

## Context-free Grammars

- Compromise between
- REs, which can't nest or specify recursive structure
- General grammars, too powerful, undecidable
- Context-free grammars are a sweet spot
- Powerful enough to describe nesting, recursion
- Easy to parse; but also allow restrictions for speed
- Not perfect
- Cannot capture semantics, as in, "variable must be declared," requiring later semantic pass
- Can be ambiguous
- EBNF, Extended Backus Naur Form, is popular notation

EBNF Syntax of initial MiniJava



- Terminals -- alphabet of language defined by CFG
- Nonterminals -- symbols defined in terms of terminals and nonterminals
- Productions -- rules for how a nonterminal (lhs) is defined in terms of a (possibly empty) sequence of terminals and nonterminals
- Recursion is allowed!
- Multiple productions allowed for a nonterminal, alternatives
- Start symbol -- root of the defining language

$$
\begin{aligned}
& \text { Program ::= Stmt } \\
& \text { Stmt }::=\text { if ( Expr ) then Stmt else Stmt } \\
& \text { Stmt }::=\text { while (Expr) do Stmt }
\end{aligned}
$$

## Syntactic Analysis

Syntactic analysis, or parsing, is the second phase of compilation: The token file is converted to an abstract syntax tree.

- Goal: Convert token stream to abstract syntax tree
- Abstract syntax tree (AST):
- Captures the structural features of the program
- Primary data structure for remainder of analysis
- Three Part Plan
- Study how context-free grammars specify syntax
- Study algorithms for parsing / building ASTs
- Study the miniJava Implementation




## RE Specification of initial MiniJava Lex

Program ::= (Token | Whitespace)*
Token ::= ID | Integer | ReservedWord | Operator | Delimiter
ID ::= Letter (Letter | Digit)*
Letter : : = a $|\ldots| \mathbf{z}|\mathbf{A}| \ldots \mid \mathbf{z}$
Digit ::=0|...| 9
Integer ::= Digit ${ }^{+}$
ReservedWord::= class | public | static | extends void | int | boolean | if | else |
while|return|true|false| this | new | String main System.out.println
Operator $::=+|-|*|||<|<=|>=|>|==|$ $!=|\& \&|!$
Delimiter : : = ; | . | , $|=|(\mid)|\{\mid\}|[\mid]$ Whitespace : := <space> | <tab> | <newline>

## Example Grammar

E : : = E op E| - E| (E) | id
op $::=+|-|*| /$


Famous Ambiguity: "Dangling Else"
Stmt : : = ...
if ( Expr ) Stmt
if ( Expr ) Stmt else Stmt
if $\left(e_{1}\right)$ if $\left(e_{2}\right) s_{1}$ else $s_{2}$ : if ( $e_{1}$ ) if $\left(e_{2}\right) \quad s_{1}$ else $s_{2}$

## Resolving Ambiguity

- Option 1: add a meta-rule
- For example "else associates with closest previous if"
- works, keeps original grammar intact
- ad hoc and informal


## Resolving Ambiguity [continued]

Option 2: rewrite the grammar to resolve ambiguity explicitly

Stmt ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::=...|
if ( Expr ) MatchedStmt else MatchedStmt
UnmatchedStmt ::= if ( Expr ) Stmt |
if ( Expr ) MatchedStmt else UnmatchedStmt

- formal, no additional rules beyond syntax
- sometimes obscures original grammar


## Resolving Ambiguity [continued]

Option 3: redesign the language to remove the ambiguity

```
Stmt ::= ...
            if Expr then Stmt end |
            if Expr then Stmt else Stmt end
- formal, clear, elegant
- allows sequence of stmts in then and else
        branches, no {, } needed
    - extra end required for every if
```


## Resolving Ambiguity (Option 1)

Add some meta-rules, e.g. precedence and associativity rules
Example:

E::= EOPE|-E|E++
op::= + | - | * | / |
$|* *|==|<| \& \&$
| ||

| Operator | Preced | Assoc |
| :--- | :--- | :--- |
| Postfix ++ | Highest | Left |
| Prefix - |  | Right |
| ${ }^{* *}$ (Exp) |  | Right |
| ${ }^{*}, /, \%$ |  | Left |
| ,+- |  | Left |
| $==,<$ |  | None |
| $\& \&$ |  | Left |
| $\\|$ | Lowest | Left |

## Removing Ambiguity (Option 2)

Option2: Modify the grammar to explicitly resolve the ambiguity
Strategy:

- create a nonterminal for each precedence level
- expr is lowest precedence nonterminal,
each nonterminal can be rewritten with higher precedence operator, highest precedence operator includes atomic exprs
- at each precedence level, use:
- left recursion for left-associative operators
- right recursion for right-associative operators
- no recursion for non-associative operators


## Parsing Algorithms

Given a grammar, want to parse the input programs

- Check legality
- Produce AST representing the structure
- Be efficient
- Kinds of parsing algorithms
- Top down (LL(1), Recursive Descent)
- Bottom up (LR(1), Operator Precedence)


## Redone Example

## E : : = E0

E0 ::= E0 || E1 | E1 left associative
$::=$ E1 \&\& E2 | E2 left associative
$::=$ E3 $(==\mid<)$ E3 | E3 non associative
$::=$ E3 (+ | -) E4 | E4 left associative
$::=\mathrm{E} 4$ (* | / | \%) E5 | E5 left associative
::= E6 ** E5 | E6
right associative
right associative
left associative
$::=\mathrm{E} 7++$ E8

## Operator Precedence Example

E : := E0
E0 : := E0 || E1 | E1
1 $::=$ E1 \&\& E2 $\mid$ E2
$::=$ E3 (== | <) E3 | E3
$::=$ E3 (+ | -) E4 | E4
$::=\mathrm{E} 4$ (* $|/|$ \%) E5 | E5
$::=\mathrm{E} 6$ ** $\mathrm{E} 5 \mid \mathrm{E} 6$
$::=-\mathrm{E} 6 \mid \mathrm{E7}$
$::=\mathrm{E} 7++$ E8
::= id | (E)
$\begin{array}{llll}+ & b & * & c \\ d & \text { id } & \text { * } & \text { id }\end{array}$

| $:$ | $:$ | $:$ | $:$ |
| :--- | :--- | :--- | :--- |
| + | E4 | $\star$ | E5 |
| + | E 4 |  |  |


| $:$ | $:$ | $:$ | $:$ |
| :--- | :--- | :--- | :--- |
| + | E4 | $\star$ | E5 |
| + | E4 |  |  |

E3
E
left associative
left associative
non associative
left associative
left associative
right associative
right associative
left associative
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## Designing A Grammar

## Concerns:

- Accuracy
- Unambiguity
- Formality
- Readability, Clarity
- Ability to be parsed by a particular algorithm:
- Top down parser $==>\operatorname{LL}(\mathrm{k})$ Grammar
- Bottom up Parser ==> LR(k) Grammar
- Ability to be implemented using particular approach
- By hand
- By automatic tools


## Top Down Parsing

Build parse tree from the top (start symbol) down to leaves (terminals)

- Pick a production \& try to match the input
- Bad "pick" $\Rightarrow$ may need to backtrack
- Some grammars are backtrack-free (predictive parsing)

Basic issue: when "expanding" a nonterminal with some r.h.s., how to pick which r.h.s.?
E.g.

Stmts $::=$ Call | Assign | If | While
Call
$:=$
$=1 d$


While ::= while Test do Stmts end
Solution: look at input tokens to help decide

## Predictive Parser

Predictive parser: top-down parser that can select rhs by looking at most $k$ input tokens (the lookahead)

## Efficient:

- no backtracking needed
- linear time to parse

Implementation of predictive parsers:

- recursive-descent parser
- each nonterminal parsed by a procedure
- call other procedures to parse sub-nonterminals, recursively
- typically written by hand
- table-driven parser
- PDA:like table-driven FSA, plus stack to do recursive FSA calls
- typically generated by a tool from a grammar specification


## Eliminating common prefixes

Can left factor common prefixes to eliminate them

- create new nonterminal for different suffixes
- delay choice till after common prefix
- Before:
If ::= if Test then Stmts end |
if Test then Stmts else Stmts end
- After:

$$
\text { If } \quad:=\text { if Test then Stmts IfCont }
$$

$$
\text { IfCont }::=\text { end } \mid \text { else Stmts end }
$$

## LL(k) Grammars

Can construct predictive parser automatically / easily if grammar is $\mathrm{LL}(\mathrm{k})$

- Left-to-right scan of input, Leftmost derivation (replace leftmost NT at each step)
- $\mathbf{k}$ tokens of look ahead needed, $\geq 1$

Some restrictions:

- no ambiguity (true for any parsing algorithm)
- no common prefixes of length $\geq k$ :

If $::=$ if Test then Stmts end |
if Test then Stmts else Stmts end

- no left recursion:

E ::= E Op E | ...

- a few others (First() and Follow() rules - see text.)

Restrictions guarantee that, given k input tokens, can always select correct rhs to expand nonterminal. Easy to do by hand in recursive-descent parser

## Building Top-down Parsers

Given an $L L(1)$ grammar and its FIRST \& FOLLOW sets

- Emit a routine for each non-terminal
- Nest of if-then-else statements to check alternate rhs's
- Each returns true on success and throws an error on false
- Simple, working (, perhaps ugly,) code
- This automatically constructs a recursive-descent parser Improving matters
- Nest of if-then-else statements may be slow
- Good case statement implementation would be better
- What about a table to encode the options?
- Interpret the table with a skeleton, as we did in scanning


## Eliminating Left Recursion

- Can Rewrite the grammar to eliminate left recursion
- Before

E :: = E + T| T
T: := $T$ * $\mid F$
F : : = id | ...

- After

E : := T ECon
ECon ::= + T ECon | $\varepsilon$
T : := F TCon
TCon : : = * F TCon | $\varepsilon$
F : : = id | ...

Recursive Descent Parsing Example
A couple of routines from the expression parser

```
Parse()
    token \leftarrow rext_token();
    if (Expr() = true & token = EOF)
        then next compilation step;
        else
            report syntax error;
            return false
Expr()
    if (Term() = false)
    then return false;
    else return ECon();
```

Factor()
if (token = Number) then
token $\leftarrow$ next_token() return true;
else if (token = Identifier) then
token $\leftarrow$ next_token(); return true;
$\stackrel{\text { ret }}{\text { else }}$
report syntax error return false;

ECon, Term, and TCon are constructed in a similar manner

## Building Top-down Parsers

## Strategy

- Encode knowledge in a table
- Need a row for every NT and a column for every $T$
- Use a standard "skeleton" parser to interpret the table


## Bottom Up Parsing

Construct parse tree for input from leaves up

- reducing a string of tokens to single start symbol (inverse of deriving a string of tokens from start symbol)
"Shift-reduce" strategy:
- read ("shift") tokens until seen r.h.s. of "correct" production xyzabcdef A ::= bc.D
- reduce handle to I.h.s. nonterminal, then continue
- done when all input read and reduced to start nonterminal

| LR(k) |
| :---: |
| - LR(k) parsing <br> - Left-to-right scan of input, Rightmost derivation <br> - $\boldsymbol{k}$ tokens of look ahead <br> - Strictly more general than $\operatorname{LL}(k)$ <br> - Gets to look at whole rhs of production before deciding what to do, not just first $k$ tokens of rhs <br> - can handle left recursion and common prefixes fine <br> - Still as efficient as any top-down or bottom-up parsing method <br> - Complex to implement <br> - need automatic tools to construct parser from grammar |
|  |  |
|  |  |
|  |  |

## LALR-Look Ahead LR

$\operatorname{LALR}(k)$ algorithm has fewer states ==> smaller tables

- less general than $\operatorname{LR}(k)$, but still good in practice - size of tables acceptable in practice
- $k==1$ in practice
- most parser generators, including yacc and CUP, are LALR(1)


## Global Plan for LR(0) Parsing

- Goal: Set up the tables for parsing an $\operatorname{LR}(0)$ grammar
- Add $S^{\prime} \quad::=\mathrm{S} \$$ to the grammar, (i.e. We will be solving the problem for a new grammar with a terminator)
- Compute parser states by starting with state 1 containing added production, $\mathrm{S}^{\prime}$ : : = . S\$
- Form closures of states and shifting to complete diagram
- Convert diagram to transition table for PDA
- Step through parse using table and stack


## LR(0) Parser Generation

- Key idea: simulate where input might be in grammar as it reads tokens
- "Where input might be in grammar" captured by set of items, which forms a state in the parser's FSA
- LR(0) item: lhs : : = rhs production, with a dot in rhs somewhere marking what's been read (shifted) so far.
Example:
Initial item: $S^{\prime} \quad::=$. S \$
- (LR(k) item: also add $k$ tokens of lookahead to each item )


## LR(0) Parser Generation Example

Example grammar:
S ::= beep | \{ L \}
L : : = S | L ; S

- Add an initial start production to the grammar:
s' : := s \$
(\$ represents end of input)

Modified Example grammar:
$S^{\prime}::=$ S \$ // Always add this production
S ::= beep | \{ L \}
$\mathrm{L}::=\mathrm{S} \mid \mathrm{L}$; S

- Initial item:

S' : := . S \$

## State Transitions (Shifting)

Given a set of items, compute new state(s) for each symbol (terminal and non-terminal) after dot

- state transitions correspond to shift actions

A new item is derived from an old item by shifting the dot over the symbol

- then do closure on this item to computer new state

1. Add all productions for that non-terminal, and
2. Put a dot at the start of the RHS of each production.

Initial item (1):
s'::= . s \$


| Grammar: <br> S' : := S \$ | Example |  |
| :---: | :---: | :---: |
| S : : = beep \| \{ L \} |  |  |
| L : : = S \| L ; S |  | S' : := . S \$ |
| State (1): |  | S $\mathrm{S}::=\mathrm{=}$. $\{\mathrm{L}$ L \} |

State (2) (reached on transition that shifts S) :
$\mathrm{S}^{\prime}::=\mathrm{S} . \$$
State (3) (reached on transition that shifts beep):


State (4) (reached on transition that shifts \{ ):

## Accepting \& Reducing

Other than shifting symbols there are two other actions we might take:

- accepting:
- at the end of a successful parse
- reducing:
- applying a production to symbols on our stack that match the RHS of the production.


## Accepting Transitions

If a state has an item with the dot before the \$, e.g. :

$$
S^{\prime}::=S \text {. \$ }
$$

then we will add a transition from this state labeled \$ that goes to the accept action (in the transition table).

For example, State (2):
s' ::= s . \$
has a transition labeled \$ to the accept action


## Example

S : . = . S \$
S : : = • beep
S :: = . \{ L \}
S : := beep .

|  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
| L : := . L ; |  |  |  |  |  |
| S : := . beep |  |  |  |  |  |
| . 1 |  |  |  |  |  |

$\mathrm{S}^{\prime}::=\mathrm{S} . \$$

Rest of the States (Part 2)

State (7):

reduce $s::=\{L\}$
State (8):
$\begin{array}{llll}\mathrm{L} & ::=\mathrm{L} & \text {; } \cdot \mathrm{S} \\ \mathrm{S}: & := & \text { beep }\end{array}$
$\begin{array}{lll}S & : & := \\ S & \text { beep } \\ S & := & \text {. } L\}\end{array}$
State (8): on beep,
State (8): on \{,
State (8): on S,
State (9):
L : := L ; S .
reduce L ::= L ; S

## Reducing States

If state has an item with a dot at the end, e.g.:

$$
\text { lhs }::=\text { rhs . }
$$

then it has a reduce lhs : := rhs action.
For example, state (3):
S ::= beep .
has a reduce $S::=$ beep action
We will add this in our transition table as the action to take when in this state regardless of the next symbol.

Hmm.....Conflicting Actions?

- what if other items in this state shift?
- what if other items in this state reduce differently?


## Rest of the States, Part 1




## Building Table of States \& Transitions

Create a row for each state
Create a column for each terminal, non-terminal, and \$
For every "state ( $i$ ): if shift $X$ goto state ( $j$ )" transition:

- if $X$ is a terminal, put "shift, goto $j$ " action in row $i$, column $X$
- if $X$ is a non-terminal, put "goto $j$ " action in row $i$, column $X$

For every "state (i): if \$ accept" transition:

- put "accept" action in row $i$, column \$

For every "state ( 1 ): lhs : := rhs." action:

- put "reduce 1 hs $::=r h s$ " action in all columns of row $i$


## Execution of Parsing Table

- Parser State:
- stack of:
- states, (initialized to state "1") and
- shifted/reduced symbols, (initially empty)
- unconsumed tokens, (initialized to input tokens)
- To run the parser, repeat these steps:
- Do action( $\mathrm{S}, \mathrm{x}$ ) where S is the state on top of stack, and $x$ is the next unconsumed token.
- If the action was a goto(S), push state $S$ onto the stack
- If action ( $\mathrm{S}, \mathrm{x}$ ) is empty, report syntax error

Table of This Grammar

| State | \{ | \} | beep | ; | S | L | \$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | s,g4 |  | s,g3 |  | g2 |  |  |
| 2 |  |  |  |  |  |  | a! |
| 3 | reduce S : : = beep |  |  |  |  |  |  |
| 4 | s,g4 |  | s,g3 |  | g5 | g6 |  |
| 5 | reduce L : : = S |  |  |  |  |  |  |
| 6 |  | s,g7 |  | s,g8 |  |  |  |
| 7 | reduce S : := \{ L \} |  |  |  |  |  |  |
| 8 | s,g4 |  | s,g3 |  | g9 |  |  |
| 9 | reduce L : := L ; S |  |  |  |  |  |  |



## Problems In Shift-Reduce Parsing

Can write grammars that cannot be handled with shift-reduce parsing

## Shift/reduce conflict:

- state has both shift action(s) and reduce actions Reduce/reduce conflict:
- state has more than one reduce action

$$
\begin{aligned}
& \text { LR(0) example: } \\
& \text { E ::=E + T | T } \\
& \text { State: } \begin{array}{l}
\mathrm{E}::=\mathrm{E} . \quad+\mathrm{T} \\
\mathrm{E}::=\mathrm{T} . \\
\text { - Can shift + } \\
\text { - Can reduce E }::=\mathrm{T} \\
\text { LR(k) example: }
\end{array}
\end{aligned}
$$

    S : := if E then \(S\) |
                if \(E\) then \(S\) else \(S \mid \ldots\)
    State: $s::=$ if $E$ then $S$.
S : := if E then S . else S
- Can reduce $S$ ::= if E then

## Reduce/Reduce Conflicts

Example:
Stmt ::= Type id ; | LHS = Expr ; | ...
...
LHS : := id | LHS [ Expr ] | ...

Type ::= id | Type [] | ..
State $\begin{aligned} & \text { Type }::=\text { id } . \\ & \text { LHS } \quad::=i d .\end{aligned}$
Can reduce type : := id
Can reduce lhs ::= id

## Abstract Syntax Trees

The parser's output is an abstract syntax tree (AST) representing the grammatical structure of the parsed input

- ASTs represent only semantically meaningful aspects of input program, unlike concrete syntax trees which record the complete textual form of the input
- There's no need to record keywords or punctuation like (), ; else
- The rest of compiler only cares about the abstract structure


## AST Node Classes

Each node in an AST is an instance of an AST class

- IfStmt, AssignStmt, AddExpr, VarDecl, etc.

Each AST class declares its own instance variables holding its AST subtrees

- IfStmt has testExpr, thenStmt, and elseStmt
- AssignStmt has lhsVar and rhsExpr
- AddExpr has arg1Expr and arg2Expr
- VarDecl has typeExpr and varName


## AST Class Hierarchy

AST classes are organized into an inheritance hierarchy based on commonalities of meaning and structure

- Each "abstract non-terminal" that has multiple alternative concrete forms will have an abstract class that's the superclass of the various alternative forms
- Stmt is abstract superclass of IfStmt, AssignStmt, etc.
- Expr is abstract superclass of AddExpr, VarExpr, etc.
- Type is abstract superclass of Int Type, ClassType, etc.


## Automatic Parser Generation in MiniJava

We use the CUP tool to automatically create a parser from a specification file, Parser/minijava. cup
The MiniJava Makefile automatically rebuilds the parser whenever its specification file changes

A CUP file has several sections:

- introductory declarations included with the generated parser
- declarations of the terminals and nonterminals with their types
- The AST node or other value returned when finished parsing that nonterminal or terminal
- precedence declarations
- productions + actions


## Precedence Declarations

Can specify precedence and associativity of operators

- equal precedence in a single declaration
- lowest precedence textually first
- specify left, right, or nonassoc with each declaration


## Examples:

precedence left AND_AND;
precedence nonassoc EQUALS_EQUALS, EXCLAIM_EQUALS;
precedence left LESSTHAN, LESSEQUAL, GREATEREQUAL, GREATERTHAN;
precedence left PLUS, MINUS;
precedence left STAR, SLASH;
precedence left ExCLAIM;
precedence left PERIOD;

## AST Extensions For Project

New variable declarations:

- StaticVarDecl

New types:

- DoubleType
- ArrayType

New/changed statements:

- IfStmt can omit else branch
- Forstmt
- BreakStmt
- ArrayAssignStmt

New expressions:

- DoubleLiteralExpr
- OrExpr
- ArrayLookupExpr
- ArrayLengthExpr
- ArrayNewExpr


## Terminal and Nonterminal Declarations

Terminal declarations we saw before:
/* reserved words: */
terminal CLASS, PUBLIC, STATIC, EXTENDS;
...
ens with values: */
terminal String IDENTIFIER;
terminal Integer INT_LITERAL;
Nonterminals are similar:
nonterminal Program Program;
nonterminal MainClassDecl MainClassDecl;
nonterminal List/*<...>*/ ClassDecls;
nonterminal RegularClassDecl ClassDecl;
nonterminal List/*<Stmt>*/ Stmts;
nonterminal Stmt Stmt;
nonterminal List/*<Expr>*/ Exprs;
nonterminal List/*<Expr>*/ MoreExprs;
nonterminal Expr Expr;
nonterminal String Identifier;

All of the form:
LHS ::= RHS1 \{: Java code 1 :\}
RHS2 \{: Java code 2 :\}
| ...
RHSn \{: Java code $n$ :\};
Can label symbols in RHS with : var suffix to refer to its result value in Java code

- varleft is set to line in input where var symbol was
E.g.: Expr ::= Expr:arg1 PLUS Expr:arg2
\{: RESULT = new AddExpr ( arg1,arg2,arg1left);:\}
| INT_LITERAL:value\{: RESULT = new IntLiteralExpr ( value.intValue(), valueleft);:\}
| Expr:rcvr PERIOD Identifier:message OPEN_PAREN Exprs:args CLOSE_PAREN
\{: RESULT = new MethodCallexpr ( rcvr,message, args, rcvrleft);:
| ... ;


## Error Handling

How to handle syntax error?
Option 1: quit compilation

+ easy
- inconvenient for programmer

Option 2: error recovery

+ try to catch as many errors as possible on one compile - difficult to avoid streams of spurious errors

Option 3: error correction

+ fix syntax errors as part of compilation - hard!!


## Panic Mode Error Recovery

When finding a syntax error, skip tokens until reaching a "landmark"

- landmarks in MiniJava: ;, ), \}
- once a landmark is found, hope to have gotten back on track

In top-down parser, maintain set of landmark tokens as recursive descent proceeds

- landmarks selected from terminals later in production
as parsing proceeds, set of landmarks will change, depending as parsing proceeds, se
on the parsing context
In bottom-up parser, can add special erro nonterminals, followed by landmarks
- if syntax error, then will skip tokens till seeing landmark, then reduce and continue normally
- E.g. Stmt : := ... | error ; | \{ error \}

Expr ::= ... ( error)

