CSE 401/M501 – Compilers

Parsing & Context-Free Grammars Hal Perkins Autumn 2018

Administrivia

- Reminders:
 - Project partner signup. Please fill out the form with your and your partner's names and cse netids
 - Only one form per group, please; +1 point each if it's right
 - Please finish by tomorrow, 11 pm
 - Who's still looking for a partner? 401? M501?
 - How do we match people up? Speed dating? Discussion group postings? Random lottery? ???
 - hw1 due Thur. night (regexps, etc.) via gradescope
 - Use cse401-staff@cs... if you need to send email helps us keep organized. Thanks.

Agenda for Today

- Parsing overview
- Context free grammars
- Ambiguous grammars
- Reading: Cooper & Torczon 3.1-3.2
 - Dragon book is also particularly strong on grammars and languages

Syntactic Analysis / Parsing

- Goal: Convert token stream to an abstract syntax tree
- Abstract syntax tree (AST):
 - Captures the structural features of the program
 - Primary data structure for next phases of compilation
- Plan
 - Study how context-free grammars specify syntax
 - Study algorithms for parsing and building ASTs

Context-free Grammars

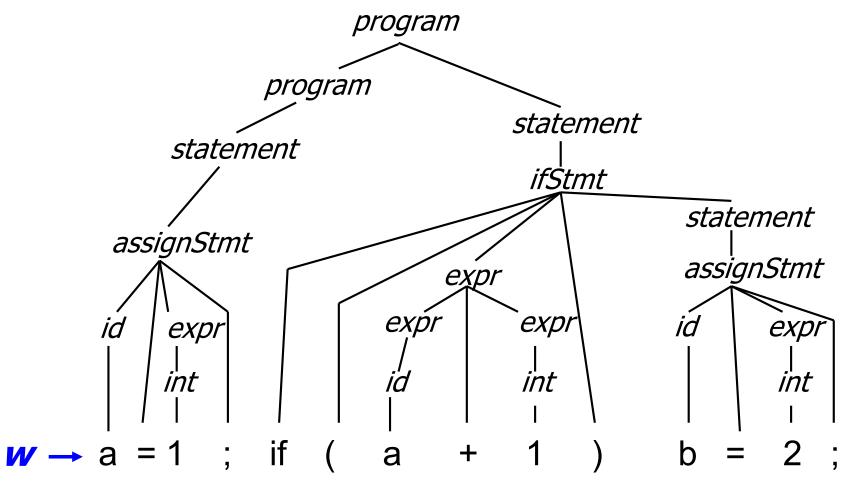
- The syntax of most programming languages can be specified by a context-free grammar (CGF)
- Compromise between
 - REs: can't nest or specify recursive structure
 - General grammars: too powerful, undecidable
- Context-free grammars are a sweet spot
 - Powerful enough to describe nesting, recursion
 - Easy to parse; but also allow restrictions for speed
- Not perfect
 - Cannot capture semantics, like "must declare every variable" or "must be int" – requires later semantic pass
 - Can be ambiguous

Derivations and Parse Trees

- Derivation: a sequence of expansion steps, beginning with a start symbol and leading to a sequence of terminals
- Parsing: inverse of derivation
 - Given a sequence of terminals (aka tokens) want to recover (discover) the nonterminals and structure, i.e., the parse (concrete syntax) tree

Old Example

program ::= statement | program statement
 statement ::= assignStmt | ifStmt
 assignStmt ::= id = expr ;
 ifStmt ::= if (expr) statement
 expr ::= id | int | expr + expr
 id ::= a | b | c | i | j | k | n | x | y | z
 int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9



UW CSE 401/M501 Autumn 2018

Parsing

- Parsing: Given a grammar G and a sentence w in L(G), traverse the derivation (parse tree) for w in some standard order and do something useful at each node
 - The tree might not be produced explicitly, but the control flow of the parser will correspond to a traversal

"Standard Order"

- For practical reasons we want the parser to be deterministic (no backtracking), and we want to examine the source program from *left to right*.
 - (i.e., parse the program in linear time in the order it appears in the source file)

Common Orderings

- Top-down
 - Start with the root
 - Traverse the parse tree depth-first, left-to-right (leftmost derivation)
 - LL(k), recursive-descent
- Bottom-up
 - Start at leaves and build up to the root
 - Effectively a rightmost derivation in reverse(!)
 - LR(k) and subsets (LALR(k), SLR(k), etc.)

"Something Useful"

- At each point (node) in the traversal, perform some semantic action
 - Construct nodes of full parse tree (rare)
 - Construct abstract syntax tree (AST) (common)
 - Construct linear, lower-level representation (often produced by traversing initial AST in later phases of production compilers)
 - Generate target code on the fly (used in 1-pass compiler; not common in production compilers)
 - Can't generate great code in one pass, but useful if you need a quick 'n dirty working compiler

Context-Free Grammars

- Formally, a grammar G is a tuple <N,Σ,P,S> where
 - *N* is a finite set of *non-terminal* symbols
 - $-\Sigma$ is a finite set of *terminal* symbols (alphabet)
 - *P* is a finite set of *productions*
 - A subset of $N \times (N \cup \Sigma)^*$
 - S is the start symbol, a distinguished element of N
 - If not specified otherwise, this is usually assumed to be the non-terminal on the left of the first production

Standard Notations

- a, b, c elements of Σ
- w, x, y, z elements of Σ^*
- A, B, C elements of N
- X, Y, Z elements of $N \cup \Sigma$
- α, β, γ elements of (NUS)*
- A $\rightarrow \alpha$ or A ::= α if <A, α > in P

Derivation Relations (1)

- $\alpha \land \gamma \Rightarrow \alpha \land \beta \gamma$ iff $A ::= \beta in P$ - derives
- A =>* α if there is a chain of productions starting with A that generates α

transitive closure

Derivation Relations (2)

- w A $\gamma =>_{Im} w \beta \gamma$ iff A ::= β in P – derives leftmost
- $\alpha A w = \sum_{rm} \alpha \beta w$ iff $A ::= \beta in P$ - derives rightmost
- We will only be interested in leftmost and rightmost derivations – not random orderings

Languages

- For A in N, define L(A) = { w | A =>* w }
- If S is the start symbol of grammar G, define
 L(G) = L(S)
 - Nonterminal on left of first rule is taken to be the start symbol if one is not specified explicitly

Reduced Grammars

• Grammar G is *reduced* iff for every production A ::= α in G there is a derivation

 $S = x \land z =$

- i.e., no production is useless

- Convention: we will use only reduced grammars
 - There are algorithms for pruning useless productions from grammars – see a formal language or compiler book for details

Ambiguity

- Grammar G is *unambiguous* iff every w in L(G) has a unique leftmost (or rightmost) derivation
 - Fact: unique leftmost or unique rightmost implies the other
- A grammar without this property is *ambiguous*
 - Note that other grammars that generate the same language may be unambiguous
- We need unambiguous grammars for parsing

Example: Ambiguous Grammar for Arithmetic Expressions

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

- Exercise: show that this is ambiguous
 - How? Show two different leftmost or rightmost derivations for the same string
 - Equivalently: show two different parse trees for the same string

Example (cont)

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a leftmost derivation of 2+3*4 and show the parse tree

Example (cont)

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a different leftmost derivation of 2+3*4 and show the parse tree

Another example

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

• Give two different derivations of 5+6+7

What's going on here?

- The grammar has no notion of precedence or associatively
- Traditional solution
 - Create a non-terminal for each level of precedence
 - Isolate the corresponding part of the grammar
 - Force the parser to recognize higher precedence subexpressions first
 - Use left- or right-recursion for left- or right-associative operators (non-associative operators are not recursive)

Classic Expression Grammar (first used in ALGOL 60)

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check: Derive 2 + 3 * 4

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check: Derive 5 + 6 + 7

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

 Note interaction between left- vs right-recursive rules and resulting associativity

Check: Derive 5 + (6 + 7)

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Another Classic Example

- Grammar for conditional statements
 stmt ::= if (cond) stmt
 | if (cond) stmt else stmt
 - Exercise: show that this is ambiguous
 - How?

One Derivation

if (cond) if (cond) stmt else stmt

UW CSE 401/M501 Autumn 2018

Another Derivation

if (cond) if (cond) stmt else stmt

UW CSE 401/M501 Autumn 2018

Solving "if" Ambiguity

- Fix the grammar to separate if statements with else clause and if statements with no else
 - Done in Java reference grammar
 - Adds lots of non-terminals
- or, Change the language
 But it'd better be ok to do this
- or, Use some ad-hoc rule in the parser
 - "else matches closest unpaired if"

Resolving Ambiguity with Grammar (1)

```
Stmt ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
    if ( Expr ) MatchedStmt else MatchedStmt
UnmatchedStmt ::= ... |
    if ( Expr ) Stmt |
    if ( Expr ) MatchedStmt else UnmatchedStmt
```

- formal, no additional rules beyond syntax
- can be more obscure than original grammar

Check

Stmt ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
 if (Expr) MatchedStmt else MatchedStmt
UnmatchedStmt ::= if (Expr) Stmt |
 if (Expr) MatchedStmt else UnmatchedStmt

if (cond) if (cond) stmt else stmt

Resolving Ambiguity with Grammar (2)

If you can (re-)design the language, just avoid the problem entirely

Stmt ::= ... | **if** Expr **then** Stmt **end** | **if** Expr **then** Stmt **else** Stmt **end**

- formal, clear, elegant
- allows sequence of Stmts in then and else branches, no { , } needed
- extra end required for every if
 (But maybe this is a good idea anyway?)

Parser Tools and Operators

- Most parser tools can cope with ambiguous grammars
 - Makes life simpler if used with discipline
- Usually can specify precedence & associativity
 - Allows simpler, ambiguous grammar with fewer nonterminals as basis for parser – let the tool handle the details (but only when it makes sense)
 - (i.e., expr ::= expr+expr | expr*expr | ... with assoc. & precedence declarations can be the best solution)
- Take advantage of this to simplify the grammar when using parser-generator tools

Parser Tools and Ambiguous Grammars

- Possible rules for resolving other problems
 - Earlier productions in the grammar preferred to later ones (danger here if parser input changes)
 - Longest match used if there is a choice (good solution for dangling if and similar things)
- Parser tools normally allow for this
 - But be sure that what the tool does is really what you want
 - And that it's part of the tool spec, so that v2 won't do something different (that you *don't* want!)

Coming Attractions

Next topic: LR parsing
 – Continue reading ch. 3