Design of Digital Circuits and Systems Pipelining

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Relevant Course Information

- Quiz 3 starts at 11:50 am
- Lab 4 due Friday (5/3), demos next week
- Homework 5 released today, due next Friday (5/10)
 - Static Timing Analysis and Pipelining
- Lab 5 released today, due in two weeks (5/17)
 - Hardest lab for many students
 - You will need to use the VGA interface on LabsLand
 - There's a creative component and opportunity for extra credit

CLK

In

DATen

Review: Timing Closure (setup and hold slack)

- Fixing hold violations: caused by fast data path and destination register's clock latency
 - Add delay in the data path with buffers or pairs of inverters (done automatically by Quartus)
- Fixing setup violations: data arrives too late compared to the destination register's clock speed
 - Slow down the clock (undesirable)
 - Tell fitter to try harder or confine logic to a smaller area
 - Rewrite code to simplify logic
- Add pipelining (today!)

Pipelining

- Pipelining is a set of data processing elements connected in series with buffer storage inserted between
 - In digital systems, the buffer storage are <u>FFs & registers</u> and data processing elements are <u>stages</u> of combinational logic
 - In its simplest form, can be thought of as adding registers in the middle of a computation to reduce our clock period



Performance

- What does it mean to say X performs better than Y?
- Silly example: a Tesla vs. a school bus
 - 2015 Tesla Model S P90D
 - 5 passengers, 2.8 secs in quarter mile
 - 2011 Type D school bus
 - Up to 90 passengers, quarter mile time?



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Measurements of Performance

- Latency (or response time or execution time)
 - Time to complete one task
- Throughput (or bandwidth)
 - Tasks completed per unit time

Analogy: Doing Laundry

- Deepti, Gayathri, Jared, and Lancelot each have one load of clothes to
 wash, dry, fold, and put away
 - Washer takes 30 minutes
 - Dryer takes 30 minutes
 - "Folder" takes 30 minutes
 - "Stasher" takes 30 minutes to put clothes into drawers





Sequential Laundry



Sequential laundry takes 8 hours for 4 loads only 1 person in laundry room at a time!

Pipelined Laundry



Pipelining Notes

- Pipelining helps <u>throughput</u> of overall workload, but not <u>latency</u> of single task
 - Reduction in critical pathway allows for shorter clock period



- Multiple tasks operating
 Simultaneously using different resources
 - Executing different parts of multiple computations at the same time using the same hardware – like an assembly line
 - Greater utilization of logic resources

Pipelined Performance Example

- * Assume t_{CO} = 10 ns, t_{add} = 90 ns, t_{shl} = 50 ns
 - For simplicity, assume $t_{clk} = t_{wire} = t_h = t_{su} = 0$
- Solve for the minimum clock period for each circuit
 - Given this minimum clock period, solve for the latency and throughput of each circuit



Pipeline Performance

 In theory, can measure "speedup" as the ratio in time per completion (TC) of computations

• speedup =
$$\frac{TC_{original}}{TC_{pipelined}}$$

- speedup_{max} = # of pipeline stages
- Speedup is reduced by unbalanced stages (and t_{CO}):



Technology

Break

Pipeline Registers

- Where to add pipeline registers?
 - For a given computation, all paths from any input to output must pass through the *same number* of pipeline registers
- * Example: $y_i = (a_i \times b_i) \times c_i + d_i$



Pipeline Registers

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Signal flow:



Data Flow Graph

- A data flow graph (DFG) is a visualization tool that can be used to simplify circuits into *directed graphs*
 - Nodes are computations (and their delays)
 - Edges represent data dependencies



Pipeline Cutset

- A cutset is a set of edges that form two disjoint graphs when removed/cut
 - Feedforward cutset: data travels only forward in the cutset
 - *Feedback* cutset: data travels in both directions in the cutset
- Pipelining is done by placing a register along every edge in a pipeline (feedforward) cutset:



- The following data flow graph shows the propagation delay in each node
 - For simplicity, assume $t_{CO} = 0$
 - Original (non-pipelined) performance:



- The following data flow graph shows the propagation delay in each node
 - Create 2-3 different pipelined versions of this DFG and compute the maximum delay of each stage and minimum clock period for the pipelined computation



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Pipeline Design Questions

- When should I add pipelining?
 - Check if it is possible first (*i.e.*, a pipeline cutset must exist)
 - Want to reduce the critical path in your computation/system
 - Your system can afford the increase in latency and hardware
- Where do the pipeline registers go?
 - Must be placed at proper pipeline cutsets
 - Want to make pipeline stages as balanced as possible to maximize speedup

Design Example: 16-bit Ripple-Carry Adder

* Problem: C_n takes a long time to compute!



* 2-stage pipeline: which cutset to use? (ut evenly in half



Design Example: 16-bit Pipelined Adder



Design Example: 16-bit Pipelined Adder



Design Example: FIR Filter



Design Example: Pipelined FIR Filter



