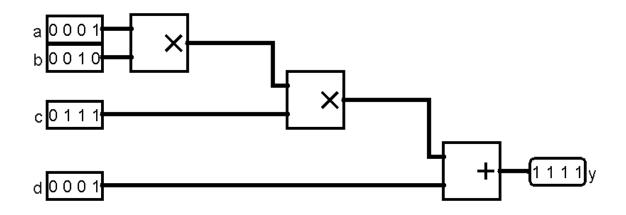


Technology

Break

Pipeline Registers

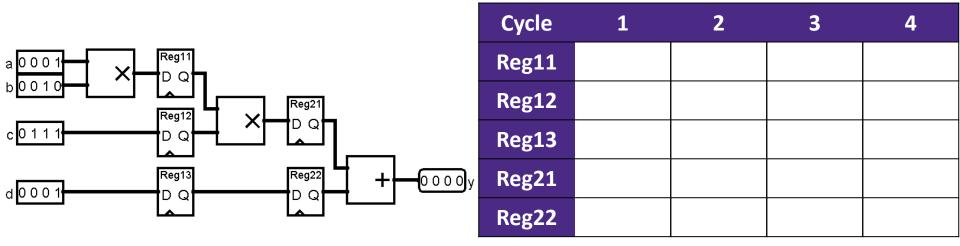
- Where to add pipeline registers?
 - For a given computation, all paths from any input to output must pass through the *same number* of pipeline registers
- * Example: $y_i = (a_i \times b_i) \times c_i + d_i$



Pipeline Registers

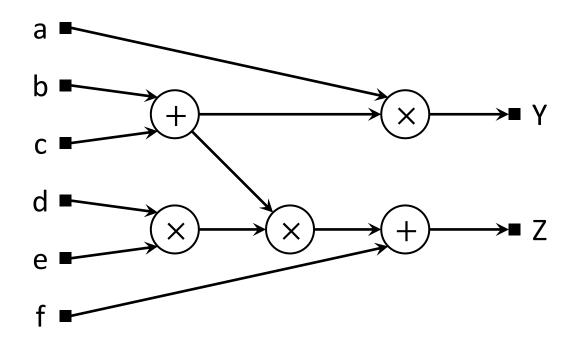
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Signal flow:



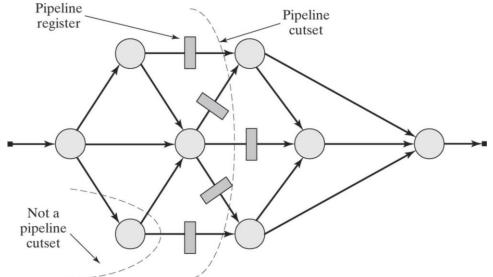
Data Flow Graph

- A data flow graph (DFG) is a visualization tool that can be used to simplify circuits into *directed graphs*
 - Nodes are computations (and their delays)
 - Edges represent data dependencies

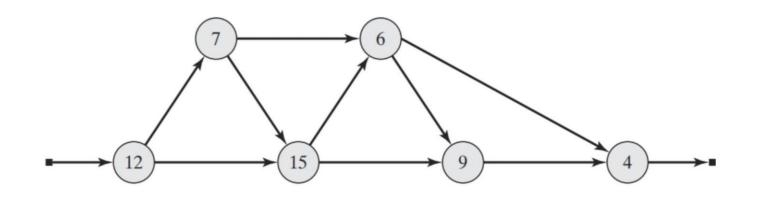


Pipeline Cutset

- A cutset is a set of edges that form two disjoint graphs when removed/cut
 - *Feedforward* cutset: data travels only forward in the cutset
 - *Feedback* cutset: data travels in both directions in the cutset
- Pipelining is done by placing a register along every edge in a pipeline (feedforward) cutset:

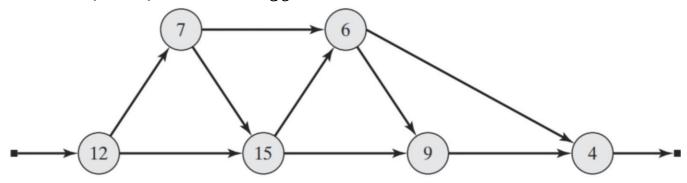


- The following data flow graph shows the propagation delay in each node
 - For simplicity, assume $t_{CO} = 0$
 - Original (non-pipelined) performance:



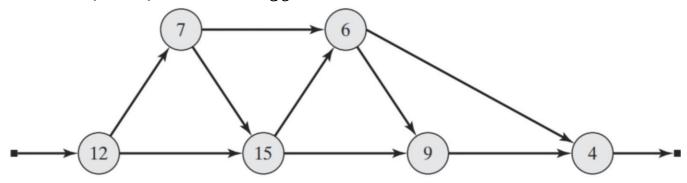
- The following data flow graph shows the propagation delay in each node
 - Create 2-3 different pipelined versions of this DFG and compute the maximum delay of each stage and minimum clock period for the pipelined computation

• For simplicity, assume
$$t_{CO} = 0$$



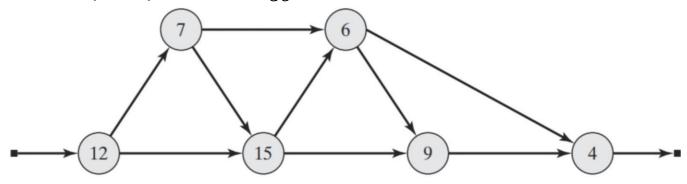
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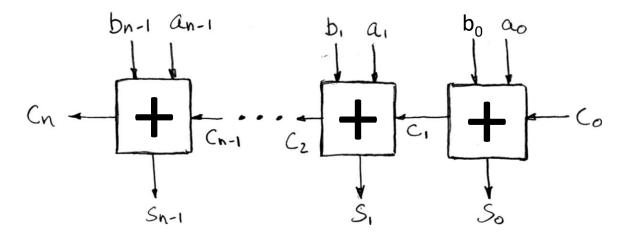


Pipeline Design Questions

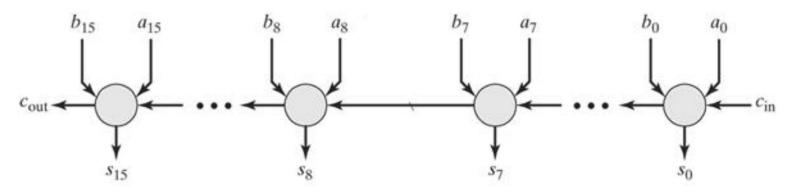
- When should I add pipelining?
 - Check if it is possible first (*i.e.*, a pipeline cutset must exist)
 - Want to reduce the critical path in your computation/system
 - Your system can afford the increase in latency and hardware
- Where do the pipeline registers go?
 - Must be placed at proper pipeline cutsets
 - Want to make pipeline stages as balanced as possible to maximize speedup

Design Example: 16-bit Ripple-Carry Adder

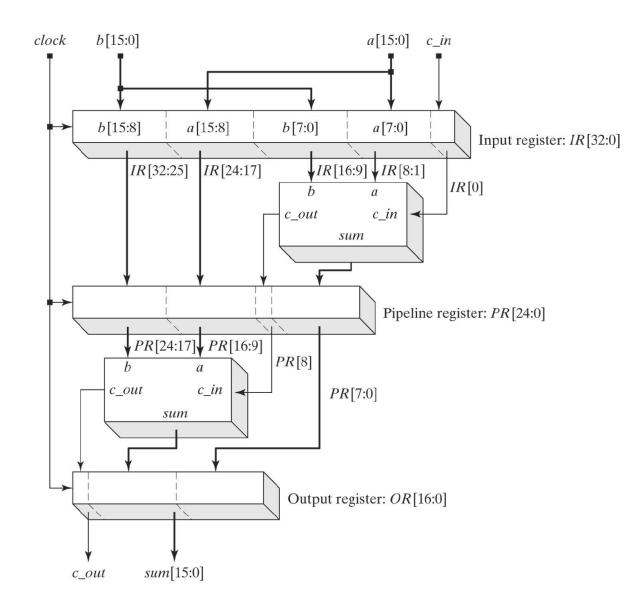
* Problem: C_n takes a long time to compute!



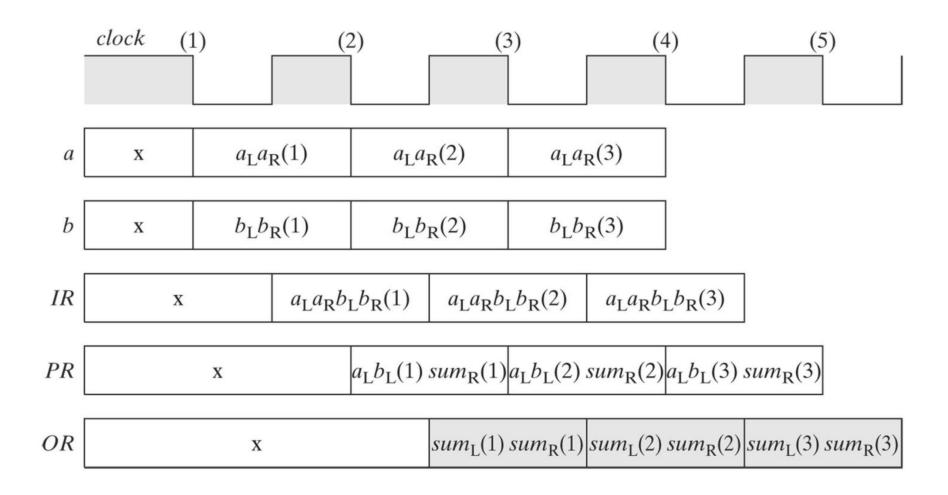
2-stage pipeline: which cutset to use?



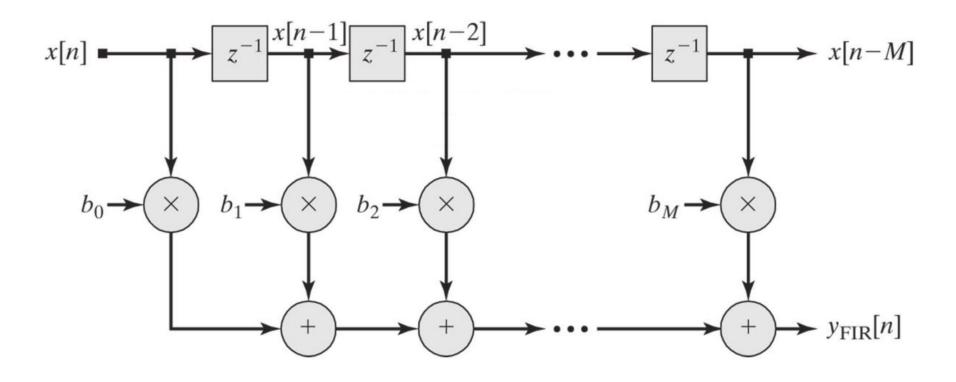
Design Example: 16-bit Pipelined Adder



Design Example: 16-bit Pipelined Adder



Design Example: FIR Filter



Design Example: Pipelined FIR Filter

